

Systems Data

- IEEE-24 Bus System

| Generation and load levels | | | | | | | |
|----------------------------|--------------------------|-------------|-------------|-------------|-------------|-------------|-----------|
| Bus | Generation capacity (MW) | Generation | | | | | Load (MW) |
| | | - G0 - (MW) | - G1 - (MW) | - G2 - (MW) | - G3 - (MW) | - G4 - (MW) | |
| 1 | 576 | 576 | 576 | 465 | 576 | 520 | 324 |
| 2 | 576 | 576 | 576 | 576 | 576 | 520 | 291 |
| 3 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 540 |
| 4 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 222 |
| 5 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 213 |
| 6 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 408 |
| 7 | 900 | 900 | 900 | 722 | 900 | 812 | 375 |
| 8 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 513 |
| 9 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 525 |
| 10 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 585 |
| 11 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 12 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 13 | 1773 | 1773 | 1773 | 1424 | 1457 | 1599 | 795 |
| 14 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 582 |
| 15 | 645 | 645 | 645 | 645 | 325 | 581 | 951 |
| 16 | 465 | 465 | 465 | 465 | 282 | 419 | 300 |
| 17 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 18 | 1200 | 1200 | 1200 | 1200 | 603 | 718 | 999 |
| 19 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 543 |
| 20 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 384 |
| 21 | 1200 | 1200 | 1200 | 1200 | 951 | 1077 | 0.0 |
| 22 | 900 | 900 | 900 | 900 | 900 | 900 | 0.0 |
| 23 | 1980 | 1980 | 315 | 953 | 1980 | 1404 | 0.0 |
| 24 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |

Transmission Network Expansion Problem

| Existing circuits in the base topology | | | |
|--|-------------------|------------------------|---------------|
| Transmission line | Existing circuits | Reactance (Ω) | Capacity (MW) |
| 1-2 | 1 | 1.39 | 175 |
| 1-3 | 1 | 21.12 | 175 |
| 1-5 | 1 | 8.45 | 175 |
| 2-4 | 1 | 12.67 | 175 |
| 2-6 | 1 | 19.20 | 175 |
| 3-9 | 1 | 11.90 | 175 |
| 3-24 | 2 | 8.39 | 400 |
| 4-9 | 2 | 10.37 | 175 |
| 5-10 | 1 | 8.83 | 175 |
| 6-10 | 2 | 6.05 | 175 |
| 7-8 | 2 | 6.14 | 175 |
| 8-9 | 2 | 16.51 | 175 |
| 8-10 | 1 | 16.51 | 175 |
| 9-11 | 1 | 8.39 | 400 |
| 9-12 | 1 | 8.39 | 400 |
| 10-11 | 1 | 8.39 | 400 |
| 10-12 | 1 | 8.39 | 400 |
| 11-13 | 1 | 4.76 | 500 |
| 11-14 | 1 | 4.18 | 500 |
| 12-13 | 1 | 4.76 | 500 |
| 12-23 | 1 | 9.66 | 500 |
| 13-23 | 1 | 8.65 | 500 |
| 14-16 | 1 | 3.89 | 500 |
| 15-16 | 1 | 1.73 | 500 |
| 15-21 | 2 | 4.90 | 500 |
| 15-24 | 1 | 5.19 | 500 |
| 16-17 | 1 | 2.59 | 500 |
| 16-19 | 1 | 2.31 | 500 |
| 17-18 | 1 | 1.44 | 500 |
| 17-22 | 1 | 10.53 | 500 |
| 18-21 | 2 | 2.59 | 500 |
| 19-20 | 2 | 3.96 | 500 |
| 20-23 | 2 | 2.16 | 500 |
| 21-22 | 1 | 6.78 | 500 |

Transmission Network Expansion Problem

| Transmission line | Candidate circuits | | |
|-------------------|---------------------------|------------------|--------------------------------------|
| | Reactance (Ω) | Capacity (MW) | Investment cost (million dollars) |
| 1-8 | 13.44 | 500 | 35 |
| 2-8 | 12.67 | 500 | 33 |
| 6-7 | 19.20 | 500 | 50 |
| 13-14 | 4.47 | 500 | 62 |
| 14-23 | 6.20 | 500 | 86 |
| 16-23 | 8.22 | 500 | 114 |
| 19-23 | 6.06 | 500 | 84 |
| 1-2 | 1.39 | 175 | 3 |
| 1-3 | 21.12 | 175 | 55 |
| 1-5 | 8.45 | 175 | 22 |
| 2-4 | 12.67 | 175 | 33 |
| 2-6 | 19.20 | 175 | 50 |
| 3-9 | 11.90 | 175 | 31 |
| 3-24 | 8.39 | 400 | 50 |
| 4-9 | 10.37 | 175 | 27 |
| 5-10 | 8.83 | 175 | 23 |
| 6-10 | 6.05 | 175 | 16 |
| 7-8 | 6.14 | 175 | 16 |
| 8-9 | 16.51 | 175 | 43 |
| 8-10 | 16.51 | 175 | 43 |
| 9-11 | 8.39 | 400 | 50 |
| 9-12 | 8.39 | 400 | 50 |
| 10-11 | 8.39 | 400 | 50 |
| 10-12 | 8.39 | 400 | 50 |
| 11-13 | 4.76 | 500 | 66 |
| 11-14 | 4.18 | 500 | 58 |
| 12-13 | 4.76 | 500 | 66 |
| 12-23 | 9.66 | 500 | 134 |
| 13-23 | 8.65 | 500 | 120 |
| 14-16 | 3.89 | 500 | 54 |
| 15-16 | 1.73 | 500 | 24 |
| 15-21 | 4.90 | 500 | 68 |
| 15-24 | 5.19 | 500 | 72 |
| 16-17 | 2.59 | 500 | 36 |
| 16-19 | 2.31 | 500 | 32 |
| 17-18 | 1.44 | 500 | 20 |
| 17-22 | 10.53 | 500 | 146 |
| 18-21 | 2.59 | 500 | 36 |
| 19-20 | 3.96 | 500 | 55 |
| 20-23 | 2.16 | 500 | 30 |
| 21-22 | 6.78 | 500 | 94 |

Transmission Network Expansion Problem

- **South Brazilian System**

| Generation and load levels | | | |
|----------------------------|-----------------------------|--------------------|--------------|
| Bus | Generation capacity (MW) | Generation (MW) | Load (MW) |
| 1 | 0.0 | 0.0 | 0.0 |
| 2 | 0.0 | 0.0 | 443.1 |
| 3 | 0.0 | 0.0 | 0.0 |
| 4 | 0.0 | 0.0 | 300.7 |
| 5 | 0.0 | 0.0 | 238 |
| 6 | 0.0 | 0.0 | 0.0 |
| 7 | 0.0 | 0.0 | 0.0 |
| 8 | 0.0 | 0.0 | 72.2 |
| 9 | 0.0 | 0.0 | 0.0 |
| 10 | 0.0 | 0.0 | 0.0 |
| 11 | 0.0 | 0.0 | 0.0 |
| 12 | 0.0 | 0.0 | 511.9 |
| 13 | 0.0 | 0.0 | 185.8 |
| 14 | 1257 | 944 | 0.0 |
| 15 | 0.0 | 0.0 | 0.0 |
| 16 | 2000 | 1366 | 0.0 |
| 17 | 1050 | 1000 | 0.0 |
| 18 | 0.0 | 0.0 | 0.0 |
| 19 | 1670 | 773 | 0.0 |
| 20 | 0.0 | 0.0 | 1091 |
| 21 | 0.0 | 0.0 | 0.0 |
| 22 | 0.0 | 0.0 | 81.9 |
| 23 | 0.0 | 0.0 | 458.1 |
| 24 | 0.0 | 0.0 | 478.2 |
| 25 | 0.0 | 0.0 | 0.0 |
| 26 | 0.0 | 0.0 | 231.9 |
| 27 | 220 | 54 | 0.0 |
| 28 | 800 | 730 | 0.0 |
| 29 | 0.0 | 0.0 | 0.0 |
| 30 | 0.0 | 0.0 | 0.0 |
| 31 | 700 | 310 | 0.0 |
| 32 | 500 | 450 | 0.0 |
| 33 | 0.0 | 0.0 | 229.1 |
| 34 | 748 | 221 | 0.0 |
| 35 | 0.0 | 0.0 | 216.0 |
| 36 | 0.0 | 0.0 | 90.1 |
| 37 | 300 | 212 | 0.0 |
| 38 | 0.0 | 0.0 | 216 |
| 39 | 600 | 221 | 0.0 |
| 40 | 0.0 | 0.0 | 262.1 |
| 41 | 0.0 | 0.0 | 0.0 |
| 42 | 0.0 | 0.0 | 1607 |
| 43 | 0.0 | 0.0 | 0.0 |
| 44 | 0.0 | 0.0 | 79.1 |
| 45 | 0.0 | 0.0 | 86.7 |
| 46 | 700 | 599 | 0.0 |

Transmission Network Expansion Problem

| Transmission line | Existing circuits in the base topology | | |
|-------------------|--|------------------------|---------------|
| | Existing circuits | Reactance (Ω) | Capacity (MW) |
| 1-7 | 1 | 6.16 | 270 |
| 1-2 | 2 | 10.65 | 270 |
| 4-9 | 1 | 9.24 | 270 |
| 5-9 | 1 | 11.73 | 270 |
| 5-8 | 1 | 11.32 | 270 |
| 7-8 | 1 | 10.23 | 270 |
| 4-5 | 2 | 5.66 | 270 |
| 2-5 | 2 | 3.24 | 270 |
| 8-13 | 1 | 13.48 | 240 |
| 9-14 | 2 | 17.56 | 220 |
| 12-14 | 2 | 7.40 | 270 |
| 14-18 | 2 | 15.14 | 240 |
| 13-18 | 1 | 18.05 | 220 |
| 13-20 | 1 | 17.03 | 270 |
| 18-20 | 1 | 19.97 | 200 |
| 19-21 | 1 | 2.78 | 1500 |
| 16-17 | 1 | 0.78 | 2000 |
| 17-19 | 1 | 0.61 | 2000 |
| 14-26 | 1 | 16.14 | 220 |
| 14-22 | 1 | 8.40 | 270 |
| 22-26 | 1 | 7.90 | 270 |
| 20-23 | 2 | 9.32 | 270 |
| 23-24 | 2 | 7.74 | 270 |
| 26-27 | 2 | 8.32 | 270 |
| 24-34 | 1 | 16.47 | 220 |
| 24-33 | 1 | 14.48 | 240 |
| 33-34 | 1 | 12.65 | 270 |
| 27-36 | 1 | 9.15 | 270 |
| 27-38 | 2 | 20.8 | 200 |
| 36-37 | 1 | 10.57 | 270 |
| 34-35 | 2 | 4.91 | 270 |
| 35-38 | 1 | 19.80 | 200 |
| 37-39 | 1 | 2.83 | 270 |
| 37-40 | 1 | 12.81 | 270 |
| 37-42 | 1 | 21.05 | 200 |
| 39-42 | 3 | 20.30 | 200 |
| 40-42 | 1 | 9.32 | 270 |
| 38-42 | 3 | 9.07 | 270 |
| 32-43 | 1 | 3.09 | 1400 |
| 42-44 | 1 | 12.06 | 270 |
| 44-45 | 1 | 18.64 | 200 |
| 19-32 | 1 | 1.95 | 1800 |
| 46-19 | 1 | 2.22 | 1800 |
| 46-16 | 1 | 2.03 | 1800 |
| 18-19 | 1 | 1.25 | 600 |
| 20-21 | 1 | 1.25 | 600 |
| 42-43 | 1 | 1.25 | 600 |

Transmission Network Expansion Problem

| Transmission line | Candidate circuits | | |
|-------------------|---------------------------|------------------|--------------------------------------|
| | Reactance (Ω) | Capacity (MW) | Investment cost (million dollars) |
| 1-7 | 6.16 | 270 | 4.35 |
| 1-2 | 10.65 | 270 | 7.08 |
| 4-9 | 9.24 | 270 | 6.22 |
| 5-9 | 11.73 | 270 | 7.74 |
| 5-8 | 11.32 | 270 | 7.50 |
| 7-8 | 10.23 | 270 | 6.83 |
| 4-5 | 5.66 | 270 | 4.05 |
| 2-5 | 3.24 | 270 | 2.58 |
| 8-13 | 13.48 | 240 | 8.80 |
| 9-14 | 17.56 | 220 | 11.27 |
| 12-14 | 7.40 | 270 | 5.11 |
| 14-18 | 15.14 | 240 | 9.80 |
| 13-18 | 18.05 | 220 | 11.57 |
| 13-20 | 17.03 | 270 | 7.17 |
| 18-20 | 19.97 | 200 | 12.74 |
| 19-21 | 2.78 | 1500 | 32.64 |
| 16-17 | 0.78 | 2000 | 10.51 |
| 17-19 | 0.61 | 2000 | 8.72 |
| 14-26 | 16.14 | 220 | 10.41 |
| 14-22 | 8.40 | 270 | 5.72 |
| 22-26 | 7.90 | 270 | 5.41 |
| 20-23 | 9.32 | 270 | 6.27 |
| 23-24 | 7.74 | 270 | 5.31 |
| 26-27 | 8.32 | 270 | 5.66 |
| 24-34 | 16.47 | 220 | 10.61 |
| 24-33 | 14.48 | 240 | 9.34 |
| 33-34 | 12.65 | 270 | 8.28 |
| 27-36 | 9.15 | 270 | 6.17 |
| 27-38 | 20.8 | 200 | 13.24 |
| 36-37 | 10.57 | 270 | 7.02 |
| 34-35 | 4.91 | 270 | 3.59 |
| 35-38 | 19.80 | 200 | 12.63 |
| 37-39 | 2.83 | 270 | 2.33 |
| 37-40 | 12.81 | 270 | 8.38 |
| 37-42 | 21.05 | 200 | 13.38 |
| 39-42 | 20.30 | 200 | 12.93 |

Transmission Network Expansion Problem

| Candidate circuits | | | |
|--------------------|---------------------------|------------------|--------------------------------------|
| Transmission line | Reactance (Ω) | Capacity (MW) | Investment cost (million dollars) |
| 40-42 | 9.32 | 270 | 6.26 |
| 38-42 | 9.07 | 270 | 6.11 |
| 32-43 | 3.09 | 1400 | 35.917 |
| 42-44 | 12.06 | 270 | 7.93 |
| 44-45 | 18.64 | 200 | 11.94 |
| 19-32 | 1.95 | 1800 | 23.42 |
| 46-19 | 2.22 | 1800 | 26.36 |
| 46-16 | 2.03 | 1800 | 24.31 |
| 18-19 | 1.25 | 600 | 8.17 |
| 20-21 | 1.25 | 600 | 8.17 |
| 42-43 | 1.25 | 600 | 8.17 |
| 02-04 | 8.82 | 270 | 5.97 |
| 14-15 | 3.74 | 270 | 2.89 |
| 46-10 | 0.81 | 2000 | 10.89 |
| 04-11 | 22.46 | 240 | 14.25 |
| 05-11 | 9.15 | 270 | 6.17 |
| 46-06 | 1.28 | 2000 | 16.00 |
| 46-03 | 2.03 | 1800 | 24.32 |
| 16-28 | 2.22 | 1800 | 26.36 |
| 16-32 | 3.11 | 1400 | 36.21 |
| 17-32 | 2.32 | 1700 | 27.51 |
| 19-25 | 3.25 | 1400 | 37.75 |
| 21-25 | 1.74 | 2000 | 21.12 |
| 25-32 | 3.19 | 1400 | 37.11 |
| 31-32 | 0.46 | 2000 | 7.14 |
| 28-31 | 0.53 | 2000 | 7.82 |
| 28-30 | 0.58 | 2000 | 8.33 |
| 27-29 | 9.98 | 270 | 6.67 |
| 26-29 | 5.41 | 270 | 3.89 |
| 28-41 | 3.39 | 1300 | 39.29 |
| 28-43 | 4.06 | 1200 | 47.70 |
| 31-41 | 2.78 | 1500 | 32.63 |
| 32-41 | 3.09 | 1400 | 35.95 |
| 41-43 | 1.39 | 2000 | 17.29 |
| 40-45 | 22.05 | 180 | 13.99 |
| 15-16 | 1.25 | 600 | 8.17 |
| 46-11 | 1.25 | 600 | 8.17 |
| 24-25 | 1.25 | 600 | 8.17 |
| 29-30 | 1.25 | 600 | 8.17 |
| 40-41 | 1.25 | 600 | 8.17 |
| 02-03 | 1.25 | 600 | 8.17 |
| 05-06 | 1.25 | 600 | 8.17 |
| 09-10 | 1.25 | 600 | 8.17 |

Transmission Network Expansion Problem

- **Colombian System**

- **Generation and load levels – P1**

| Generation and load levels | | |
|----------------------------|--------------------|--------------|
| Bus | Generation (MW) | Load (MW) |
| 1 | 240 | 0.0 |
| 2 | 0.0 | 352.90 |
| 3 | 0.0 | 393.00 |
| 4 | 0.0 | 0.0 |
| 5 | 40 | 235.00 |
| 6 | 34 | 0.0 |
| 7 | 0.0 | 300.00 |
| 8 | 100 | 339.00 |
| 9 | 0.0 | 348.00 |
| 10 | 0.0 | 60.00 |
| 11 | 80 | 147.00 |
| 12 | 47 | 0.0 |
| 13 | 0.0 | 174.00 |
| 14 | 0.0 | 0.0 |
| 15 | 0.0 | 377.00 |
| 16 | 0.0 | 236.00 |
| 17 | 35 | 136.00 |
| 18 | 480 | 36.20 |
| 19 | 900 | 19.60 |
| 20 | 0.0 | 202.40 |
| 21 | 0.0 | 186.00 |
| 22 | 200 | 53.00 |
| 23 | 0.0 | 203.00 |
| 29 | 618 | 339.00 |
| 30 | 0.0 | 137.00 |
| 31 | 189 | 234.00 |
| 32 | 0.0 | 126.00 |
| 33 | 0.0 | 165.00 |
| 34 | 0.0 | 77.50 |

Transmission Network Expansion Problem

| Generation and load levels | | |
|----------------------------|-----------------|-----------|
| Bus | Generation (MW) | Load (MW) |
| 35 | 200 | 172.00 |
| 36 | 0.0 | 112.00 |
| 37 | 138 | 118.00 |
| 38 | 0.0 | 86.00 |
| 39 | 0.0 | 180.00 |
| 40 | 305 | 0.0 |
| 41 | 70 | 54.80 |
| 42 | 0.0 | 102.00 |
| 43 | 0.0 | 35.40 |
| 44 | 23 | 257.00 |
| 45 | 950 | 0.0 |
| 64 | 0.0 | 88.00 |
| 65 | 0.0 | 132.00 |
| 66 | 200 | 0.0 |
| 67 | 474 | 266.00 |
| 68 | 0.0 | 0.0 |
| 69 | 0.0 | 71.40 |
| 70 | 30 | 0.0 |
| 71 | 0.0 | 315.00 |
| 72 | 0.0 | 0.0 |
| 73 | 0.0 | 0.0 |
| 74 | 0.0 | 0.0 |
| 75 | 0.0 | 0.0 |
| 76 | 40 | 0.0 |
| 77 | 0.0 | 55.00 |
| 78 | 0.0 | 36.65 |
| 79 | 0.0 | 98.00 |
| 80 | 0.0 | 60.00 |
| 81 | 0.0 | 0.0 |
| 82 | 0.0 | 0.0 |
| 83 | 0.0 | 0.0 |
| 84 | 0.0 | 0.0 |
| 85 | 0.0 | 0.0 |
| 86 | 0.0 | 0.0 |
| 87 | 0.0 | 0.0 |
| 88 | 0.0 | 0.0 |
| 89 | 0.0 | 0.0 |
| 90 | 0.0 | 0.0 |
| 91 | 0.0 | 0.0 |
| 92 | 0.0 | 0.0 |
| 93 | 0.0 | 0.0 |

Transmission Network Expansion Problem

○ Generation and load levels – P2

| Generation and load levels | | |
|----------------------------|--------------------|--------------|
| Bus | Generation (MW) | Load (MW) |
| 1 | 240 | 0.0 |
| 2 | 165 | 406.53 |
| 3 | 0.0 | 490.50 |
| 4 | 0.0 | 0.0 |
| 5 | 40 | 293.56 |
| 6 | 34 | 0.0 |
| 7 | 0.0 | 374.26 |
| 8 | 230 | 423.00 |
| 9 | 0.0 | 434.12 |
| 10 | 0.0 | 74.21 |
| 11 | 108 | 183.90 |
| 12 | 47 | 0.0 |
| 13 | 0.0 | 217.26 |
| 14 | 0.0 | 0.0 |
| 15 | 0.0 | 470.17 |
| 16 | 0.0 | 294.00 |
| 17 | 35 | 169.57 |
| 18 | 540 | 45.20 |
| 19 | 1.340 | 24.46 |
| 20 | 0.0 | 252.50 |
| 21 | 0.0 | 231.70 |
| 22 | 200 | 66.13 |
| 23 | 0.0 | 252.50 |
| 24 | 150 | 0.0 |
| 25 | 86 | 0.0 |
| 26 | 70 | 0.0 |
| 27 | 0.0 | 331.40 |
| 28 | 0.0 | 406.30 |
| 29 | 618 | 422.60 |
| 30 | 0.0 | 166.70 |
| 31 | 189 | 327.30 |
| 32 | 0.0 | 157.30 |
| 33 | 0.0 | 206.53 |
| 34 | 0.0 | 96.70 |
| 35 | 200 | 214.60 |
| 36 | 0.0 | 140.00 |
| 37 | 138 | 147.30 |
| 38 | 15 | 108.40 |
| 39 | 0.0 | 224.00 |
| 40 | 305 | 0.0 |
| 41 | 100 | 68.40 |
| 42 | 0.0 | 127.30 |
| 43 | 0.0 | 44.20 |
| 44 | 23 | 321.30 |
| 45 | 1.208 | 0.0 |
| 46 | 150 | 151.70 |
| 47 | 0.0 | 51.50 |
| 48 | 885 | 750.00 |
| 49 | 0.0 | 162.00 |
| 50 | 240 | 528.00 |

Transmission Network Expansion Problem

| Generation and load levels | | |
|----------------------------|-----------------|-----------|
| Bus | Generation (MW) | Load (MW) |
| 51 | 0.0 | 159.00 |
| 52 | 0.0 | 46.50 |
| 53 | 320 | 0.0 |
| 54 | 0.0 | 95.30 |
| 55 | 40 | 279.00 |
| 56 | 0.0 | 0.0 |
| 57 | 130 | 281.00 |
| 58 | 190 | 0.0 |
| 59 | 160 | 0.0 |
| 60 | 1,216 | 0.0 |
| 61 | 155 | 0.0 |
| 62 | 0.0 | 0.0 |
| 63 | 1,090 | 44.00 |
| 64 | 0.0 | 110.55 |
| 65 | 0.0 | 165.00 |
| 66 | 300 | 0.0 |
| 67 | 474 | 332.45 |
| 68 | 0.0 | 0.0 |
| 69 | 0.0 | 89.00 |
| 70 | 180 | 0.0 |
| 71 | 211 | 393.00 |
| 72 | 0.0 | 0.0 |
| 73 | 0.0 | 0.0 |
| 74 | 0.0 | 0.0 |
| 75 | 0.0 | 0.0 |
| 76 | 40 | 0.0 |
| 77 | 0.0 | 70.00 |
| 78 | 0.0 | 45.10 |
| 79 | 0.0 | 123.00 |
| 80 | 0.0 | 72.00 |
| 81 | 0.0 | 0.0 |
| 82 | 0.0 | 0.0 |
| 83 | 0.0 | 0.0 |
| 84 | 0.0 | 0.0 |
| 85 | 0.0 | 0.0 |
| 86 | 300.0 | 0.0 |
| 87 | 0.0 | 0.0 |
| 88 | 0.0 | 0.0 |
| 89 | 0.0 | 0.0 |
| 90 | 0.0 | 0.0 |
| 91 | 0.0 | 0.0 |
| 92 | 0.0 | 0.0 |
| 93 | 0.0 | 0.0 |

Transmission Network Expansion Problem

○ Generation and load levels – P3

| Generation and load levels | | |
|----------------------------|--------------------|--------------|
| Bus | Generation (MW) | Load (MW) |
| 1 | 240 | 0.0 |
| 2 | 165 | 486.66 |
| 3 | 0.0 | 587.08 |
| 4 | 0.0 | 0.0 |
| 5 | 40 | 351.42 |
| 6 | 34 | 0.0 |
| 7 | 136 | 448.03 |
| 8 | 230 | 505.87 |
| 9 | 0.0 | 519.69 |
| 10 | 0.0 | 88.84 |
| 11 | 108 | 220.15 |
| 12 | 47 | 0.0 |
| 13 | 0.0 | 260.08 |
| 14 | 0.0 | 0.0 |
| 15 | 0.0 | 562.84 |
| 16 | 0.0 | 351.90 |
| 17 | 35 | 203.00 |
| 18 | 540 | 54.10 |
| 19 | 1.340 | 29.28 |
| 20 | 45 | 302.27 |
| 21 | 0.0 | 277.44 |
| 22 | 200 | 79.17 |
| 23 | 0.0 | 302.27 |
| 24 | 150 | 0.0 |
| 25 | 86 | 0.0 |
| 26 | 70 | 0.0 |
| 27 | 0.0 | 396.71 |
| 28 | 14.0 | 486.39 |
| 29 | 618 | 505.96 |
| 30 | 0.0 | 199.5 |
| 31 | 189 | 391.88 |
| 32 | 0.0 | 188.33 |
| 33 | 0.0 | 247.24 |
| 34 | 0.0 | 115.81 |
| 35 | 200 | 256.86 |
| 36 | 44 | 167.29 |
| 37 | 138 | 176.30 |
| 38 | 15 | 129.72 |
| 39 | 15 | 268.19 |
| 40 | 305 | 0.0 |
| 41 | 100 | 81.85 |
| 42 | 0.0 | 152.39 |
| 43 | 0.0 | 52.90 |
| 44 | 23 | 384.64 |
| 45 | 1.208 | 0.0 |
| 46 | 150 | 151.70 |
| 47 | 0.0 | 51.50 |
| 48 | 885 | 896.26 |
| 49 | 0.0 | 193.27 |
| 50 | 240 | 632.75 |

Transmission Network Expansion Problem

| Generation and load levels | | |
|----------------------------|-----------------|-----------|
| Bus | Generation (MW) | Load (MW) |
| 51 | 0.0 | 190.45 |
| 52 | 0.0 | 55.60 |
| 53 | 320 | 0.0 |
| 54 | 0.0 | 114.19 |
| 55 | 40 | 333.59 |
| 56 | 0.0 | 0.0 |
| 57 | 130 | 336.94 |
| 58 | 190 | 0.0 |
| 59 | 160 | 0.0 |
| 60 | 1.216 | 0.0 |
| 61 | 155 | 0.0 |
| 62 | 0.0 | 0.0 |
| 63 | 1.090 | 52.77 |
| 64 | 280 | 132.35 |
| 65 | 0.0 | 197.58 |
| 66 | 300 | 0.0 |
| 67 | 474 | 397.98 |
| 68 | 0.0 | 0.0 |
| 69 | 0.0 | 106.61 |
| 70 | 180 | 0.0 |
| 71 | 424 | 471.21 |
| 72 | 0.0 | 0.0 |
| 73 | 0.0 | 0.0 |
| 74 | 0.0 | 0.0 |
| 75 | 0.0 | 0.0 |
| 76 | 40 | 0.0 |
| 77 | 0.0 | 82.85 |
| 78 | 0.0 | 54.07 |
| 79 | 300 | 146.87 |
| 80 | 0.0 | 88.34 |
| 81 | 0.0 | 0.0 |
| 82 | 0.0 | 0.0 |
| 83 | 0.0 | 0.0 |
| 84 | 500 | 0.0 |
| 85 | 0.0 | 0.0 |
| 86 | 850 | 0.0 |
| 87 | 0.0 | 0.0 |
| 88 | 300 | 0.0 |
| 89 | 0.0 | 0.0 |
| 90 | 0.0 | 0.0 |
| 91 | 0.0 | 0.0 |
| 92 | 0.0 | 0.0 |
| 93 | 0.0 | 0.0 |

Transmission Network Expansion Problem

○ Data of transmission lines for all Colombian Systems

| Existing circuits in the base topology | | | |
|--|------------------|------------------------|---------------|
| Transmission line | Existing circuit | Reactance (Ω) | Capacity (MW) |
| 25-28 | 1 | 5.65 | 320 |
| 25-29 | 1 | 5.70 | 320 |
| 13-14 | 2 | 0.09 | 350 |
| 13-20 | 1 | 1.78 | 350 |
| 13-23 | 1 | 2.77 | 350 |
| 14-31 | 2 | 13.07 | 250 |
| 14-18 | 2 | 14.94 | 250 |
| 14-60 | 2 | 10.67 | 300 |
| 2-4 | 2 | 2.71 | 350 |
| 2-9 | 1 | 1.22 | 350 |
| 2-83 | 1 | 2.00 | 570 |
| 9-83 | 1 | 2.00 | 400 |
| 15-18 | 1 | 3.65 | 450 |
| 15-17 | 1 | 4.83 | 320 |
| 15-20 | 1 | 5.13 | 320 |
| 15-76 | 1 | 4.14 | 320 |
| 15-24 | 1 | 1.45 | 350 |
| 37-61 | 1 | 1.39 | 350 |
| 19-61 | 2 | 11.05 | 250 |
| 61-68 | 1 | 7.89 | 250 |
| 37-68 | 1 | 5.44 | 320 |
| 40-68 | 1 | 13.20 | 320 |
| 12-75 | 1 | 6.41 | 320 |
| 24-75 | 1 | 1.61 | 350 |
| 35-36 | 1 | 20.74 | 250 |
| 27-35 | 1 | 14.98 | 250 |
| 35-44 | 2 | 13.58 | 250 |
| 38-68 | 1 | 3.89 | 350 |
| 38-39 | 1 | 3.00 | 350 |
| 27-80 | 1 | 2.42 | 350 |
| 44-80 | 1 | 10.14 | 250 |
| 56-81 | 1 | 1.14 | 550 |
| 45-54 | 1 | 9.46 | 320 |
| 45-50 | 2 | 0.70 | 350 |
| 10-78 | 1 | 1.02 | 350 |
| 7-78 | 1 | 0.43 | 350 |
| 30-64 | 1 | 15.33 | 250 |
| 30-65 | 1 | 9.10 | 250 |
| 30-72 | 2 | 1.73 | 350 |
| 55-57 | 1 | 1.74 | 600 |
| 57-84 | 1 | 0.87 | 600 |
| 55-84 | 1 | 0.87 | 600 |
| 56-57 | 1 | 2.40 | 600 |
| 9-77 | 1 | 1.90 | 350 |
| 77-79 | 1 | 0.97 | 350 |
| 1-59 | 2 | 2.32 | 350 |
| 59-67 | 2 | 11.80 | 250 |
| 8-59 | 2 | 10.56 | 250 |
| 1-3 | 1 | 10.40 | 250 |
| 3-71 | 1 | 1.36 | 450 |
| 3-6 | 1 | 4.97 | 350 |

Transmission Network Expansion Problem

| Existing circuits in the base topology | | | |
|--|------------------|---------------------------|------------------|
| Transmission line | Existing circuit | Reactance (Ω) | Capacity (MW) |
| 55-62 | 1 | 2.81 | 550 |
| 47-52 | 1 | 6.44 | 350 |
| 51-52 | 1 | 8.59 | 250 |
| 29-31 | 2 | 10.42 | 250 |
| 41-42 | 1 | 0.94 | 350 |
| 40-42 | 1 | 1.53 | 350 |
| 46-53 | 2 | 10.41 | 250 |
| 46-51 | 1 | 11.41 | 250 |
| 69-70 | 2 | 2.28 | 350 |
| 66-69 | 2 | 12.17 | 250 |
| 9-69 | 2 | 10.98 | 350 |
| 60-69 | 2 | 9.06 | 350 |
| 31-32 | 1 | 2.59 | 350 |
| 32-34 | 1 | 5.40 | 350 |
| 16-18 | 1 | 6.25 | 350 |
| 16-23 | 1 | 2.38 | 350 |
| 16-21 | 1 | 2.82 | 350 |
| 31-34 | 1 | 7.92 | 250 |
| 31-33 | 2 | 2.48 | 350 |
| 31-60 | 2 | 19.44 | 250 |
| 31-72 | 2 | 2.44 | 350 |
| 47-54 | 2 | 10.03 | 250 |
| 47-49 | 2 | 9.42 | 250 |
| 18-58 | 2 | 2.12 | 350 |
| 18-20 | 1 | 5.04 | 350 |
| 18-66 | 2 | 6.64 | 350 |
| 18-21 | 1 | 3.48 | 350 |
| 18-22 | 1 | 2.09 | 350 |
| 19-22 | 1 | 6.91 | 350 |
| 4-5 | 3 | 0.49 | 350 |
| 5-6 | 2 | 0.74 | 350 |
| 17-23 | 1 | 9.13 | 250 |
| 17-76 | 1 | 0.20 | 350 |
| 12-17 | 1 | 0.86 | 350 |
| 1-71 | 2 | 8.41 | 250 |
| 1-8 | 1 | 8.10 | 250 |
| 1-11 | 1 | 7.99 | 250 |
| 4-36 | 2 | 8.50 | 250 |
| 19-58 | 1 | 8.26 | 320 |
| 27-64 | 1 | 2.80 | 350 |
| 27-28 | 1 | 2.38 | 350 |
| 27-44 | 1 | 8.93 | 250 |
| 26-27 | 1 | 6.57 | 350 |
| 27-29 | 1 | 1.66 | 350 |
| 19-66 | 1 | 5.16 | 350 |
| 73-74 | 1 | 2.14 | 600 |
| 64-65 | 1 | 7.41 | 350 |
| 29-64 | 1 | 0.63 | 350 |
| 4-34 | 2 | 10.16 | 270 |
| 34-70 | 2 | 4.15 | 350 |
| 33-34 | 1 | 11.39 | 320 |
| 8-71 | 1 | 0.75 | 400 |

Transmission Network Expansion Problem

| Existing circuits in the base topology | | | |
|--|------------------|---------------------------|------------------|
| Transmission line | Existing circuit | Reactance (Ω) | Capacity (MW) |
| 54-63 | 3 | 4.95 | 320 |
| 48-63 | 1 | 2.38 | 350 |
| 67-68 | 2 | 16.60 | 250 |
| 39-68 | 1 | 1.45 | 350 |
| 8-9 | 1 | 1.68 | 350 |
| 79-87 | 1 | 0.71 | 350 |
| 8-87 | 1 | 1.32 | 350 |
| 39-43 | 1 | 11.63 | 250 |
| 41-43 | 1 | 11.42 | 250 |
| 23-24 | 1 | 2.55 | 350 |
| 21-22 | 1 | 5.49 | 350 |
| 26-28 | 1 | 5.12 | 350 |
| 28-29 | 1 | 2.81 | 350 |
| 6-10 | 1 | 3.37 | 350 |
| 33-72 | 1 | 2.28 | 350 |
| 39-40 | 2 | 10.20 | 250 |
| 12-76 | 1 | 0.81 | 350 |
| 48-54 | 3 | 3.96 | 350 |
| 50-54 | 2 | 8.76 | 250 |
| 62-73 | 1 | 2.72 | 750 |
| 49-53 | 2 | 10.08 | 250 |
| 40-41 | 1 | 1.86 | 350 |
| 45-81 | 1 | 2.67 | 450 |
| 64-74 | 1 | 2.67 | 500 |
| 54-56 | 3 | 2.67 | 450 |
| 60-62 | 3 | 2.57 | 450 |
| 72-73 | 2 | 2.67 | 500 |
| 19-82 | 1 | 2.67 | 450 |
| 55-82 | 1 | 2.90 | 550 |
| 83-85 | 2 | 2.67 | 450 |
| 82-85 | 1 | 3.41 | 700 |
| 19-86 | 1 | 15.13 | 300 |
| 68-86 | 1 | 4.04 | 350 |
| 7-90 | 2 | 0.50 | 350 |
| 3-90 | 1 | 0.74 | 350 |
| 90-91 | 1 | 2.67 | 550 |
| 85-91 | 1 | 1.39 | 600 |
| 11-92 | 1 | 2.67 | 450 |
| 1-93 | 1 | 2.67 | 450 |
| 92-93 | 1 | 0.97 | 600 |
| 91-92 | 1 | 0.88 | 600 |

Transmission Network Expansion Problem

| Transmission line | Candidate circuits | | |
|-------------------|---------------------------|------------------|--------------------------------------|
| | Reactance (Ω) | Capacity (MW) | Investment cost (million dollars) |
| 52-88 | 9.80 | 300 | 34.190 |
| 43-88 | 18.16 | 250 | 39.56 |
| 57-81 | 2.19 | 550 | 58.89 |
| 73-82 | 3.74 | 550 | 97.96 |
| 27-89 | 2.67 | 450 | 13.27 |
| 74-89 | 0.34 | 550 | 14.57 |
| 73-89 | 2.46 | 550 | 66.65 |
| 79-83 | 4.57 | 350 | 15.40 |
| 8-67 | 22.40 | 250 | 29.20 |
| 39-86 | 5.45 | 350 | 9.88 |
| 25-28 | 5.65 | 320 | 9.767 |
| 25-29 | 5.70 | 320 | 9.88 |
| 13-14 | 0.09 | 350 | 3.90 |
| 13-20 | 1.78 | 350 | 5.742 |
| 13-23 | 2.77 | 350 | 7.007 |
| 14-31 | 13.07 | 250 | 18.622 |
| 14-18 | 14.94 | 250 | 20.232 |
| 14-60 | 10.67 | 300 | 15.977 |
| 2-4 | 2.71 | 350 | 6.662 |
| 2-9 | 1.22 | 350 | 5.282 |
| 2-83 | 2.00 | 570 | 5.972 |
| 9-83 | 2.00 | 400 | 5.972 |
| 15-18 | 3.65 | 450 | 7.927 |
| 15-17 | 4.83 | 320 | 9.422 |
| 15-20 | 5.13 | 320 | 9.652 |
| 15-76 | 4.14 | 320 | 9.882 |
| 15-24 | 1.45 | 350 | 5.282 |
| 37-61 | 1.39 | 350 | 4.937 |
| 19-61 | 11.05 | 250 | 16.092 |
| 61-68 | 7.89 | 250 | 12.412 |
| 37-68 | 5.44 | 320 | 9.652 |
| 40-68 | 13.20 | 320 | 18.162 |
| 12-75 | 6.41 | 320 | 11.492 |
| 24-75 | 1.61 | 350 | 5.512 |
| 35-36 | 20.74 | 250 | 27.362 |
| 27-35 | 14.98 | 250 | 22.072 |
| 35-44 | 13.58 | 250 | 20.347 |
| 38-68 | 3.89 | 350 | 7.927 |
| 38-39 | 3.00 | 350 | 6.317 |
| 27-80 | 2.42 | 350 | 7.007 |
| 44-80 | 10.14 | 250 | 17.587 |
| 56-81 | 1.14 | 550 | 32.858 |
| 45-54 | 9.46 | 320 | 13.562 |
| 45-50 | 0.70 | 350 | 4.362 |

Transmission Network Expansion Problem

| Candidate circuits | | | |
|--------------------|---------------------------|------------------|--------------------------------------|
| Transmission line | Reactance (Ω) | Capacity (MW) | Investment cost (million dollars) |
| 10-78 | 1.02 | 350 | 4.937 |
| 7-78 | 0.43 | 350 | 4.132 |
| 30-64 | 15.33 | 250 | 20.577 |
| 30-65 | 9.10 | 250 | 13.677 |
| 30-72 | 1.73 | 350 | 5.512 |
| 55-57 | 1.74 | 600 | 46.808 |
| 57-84 | 0.87 | 600 | 26.658 |
| 55-84 | 0.87 | 600 | 26.658 |
| 56-57 | 2.40 | 600 | 62.618 |
| 9-77 | 1.90 | 350 | 5.857 |
| 77-79 | 0.97 | 350 | 5.167 |
| 1-59 | 2.32 | 350 | 6.202 |
| 59-67 | 11.80 | 250 | 16.667 |
| 8-59 | 10.56 | 250 | 15.402 |
| 1-3 | 10.40 | 250 | 15.862 |
| 3-71 | 1.36 | 450 | 5.167 |
| 3-6 | 4.97 | 350 | 9.422 |
| 55-62 | 2.81 | 550 | 70.988 |
| 47-52 | 6.44 | 350 | 10.572 |
| 51-52 | 8.59 | 250 | 12.872 |
| 29-31 | 10.42 | 250 | 32.981 |
| 41-42 | 0.94 | 350 | 4.707 |
| 40-42 | 1.53 | 350 | 5.167 |
| 46-53 | 10.41 | 250 | 14.597 |
| 46-51 | 11.41 | 250 | 16.322 |
| 69-70 | 2.28 | 350 | 6.202 |
| 66-69 | 12.17 | 250 | 17.127 |
| 9-69 | 10.98 | 350 | 15.747 |
| 60-69 | 9.06 | 350 | 13.677 |
| 31-32 | 2.59 | 350 | 6.547 |
| 32-34 | 5.40 | 350 | 9.767 |
| 16-18 | 6.25 | 350 | 10.917 |
| 16-23 | 2.38 | 350 | 6.892 |
| 16-21 | 2.82 | 350 | 6.892 |
| 31-34 | 7.92 | 250 | 12.412 |
| 31-33 | 2.48 | 350 | 6.432 |
| 31-60 | 19.44 | 250 | 25.982 |
| 31-72 | 2.44 | 350 | 6.317 |
| 47-54 | 10.03 | 250 | 14.252 |
| 47-49 | 9.42 | 250 | 13.562 |
| 18-58 | 2.12 | 350 | 5.742 |
| 18-20 | 5.04 | 350 | 9.537 |
| 18-66 | 6.64 | 350 | 11.377 |
| 18-21 | 3.48 | 350 | 7.467 |
| 18-22 | 2.09 | 350 | 6.432 |
| 19-22 | 6.91 | 350 | 11.722 |

Transmission Network Expansion Problem

| Candidate circuits | | | |
|--------------------|---------------------------|------------------|--------------------------------------|
| Transmission line | Reactance (Ω) | Capacity (MW) | Investment cost (million dollars) |
| 4-5 | 0.49 | 350 | 4.247 |
| 5-6 | 0.74 | 350 | 4.477 |
| 17-23 | 9.13 | 250 | 12.987 |
| 17-76 | 0.20 | 350 | 3.902 |
| 12-17 | 0.86 | 350 | 4.707 |
| 1-71 | 8.41 | 250 | 14.367 |
| 1-8 | 8.10 | 250 | 13.217 |
| 1-11 | 7.99 | 250 | 12.527 |
| 4-36 | 8.50 | 250 | 13.562 |
| 19-58 | 8.26 | 320 | 11.722 |
| 27-64 | 2.80 | 350 | 6.777 |
| 27-28 | 2.38 | 350 | 6.202 |
| 27-44 | 8.93 | 250 | 16.322 |
| 26-27 | 6.57 | 350 | 10.917 |
| 27-29 | 1.66 | 350 | 5.052 |
| 19-66 | 5.16 | 350 | 9.307 |
| 73-74 | 2.14 | 600 | 58.278 |
| 64-65 | 7.41 | 350 | 11.837 |
| 29-64 | 0.63 | 350 | 4.362 |
| 4-34 | 10.16 | 270 | 14.942 |
| 34-70 | 4.15 | 350 | 8.272 |
| 33-34 | 11.39 | 320 | 16.322 |
| 8-71 | 0.75 | 400 | 4.477 |
| 54-63 | 4.95 | 320 | 9.077 |
| 48-63 | 2.38 | 350 | 6.317 |
| 67-68 | 16.60 | 250 | 22.072 |
| 39-68 | 1.45 | 350 | 5.282 |
| 8-9 | 1.68 | 350 | 5.972 |
| 79-87 | 0.71 | 350 | 4.477 |
| 8-87 | 1.32 | 350 | 5.167 |
| 39-43 | 11.63 | 250 | 16.552 |
| 41-43 | 11.42 | 250 | 16.322 |
| 23-24 | 2.55 | 350 | 6.317 |
| 21-22 | 05.49 | 350 | 9.882 |
| 26-28 | 05.12 | 350 | 9.307 |
| 28-29 | 2.81 | 350 | 6.777 |
| 6-10 | 3.37 | 350 | 7.582 |
| 33-72 | 2.28 | 350 | 6.202 |
| 39-40 | 10.20 | 250 | 16.207 |
| 12-76 | 0.81 | 350 | 4.707 |
| 48-54 | 3.96 | 350 | 8.042 |
| 50-54 | 8.76 | 250 | 12.872 |
| 62-73 | 2.72 | 750 | 73.158 |
| 49-53 | 10.08 | 250 | 14.252 |
| 40-41 | 1.86 | 350 | 5.742 |

Transmission Network Expansion Problem

| Candidate circuits | | | |
|--------------------|---------------------------|------------------|--------------------------------------|
| Transmission line | Reactance (Ω) | Capacity (MW) | Investment cost (million dollars) |
| 40-41 | 1.86 | 350 | 5.742 |
| 45-81 | 2.67 | 450 | 13.270 |
| 64-74 | 2.67 | 500 | 13.270 |
| 54-56 | 2.67 | 450 | 13.270 |
| 60-62 | 2.57 | 450 | 13.270 |
| 72-73 | 2.67 | 500 | 13.270 |
| 19-82 | 2.67 | 450 | 13.270 |
| 55-82 | 2.90 | 550 | 77.498 |
| 62-82 | 1.01 | 600 | 30.998 |
| 83-85 | 2.67 | 450 | 13.270 |
| 82-85 | 3.41 | 700 | 89.898 |
| 19-86 | 15.13 | 300 | 20.922 |
| 68-86 | 4.04 | 350 | 8.272 |
| 7-90 | 0.50 | 350 | 4.247 |
| 3-90 | 0.74 | 350 | 4.592 |
| 90-91 | 2.67 | 550 | 13.270 |
| 85-91 | 1.39 | 600 | 40.298 |
| 11-92 | 2.67 | 450 | 13.270 |
| 1-93 | 2.67 | 450 | 13.270 |
| 92-93 | 0.97 | 600 | 30.068 |
| 91-92 | 0.88 | 600 | 27.588 |