

## A Smart Numerical Gradient

February 14, 2021

Bayesian Computational Statistics and Modeling Research Group King Abdullah University of Science and Technology

## Contents

1 Test Some Functions 1

## 1 Test Some Functions

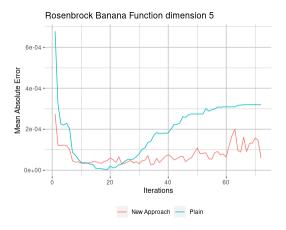


Figure 1: MSE of Rosenbrock Function (Dim 5)

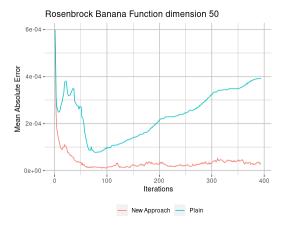
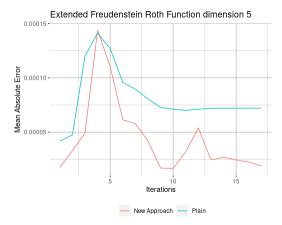


Figure 3: Rosenbrock Function (Dim 50)



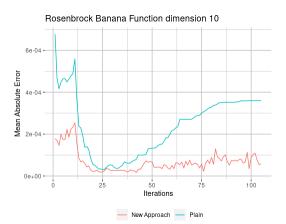


Figure 2: Rosenbrock Function (Dim 10)

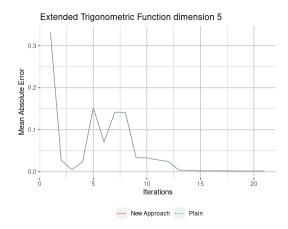


Figure 4: Ext. Trigonometric Function (Dim 5)

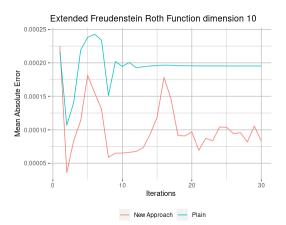
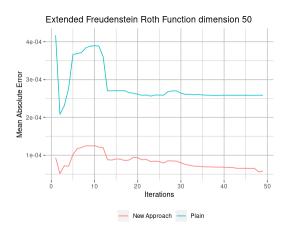


Figure 5: Ext. Freudenstein Roth Function (Dim 5) Figure 6: Ext. Freudenstein Roth Function (Dim 10)



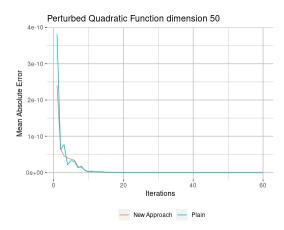
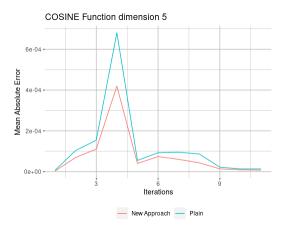


Figure 7: Ext. Freudenstein Roth Function (Dim 50) Figure 8: Perturbed Quadratic Function (Dim 50)



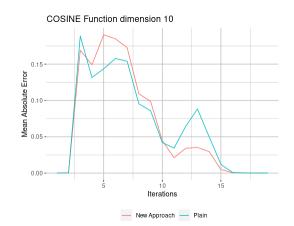
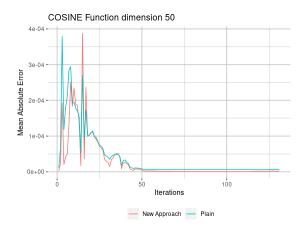


Figure 9: COSINE Function (Dim 50)

Figure 10: COSINE Function (Dim 10)



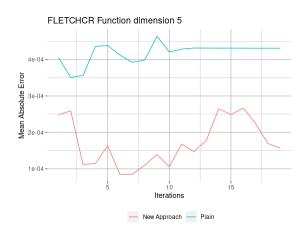
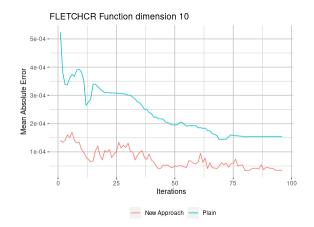


Figure 11: COSINE Function (Dim 50)

Figure 12: FLETCHCR Function (Dim 5)



FLETCHCR Function dimension 50

6e-04

6e-04

0e+00

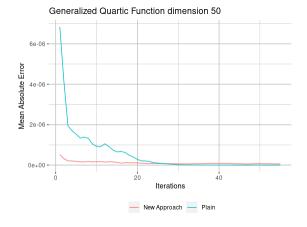
100

Iterations

Plain

Figure 13: FLETCHCR Function (Dim 10)

Figure 14: FLETCHCR Function (Dim 50)



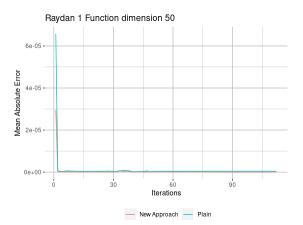


Figure 15: Generalized Quartic Function (Dim 50)

Figure 16: Raydan 1 Function (Dim 50)

| Function                            | x dimension | Average MSE<br>100 iterations<br>Default Approach | Average MSE<br>100 iterations<br>New Approach |
|-------------------------------------|-------------|---------------------------------------------------|-----------------------------------------------|
| Rosenbrock Banana Function          | 5           | 0.00026                                           | 0.000104                                      |
| Rosenbrock Banana Function          | 10          | 0.000271                                          | 7.8e-05                                       |
| Rosenbrock Banana Function          | 50          | 0.000292                                          | 7.8e-05                                       |
| Rosenbrock Banana Function          | 100         |                                                   |                                               |
| Extended Trigonometric Function     | 5           | 0.048934                                          | 0.048932                                      |
| Extended Trigonometric Function     | 10          |                                                   |                                               |
| Extended Freudenstein Roth Function | 5           | 0.000226                                          | 0.000137                                      |
| Extended Freudenstein Roth Function | 10          | 0.000262                                          | 0.000132                                      |
| Extended Freudenstein Roth Function | 50          | 0.000299                                          | 0.000106                                      |
| Perturbed Quadratic Function        | 50          | 0                                                 | 0                                             |
| COSINE Function                     | 5           | 0.0123                                            | 0.007932                                      |
| COSINE Function                     | 10          | 1.199679                                          | 1.016674                                      |
| COSINE Function                     | 50          | 0.181691                                          | 0.142211                                      |
| FLETCHCR Function                   | 5           | 0.000318                                          | 0.000139                                      |
| FLETCHCR Function                   | 10          | 0.000327                                          | 0.000104                                      |
| FLETCHCR Function                   | 50          | 0.000361                                          | 4e-05                                         |
| Generalized Quartic Function        | 50          | 1e-06                                             | 0                                             |
| Raydan 1 Function                   | 50          | 1e-06                                             | 0                                             |