Pycalcal – Literate Calendars in Python

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¹I want to thank my wife, Gilda, for the patience of having looked after all kids and things while I was *playing* with this project. I also want to thank Prof. Reingold for his his prompt reply to all my questions. Finally my gratitude goes to my parents, Alida and Mario, for the sacrifice they endevoured in order to allow me get inspired by Science.

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Chapter 1

Literate Calendrical Calculations

This document describes a Python [7] implementation of the calendrical algorithms described in the book *Calendrical Calculations* [1].

According to the authors, the book is *the companion* text of the algorithms implemented in the COMMON LISP package CC3. The source code for CC3, calendrica-3.0.cl, is made available electronically by the publisher, see [1].

I provide full reference to the original COMMON LISP and credit (and deep respect) to its authors, Prof.s Dershowitz and Reingold.

On the (long) way to complete this project, I experimented with Scons [11], Test-Driven Development [12] and web applications [2].

I tackled this task the Literate Programming way [3] using the Noweb tool. [9, 8] As such all code and documentation is generated from a single source file and prefixed with the following warning:

 $\langle generated\ code\ warning\ 1 \rangle \equiv$ AUTOMATICALLY GENERATED FROM pycalcal.nw: ANY CHANGES WILL BE OVERWRITTEN.

This code is used in chunks 4, 9, 49, 58, 64, 67, 70, 73, 76, 79, 82, 85, 88, 91, 121, 124, 127, 132, 135, 138, 141, 144, 147, 198, 201, 203, 204, 207, 213, and 244.

1.1 Structure

The software is for now a single piece of text (a.k.a. a Python file):

 $\begin{array}{ccc} 2 & & \langle \ ^* \ ^{2} \rangle \equiv \\ & & \langle \mathit{pycalcal.py} \ ^{3} \rangle \end{array}$

Root chunk (not used in this document).

It is organised as follows:

```
3
        \langle pycalcal.py 3 \rangle \equiv
            \langle testa 9 \rangle
            \langle global\ import\ statements\ 11 \rangle
            \langle basic\ code\ 13 \rangle
            ⟨egyptian and armenian calendars 65⟩
            \langle gregorian\ calendar\ 51 \rangle
            \langle julian\ calendar\ 59 \rangle
            ⟨iso calendar 68⟩
            ⟨coptic and ethiopic calendars 71⟩
            (ecclesiastical calendars 74)
            \langle islamic\ calendar\ 77 \rangle
            \langle hebrew\ calendar\ 80 \rangle
            (mayan calendars 83)
            (old hindu calendars 86)
            (balinese calendar 89)
            time and astronomy 92
            ⟨astronomical lunar calendars 105⟩
            \langle persian\ calendar\ 122 \rangle
            ⟨bahai calendar 125⟩
            (french revolutionary calendar 128)
            \langle chinese\ calendar\ 133 \rangle
            ⟨modern hindu calendars 136⟩
            \langle tibetan\ calendar\ 139 \rangle
            \langle coda \ 143 \rangle
```

This code is used in chunk 2.

There is as well a companion file with unit tests inspired by the examples spread in the book [1], its Appendix C or devised by myself.

```
\langle pycalcaltests.py | \mathbf{4} \rangle \equiv
                      # \(\langle generated code warning \)
                      ⟨LICENSE 7⟩
                      from pycalcal import *
                      from appendixCUnitTest import AppendixCTable1TestCaseBase
                      from appendixCUnitTest import AppendixCTable2TestCaseBase
                      from appendixCUnitTest import AppendixCTable3TestCaseBase
                      from appendixCUnitTest import AppendixCTable4TestCaseBase
                      from appendixCUnitTest import AppendixCTable5TestCaseBase
                      import unittest
                      ⟨basic code unit test 50⟩
                      ⟨egyptian and armenian calendars unit test 66⟩
                      ⟨gregorian calendar unit test 57⟩
                      (iso calendar unit test 69)
                      \langle julian\ calendar\ unit\ test\ 60 \rangle
                      ⟨coptic and ethiopic calendars unit test 72⟩
                      ⟨ecclesiastical calendars unit test 75⟩
                      (islamic calendar unit test 78)
                      \langle hebrew\ calendar\ unit\ test\ 81 \rangle
                      \langle mayan\ calendars\ unit\ test\ 84 \rangle
                       (old hindu calendars unit test 87)
                       \langle balinese\ calendar\ unit\ test\ 90 \rangle
                      (time and astronomy unit test 104)
                      ⟨persian calendar unit test 123⟩
                      ⟨bahai calendar unit test 126⟩
                      (french revolutionary calendar unit test 129)
                      (chinese calendar unit test 134)
                      ⟨modern hindu calendars unit test 137⟩
                      ⟨tibetan calendar unit test 140⟩
                      ⟨astronomical lunar calendars unit test 145⟩
                      ⟨execute tests 5⟩
                Root chunk (not used in this document).
                Uses AppendixCTable1TestCaseBase 149, AppendixCTable2TestCaseBase 165,
                      {\tt AppendixCTable3TestCaseBase}~{\tt 174}, {\tt AppendixCTable4TestCaseBase}~{\tt 185}, {\tt and}~{\tt AppendixCTable5TestCaseBase}~{\tt 185}, {\tt app
                      194.
               The code for tests execution is:
                \langle execute \ tests \ 5 \rangle \equiv
5
                      if __name__ == "__main__":
                                 unittest.main()
                This code is used in chunks 4, 49, 58, 64, 67, 70, 73, 76, 79, 82, 85, 88, 91, 121, 124, 127, 132, 135, 138,
                      141, 144, and 147.
```

Given I also want to be able to run a single unit tests part in isolation, i.e. when working on Persian calendar I just want to run the Persian calendar's tests, I generate a unit tests file per each part. Here is an example of how the unit tests are templated for an hypotetical xyzzy calendar/section:

```
<<xyzzyUnitTest.py>>=
# <<generated code warning>>
</import for testing>>
from appendixCUnitTest import AppendixCTable1TestCaseBase
<<xyzzy unit test>>
</execute tests>>
The following imports are to be used:
</import for testing 6>=
    from pycalcal import *
    import unittest

This code is used in chunks 49, 58, 64, 67, 70, 73, 76, 79, 82, 85, 88, 91, 121, 124, 127, 132, 135, 138, 141, 144, and 147.
```

1.2 Copyright and Legalise

My copyright notice is intended to make this work accessible and free to everybody for any type of use (i.e. commercial, educational ...). I took an MIT License.

```
\langle LICENSE \ 7 \rangle \equiv
  # Copyright (c) 2009 Enrico Spinielli
 # Permission is hereby granted, free of charge, to any person obtaining a copy
  # of this software and associated documentation files (the "Software"), to deal
  # in the Software without restriction, including without limitation the rights
  # to use, copy, modify, merge, publish, distribute, sublicense, and/or sell
  # copies of the Software, and to permit persons to whom the Software is
  # furnished to do so, subject to the following conditions:
  # The above copyright notice and this permission notice shall be included in
  # all copies or substantial portions of the Software.
 # THE SOFTWARE IS PROVIDED "AS IS", WITHOUT WARRANTY OF ANY KIND, EXPRESS OR
  # IMPLIED, INCLUDING BUT NOT LIMITED TO THE WARRANTIES OF MERCHANTABILITY,
  # FITNESS FOR A PARTICULAR PURPOSE AND NONINFRINGEMENT. IN NO EVENT SHALL THE
  # AUTHORS OR COPYRIGHT HOLDERS BE LIABLE FOR ANY CLAIM, DAMAGES OR OTHER
  # LIABILITY, WHETHER IN AN ACTION OF CONTRACT, TORT OR OTHERWISE, ARISING FROM,
  # OUT OF OR IN CONNECTION WITH THE SOFTWARE OR THE USE OR OTHER DEALINGS IN
  # THE SOFTWARE.
```

This code is used in chunks 4 and 9.

But remember that Dershowitz and Reingold have Copyrighted their algorithms!

```
8 \langle copyright \ Dershowitz \ and \ Reingold \ 8 \rangle \equiv
```

- # PLEASE READ THE COPYRIGHT IN THE FILE THAT INSPIRED THIS WORK
- # see lines 6-80 in calendrica-3.0.cl

Root chunk (not used in this document).

 $\langle testa | 9 \rangle \equiv$ """Python implementation of Dershowitz and Reingold 'Calendrica Calculations'.

Python implementation of calendrical algorithms as described in Common Lisp in calendrical-3.0.cl (and errata as made available by the authors.) The companion book is Dershowitz and Reingold 'Calendrica Calculations', 3rd Ed., 2008, Cambridge University Press.

License: MIT License for my work, but read the one for calendrica-3.0.cl which inspired this work.

Author: Enrico Spinielli """ $\langle LICENSE~7 \rangle \\ \#~ \langle generated~code~warning~1 \rangle$

This code is used in chunk 3.

The following is where I control the project version number in a centralised way. The version is number is composed of 3 integers separated by a dot, "which stand for

@<major version>.<minor version>.<increment>

Then version number 0.9.2 means revision 2 of project version 0.9.

10 $\langle project \ version \ 10 \rangle \equiv$ 1.0.0

This code is used in chunk 213.

Chapter 2

The Calendars

2.1 Scaffolding

HE accuracy of the algorithms presented require definition of constants and calculations that span many bits. I enable true division feature as in PEP 238 [14] in order to smoothly express simple constants as defined in the COMMON LISP code, i.e. 1/360

```
11 ⟨global import statements 11⟩≡
# use true division
from __future__ import division
```

This definition is continued in chunk 12. This code is used in chunk 3.

In order to insure the same precision of computations as in COMMON LISP code where numbers are postfixed with LO, meaning 50-bit precision, I use the mpmath library [5] and set the precision accordingly floating-point arithmetic.

This code is used in chunk 3.

2.2 Basics

The following are general definitions, algorithms and helper functions that will be used to perform a lot of the various calculations for the subsequent calendars.

2.2.1 Implementation

Some computations have meaningless results in certain circumstances, they will return a predefined value, BOGUS, to mark this case.

Some COMMON LISP functions are available under other names and/or in additional packages in Python or with a different semantic, so they are aliased or loaded or (re)defined accordingly. This is the case for quotient, floor and round, the COMMON LISP versions return integers while in Python they can return a float if (at least) one of the arguments is a float.

```
\langle \mathit{basic\ code\ 13} \rangle + \equiv
14
         # see lines 249-252 in calendrica-3.0.cl
         # m // n
         # The following
                 from operator import floordiv as quotient
         # is not ok, the corresponding CL code
         # uses CL 'floor' which always returns an integer
         # (the floating point equivalent is 'ffloor'), while
         # 'quotient' from operator module (or corresponding //)
         # can return a float if at least one of the operands
         # is a float...so I redefine it (and 'floor' and 'round' as well: in CL
         # they always return an integer.)
         def quotient(m, n):
             """Return the whole part of m/n towards negative infinity."""
             return ifloor(m / n)
      This code is used in chunk 3.
       Defines:
         quotient, used in chunks 55, 56, 59, 65, 68, 71, 74, 77, 80, 83, 86, 89, 122, 125, 130, 133, 136,
           and 142.
       Uses ifloor 15.
```

For floor and round I decided to make it explicit the fact that they return an integer and named them with a prefixed i (for integer):

```
15
              \langle basic\ code\ 13 \rangle + \equiv
                  # I (re)define floor: in CL it always returns an integer.
                  # I make it explicit the fact it returns an integer by
                  # naming it ifloor
                  def ifloor(n):
                            """Return the whole part of m/n."""
                           from math import floor
                           return int(floor(n))
                  # I (re)define round: in CL it always returns an integer.
                  # I make it explicit the fact it returns an integer by
                  # naming it iround
                  def iround(n):
                           """Return the whole part of m/n."""
                           from __builtin__ import round
                           return int(round(n))
                  # m % n (this works as described in book for negative integres)
                  # It is interesting to note that
                             mod(1.5, 1)
                  # returns the decimal part of 1.5, so 0.5; given a moment 'm'
                             mod(m, 1)
                  # returns the time of the day
                  from operator import mod
                  # see lines 254-257 in calendrica-3.0.cl
                  def amod(x, y):
                           """Return the same as a \% b with b instead of 0."""
                           return y + (mod(x, -y))
              This code is used in chunk 3.
              Defines:
                  amod, used in chunks 56, 61, 68, 83, 86, 89, 133, 136, and 139.
                  \textbf{ifloor}, \ used \ in \ chunks \ 14, \ 40, \ 46, \ 48, \ 86, \ 107, \ 122, \ 125, \ 130, \ 133, \ 136, \ 139, \ and \ 142.
                  iround, used in chunks 106, 119, 122, 125, 130, 133, 136, and 142.
                   \bmod, \ used \ in \ chunks \ 28, \ 38, \ 40, \ 46, \ 54, \ 55, \ 59, \ 65, \ 71, \ 74, \ 77, \ 80, \ 83, \ 86, \ 89, \ 100, \ 102, \ 105, \ 107, \ 109, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 100, \ 10
                       119, 120, 122, 125, 130, 133, 136, 139, 142, 196, and 252.
              The following definitions are a translation in Python of Common LISP macrosMacro.
              Macro definition is a very powerful tool but it does not exist in the PYTHON language.
                     The principles of the algorithms described in [1] is to quickly get an approximation
              and then refine it to get the correct result. next and final are used in the refine phase.
16
              \langle basic\ code\ 13\rangle + \equiv
                  # see lines 259-264 in calendrica-3.0.cl
                  def next(i, p):
                            """Return first integer greater or equal to initial index, i,
                           such that condition, p, holds."""
                           return i if p(i) else next(i + 1, p)
              This code is used in chunk 3.
                  next, used in chunks 18, 80, 119, 122, 125, 130, 133, 136, 142, 194, 203, and 210.
```

```
\langle basic\ code\ tests\ 17 \rangle \equiv
17
           \langle test \ next \ 18 \rangle
        This definition is continued in chunks 20, 23, 26, 29, 32, 35, 41, and 44.
        This code is used in chunk 50.
        \langle test \ next \ 18 \rangle \equiv
           def testNext(self):
                self.assertEqual(next(0, lambda i: i == 3), 3)
                self.assertEqual(next(0, lambda i: i == 0), 0)
        This code is used in chunk 17.
        Uses next 16.
        \langle basic\ code\ 13\rangle + \equiv
19
           # see lines 266-271 in calendrica-3.0.cl
           def final(i, p):
                """Return last integer greater or equal to initial index, i,
                such that condition, p, holds."""
                return i - 1 if not p(i) else final(i + 1, p)
        This code is used in chunk 3.
           final, used in chunks 21, 80, 119, and 139.
        \langle basic\ code\ tests\ 17 \rangle + \equiv
20
           \langle test \ final \ 21 \rangle
        This code is used in chunk 50.
21
        \langle test \ final \ 21 \rangle \equiv
           def testFinal(self):
                self.assertEqual(final(0, lambda i: i == 3), -1)
                {\tt self.assertEqual(final(0, lambda i: i < 3), 2)}
                self.assertEqual(final(0, lambda i: i < 0), -1)
        This code is used in chunk 20.
        Defines:
           testFinal, never used.
        Uses final 19.
```

The following functions are used mainly in the astronomical algorithms in order to evaluate polynomial approximations of equations of motion.

```
22
       \langle basic\ code\ 13 \rangle + \equiv
         # see lines 273-281 in calendrica-3.0.cl
         def summa(f, k, p):
              """Return the sum of f(i) from i=k, k+1, ... till p(i) holds true or 0.
              This is a tail recursive implementation."""
              return 0 if not p(k) else f(k) + summa(f, k + 1, p)
         def altsumma(f, k, p):
              """Return the sum of f(i) from i=k, k+1, ... till p(i) holds true or 0.
              This is an implementation of the Summation formula from Kahan,
              see Theorem 8 in Goldberg, David 'What Every Computer Scientist
              Should Know About Floating-Point Arithmetic', ACM Computer Survey,
              Vol. 23, No. 1, March 1991."""
              if not p(k):
                  return 0
              else:
                  S = f(k)
                  C = 0
                  j = k + 1
                  while p(j):
                       Y = f(j) - C
                       T = S + Y
                       C = (T - S) - Y
                       S = T
                       j += 1
              return S
       This code is used in chunk 3.
       Defines:
         altsumma, used in chunk 24.
         summa, used in chunks 24 and 80.
23
       \langle basic\ code\ tests\ 17 \rangle + \equiv
         \langle test \ summa \ 24 \rangle
       This code is used in chunk 50.
       \langle \mathit{test summa 24} \rangle \equiv
24
         def testSumma(self):
              self.assertEqual(summa(lambda x: 1, 1, lambda i: i<=4), 4)</pre>
              self.assertEqual(summa(lambda x: 1, 0, lambda i: i>=4), 0)
              self.assertEqual(summa(lambda x: x**2, 1, lambda i: i<=4), 30)</pre>
         def testAltSumma(self):
              # I should add more tests with floating point arithmetic...
              self.assertEqual(altsumma(lambda x: 1.0, 1, lambda i: i<=4), 4)</pre>
              self.assertEqual(altsumma(lambda x: 1.0, 0, lambda i: i>=4), 0)
              self.assertEqual(altsumma(lambda x: x**2, 1, lambda i: i<=4), 30)</pre>
       This code is used in chunk 23.
       Defines:
         testAltSumma, never used.
         testSumma, never used.
       Uses altsumma 22 and summa 22.
```

binary_search is looking for a value of a function within an interval given a precision criteria to satify.

```
\langle basic\ code\ 13 \rangle + \equiv
25
         # see lines 283-293 in calendrica-3.0.cl
         def binary_search(lo, hi, p, e):
              """Bisection search for x in [lo, hi] such that condition 'e' holds.
              {\tt p} determines when to go left."""
              x = (lo + hi) / 2
              if p(lo, hi):
                  return x
              elif e(x):
                  return binary_search(lo, x, p, e)
              else:
                  return binary_search(x, hi, p, e)
       This code is used in chunk 3.
       Defines:
         binary_search, used in chunks 27, 28, 102, and 136.
26
       \langle basic\ code\ tests\ 17 \rangle + \equiv
         ⟨test binary search 27⟩
       This code is used in chunk 50.
27
       \langle test\ binary\ search\ 27 \rangle \equiv
         def testBinarySearch(self):
              fminusy = lambda x, y: fx(x) - y
              p = lambda a, b: abs(fminusy(0.5 * (a+b), y)) <= 10**-5
              e = lambda x: fminusy(x, y) >= 0
              # function y = f(x), f(x) = x, y0 = 1.0; solution is x0 = 1.0
              fx = lambda x: x
              y = 1.0
              x0 = 1.0
              self.assertTrue(binary_search(0.0, 3.1, p, e) - x0 <= 10 ** -5)
              # new function y = f(x), f(x) = x**2 - 4*x + 4, y0 = 0.0; solution x0=2.0
              y = 0.0
             x0 = 2.0
             fx = lambda x: x**2 -4 * x + 4.0
              self.assertTrue(binary_search(1.5, 2.5, p, e) - x0 <= 10 ** -5)
       This code is used in chunk 26.
         testBinarySearch, never used.
       Uses binary_search 25.
```

```
\langle \mathit{basic\ code\ 13} \rangle + \equiv
28
           # see lines 295-302 in calendrica-3.0.cl
           def invert_angular(f, y, a, b, prec=10 ** -5):
                """Find inverse of angular function 'f' at 'y' within interval [a,b].
                Default precision is 0.00001"""
                return binary_search(a, b,
                                             (lambda l, h: ((h - l) \le prec)),
                                             (lambda x: mod((f(x) - y), 360) < 180))
           #def invert_angular(f, y, a, b):
                    from scipy.optimize import brentq
                  \texttt{return}(\texttt{brentq}((\texttt{lambda} \ \texttt{x} \colon \ \texttt{mod}(\texttt{f}(\texttt{x}) \ \texttt{-} \ \texttt{y}) \,, \ \texttt{360})) \,, \ \texttt{a, b, xtol=error})
        This code is used in chunk 3.
        Defines:
           invert_angular, used in chunks 30, 109, 119, and 136.
        Uses binary_search 25, interval 47, and mod 15.
29
        \langle basic\ code\ tests\ 17 \rangle + \equiv
           \langle test\ invert\ angular\ 30 \rangle
        This code is used in chunk 50.
30
        \langle test \ invert \ angular \ 30 \rangle \equiv
           def testInvertAngular(self):
                from math import tan, radians
                # find angle theta such that tan(theta) = 1
                # assert that theta - pi/4 \le 10**-5
                self.assertTrue(invert_angular(tan,
                                                      1.0,
                                                      radians(60.0)) - radians(45.0) <= 10**-5)
        This code is used in chunk 29.
        Defines:
           {\tt testInvertAngular}, \ {\rm never} \ {\rm used}.
        Uses angle 100 and invert_angular 28 28.
```

sigma is used expecially for astronomical formulas in order to go thru tables of value, see 2.14. This implementation is really horrible...but I will not touch it untill I will have time and courage to go thru understanding it again!

```
\langle basic\ code\ 13 \rangle + \equiv
31
         # see lines 304-313 in calendrica-3.0.cl
         def sigma(1, b):
              """Return the sum of body 'b' for indices i1..in
              running simultaneously thru lists 11..ln.
              List 'l' is of the form [[i1 l1]..[in ln]]"""
              # 'l' is a list of 'n' lists of the same lenght 'L' [11, 12, 13, ...]
              # 'b' is a lambda with 'n' args
              # 'sigma' sums all 'L' applications of 'b' to the relevant tuple of args
              # \gg a = [1, 2, 3, 4]
              # \gg b = [5, 6, 7, 8]
              # \gg c = [ 9,10,11,12]
              # >> 1 = [a,b,c]
              \# \gg z = zip(*1)
              # »> z
              # [(1, 5, 9), (2, 6, 10), (3, 7, 11), (4, 8, 12)]
              \# \gg b = lambda x, y, z: x * y * z
              # \gg b(*z[0]) # apply b to first elem of i
              # 45
              # >> temp = []
              \# \gg z = zip(*1)
              # >> for e in z: temp.append(b(*e))
              # >> temp
              # [45, 120, 231, 384]
              # >> from operator import add
              # >> reduce(add, temp)
              # 780
              return sum(b(*e) for e in zip(*l))
       This code is used in chunk 3.
       Defines:
         sigma, used in chunks 33, 107, 119, and 120.
32
       \langle basic\ code\ tests\ 17 \rangle + \equiv
         \langle test \ sigma \ 33 \rangle
       This code is used in chunk 50.
33
       \langle test \ sigma \ 33 \rangle \equiv
         def testSigma(self):
              a = [1, 2, 3, 4]
              b = [5, 6, 7, 8]
              c = [9,10,11,12]
              ell = [a,b,c]
              bi = lambda x, y, z: x * y * z
              self.assertEqual(sigma(ell, bi), 780)
       This code is used in chunk 32.
       Defines:
         testSigma, never used.
       Uses sigma 31.
```

```
34
       \langle basic\ code\ 13 \rangle + \equiv
          # see lines 315-321 in calendrica-3.0.cl
          from copy import copy
          def poly(x, a):
               """Calculate polynomial with coefficients 'a' at point x.
              The polynomial is a[0] + a[1] * x + a[2] * x^2 + ...a[n-1]x^(n-1)
              the result is
              a[0] + x(a[1] + x(a[2] + ... + x(a[n-1])...)"""
              # This implementation is also known as Horner's Rule.
              n = len(a) - 1
              p = a[n]
              for i in range(1, n+1):
                   p = p * x + a[n-i]
              return p
       This code is used in chunk 3.
       Defines:
          poly, used in chunks 36, 101, 102, 107, 109, 111, 113, 115, 117, 119, and 120.
35
       \langle basic\ code\ tests\ 17 \rangle + \equiv
          \langle test \ poly \ 36 \rangle
       This code is used in chunk 50.
36
       \langle test \ poly \ 36 \rangle \equiv
          def testPoly(self):
              self.assertEqual(poly(0, [2, 2, 1]), 2)
              self.assertEqual(poly(1, [2, 2, 1]), 5)
       This code is used in chunk 35.
       Defines:
          testPoly, never used.
       Uses poly 34.
           Now it is time to begin with calendars: let's define the instant in time when time is
       counted from:
       \langle basic\ code\ 13 \rangle + \equiv
37
          # see lines 323-329 in calendrica-3.0.cl
          # Epoch definition. I took it out explicitly from rd().
               """Epoch definition. For Rata Diem, R.D., it is 0 (but any other reference
              would do.)"""
              return 0
          def rd(tee):
               """Return rata diem (number of days since epoch) of moment in time, tee."""
              return tee - epoch()
       This code is used in chunk 3.
       Defines:
          epoch, used in chunks 80 and 86.
          rd, used in chunks 38, 48, 52, 65, 68, 84, 104, 133, 149, 151, 153, 155, 157, 158, 160, 161, 164, 165,
            167, 169, 171, 173, 174, 176, 178, 180, 182, 184, 185, 187, 189, 191, 193, 194, 196, and 253.
```

And here are some other basilar (and arbitrary) definitions: days of the week, date and time data structures.

The days of the week constants are defined as constants from 1 to 7, where Sunday is (arbitrarily) assigned 0.

```
\langle \mathit{basic\ code\ 13} \rangle + \equiv
38
         # see lines 331-334 in calendrica-3.0.cl
         SUNDAY = 0
         # see lines 10-15 in calendrica-3.0.errata.cl
         # see lines 17-20 in calendrica-3.0.errata.cl
         TUESDAY = 2
         # see lines 22-25 in calendrica-3.0.errata.cl
         WEDNESDAY = 3
         # see lines 27-30 in calendrica-3.0.errata.cl
         THURSDAY = 4
         # see lines 32-35 in calendrica-3.0.errata.cl
         FRIDAY = 5
         # see lines 37-40 in calendrica-3.0.errata.cl
         SATURDAY = SUNDAY + 6
         DAYS_OF_WEEK_NAMES = {
              SUNDAY
                        : "Sunday",
              MONDAY
                         : "Monday",
              TUESDAY
                        : "Tuesday",
              WEDNESDAY : "Wednesday",
              THURSDAY : "Thursday",
              FRIDAY
                         : "Friday",
              SATURDAY : "Saturday"}
         # see lines 366-369 in calendrica-3.0.cl
         def day_of_week_from_fixed(date):
              """Return day of the week from a fixed date 'date'."""
              return mod(date - rd(0) - SUNDAY, 7)
       This code is used in chunk 3.
       Defines:
         day_of_week_from_fixed, used in chunks 56, 68, 80, and 151.
         FRIDAY, used in chunks 56, 80, and 149.
         MONDAY, used in chunks 56, 80, 81, and 149.
         SATURDAY, used in chunks 80, 81, and 149.
         SUNDAY, used in chunks 56, 68, 74, 80, 142, and 149.
         THURSDAY, used in chunks 68, 80, 81, and 149.
         TUESDAY, used in chunks 56, 80, 81, and 149.
         WEDNESDAY, used in chunks 80, 81, 136, and 149.
       Uses mod 15 and rd 37.
```

```
39
       \langle basic\ code\ 13 \rangle + \equiv
          # see lines 371-374 in calendrica-3.0.cl
          def standard_month(date):
              """Return the month of date 'date'."""
              return date[1]
          # see lines 376-379 in calendrica-3.0.cl
          def standard_day(date):
               """Return the day of date 'date'."""
              return date[2]
          # see lines 381-384 in calendrica-3.0.cl
          def standard_year(date):
              """Return the year of date 'date'."""
              return date[0]
          # see lines 386-388 in calendrica-3.0.cl
          def time_of_day(hour, minute, second):
               """Return the time of day data structure."""
              return [hour, minute, second]
          # see lines 390-392 in calendrica-3.0.cl
          def hour(clock):
               """Return the hour of clock time 'clock'."""
              return clock[0]
          # see lines 394-396 in calendrica-3.0.cl
          def minute(clock):
               """Return the minutes of clock time 'clock'."""
              return clock[1]
          # see lines 398-400 in calendrica-3.0.cl
          def seconds(clock):
               """Return the seconds of clock time 'clock'."""
              return clock[2]
       This code is used in chunk 3.
       Defines:
          hour, used in chunks 40, 42, 43, 96, 98, and 105-107.
          minute, used in chunks 40, 42, 43, 106, and 136.
          seconds, used in chunks 42, 43, 46, 100, and 106.
          standard_day, used in chunks 55, 56, 59, 61, 65, 71, 77, 80, 86, 122, 130, 136, and 142.
          \mathtt{standard\_month}, \, used \, \, in \, \, chunks \, \, 55, \, \, 56, \, \, 59, \, \, 61, \, \, 65, \, \, 71, \, \, 77, \, \, 80, \, \, 86, \, \, 122, \, \, 130, \, \, 136, \, \, and \, \, 142.
          standard_year, used in chunks 55, 56, 59, 61, 63, 65, 71, 77, 80, 86, 122, 130, 136, 142, and 155.
          time_of_day, used in chunk 40.
```

The following functions convert from moment to fixed date, extract the time of the day from a moment.

```
\langle basic\ code\ 13 \rangle + \equiv
          # see lines 402-405 in calendrica-3.0.cl
          def fixed_from_moment(tee):
              """Return fixed date from moment 'tee'."""
              return ifloor(tee)
          # see lines 407-410 in calendrica-3.0.cl
          def time_from_moment(tee):
              """Return time from moment 'tee'."""
              return mod(tee, 1)
          # see lines 412-419 in calendrica-3.0.cl
          def clock_from_moment(tee):
              """Return clock time hour:minute:second from moment 'tee'."""
              time = time_from_moment(tee)
              hour = ifloor(time * 24)
              minute = ifloor(mod(time * 24 * 60, 60))
              second = mod(time * 24 * 60 * 60, 60)
              return time_of_day(hour, minute, second)
       This code is used in chunk 3.
       Defines:
          {\tt clock\_from\_moment}, \ {\tt used} \ {\tt in} \ {\tt chunks} \ {\tt 42} \ {\tt and} \ {\tt 106}.
          fixed_from_moment, used in chunks 102, 105, and 136.
          time_from_moment, used in chunk 102.
       Uses hour 39, ifloor 15, minute 39, mod 15, and time_of_day 39.
41
       \langle basic\ code\ tests\ 17 \rangle + \equiv
          ⟨test clock from moment 42⟩
       This code is used in chunk 50.
42
       \langle test \ clock \ from \ moment \ 42 \rangle \equiv
          def testClockFromMoment(self):
              c = clock_from_moment(3.5)
              self.assertEqual(hour(c), 12)
              self.assertEqual(minute(c), 0)
              self.assertAlmostEqual(seconds(c), 0, 2)
              c = clock_from_moment(3.75)
              self.assertEqual(hour(c), 18)
              self.assertEqual(minute(c), 0)
              self.assertAlmostEqual(seconds(c), 0, 2)
              c = clock_from_moment(3.8)
              self.assertEqual(hour(c), 19)
              self.assertEqual(minute(c), 11)
              self.assertAlmostEqual(seconds(c), 59.9999, 2)
       This code is used in chunk 41.
       Defines:
          testClockFromMoment, never used.
       Uses clock_from_moment 40, hour 39, minute 39, and seconds 39.
```

```
43
        \langle basic\ code\ 13 \rangle + \equiv
          # see lines 421-427 in calendrica-3.0.cl
          def time_from_clock(hms):
               """Return time of day from clock time 'hms'."""
               h = hour(hms)
               m = minute(hms)
               s = seconds(hms)
               return(1/24 * (h + ((m + (s / 60)) / 60)))
        This code is used in chunk 3.
        Defines:
          {\tt time\_from\_clock}, \, {\tt used} \, \, {\tt in} \, \, {\tt chunks} \, \, {\tt 45} \, \, {\tt and} \, \, {\tt 106}.
        Uses hour 39, minute 39, and seconds 39.
44
        \langle basic\ code\ tests\ 17 \rangle + \equiv
          ⟨test time from clock 45⟩
       This code is used in chunk 50.
45
        \langle test \ time \ from \ clock \ 45 \rangle \equiv
          def testTimeFromClock(self):
               self.assertAlmostEqual(time_from_clock([12, 0, 0]), 0.5, 2)
               self.assertAlmostEqual(time_from_clock([18, 0, 0]), 0.75, 2)
               self.assertAlmostEqual(time_from_clock([19, 12, 0]), 0.8, 2)
       This code is used in chunk 44.
        Defines:
          {\tt testTimeFromClock}, \ {\rm never} \ {\rm used}.
        Uses time_from_clock 43.
        Here we define the angular data structure and relative helper functions.
46
        \langle basic\ code\ 13 \rangle + \equiv
          # see lines 429-431 in calendrica-3.0.cl
          def degrees_minutes_seconds(d, m, s):
               """Return the angular data structure."""
               return [d, m, s]
          # see lines 433-440 in calendrica-3.0.cl
          def angle_from_degrees(alpha):
               """Return an angle in degrees:minutes:seconds from angle,
               'alpha' in degrees."""
               d = ifloor(alpha)
               m = ifloor(60 * mod(alpha, 1))
               s = mod(alpha * 60 * 60, 60)
               return degrees_minutes_seconds(d, m, s)
        This code is used in chunk 3.
       Defines:
          angle_from_degrees, never used.
          degrees_minutes_seconds, never used.
        Uses angle 100, ifloor 15, mod 15, and seconds 39.
```

These helper functions are used to deal with intervals and ranges of events:

```
47
       \langle basic\ code\ 13 \rangle + \equiv
          # see lines 502-510 in calendrica-3.0.cl
          def list_range(ell, range):
               """Return those moments in list ell that occur in range 'range'."""
              return filter(lambda x: is_in_range(x, range), ell)
          # see lines 482-485 in calendrica-3.0.cl
          def interval(t0, t1):
               """Return the range data structure."""
              return [t0, t1]
          # see lines 487-490 in calendrica-3.0.cl
          def start(range):
              """Return the start of range 'range'."""
              return range[0]
          # see lines 492-495 in calendrica-3.0.cl
          def end(range):
              """Return the end of range 'range'."""
              return range[1]
          # see lines 497-500 in calendrica-3.0.cl
          def is_in_range(tee, range):
              """Return True if moment 'tee' falls within range 'range',
              False otherwise."""
              return start(range) <= tee <= end(range)</pre>
       This code is used in chunk 3.
       Defines:
          end, used in chunks 56, 89, 105, 128, 133, and 136.
          interval, used in chunks 28, 56, 89, and 136.
          is_in_range, used in chunks 56 and 136.
          \verb|list_range|, used in chunks 63, 71, 77, 80, 136, and 139.
          \mathtt{start}, \ \mathrm{used} \ \mathrm{in} \ \mathrm{chunks} \ 56, \, 80, \, 89, \, 105, \, 125, \, 128, \, 133, \, 136, \, 142, \, \mathrm{and} \ 196.
```

```
Julian days are of basic importance expecially in Astronomy.
       \langle basic\ code\ 13 \rangle + \equiv
48
         # see lines 442-445 in calendrica-3.0.cl
         JD_EPOCH = rd(mpf(-1721424.5))
         # see lines 447-450 in calendrica-3.0.cl
         def moment_from_jd(jd):
              """Return the moment corresponding to the Julian day number 'jd'."""
              return jd + JD_EPOCH
         # see lines 452-455 in calendrica-3.0.cl
         def jd_from_moment(tee):
              """Return the Julian day number corresponding to moment 'tee'."""
              return tee - JD_EPOCH
         # see lines 457-460 in calendrica-3.0.cl
         def fixed_from_jd(jd):
              """Return the fixed date corresponding to Julian day number 'jd'."""
              return ifloor(moment_from_jd(jd))
         # see lines 462-465 in calendrica-3.0.cl
         def jd_from_fixed(date):
              """Return the Julian day number corresponding to fixed date 'rd'."""
              return jd_from_moment(date)
         # see lines 467-470 in calendrica-3.0.cl
         MJD EPOCH = rd(678576)
         # see lines 472-475 in calendrica-3.0.cl
         def fixed_from_mjd(mjd):
              """Return the fixed date corresponding to modified Julian day 'mjd'."""
              return mjd + MJD_EPOCH
         # see lines 477-480 in calendrica-3.0.cl
         def mjd_from_fixed(date):
              """Return the modified Julian day corresponding to fixed date 'rd'."""
              return date - MJD_EPOCH
       This code is used in chunk 3.
       Defines:
         fixed_from_jd, used in chunks 65, 83, 89, and 153.
         fixed_from_mjd, used in chunk 153.
         JD_EPOCH, never used.
         jd_from_fixed, used in chunk 153.
         jd_from_moment, never used.
         MJD_EPOCH, never used.
         mjd_from_fixed, used in chunk 153.
         moment_from_jd, never used.
       Uses ifloor 15 and rd 37.
       2.2.2
                 Unit tests
       The relevant tests are available to be run in isolation in basicCodeUnitTest.py
       \langle basicCodeUnitTest.py 49 \rangle \equiv
49
         # \langle generated \ code \ warning \ 1 \rangle
         ⟨import for testing 6⟩
         from appendixCUnitTest import AppendixCTable1TestCaseBase
         \langle basic\ code\ unit\ test\ 50 \rangle
         \langle execute \ tests \ 5 \rangle
       Root chunk (not used in this document).
       Uses AppendixCTable1TestCaseBase 149.
```

```
and grouped together so that they can be included in pycalcaltests.py  \langle basic\ code\ unit\ test\ 50 \rangle \equiv \\  \quad \text{class BasicCodeTestCase(unittest.TestCase):} \\  \quad \langle basic\ code\ tests\ 17 \rangle  This definition is continued in chunk 150. This code is used in chunks 4 and 49.
```

2.3 Gregorian Calendar

```
\langle gregorian \ calendar \ 51 \rangle \equiv
51
          # gregorian calendar algorithms #
          \langle gregorian \ date \ and \ epoch \ 52 \rangle
          \langle gregorian \ months \ 53 \rangle
          \langle gregorian \ leap \ year \ function \ 54 \rangle
          ⟨gregorian conversion functions 55⟩
          (gregorian year start and end 56)
       This code is used in chunk 3.
52
       \langle gregorian \ date \ and \ epoch \ 52 \rangle \equiv
          # see lines 586-589 in calendrica-3.0.cl
          def gregorian_date(year, month, day):
               """Return a Gregorian date data structure."""
              return [year, month, day]
          # see lines 591-595 in calendrica-3.0.cl
          GREGORIAN_EPOCH = rd(1)
       This code is used in chunk 51.
       Defines:
          gregorian_date, used in chunks 56, 57, 59, 68, 74, 102, 106-108, 125, 128, 129, 133, 139, 149, 174,
          GREGORIAN_EPOCH, used in chunks 55, 56, and 74.
       Uses rd 37.
```

```
53
       \langle gregorian \ months \ 53 \rangle \equiv
         # see lines 597-600 in calendrica-3.0.cl
         JANUARY = 1
         # see lines 602-605 in calendrica-3.0.cl
         FEBRUARY = 2
         # see lines 607-610 in calendrica-3.0.cl
         MARCH = 3
         # see lines 612-615 in calendrica-3.0.cl
         APRIL = 4
         # see lines 617-620 in calendrica-3.0.cl
         MAY = 5
         # see lines 622-625 in calendrica-3.0.cl
         JUNE = 6
         # see lines 627-630 in calendrica-3.0.cl
         JULY = 7
         # see lines 632-635 in calendrica-3.0.cl
         AUGUST = 8
         # see lines 637-640 in calendrica-3.0.cl
         SEPTEMBER = 9
         # see lines 642-645 in calendrica-3.0.cl
         OCTOBER = 10
         # see lines 647-650 in calendrica-3.0.cl
         NOVEMBER = 11
         # see lines 652-655 in calendrica-3.0.cl
         DECEMBER = 12
       This code is used in chunk 51.
       Defines:
         APRIL, used in chunks 74, 108, and 133.
         AUGUST, used in chunks 71, 83, and 133.
         DECEMBER, used in chunks 56, 59, 63, 68, and 139.
         FEBRUARY, used in chunks 61, 86, 106, and 133.
         {\tt JANUARY, used in \ chunks\ 56,\ 57,\ 59,\ 102,\ 107,\ and\ 133}.
         JULY, used in chunks 56, 61, 77, 107, and 133.
         JUNE, never used.
         MARCH, used in chunks 56, 57, 59, 61, 122, 125, and 133.
         MAY, used in chunks 56 and 61.
         NOVEMBER, used in chunks 56, 57, 60, and 62.
         OCTOBER, used in chunks 60, 61, 80, and 129.
         SEPTEMBER, used in chunks 56 and 128.
       \langle gregorian\ leap\ year\ function\ 54 \rangle \equiv
54
         # see lines 657-663 in calendrica-3.0.cl
         def is_gregorian_leap_year(g_year):
              """Return True if Gregorian year 'g_year' is leap."""
              return (mod(g_year, 4) == 0) and (mod(g_year, 400)) not in [100, 200, 300])
       This code is used in chunk 51.
       Defines:
         is_gregorian_leap_year, used in chunks 55-57 and 125.
       Uses mod 15.
```

```
55
       \langle gregorian\ conversion\ functions\ 55 \rangle \equiv
         # see lines 665-687 in calendrica-3.0.cl
         def fixed_from_gregorian(g_date):
             """Return the fixed date equivalent to the Gregorian date 'g_date'."""
             month = standard_month(g_date)
             day = standard_day(g_date)
             year = standard_year(g_date)
             return ((GREGORIAN_EPOCH - 1) +
                      (365 * (year -1)) +
                     quotient(year - 1, 4) -
                      quotient(year - 1, 100) +
                      quotient(year - 1, 400) +
                      quotient((367 * month) - 362, 12) +
                      (0 if month <= 2
                       else (-1 if is_gregorian_leap_year(year) else -2)) +
                     day)
         # see lines 689-715 in calendrica-3.0.cl
         def gregorian_year_from_fixed(date):
             """Return the Gregorian year corresponding to the fixed date 'date'."""
                 = date - GREGORIAN_EPOCH
             n400 = quotient(d0, 146097)
             d1 = mod(d0, 146097)
             n100 = quotient(d1, 36524)
             d2 = mod(d1, 36524)
             n4
                 = quotient(d2, 1461)
             d3 = mod(d2, 1461)
             n1 = quotient(d3, 365)
             year = (400 * n400) + (100 * n100) + (4 * n4) + n1
             return year if (n100 == 4) or (n1 == 4) else (year + 1)
      This code is used in chunk 51.
       Defines:
         fixed_from_gregorian, used in chunks 56, 57, 59, 74, 102, 106, 108, 125, 128, 129, 133, 139, 155,
         gregorian_year_from_fixed, used in chunks 56, 68, 80, 107, 122, 125, 133, 142, 155, and 178.
       Uses GREGORIAN_EPOCH 52, is_gregorian_leap_year 54, mod 15, quotient 14 14, standard_day 39,
         standard_month 39, and standard_year 39.
```

```
56
      \langle gregorian \ year \ start \ and \ end \ 56 \rangle \equiv
        # see lines 717-721 in calendrica-3.0.cl
        def gregorian_new_year(g_year):
             """Return the fixed date of January 1 in Gregorian year 'g_year'."""
            return fixed_from_gregorian(gregorian_date(g_year, JANUARY, 1))
        # see lines 723-727 in calendrica-3.0.cl
        def gregorian_year_end(g_year):
             """Return the fixed date of December 31 in Gregorian year 'g_year'."""
            return fixed_from_gregorian(gregorian_date(g_year, DECEMBER, 31))
        # see lines 729-733 in calendrica-3.0.cl
        def gregorian_year_range(g_year):
            """Return the range of fixed dates in Gregorian year 'g_year'."""
            return interval(gregorian_new_year(g_year), gregorian_year_end(g_year))
        # see lines 735-756 in calendrica-3.0.cl
        def gregorian_from_fixed(date):
             """Return the Gregorian date corresponding to fixed date 'date'."""
            year = gregorian_year_from_fixed(date)
            prior_days = date - gregorian_new_year(year)
            correction = (0
                           if (date < fixed_from_gregorian(gregorian_date(year,</pre>
                                                                           1)))
                           else (1 if is_gregorian_leap_year(year) else 2))
            month = quotient((12 * (prior_days + correction)) + 373, 367)
            day = 1 + (date - fixed_from_gregorian(gregorian_date(year, month, 1)))
            return gregorian_date(year, month, day)
        # see lines 758-763 in calendrica-3.0.cl
        def gregorian_date_difference(g_date1, g_date2):
             """Return the number of days from Gregorian date 'g_date1'
            till Gregorian date 'g_date2'."""
            return fixed_from_gregorian(g_date2) - fixed_from_gregorian(g_date1)
        # see lines 42-49 in calendrica-3.0.errata.cl
        def day_number(g_date):
            """Return the day number in the year of Gregorian date 'g_date'."""
            return gregorian_date_difference(
                 gregorian_date(standard_year(g_date) - 1, DECEMBER, 31),
                 g_date)
        # see lines 53-58 in calendrica-3.0.cl
        def days_remaining(g_date):
            """Return the days remaining in the year after Gregorian date 'g_date'."""
            return gregorian_date_difference(
                 g_date,
                 gregorian_date(standard_year(g_date), DECEMBER, 31))
        # see lines 779-801 in calendrica-3.0.cl
        def alt_fixed_from_gregorian(g_date):
            """Return the fixed date equivalent to the Gregorian date 'g_date'.
            Alternative calculation."""
            month = standard_month(g_date)
            day = standard_day(g_date)
            year = standard_year(g_date)
                  = amod(month - 2, 12)
                  = year + quotient(month + 9, 12)
            return ((GREGORIAN_EPOCH - 1) +
                     -306
```

```
365 * (y - 1)
            quotient(y - 1, 4)
            -quotient(y - 1, 100) +
           quotient(y - 1, 400) +
            quotient(3 * m - 1, 5) +
            30 * (m - 1)
           day)
# see lines 803-825 in calendrica-3.0.cl
def alt_gregorian_from_fixed(date):
    """Return the Gregorian date corresponding to fixed date 'date'.
   Alternative calculation."""
   y = gregorian_year_from_fixed(GREGORIAN_EPOCH - 1 + date + 306)
   prior_days = date - fixed_from_gregorian(gregorian_date(y - 1, MARCH, 1))
   month = amod(quotient(5 * prior_days + 2, 153) + 3, 12)
   year = y - quotient(month + 9, 12)
   day = date - fixed_from_gregorian(gregorian_date(year, month, 1)) + 1
   return gregorian_date(year, month, day)
# see lines 827-841 in calendrica-3.0.cl
def alt_gregorian_year_from_fixed(date):
    """Return the Gregorian year corresponding to the fixed date 'date'.
   Alternative calculation."""
   approx = quotient(date - GREGORIAN_EPOCH +2, 146097/400)
   start = (GREGORIAN_EPOCH
             (365 * approx)
             quotient(approx, 4)
             -quotient(approx, 100) +
             quotient(approx, 400))
   return approx if (date < start) else (approx + 1)
# see lines 843-847 in calendrica-3.0.cl
def independence_day(g_year):
    """Return the fixed date of United States Independence Day in
   Gregorian year 'g_year'."""
   return fixed_from_gregorian(gregorian_date(g_year, JULY, 4))
# see lines 849-853 in calendrica-3.0.cl
def kday_on_or_before(k, date):
   """Return the fixed date of the k-day on or before fixed date 'date'.
   k=0 means Sunday, k=1 means Monday, and so on."""
   return date - day_of_week_from_fixed(date - k)
# see lines 855-859 in calendrica-3.0.cl
def kday_on_or_after(k, date):
    """Return the fixed date of the k-day on or after fixed date 'date'.
   k=0 means Sunday, k=1 means Monday, and so on."""
   return kday_on_or_before(k, date + 6)
# see lines 861-865 in calendrica-3.0.cl
def kday_nearest(k, date):
   """Return the fixed date of the k-day nearest fixed date 'date'.
   k=0 means Sunday, k=1 means Monday, and so on."""
   return kday_on_or_before(k, date + 3)
# see lines 867-871 in calendrica-3.0.cl
def kday_after(k, date):
    """Return the fixed date of the k-day after fixed date 'date'.
```

```
k=0 means Sunday, k=1 means Monday, and so on."""
   return kday_on_or_before(k, date + 7)
# see lines 873-877 in calendrica-3.0.cl
def kday_before(k, date):
    """Return the fixed date of the k-day before fixed date 'date'.
   k=0 means Sunday, k=1 means Monday, and so on."""
   return kday_on_or_before(k, date - 1)
# see lines 62-74 in calendrica-3.0.errata.cl
def nth_kday(n, k, g_date):
   """Return the fixed date of n-th k-day after Gregorian date 'g_date'.
   If n>0, return the n-th k-day on or after 'g_date'.
   If n<0, return the n-th k-day on or before 'g_date'.
   If n=0, return BOGUS.
   A k-day of 0 means Sunday, 1 means Monday, and so on."""
   if n > 0:
       return 7*n + kday_before(k, fixed_from_gregorian(g_date))
   elif n < 0:
       return 7*n + kday_after(k, fixed_from_gregorian(g_date))
        return BOGUS
# see lines 892-897 in calendrica-3.0.cl
def first_kday(k, g_date):
    """Return the fixed date of first k-day on or after Gregorian date 'g_date'.
   A k-day of 0 means Sunday, 1 means Monday, and so on."""
   return nth_kday(1, k, g_date)
# see lines 899-904 in calendrica-3.0.cl
def last_kday(k, g_date):
    """Return the fixed date of last k-day on or before Gregorian date 'g_date'.
   A k-day of 0 means Sunday, 1 means Monday, and so on."""
   return nth_kday(-1, k, g_date)
# see lines 906-910 in calendrica-3.0.cl
def labor_day(g_year):
    """Return the fixed date of United States Labor Day in Gregorian
   year 'g_year' (the first Monday in September)."""
   return first_kday(MONDAY, gregorian_date(g_year, SEPTEMBER, 1))
# see lines 912-916 in calendrica-3.0.cl
def memorial_day(g_year):
   """Return the fixed date of United States' Memorial Day in Gregorian
   year 'g_year' (the last Monday in May)."""
   return last_kday(MONDAY, gregorian_date(g_year, MAY, 31))
# see lines 918-923 in calendrica-3.0.cl
def election_day(g_year):
    """Return the fixed date of United States' Election Day in Gregorian
   year 'g_year' (the Tuesday after the first Monday in November)."""
   return first_kday(TUESDAY, gregorian_date(g_year, NOVEMBER, 2))
# see lines 925-930 in calendrica-3.0.cl
def daylight_saving_start(g_year):
   """Return the fixed date of the start of United States daylight
   saving time in Gregorian year 'g_year' (the second Sunday in March)."""
   return nth_kday(2, SUNDAY, gregorian_date(g_year, MARCH, 1))
# see lines 932-937 in calendrica-3.0.cl
def daylight_saving_end(g_year):
```

```
"""Return the fixed date of the end of United States daylight saving
      time in Gregorian year 'g_year' (the first Sunday in November)."""
      return first_kday(SUNDAY, gregorian_date(g_year, NOVEMBER, 1))
  # see lines 939-943 in calendrica-3.0.cl
  def christmas(g_year):
      """Return the fixed date of Christmas in Gregorian year 'g_year'."""
      return fixed_from_gregorian(gregorian_date(g_year, DECEMBER, 25))
  # see lines 945-951 in calendrica-3.0.cl
  def advent(g_year):
      """Return the fixed date of Advent in Gregorian year 'g_year'
      (the Sunday closest to November 30)."""
      return kday_nearest(SUNDAY,
                           fixed_from_gregorian(gregorian_date(g_year,
                                                                  30)))
  # see lines 953-957 in calendrica-3.0.cl
  def epiphany(g_year):
      """Return the fixed date of Epiphany in U.S. in Gregorian year 'g_year'
      (the first Sunday after January 1)."""
      return first_kday(SUNDAY, gregorian_date(g_year, JANUARY, 2))
  def epiphany_it(g_year):
      """Return fixed date of Epiphany in Italy in Gregorian year 'g_year'."""
      return gregorian_date(g_year, JANUARY, 6)
  # see lines 959-974 in calendrica-3.0.cl
  def unlucky_fridays_in_range(range):
      """Return the list of Fridays within range 'range' of fixed dates that
      are day 13 of the relevant Gregorian months."""
           = start(range)
      b
           = end(range)
      fri = kday_on_or_after(FRIDAY, a)
      date = gregorian_from_fixed(fri)
      ell = [fri] if (standard_day(date) == 13) else []
      if is_in_range(fri, range):
          ell[:0] = unlucky_fridays_in_range(interval(fri + 1, b))
          return ell
      else:
          return []
This code is used in chunk 51.
Defines:
  advent, never used.
  alt_fixed_from_gregorian, used in chunk 155.
  alt_gregorian_from_fixed, used in chunk 155.
  alt_gregorian_year_from_fixed, used in chunk 155.
  christmas, never used.
  day_number, used in chunk 57.
  daylight_saving_end, never used.
  daylight_saving_start, never used.
  days_remaining, never used.
  election_day, never used.
  epiphany, never used.
  epiphany_it, never used.
  first_kday, never used.
  gregorian_date_difference, used in chunk 107.
  gregorian_from_fixed, used in chunks 57, 155, and 178.
  gregorian_new_year, used in chunks 63, 68, 71, 77, 80, 107, 133, 136, and 142.
```

```
gregorian_year_end, used in chunks 68 and 139.
          gregorian_year_range, used in chunks 63, 71, 77, 80, 89, 136, and 139.
          independence_day, never used.
          kday_after, used in chunks 74 and 142.
          kday_before, used in chunk 80.
          kday_nearest, never used.
          kday_on_or_after, used in chunk 136.
          kday_on_or_before, never used.
          labor_day, never used.
          last_kday, never used.
          memorial_day, never used.
          nth_kday, used in chunk 68.
          unlucky_fridays_in_range, never used.
        Uses amod 15, BOGUS 13, day_of_week_from_fixed 38, DECEMBER 53, end 47, fixed_from_gregorian 55,
          FRIDAY 38, gregorian_date 52, GREGORIAN_EPOCH 52, gregorian_year_from_fixed 55, interval 47,
           \texttt{is\_gregorian\_leap\_year 54}, \ \texttt{is\_in\_range 47}, \ \texttt{JANUARY 53}, \ \texttt{JULY 53}, \ \texttt{MARCH 53}, \ \texttt{MAY 53}, \ \texttt{MONDAY 38}, \\ 
          NOVEMBER 53, quotient 14 14, SEPTEMBER 53, standard_day 39, standard_month 39, standard_year 39,
          start 47, SUNDAY 38, and TUESDAY 38.
57
        \langle gregorian\ calendar\ unit\ test\ 57 \rangle \equiv
          {\tt class} \  \, {\tt GregorianCalendarSmokeTestCase} (unittest. {\tt TestCase}): \\
               def setUp(self):
                    self.testvalue = 710347
                    self.aDate = gregorian_date(1945, NOVEMBER, 12)
                    self.myDate = gregorian_date(1967, JANUARY, 30)
                    self.aLeapDate = gregorian_date(1900, MARCH, 1)
               def testConversionFromFixed(self):
                    self.assertEqual(
                         gregorian_from_fixed(self.testvalue), self.aDate)
               def testConversionToFixed(self):
                    self.assertEqual(
                         self.testvalue, fixed_from_gregorian(self.aDate))
               def testLeapYear(self):
                    self.assertTrue(is_gregorian_leap_year(2000))
                    self.assertTrue(not is_gregorian_leap_year(1900))
               def testDayNumber(self):
                    self.assertEqual(day_number(self.myDate), 30)
                    self.assertEqual(day_number(self.aLeapDate), 60)
       This definition is continued in chunk 154.
        This code is used in chunks 4 and 58.
        Defines:
          GregorianCalendarSmokeTestCase, never used.
        Uses day_number 56, fixed_from_gregorian 55, gregorian_date 52, gregorian_from_fixed 56,
          is_gregorian_leap_year 54, JANUARY 53, MARCH 53, and NOVEMBER 53.
        2.3.1
                  Unit tests
        As usual the unit tests are as follows
        \langle gregorianCalendarUnitTest.py 58 \rangle \equiv
58
          # \(\langle generated code warning \mathbf{1}\rangle\)
          (import for testing 6)
          from appendixCUnitTest import AppendixCTable1TestCaseBase
          ⟨gregorian calendar unit test 57⟩
          \langle execute \ tests \ 5 \rangle
        Root chunk (not used in this document).
        Uses AppendixCTable1TestCaseBase 149.
```

2.4 Julian Calendar

```
59
      \langle julian\ calendar\ 59 \rangle \equiv
        #####################################
        # julian calendar algorithms #
        ####################################
        # see lines 1037-1040 in calendrica-3.0.cl
        def julian_date(year, month, day):
             """Return the Julian date data structure."""
            return [year, month, day]
        # see lines 1042-1045 in calendrica-3.0.cl
        JULIAN_EPOCH = fixed_from_gregorian(gregorian_date(0, DECEMBER, 30))
        # see lines 1047-1050 in calendrica-3.0.cl
        def bce(n):
             """Retrun a negative value to indicate a BCE Julian year."""
            return -n
        # see lines 1052-1055 in calendrica-3.0.cl
        def ce(n):
            """Return a positive value to indicate a CE Julian year."""
            return n
        # see lines 1057-1060 in calendrica-3.0.cl
        def is_julian_leap_year(j_year):
             """Return True if Julian year 'j_year' is a leap year in
            the Julian calendar."""
            return mod(j_year, 4) == (0 if j_year > 0 else 3)
        # see lines 1062-1082 in calendrica-3.0.cl
        def fixed_from_julian(j_date):
             """Return the fixed date equivalent to the Julian date 'j_date'."""
            month = standard_month(j_date)
            day = standard_day(j_date)
            year = standard_year(j_date)
                  = year + 1 if year < 0 else year
            return (JULIAN_EPOCH - 1 +
                     (365 * (y - 1)) +
                     quotient(y - 1, 4) +
                     quotient(367*month - 362, 12) +
                     (0 if month <= 2 else (-1 if is_julian_leap_year(year) else -2)) +
                     day)
        # see lines 1084-1111 in calendrica-3.0.cl
        def julian_from_fixed(date):
             """Return the Julian date corresponding to fixed date 'date'."""
                        = quotient(((4 * (date - JULIAN_EPOCH))) + 1464, 1461)
            approx
                        = approx - 1 if approx <= 0 else approx
            year
            prior_days = date - fixed_from_julian(julian_date(year, JANUARY, 1))
            correction = (0 if date < fixed_from_julian(julian_date(year, MARCH, 1))</pre>
                           else (1 if is_julian_leap_year(year) else 2))
            month
                        = quotient(12*(prior_days + correction) + 373, 367)
                        = 1 + (date - fixed_from_julian(julian_date(year, month, 1)))
            dav
            return julian_date(year, month, day)
```

This definition is continued in chunks 61 and 63. This code is used in chunk 3. Defines:

```
bce, used in chunks 61, 80, and 86.
          ce, used in chunks 71, 77, 122, and 136.
          fixed_from_julian, used in chunks 60, 61, 63, 71, 74, 77, 80, 83, 86, 122, and 158.
          is\_julian\_leap\_year, used in chunks 60 and 61.
          {\tt julian\_date, used in \ chunks \ 60, \ 61, \ 63, \ 71, \ 74, \ 77, \ 80, \ 83, \ 86, \ 122, \ 149, \ and \ 174.}
          JULIAN_EPOCH, never used.
          julian_from_fixed, used in chunks 60, 61, 63, and 158.
       Uses DECEMBER 53, fixed_from_gregorian 55, gregorian_date 52, JANUARY 53, MARCH 53, mod 15,
          quotient 14 14, standard_day 39, standard_month 39, and standard_year 39.
60
       \langle julian\ calendar\ unit\ test\ 60 \rangle \equiv
          class JulianSmokeTestCase(unittest.TestCase):
              def setUp(self):
                   self.testvalue = 710347
              def testConversionFromFixed(self):
                   self.assertEqual(
                        julian_from_fixed(self.testvalue), julian_date(1945, OCTOBER, 30))
                   self.assertEqual(
                        roman_from_fixed(self.testvalue),
                        roman_date(1945, NOVEMBER, KALENDS, 3, is_julian_leap_year(1945)))
              def testConversionToFixed(self):
                   self.assertEqual(self.testvalue,
                                 fixed_from_julian(julian_date(1945, OCTOBER, 30)))
                   self.assertEqual(
                        self.testvalue,
                        fixed_from_roman(roman_date(1945, NOVEMBER, KALENDS, 3,
                                                         is_julian_leap_year(1945))))
              def testLeapYear(self):
                   self.assertTrue(is_julian_leap_year(2000))
                   self.assertTrue(is_julian_leap_year(1900))
       This definition is continued in chunks 62, 152, and 159.
       This code is used in chunks 4 and 64.
       Defines:
          {\tt JulianSmokeTestCase}, \ {\tt never} \ {\tt used}.
       Uses fixed_from_julian 59, fixed_from_roman 61, is_julian_leap_year 59, julian_date 59,
          julian_from_fixed 59, KALENDS 61, NOVEMBER 53, OCTOBER 53, roman_date 61, and roman_from_fixed
```

And here is the Roman representation of the Julian calendar:

```
61
      \langle iulian\ calendar\ 59 \rangle + \equiv
        # see lines 1113-1116 in calendrica-3.0.cl
        KALENDS = 1
        # see lines 1118-1121 in calendrica-3.0.cl
        NONES = 2
        # see lines 1123-1126 in calendrica-3.0.cl
        TDES = 3
        # see lines 1128-1131 in calendrica-3.0.cl
        def roman_date(year, month, event, count, leap):
             """Return the Roman date data structure."""
            return [year, month, event, count, leap]
        # see lines 1133-1135 in calendrica-3.0.cl
        def roman_year(date):
            """Return the year of Roman date 'date'."""
            return date[0]
        # see lines 1137-1139 in calendrica-3.0.cl
        def roman month(date):
            """Return the month of Roman date 'date'."""
            return date[1]
        # see lines 1141-1143 in calendrica-3.0.cl
        def roman_event(date):
            """Return the event of Roman date 'date'."""
            return date[2]
        # see lines 1145-1147 in calendrica-3.0.cl
        def roman count(date):
            """Return the count of Roman date 'date'."""
            return date[3]
        # see lines 1149-1151 in calendrica-3.0.cl
        def roman_leap(date):
             """Return the leap indicator of Roman date 'date'."""
            return date[4]
        # see lines 1153-1158 in calendrica-3.0.cl
        def ides_of_month(month):
             """Return the date of the Ides in Roman month 'month'."""
            return 15 if month in [MARCH, MAY, JULY, OCTOBER] else 13
        # see lines 1160-1163 in calendrica-3.0.cl
        def nones_of_month(month):
             """Return the date of Nones in Roman month 'month'."""
            return ides_of_month(month) - 8
        # see lines 1165-1191 in calendrica-3.0.cl
        def fixed_from_roman(r_date):
            """Return the fixed date corresponding to Roman date 'r_date'."""
            leap = roman_leap(r_date)
            count = roman_count(r_date)
            event = roman_event(r_date)
            month = roman_month(r_date)
            year = roman_year(r_date)
            return ({KALENDS: fixed_from_julian(julian_date(year, month, 1)),
                      NONES: fixed_from_julian(julian_date(year,
```

```
month,
                                                     nones_of_month(month))),
             IDES:
                      fixed_from_julian(julian_date(year,
                                                     ides_of_month(month)))
            }[event] -
            count +
            (0 if (is_julian_leap_year(year) and
                   (month == MARCH) and
                   (event == KALENDS) and
                   (16 \ge count \ge 6)
             else 1) +
            (1 if leap else 0))
# see lines 1193-1229 in calendrica-3.0.cl
def roman_from_fixed(date):
    """Return the Roman name corresponding to fixed date 'date'."""
   j_date = julian_from_fixed(date)
   month = standard_month(j_date)
          = standard_day(j_date)
   year = standard_year(j_date)
   month_prime = amod(1 + month, 12)
   year_prime = (year if month_prime != 1
                   else (year + 1 if (year != -1) else 1))
   kalends1 = fixed_from_roman(
       roman_date(year_prime, month_prime, KALENDS, 1, False))
   if day == 1:
        res = roman_date(year, month, KALENDS, 1, False)
   elif day <= nones_of_month(month):</pre>
        res = roman_date(year,
                         NONES,
                         nones_of_month(month) - day + 1,
                         False)
   elif day <= ides_of_month(month):</pre>
        res = roman_date(year,
                         month.
                         IDES,
                         ides_of_month(month) - day + 1,
                         False)
   elif (month != FEBRUARY) or not is_julian_leap_year(year):
        res = roman_date(year_prime,
                         month_prime,
                         KALENDS,
                         kalends1 - date + 1,
                         False)
   elif day < 25:
       res = roman_date(year, MARCH, KALENDS, 30 - day, False)
       res = roman_date(year, MARCH, KALENDS, 31 - day, day == 25)
# see lines 1231-1234 in calendrica-3.0.cl
YEAR_ROME_FOUNDED = bce(753)
# see lines 1236-1241 in calendrica-3.0.cl
def julian_year_from_auc_year(year):
    """Return the Julian year equivalent to AUC year 'year'."""
   return ((year + YEAR_ROME_FOUNDED - 1)
```

```
if (1 <= year <= (year - YEAR_ROME_FOUNDED))</pre>
                        else (year + YEAR_ROME_FOUNDED))
          # see lines 1243-1248 in calendrica-3.0.cl
          def auc_year_from_julian_year(year):
               """Return the AUC year equivalent to Julian year 'year'."""
              return ((year - YEAR_ROME_FOUNDED - 1)
                        if (YEAR_ROME_FOUNDED <= year <= -1)</pre>
                        else (year - YEAR_ROME_FOUNDED))
       This code is used in chunk 3.
       Defines:
          auc_year_from_julian_year, never used.
          {\tt fixed\_from\_roman, used in chunks 60, 62, and 158.}
          IDES, never used.
          ides_of_month, never used.
          julian_year_from_auc_year, never used.
          KALENDS, used in chunks 60 and 62.
          NONES, never used.
          nones_of_month, never used.
          roman_count, never used.
          roman_date, used in chunks 60, 62, and 149.
          roman_event, never used.
          {\tt roman\_from\_fixed}, \ {\tt used} \ {\tt in} \ {\tt chunks} \ {\tt 60}, \ {\tt 62}, \ {\tt and} \ {\tt 158}.
          roman_leap, never used.
          roman_month, never used.
          roman_year, never used.
          YEAR_ROME_FOUNDED, never used.
       Uses amod 15, bce 59, FEBRUARY 53, fixed_from_julian 59, is_julian_leap_year 59, julian_date 59,
          julian_from_fixed 59, JULY 53, MARCH 53, MAY 53, OCTOBER 53, standard_day 39, standard_month 39,
          and standard_year 39.
62
       \langle julian\ calendar\ unit\ test\ 60\rangle + \equiv
          class RomanSmokeTestCase(unittest.TestCase):
              def setUp(self):
                   self.testvalue = 710347
              def testConversionFromFixed(self):
                   self.assertEqual(
                        roman_from_fixed(self.testvalue),
                        roman_date(1945, NOVEMBER, KALENDS, 3, False))
              def testConversionToFixed(self):
                   self.assertEqual(self.testvalue,
                                  fixed_from_roman(roman_date(1945,
                                                                    NOVEMBER,
                                                                    KALENDS.
                                                                    3,
                                                                   False)))
       This code is used in chunks 4 and 64.
       Defines:
          RomanSmokeTestCase, never used.
       Uses fixed_from_roman 61, KALENDS 61, NOVEMBER 53, roman_date 61, and roman_from_fixed 61.
```

Here are some other interesting helper functions:

Uses AppendixCTable1TestCaseBase 149.

```
\langle julian\ calendar\ 59 \rangle + \equiv
63
         # see lines 1250-1266 in calendrica-3.0.cl
         def julian_in_gregorian(j_month, j_day, g_year):
              """Return the list of the fixed dates of Julian month 'j_month', day
              'j_day' that occur in Gregorian year 'g_year'.""
              jan1 = gregorian_new_year(g_year)
                   = standard_year(julian_from_fixed(jan1))
              y_prime = 1 if (y == -1) else (y + 1)
              date1 = fixed_from_julian(julian_date(y, j_month, j_day))
              date2 = fixed_from_julian(julian_date(y_prime, j_month, j_day))
              return list_range([date1, date2], gregorian_year_range(g_year))
         # see lines 1268-1272 in calendrica-3.0.cl
         def eastern_orthodox_christmas(g_year):
              """Return the list of zero or one fixed dates of Eastern Orthodox Christmas
              in Gregorian year 'g_year'."""
              return julian_in_gregorian(DECEMBER, 25, g_year)
       This code is used in chunk 3.
       Defines:
         \verb"eastern_orthodox_christmas", never used.
         julian_in_gregorian, never used.
       Uses DECEMBER 53, fixed_from_julian 59, gregorian_new_year 56, gregorian_year_range 56,
         julian_date 59, julian_from_fixed 59, list_range 47, and standard_year 39.
       2.4.1
                 Unit tests
       \langle julianCalendarUnitTest.py 64 \rangle \equiv
64
         # \(\langle generated code warning \mathbf{1}\rangle\)
         ⟨import for testing 6⟩
         from appendixCUnitTest import AppendixCTable1TestCaseBase
          ⟨julian calendar unit test 60⟩
          \langle execute \ tests \ 5 \rangle
       Root chunk (not used in this document).
```

2.5 Egyptian/Armenian Calendars

```
\langle egyptian \ and \ armenian \ calendars \ 65 \rangle \equiv
65
        # egyptian and armenian calendars algorithms #
        # see lines 515-518 in calendrica-3.0.cl
        def egyptian_date(year, month, day):
             """Return the Egyptian date data structure."""
            return [year, month, day]
        # see lines 520-525 in calendrica-3.0.cl
        EGYPTIAN_EPOCH = fixed_from_jd(1448638)
        # see lines 527-536 in calendrica-3.0.cl
        def fixed_from_egyptian(e_date):
            """Return the fixed date corresponding to Egyptian date 'e_date'."""
            month = standard_month(e_date)
            day = standard_day(e_date)
            year = standard_year(e_date)
            return EGYPTIAN_EPOCH + (365*(year - 1)) + (30*(month - 1)) + (day - 1)
        # see lines 538-553 in calendrica-3.0.cl
        def egyptian_from_fixed(date):
             """Return the Egyptian date corresponding to fixed date 'date'."""
            days = date - EGYPTIAN_EPOCH
            year = 1 + quotient(days, 365)
            month = 1 + quotient(mod(days, 365), 30)
            day = days - (365*(year - 1)) - (30*(month - 1)) + 1
            return egyptian_date(year, month, day)
        # see lines 555-558 in calendrica-3.0.cl
        def armenian_date(year, month, day):
             """Return the Armenian date data structure."""
            return [year, month, day]
        # see lines 560-564 in calendrica-3.0.cl
        ARMENIAN\_EPOCH = rd(201443)
        # see lines 566-575 in calendrica-3.0.cl
        def fixed_from_armenian(a_date):
             """Return the fixed date corresponding to Armenian date 'a_date'."""
            month = standard_month(a_date)
            day = standard_day(a_date)
            year = standard_year(a_date)
            return (ARMENIAN_EPOCH +
                     fixed_from_egyptian(egyptian_date(year, month, day)) -
                     EGYPTIAN_EPOCH)
        # see lines 577-581 in calendrica-3.0.cl
        def armenian_from_fixed(date):
             """Return the Armenian date corresponding to fixed date 'date'."""
            return egyptian_from_fixed(date + (EGYPTIAN_EPOCH - ARMENIAN_EPOCH))
      This code is used in chunk 3.
      Defines:
        armenian_date, used in chunks 66 and 149.
        ARMENIAN_EPOCH, never used.
        {\tt armenian\_from\_fixed}, \, {\rm used} \, \, {\rm in} \, \, {\rm chunks} \, \, 66 \, \, {\rm and} \, \, 161.
        egyptian_date, used in chunks 66 and 149.
        EGYPTIAN_EPOCH, never used.
        egyptian_from_fixed, used in chunks 66 and 160.
```

```
fixed_from_armenian, used in chunks 66 and 161.
         fixed_from_egyptian, used in chunks 66 and 160.
       Uses fixed_from_jd 48, mod 15, quotient 14 14, rd 37, standard_day 39, standard_month 39,
         and standard_year 39.
          and now the tests ...
66
       \langle egyptian \ and \ armenian \ calendars \ unit \ test \ 66 \rangle \equiv
         class EgyptianSmokeTestCase(unittest.TestCase):
             def setUp(self):
                  self.testvalue = 710347
                  self.aDate = egyptian_date(2694, 7, 10)
             def testConversionFromFixed(self):
                  self.assertEqual(
                      egyptian_from_fixed(self.testvalue), self.aDate)
             def testConversionToFixed(self):
                  self.assertEqual(
                      self.testvalue, fixed_from_egyptian(self.aDate))
         class ArmenianSmokeTestCase(unittest.TestCase):
             def setUp(self):
                  self.testvalue = 710347
                  self.aDate = armenian_date(1395, 4, 5)
             def testConversionFromFixed(self):
                  self.assertEqual(
                      armenian_from_fixed(self.testvalue), self.aDate)
             def testConversionToFixed(self):
                  self.assertEqual(
                      self.testvalue, fixed_from_armenian(self.aDate))
       This definition is continued in chunk 162.
       This code is used in chunks 4 and 67.
       Defines:
         ArmenianSmokeTestCase, never used.
         EgyptianSmokeTestCase, never used.
       Uses armenian_date 65, armenian_from_fixed 65, egyptian_date 65, egyptian_from_fixed 65,
         fixed_from_armenian 65, and fixed_from_egyptian 65.
       2.5.1
                Unit tests
       The tests for Egyptian and Armenian calendars are following the usual pattern as de-
       scribed in section 1.1.
```

```
67
         \langle egyptianAndArmenianCalendarsUnitTest.py 67 \rangle \equiv
            # \(\langle generated code warning \mathbf{1}\rangle\)
            \langle import\ for\ testing\ 6 \rangle
            from appendixCUnitTest import AppendixCTable1TestCaseBase
            ⟨egyptian and armenian calendars unit test 66⟩
            \langle execute \ tests \ 5 \rangle
         Root chunk (not used in this document).
         Uses AppendixCTable1TestCaseBase 149.
```

2.6 ISO Calendar

```
68
      \langle iso\ calendar\ 68 \rangle \equiv
         #####################################
         # ISO calendar algorithms #
         ############################
         # see lines 979-981 in calendrica-3.0.cl
         def iso_date(year, week, day):
             """Return the ISO date data structure."""
             return [year, week, day]
         # see lines 983-985 in calendrica-3.0.cl
         def iso_week(date):
             """Return the week of ISO date 'date'."""
             return date[1]
         # see lines 987-989 in calendrica-3.0.cl
         def iso_day(date):
             """Return the day of ISO date 'date'."""
             return date[2]
         # see lines 991-993 in calendrica-3.0.cl
         def iso_year(date):
             """Return the year of ISO date 'date'."""
             return date[0]
         # see lines 995-1005 in calendrica-3.0.cl
         def fixed_from_iso(i_date):
             """Return the fixed date equivalent to ISO date 'i_date'."""
             week = iso_week(i_date)
             day = iso_day(i_date)
             year = iso_year(i_date)
             return nth_kday(week, SUNDAY, gregorian_date(year - 1, DECEMBER, 28)) + day
         # see lines 1007-1022 in calendrica-3.0.cl
         def iso_from_fixed(date):
             """Return the ISO date corresponding to the fixed date 'date'."""
             approx = gregorian_year_from_fixed(date - 3)
                    = (approx +
                       1 if date >= fixed_from_iso(iso_date(approx + 1, 1, 1))
                       else approx)
                    = 1 + quotient(date - fixed_from_iso(iso_date(year, 1, 1)), 7)
             week
                    = amod(date - rd(0), 7)
             day
             return iso_date(year, week, day)
         # see lines 1024-1032 in calendrica-3.0.cl
         def is_iso_long_year(i_year):
             """Return True if ISO year 'i_year' is a long (53-week) year."""
             jan1 = day_of_week_from_fixed(gregorian_new_year(i_year))
             dec31 = day_of_week_from_fixed(gregorian_year_end(i_year))
             return (jan1 == THURSDAY) or (dec31 == THURSDAY)
      This code is used in chunk 3.
        fixed_from_iso, used in chunks 69 and 157.
         is_iso_long_year, never used.
        iso_date, used in chunks 69 and 149.
        iso_day, never used.
         iso_from_fixed, used in chunks 69 and 157.
        iso_week, never used.
         iso_year, never used.
```

```
Uses amod 15, day_of_week_from_fixed 38, DECEMBER 53, gregorian_date 52, gregorian_new_year 56,
          gregorian_year_end 56, gregorian_year_from_fixed 55, nth_kday 56, quotient 14 14, rd 37, SUNDAY 38, and THURSDAY 38.
69
        \langle iso\ calendar\ unit\ test\ 69 \rangle \equiv
           class ISOSmokeTestCase(unittest.TestCase):
               def setUp(self):
                     self.testvalue = 710347
                     self.aDate = iso_date(1945, 46, 1)
               def testConversionFromFixed(self):
                     self.assertEqual(
                          iso_from_fixed(self.testvalue), self.aDate)
               def testConversionToFixed(self):
                     self.assertEqual(
                          self.testvalue, fixed_from_iso(self.aDate))
        This definition is continued in chunk 156.
        This code is used in chunks 4 and 70.
          ISOSmokeTestCase, never used.
        Uses fixed_from_iso 68, iso_date 68, and iso_from_fixed 68.
        2.6.1
                   Unit tests
        \langle isoCalendarUnitTest.py 70 \rangle \equiv
70
          # \langle generated\ code\ warning\ {\color{red} 1} \rangle
           \langle import\ for\ testing\ {\color{red}6} \rangle
          from appendixCUnitTest import AppendixCTable1TestCaseBase
           (iso calendar unit test 69)
           \langle execute \ tests \ 5 \rangle
        Root chunk (not used in this document).
        Uses AppendixCTable1TestCaseBase 149.
```

2.7 Coptic and Ethiopic Calendars

```
\langle coptic \ and \ ethiopic \ calendars \ 71 \rangle \equiv
  # see lines 1277-1279 in calendrica-3.0.cl
  # coptic and ethiopic calendars algorithms #
  def coptic_date(year, month, day):
      """Return the Coptic date data structure."""
     return [year, month, day]
  # see lines 1281-1284 in calendrica-3.0.cl
  COPTIC_EPOCH = fixed_from_julian(julian_date(ce(284), AUGUST, 29))
  # see lines 1286-1289 in calendrica-3.0.cl
  def is_coptic_leap_year(c_year):
      """Return True if Coptic year 'c_year' is a leap year
     in the Coptic calendar."""
     return mod(c_year, 4) == 3
  # see lines 1291-1301 in calendrica-3.0.cl
  def fixed_from_coptic(c_date):
      """Return the fixed date of Coptic date 'c_date'."""
     month = standard_month(c_date)
     day = standard_day(c_date)
     year = standard_year(c_date)
     return (COPTIC_EPOCH - 1 +
             365 * (year - 1)
             quotient(year, 4) +
             30 * (month - 1) +
             day)
  # see lines 1303-1318 in calendrica-3.0.cl
  def coptic_from_fixed(date):
      """Return the Coptic date equivalent of fixed date 'date'."""
     year = quotient((4 * (date - COPTIC_EPOCH)) + 1463, 1461)
     month = 1 + quotient(date - fixed_from_coptic(coptic_date(year, 1, 1)), 30)
          = date + 1 - fixed_from_coptic(coptic_date(year, month, 1))
     return coptic_date(year, month, day)
  # see lines 1320-1323 in calendrica-3.0.cl
  def ethiopic_date(year, month, day):
      """Return the Ethiopic date data structure."""
     return [year, month, day]
  # see lines 1325-1328 in calendrica-3.0.cl
  ETHIOPIC_EPOCH = fixed_from_julian(julian_date(ce(8), AUGUST, 29))
  # see lines 1330-1339 in calendrica-3.0.cl
  def fixed_from_ethiopic(e_date):
      """Return the fixed date corresponding to Ethiopic date 'e_date'."""
     month = standard_month(e_date)
     day = standard_day(e_date)
     year = standard_year(e_date)
     return (ETHIOPIC_EPOCH +
             fixed_from_coptic(coptic_date(year, month, day)) - COPTIC_EPOCH)
  # see lines 1341-1345 in calendrica-3.0.cl
  def ethiopic_from_fixed(date):
      """Return the Ethiopic date equivalent of fixed date 'date'."""
     return coptic_from_fixed(date + (COPTIC_EPOCH - ETHIOPIC_EPOCH))
```

```
# see lines 1347-1360 in calendrica-3.0.cl
  def coptic_in_gregorian(c_month, c_day, g_year):
      """Return the list of the fixed dates of Coptic month 'c_month',
      day 'c_day' that occur in Gregorian year 'g_year'."""
      jan1 = gregorian_new_year(g_year)
             = standard_year(coptic_from_fixed(jan1))
      date1 = fixed_from_coptic(coptic_date(y, c_month, c_day))
      date2 = fixed_from_coptic(coptic_date(y+1, c_month, c_day))
      return list_range([date1, date2], gregorian_year_range(g_year))
  # see lines 1362-1366 in calendrica-3.0.cl
  def coptic_christmas(g_year):
      """Retuen the list of zero or one fixed dates of Coptic Christmas
      dates in Gregorian year 'g_year'."""
      return coptic_in_gregorian(4, 29, g_year)
This code is used in chunk 3.
Defines:
  {\tt coptic\_christmas}, \ {\rm never} \ {\rm used}.
  coptic_date, used in chunks 72 and 149.
  COPTIC_EPOCH, never used.
  coptic_from_fixed, used in chunks 72, 80, and 164.
  coptic_in_gregorian, used in chunk 80.
  ethiopic_date, used in chunks 72 and 165.
  ETHIOPIC_EPOCH, never used.
  ethiopic_from_fixed, used in chunks 72 and 167.
  fixed_from_coptic, used in chunks 72 and 164.
  fixed_from_ethiopic, used in chunks 72 and 167.
  is_coptic_leap_year, never used.
Uses AUGUST 53, ce 59, fixed_from_julian 59, gregorian_new_year 56, gregorian_year_range 56,
  julian_date 59, list_range 47, mod 15, quotient 14 14, standard_day 39, standard_month 39,
  and standard_year 39.
```

```
72
       \langle coptic \ and \ ethiopic \ calendars \ unit \ test \ 72 \rangle \equiv
          class CopticSmokeTestCase(unittest.TestCase):
               def setUp(self):
                    self.testvalue = 710347
               def testConversionFromFixed(self):
                    self.assertEqual(
                        coptic_from_fixed(self.testvalue), coptic_date(1662, 3, 3))
               def testConversionToFixed(self):
                    self.assertEqual(
                        self.testvalue, fixed_from_coptic(coptic_date(1662, 3, 3)))
          class EthiopicSmokeTestCase(unittest.TestCase):
               def setUp(self):
                    self.testvalue = 710347
               def testConversionFromFixed(self):
                    self.assertEqual(
                        ethiopic_from_fixed(self.testvalue), ethiopic_date(1938, 3, 3))
               def testConversionToFixed(self):
                    self.assertEqual(
                        self.testvalue, fixed_from_ethiopic(ethiopic_date(1938, 3, 3)))
       This definition is continued in chunks 163 and 166.
       This code is used in chunks 4 and 73.
       Defines:
          CopticSmokeTestCase, never used.
          {\tt EthiopicSmokeTestCase}, \ never \ used.
       Uses coptic_date 71, coptic_from_fixed 71, ethiopic_date 71, ethiopic_from_fixed 71,
          fixed_from_coptic 71, and fixed_from_ethiopic 71.
       2.7.1
                  Unit tests
73
       \langle copticAndEthiopicCalendarsUnitTest.py 73 \rangle \equiv
          # \(\langle generated code warning \mathbf{1}\rangle\)
          ⟨import for testing 6⟩
          from appendixCUnitTest import AppendixCTable1TestCaseBase
          {\tt from\ appendix CUnit Test\ import\ Appendix CTable 2 Test Case Base}
          \langle coptic\ and\ ethiopic\ calendars\ unit\ test\ {\bf 72} \rangle
          \langle execute\ tests\ {\color{red}5}\rangle
       Root chunk (not used in this document).
       Uses AppendixCTable1TestCaseBase 149 and AppendixCTable2TestCaseBase 165.
```

2.8 Ecclesiastical Calendars

```
74
      \langle ecclesiastical\ calendars\ 74 \rangle \equiv
        # ecclesiastical calendars algorithms #
        # see lines 1371-1385 in calendrica-3.0.cl
        def orthodox_easter(g_year):
            """Return fixed date of Orthodox Easter in Gregorian year g_year."""
            shifted_epact = mod(14 + 11 * mod(g_year, 19), 30)
                         = g_year if g_year > 0 else g_year - 1
            paschal_moon = fixed_from_julian(
                julian_date(j_year, APRIL, 19)) - shifted_epact
            return kday_after(SUNDAY, paschal_moon)
        # see lines 76-91 in calendrica-3.0.errata.cl
        def alt_orthodox_easter(g_year):
            """Return fixed date of Orthodox Easter in Gregorian year g_year.
            Alternative calculation."""
            paschal_moon = (354 * g_year +
                            30 * quotient((7 * g_year) + 8, 19) +
                            quotient(g_year, 4)
                            quotient(g_year, 19) -
                            273 +
                            GREGORIAN_EPOCH)
            return kday_after(SUNDAY, paschal_moon)
        # see lines 1401-1426 in calendrica-3.0.cl
        def easter(g_year):
            """Return fixed date of Easter in Gregorian year g_year."""
            century = quotient(g_year, 100) + 1
            shifted_epact = mod(14 +
                                 11 * mod(g_year, 19) -
                                 quotient(3 * century, 4) +
                                 quotient(5 + (8 * century), 25), 30)
            adjusted_epact = ((shifted_epact + 1)
                               if ((shifted_epact == 0) or ((shifted_epact == 1) and
                                                           (10 < mod(g_year, 19)))
                               else shifted_epact)
            paschal_moon = (fixed_from_gregorian(gregorian_date(g_year, APRIL, 19)) -
                            adjusted_epact)
            return kday_after(SUNDAY, paschal_moon)
        # see lines 1429-1431 in calendrica-3.0.cl
        def pentecost(g_year):
            """Return fixed date of Pentecost in Gregorian year g_year."""
            return easter(g_year) + 49
      This code is used in chunk 3.
      Defines:
        alt_orthodox_easter, used in chunk 178.
        easter, used in chunks 174 and 178.
        orthodox_easter, used in chunk 178.
        pentecost, never used.
      Uses APRIL 53, fixed_from_gregorian 55, fixed_from_julian 59, gregorian_date 52,
        GREGORIAN_EPOCH 52, julian_date 59, kday_after 56, mod 15, quotient 14 14, and SUNDAY 38.
```

75 $\langle ecclesiastical\ calendars\ unit\ test\ 75 \rangle \equiv$

This definition is continued in chunk 177. This code is used in chunks 4 and 76.

2.8.1 Unit tests

76 $\langle ecclesiasticalCalendarsUnitTest.py~76 \rangle \equiv$ # $\langle generated~code~warning~1 \rangle$ $\langle import~for~testing~6 \rangle$ from appendixCUnitTest import AppendixCTable3TestCaseBase $\langle ecclesiastical~calendars~unit~test~75 \rangle$ $\langle execute~tests~5 \rangle$

Root chunk (not used in this document). Uses ${\tt AppendixCTable3TestCaseBase} \ {\tt 174}.$

2.9 Islamic Calendar

```
\langle islamic\ calendar\ 77 \rangle \equiv
  #################################
  # islamic calendar algorithms #
  ##################################
  # see lines 1436-1439 in calendrica-3.0.cl
  def islamic_date(year, month, day):
      """Return an Islamic date data structure."""
      return [year, month, day]
  # see lines 1441-1444 in calendrica-3.0.cl
  ISLAMIC_EPOCH = fixed_from_julian(julian_date(ce(622), JULY, 16))
  # see lines 1446-1449 in calendrica-3.0.cl
  def is_islamic_leap_year(i_year):
      """Return True if i_year is an Islamic leap year."""
      return mod(14 + 11 * i_year, 30) < 11
  # see lines 1451-1463 in calendrica-3.0.cl
  def fixed_from_islamic(i_date):
      """Return fixed date equivalent to Islamic date i_date."""
      month = standard_month(i_date)
      day = standard_day(i_date)
      year = standard_year(i_date)
      return (ISLAMIC_EPOCH - 1 +
              (year - 1) * 354 +
              quotient(3 + 11 * year, 30) +
              29 * (month - 1) +
              quotient(month, 2) +
              day)
  # see lines 1465-1483 in calendrica-3.0.cl
  def islamic_from_fixed(date):
      """Return Islamic date (year month day) corresponding to fixed date date."""
                = quotient(30 * (date - ISLAMIC_EPOCH) + 10646, 10631)
      prior_days = date - fixed_from_islamic(islamic_date(year, 1, 1))
                = quotient(11 * prior_days + 330, 325)
      month
                 = date - fixed_from_islamic(islamic_date(year, month, 1)) + 1
      day
      return islamic_date(year, month, day)
  # see lines 1485-1501 in calendrica-3.0.cl
  def islamic_in_gregorian(i_month, i_day, g_year):
      """Return list of the fixed dates of Islamic month i_month, day i_day that
      occur in Gregorian year g_year."""
      jan1 = gregorian_new_year(g_year)
           = standard_year(islamic_from_fixed(jan1))
      date1 = fixed_from_islamic(islamic_date(y, i_month, i_day))
      date2 = fixed_from_islamic(islamic_date(y + 1, i_month, i_day))
      date3 = fixed_from_islamic(islamic_date(y + 2, i_month, i_day))
      return list_range([date1, date2, date3], gregorian_year_range(g_year))
  # see lines 1503-1507 in calendrica-3.0.cl
  def mawlid_an_nabi(g_year):
      """Return list of fixed dates of Mawlid an Nabi occurring in Gregorian
      year g_year."""
      return islamic_in_gregorian(3, 12, g_year)
```

This code is used in chunk 3.

```
Defines:
           {\tt fixed\_from\_islamic}, \, {\tt used} \, \, {\tt in} \, \, {\tt chunks} \, \, {\tt 78} \, \, {\tt and} \, \, {\tt 169}.
           \verb"is_islamic_leap_year", never used.
           islamic_date, used in chunks 78, 142, and 165.
           ISLAMIC_EPOCH, used in chunk 142.
           islamic_from_fixed, used in chunks 78 and 169.
           islamic_in_gregorian, never used.
           {\tt mawlid\_an\_nabi}, \ {\tt never} \ {\tt used}.
        Uses ce 59, fixed_from_julian 59, gregorian_new_year 56, gregorian_year_range 56, julian_date 59,
           JULY 53, list_range 47, mod 15, quotient 14 14, standard_day 39, standard_month 39,
           and standard_year 39.
        \langle islamic\ calendar\ unit\ test\ 78 \rangle \equiv
78
           class IslamicSmokeTestCase(unittest.TestCase):
                def setUp(self):
                     self.testvalue = 710347
                def testConversionFromFixed(self):
                     self.assertEqual(
                           islamic_from_fixed(self.testvalue), islamic_date(1364, 12, 6))
                def testConversionToFixed(self):
                     self.assertEqual(
                           self.testvalue, fixed_from_islamic(islamic_date(1364, 12, 6)))
        This definition is continued in chunk 168.
        This code is used in chunks 4 and 79.
        Defines:
           IslamicSmokeTestCase, never used.
        Uses fixed_from_islamic 77, islamic_date 77, and islamic_from_fixed 77.
        2.9.1
                    Unit tests
        \langle islamicCalendarUnitTest.py 79 \rangle \equiv
79
           # \(\langle generated code warning 1 \rangle \)
           ⟨import for testing 6⟩
           {\tt from\ appendixCUnitTest\ import\ AppendixCTable2TestCaseBase}
           \langle islamic\ calendar\ unit\ test\ 78 \rangle
           \langle execute \ tests \ 5 \rangle
        Root chunk (not used in this document).
        Uses AppendixCTable2TestCaseBase 165.
```

2.10 Hebrew Calendar

```
\langle hebrew\ calendar\ 80 \rangle \equiv
80
         ####################################
         # hebrew calendar algorithms #
         ######################################
         # see lines 1512-1514 in calendrica-3.0.cl
         def hebrew_date(year, month, day):
             """Return an Hebrew date data structure."""
             return [year, month, day]
         # see lines 1516-1519 in calendrica-3.0.cl
        NISAN = 1
         # see lines 1521-1524 in calendrica-3.0.cl
        IYYAR = 2
         # see lines 1526-1529 in calendrica-3.0.cl
        SIVAN = 3
         # see lines 1531-1534 in calendrica-3.0.cl
        TAMMUZ = 4
         # see lines 1536-1539 in calendrica-3.0.cl
         # see lines 1541-1544 in calendrica-3.0.cl
         EI.UI. = 6
         # see lines 1546-1549 in calendrica-3.0.cl
         TISHRI = 7
         # see lines 1551-1554 in calendrica-3.0.cl
         MARHESHVAN = 8
         # see lines 1556-1559 in calendrica-3.0.cl
         KISLEV = 9
         # see lines 1561-1564 in calendrica-3.0.cl
         TEVET = 10
         # see lines 1566-1569 in calendrica-3.0.cl
         SHEVAT = 11
         # see lines 1571-1574 in calendrica-3.0.cl
         # see lines 1576-1579 in calendrica-3.0.cl
         ADARTT = 13
         # see lines 1581-1585 in calendrica-3.0.cl
        HEBREW_EPOCH = fixed_from_julian(julian_date(bce(3761), OCTOBER, 7))
         # see lines 1587-1590 in calendrica-3.0.cl
         def is_hebrew_leap_year(h_year):
             """Return True if h_year is a leap year on Hebrew calendar."""
             return mod(7 * h_year + 1, 19) < 7
         # see lines 1592-1597 in calendrica-3.0.cl
         def last_month_of_hebrew_year(h_year):
             """Return last month of Hebrew year."""
```

```
return ADARII if is_hebrew_leap_year(h_year) else ADAR
# see lines 1599-1603 in calendrica-3.0.cl
def is_hebrew_sabbatical_year(h_year):
    """Return True if h_year is a sabbatical year on the Hebrew calendar."""
   return mod(h_year, 7) == 0
# see lines 1605-1617 in calendrica-3.0.cl
def last_day_of_hebrew_month(h_month, h_year):
    """Return last day of month h_month in Hebrew year h_year."""
    if ((h_month in [IYYAR, TAMMUZ, ELUL, TEVET, ADARII])
        or ((h_month == ADAR) and (not is_hebrew_leap_year(h_year)))
        or ((h_month == MARHESHVAN) and (not is_long_marheshvan(h_year)))
        or ((h_month == KISLEV) and is_short_kislev(h_year))):
        return 29
   else:
        return 30
# see lines 1619-1634 in calendrica-3.0.cl
def molad(h_month, h_year):
    """Return moment of mean conjunction of h_month in Hebrew h_year."""
   y = (h_year + 1) if (h_month < TISHRI) else h_year
   months_elapsed = h_month - TISHRI + quotient(235 * y - 234, 19)
   return (HEBREW_EPOCH -
          876/25920 +
          months_elapsed * (29 + days_from_hours(12) + 793/25920))
# see lines 1636-1663 in calendrica-3.0.cl
def hebrew_calendar_elapsed_days(h_year):
    """Return number of days elapsed from the (Sunday) noon prior
   to the epoch of the Hebrew calendar to the mean
   conjunction (molad) of Tishri of Hebrew year h_year,
   or one day later."""
   months_elapsed = quotient(235 * h_year - 234, 19)
   parts_elapsed = 12084 + 13753 * months_elapsed
   days = 29 * months_elapsed + quotient(parts_elapsed, 25920)
   return (days + 1) if (mod(3 * (days + 1), 7) < 3) else days
# see lines 1665-1670 in calendrica-3.0.cl
def hebrew_new_year(h_year):
    """Return fixed date of Hebrew new year h_year."""
   return (HEBREW_EPOCH +
          hebrew_calendar_elapsed_days(h_year) +
          hebrew_year_length_correction(h_year))
# see lines 1672-1684 in calendrica-3.0.cl
def hebrew_year_length_correction(h_year):
    """Return delays to start of Hebrew year h_year to keep ordinary
   year in range 353-356 and leap year in range 383-386."""
   # I had a bug... h_year = 1 instead of h_year - 1!!!
   ny0 = hebrew_calendar_elapsed_days(h_year - 1)
   ny1 = hebrew_calendar_elapsed_days(h_year)
   ny2 = hebrew_calendar_elapsed_days(h_year + 1)
   if ((ny2 - ny1) == 356):
        return 2
    elif ((ny1 - ny0) == 382):
       return 1
   else:
        return 0
# see lines 1686-1690 in calendrica-3.0.cl
```

```
def days_in_hebrew_year(h_year):
    """Return number of days in Hebrew year h_year."""
   return hebrew_new_year(h_year + 1) - hebrew_new_year(h_year)
# see lines 1692-1695 in calendrica-3.0.cl
def is_long_marheshvan(h_year):
    """Return True if Marheshvan is long in Hebrew year h_year."""
   return days_in_hebrew_year(h_year) in [355, 385]
# see lines 1697-1700 in calendrica-3.0.cl
def is_short_kislev(h_year):
   """Return True if Kislev is short in Hebrew year h_year."""
   return days_in_hebrew_year(h_year) in [353, 383]
# see lines 1702-1721 in calendrica-3.0.cl
def fixed_from_hebrew(h_date):
   """Return fixed date of Hebrew date h_date."""
   month = standard_month(h_date)
   day = standard_day(h_date)
   year = standard_year(h_date)
   if (month < TISHRI):</pre>
        tmp = (summa(lambda m: last_day_of_hebrew_month(m, year),
                     lambda m: m <= last_month_of_hebrew_year(year)) +</pre>
               summa(lambda m: last_day_of_hebrew_month(m, year),
                     NISAN.
                     lambda m: m < month))</pre>
   else:
        tmp = summa(lambda m: last_day_of_hebrew_month(m, year),
                    TISHRI.
                    lambda m: m < month)</pre>
   return hebrew_new_year(year) + day - 1 + tmp
# see lines 1723-1751 in calendrica-3.0.cl
def hebrew_from_fixed(date):
    """Return Hebrew (year month day) corresponding to fixed date date.
   # The fraction can be approximated by 365.25."""
   approx = quotient(date - HEBREW_EPOCH, 35975351/98496) + 1
   year = final(approx - 1, lambda y: hebrew_new_year(y) <= date)</pre>
   start = (TISHRI
             if (date < fixed_from_hebrew(hebrew_date(year, NISAN, 1)))</pre>
             else NISAN)
   month = next(start, lambda m: date <= fixed_from_hebrew(</pre>
       hebrew_date(year, m, last_day_of_hebrew_month(m, year))))
   day = date - fixed_from_hebrew(hebrew_date(year, month, 1)) + 1
   return hebrew_date(year, month, day)
# see lines 1753-1761 in calendrica-3.0.cl
def yom_kippur(g_year):
    """Return fixed date of Yom Kippur occurring in Gregorian year g_year."""
   hebrew_year = g_year - gregorian_year_from_fixed(HEBREW_EPOCH) + 1
   return fixed_from_hebrew(hebrew_date(hebrew_year, TISHRI, 10))
# see lines 1763-1770 in calendrica-3.0.cl
def passover(g_year):
    """Return fixed date of Passover occurring in Gregorian year g_year."""
   hebrew_year = g_year - gregorian_year_from_fixed(HEBREW_EPOCH)
   return fixed_from_hebrew(hebrew_date(hebrew_year, NISAN, 15))
```

```
# see lines 1772-1782 in calendrica-3.0.cl
def omer(date):
    """Return the number of elapsed weeks and days in the omer at date date.
   Returns BOGUS if that date does not fall during the omer."""
   c = date - passover(gregorian_year_from_fixed(date))
   return [quotient(c, 7), mod(c, 7)] if (1 <= c <= 49) else BOGUS
# see lines 1784-1793 in calendrica-3.0.cl
def purim(g_year):
    """Return fixed date of Purim occurring in Gregorian year g_year."""
   hebrew_year = g_year - gregorian_year_from_fixed(HEBREW_EPOCH)
   last_month = last_month_of_hebrew_year(hebrew_year)
   return fixed_from_hebrew(hebrew_date(hebrew_year, last_month, 14))
# see lines 1795-1805 in calendrica-3.0.cl
def ta_anit_esther(g_year):
    """Return fixed date of Ta'anit Esther occurring in Gregorian
   year g_year."""
   purim_date = purim(g_year)
   return ((purim_date - 3)
            if (day_of_week_from_fixed(purim_date) == SUNDAY)
            else (purim_date - 1))
# see lines 1807-1821 in calendrica-3.0.cl
def tishah_be_av(g_year):
    """Return fixed date of Tishah be_Av occurring in Gregorian year g_year."""
   hebrew_year = g_year - gregorian_year_from_fixed(HEBREW_EPOCH)
   av9 = fixed_from_hebrew(hebrew_date(hebrew_year, AV, 9))
   return (av9 + 1) if (day_of_week_from_fixed(av9) == SATURDAY) else av9
# see lines 1823-1834 in calendrica-3.0.cl
def birkath_ha_hama(g_year):
    """Return the list of fixed date of Birkath ha_Hama occurring in
   Gregorian year g_year, if it occurs."""
   dates = coptic_in_gregorian(7, 30, g_year)
   return (dates
            if ((not (dates == [])) and
                (mod(standard_year(coptic_from_fixed(dates[0])), 28) == 17))
            else [])
# see lines 1836-1840 in calendrica-3.0.cl
def sh_ela(g_year):
   """Return the list of fixed dates of Sh'ela occurring in
   Gregorian year g_year."""
   return coptic_in_gregorian(3, 26, g_year)
\# exercise for the reader from pag 104
def hebrew_in_gregorian(h_month, h_day, g_year):
   """Return list of the fixed dates of Hebrew month, h_month, day, h_day,
   that occur in Gregorian year g_year."""
   jan1 = gregorian_new_year(g_year)
         = standard_year(hebrew_from_fixed(jan1))
   date1 = fixed_from_hebrew(hebrew_date(y, h_month, h_day))
   date2 = fixed_from_hebrew(hebrew_date(y + 1, h_month, h_day))
   # Hebrew and Gregorian calendar are aligned but certain
   # holidays, i.e. Tzom Tevet, can fall on either side of Jan 1.
   # So we can have 0, 1 or 2 occurences of that holiday.
   dates = [date1, date2]
   return list_range(dates, gregorian_year_range(g_year))
# see pag 104
```

```
def tzom_tevet(g_year):
    """Return the list of fixed dates for Tzom Tevet (Tevet 10) that
   occur in Gregorian year g_year. It can occur 0, 1 or 2 times per
   Gregorian year."""
   jan1 = gregorian_new_year(g_year)
         = standard_year(hebrew_from_fixed(jan1))
   d1 = fixed_from_hebrew(hebrew_date(y, TEVET, 10))
   d1 = (d1 + 1) if (day_of_week_from_fixed(d1) == SATURDAY) else d1
   d2 = fixed_from_hebrew(hebrew_date(y + 1, TEVET, 10))
   d2 = (d2 + 1) if (day_of_week_from_fixed(d2) == SATURDAY) else d2
   dates = [d1, d2]
   return list_range(dates, gregorian_year_range(g_year))
# this is a simplified version where no check for SATURDAY
# is performed: from hebrew year 1 till 2000000
# there is no TEVET 10 falling on Saturday...
def alt_tzom_tevet(g_year):
    """Return the list of fixed dates for Tzom Tevet (Tevet 10) that
   occur in Gregorian year g_year. It can occur 0, 1 or 2 times per
   Gregorian year.""
   return hebrew_in_gregorian(TEVET, 10, g_year)
# see lines 1842-1859 in calendrica-3.0.cl
def yom_ha_zikkaron(g_year):
    """Return fixed date of Yom ha_Zikkaron occurring in Gregorian
   year g_year."""
   hebrew_year = g_year - gregorian_year_from_fixed(HEBREW_EPOCH)
   iyyar4 = fixed_from_hebrew(hebrew_date(hebrew_year, IYYAR, 4))
   if (day_of_week_from_fixed(iyyar4) in [THURSDAY, FRIDAY]):
        return kday_before(WEDNESDAY, iyyar4)
    elif (SUNDAY == day_of_week_from_fixed(iyyar4)):
        return iyyar4 + 1
    else:
       return iyyar4
# see lines 1861-1879 in calendrica-3.0.cl
def hebrew_birthday(birthdate, h_year):
    """Return fixed date of the anniversary of Hebrew birth date
   birthdate occurring in Hebrew h_year."""
   birth_day = standard_day(birthdate)
   birth_month = standard_month(birthdate)
   birth_year = standard_year(birthdate)
   if (birth_month == last_month_of_hebrew_year(birth_year)):
        return fixed_from_hebrew(hebrew_date(h_year,
                                             last_month_of_hebrew_year(h_year),
                                             birth_day))
   else:
       return (fixed_from_hebrew(hebrew_date(h_year, birth_month, 1)) +
               birth_day - 1)
# see lines 1881-1893 in calendrica-3.0.cl
def hebrew_birthday_in_gregorian(birthdate, g_year):
   """Return the list of the fixed dates of Hebrew birthday
   birthday that occur in Gregorian g_year."""
   jan1 = gregorian_new_year(g_year)
   y = standard_year(hebrew_from_fixed(jan1))
   date1 = hebrew_birthday(birthdate, y)
   date2 = hebrew_birthday(birthdate, y + 1)
   return list_range([date1, date2], gregorian_year_range(g_year))
```

```
# see lines 1895-1937 in calendrica-3.0.cl
def yahrzeit(death_date, h_year):
    """Return fixed date of the anniversary of Hebrew death date death_date
   occurring in Hebrew h_year."""
   death_day = standard_day(death_date)
   death_month = standard_month(death_date)
   death_year = standard_year(death_date)
   if ((death_month == MARHESHVAN) and
        (death_day == 30) and
        (not is_long_marheshvan(death_year + 1))):
        return fixed_from_hebrew(hebrew_date(h_year, KISLEV, 1)) - 1
    elif ((death_month == KISLEV) and
          (death_day == 30) and
          is_short_kislev(death_year + 1)):
        return fixed_from_hebrew(hebrew_date(h_year, TEVET, 1)) - 1
    elif (death_month == ADARII):
        return fixed_from_hebrew(hebrew_date(h_year,
                                             last_month_of_hebrew_year(h_year),
                                             death_day))
   elif ((death_day == 30) and
          (death_month == ADAR) and
          (not is_hebrew_leap_year(h_year))):
        return fixed_from_hebrew(hebrew_date(h_year, SHEVAT, 30))
        return (fixed_from_hebrew(hebrew_date(h_year, death_month, 1)) +
               death_day - 1)
# see lines 1939-1951 in calendrica-3.0.cl
def yahrzeit_in_gregorian(death_date, g_year):
    """Return the list of the fixed dates of death date death_date (yahrzeit)
   that occur in Gregorian year g_year."""
   jan1 = gregorian_new_year(g_year)
   y = standard_year(hebrew_from_fixed(jan1))
   date1 = yahrzeit(death_date, y)
   date2 = yahrzeit(death_date, y + 1)
   return list_range([date1, date2], gregorian_year_range(g_year))
# see lines 1953-1960 in calendrica-3.0.cl
def shift_days(l, cap_Delta):
    """Shift each weekday on list 1 by cap_Delta days."""
   return map(lambda x: day_of_week_from_fixed(x + cap_Delta), 1)
# see lines 480-504 in calendrica-3.0.errata.cl
def possible_hebrew_days(h_month, h_day):
   """Return a list of possible days of week for Hebrew day h_{day}
   and Hebrew month h_month."""
   h_date0 = hebrew_date(5, NISAN, 1)
   h_year = 6 if (h_month > ELUL) else 5
   h_date = hebrew_date(h_year, h_month, h_day)
           = fixed_from_hebrew(h_date) - fixed_from_hebrew(h_date0)
   basic = [TUESDAY, THURSDAY, SATURDAY]
   if (h_month == MARHESHVAN) and (h_day == 30):
        extra = []
    elif (h_month == KISLEV) and (h_day < 30):</pre>
        extra = [MONDAY, WEDNESDAY, FRIDAY]
    elif (h_month == KISLEV) and (h_day == 30):
        extra = [MONDAY]
    elif h_month in [TEVET, SHEVAT]:
        extra = [SUNDAY, MONDAY]
```

```
elif (h_month == ADAR) and (h_day < 30):
            extra = [SUNDAY, MONDAY]
       else:
            extra = [SUNDAY]
       basic.extend(extra)
       return shift_days(basic, n)
This code is used in chunk 3.
Defines:
  ADAR, never used.
  ADARII, never used.
  alt_tzom_tevet, never used.
  AV. never used.
  birkath_ha_hama, used in chunk 81.
  days_in_hebrew_year, never used.
  ELUL, never used.
  fixed_from_hebrew, used in chunks 81, 142, and 176.
  hebrew_birthday, never used.
  hebrew_birthday_in_gregorian, never used.
  hebrew_calendar_elapsed_days, never used.
  hebrew_date, used in chunks 81, 142, 174, and 253.
  HEBREW_EPOCH, never used.
  hebrew_from_fixed, used in chunks 81, 142, and 176.
  hebrew_in_gregorian, never used.
  hebrew_new_year, never used.
  {\tt hebrew\_year\_length\_correction}, \ never \ used.
  is_hebrew_leap_year, never used.
  is_hebrew_sabbatical_year, never used.
  is_long_marheshvan, never used.
  is_short_kislev, never used.
  IYYAR, never used.
  KISLEV, used in chunk 81.
  last_day_of_hebrew_month, never used.
  last_month_of_hebrew_year, never used.
  MARHESHVAN, never used.
  molad, never used.
  NISAN, used in chunk 142.
  omer, never used.
  passover, never used.
  possible_hebrew_days, used in chunk 81.
  purim, never used.
  sh_ela, never used.
  SHEVAT, used in chunk 81.
  shift_days, never used.
  SIVAN, never used.
  ta_anit_esther, never used.
  TAMMUZ, never used.
  TEVET, never used.
  tishah_be_av, never used.
  TISHRI, used in chunk 142.
  tzom_tevet, used in chunk 81.
  yahrzeit, never used.
  yahrzeit_in_gregorian, never used.
  yom_ha_zikkaron, never used.
  yom_kippur, never used.
Uses bce 59, BOGUS 13, coptic_from_fixed 71, coptic_in_gregorian 71, day_of_week_from_fixed 38,
  days_from_hours 100, epoch 37, final 19, fixed_from_julian 59, FRIDAY 38, gregorian_new_year 56,
  gregorian_year_from_fixed 55, gregorian_year_range 56, julian_date 59, kday_before 56,
  list_range 47, mod 15, MONDAY 38, next 16, OCTOBER 53, quotient 14 14, SATURDAY 38,
  standard_day 39, standard_month 39, standard_year 39, start 47, summa 22, SUNDAY 38,
  THURSDAY 38, TUESDAY 38, and WEDNESDAY 38.
```

```
81
       \langle hebrew\ calendar\ unit\ test\ 81 \rangle \equiv
         class HebrewSmokeTestCase(unittest.TestCase):
              def setUp(self):
                   self.testvalue = 710347
              def testConversionFromFixed(self):
                   self.assertEqual(
                       hebrew_from_fixed(self.testvalue), hebrew_date(5706, KISLEV, 7))
              def testConversionToFixed(self):
                   self.assertEqual(
                       self.testvalue, fixed_from_hebrew(hebrew_date(5706, KISLEV, 7)))
         class HebrewHolidaysTestCase(unittest.TestCase):
              def testBirkathHaHama(self):
                   self.assertNotEqual(birkath_ha_hama(1925), [])
                   self.assertEqual(birkath_ha_hama(1926), [])
                   self.assertNotEqual(birkath_ha_hama(1925+28), [])
              def testTzomTevet(self):
                   """test tzom tevet (Tevet 10): see page 104"""
                   self.assertEqual(len(tzom_tevet(1982)), 2)
                   self.assertEqual(len(tzom_tevet(1984)), 0)
              def testPossibleHebrewDays(self):
                   """see page 110, Calendrical Calculations, 3rd edition."""
                   self.assertEqual(set(possible_hebrew_days(SHEVAT, 15)),
                                set([THURSDAY, SATURDAY, MONDAY, TUESDAY, WEDNESDAY]))
       This definition is continued in chunk 175.
       This code is used in chunks 4 and 82.
       Defines:
         HebrewHolidaysTestCase, never used.
         HebrewSmokeTestCase, never used.
         testBirkathHaHama, never used.
         testPossibleHebrewDays, never used.
         testTzomTevet, never used.
       Uses birkath_ha_hama 80, fixed_from_hebrew 80, hebrew_date 80, hebrew_from_fixed 80, KISLEV 80,
         MONDAY 38, possible_hebrew_days 80, SATURDAY 38, SHEVAT 80, THURSDAY 38, TUESDAY 38,
         tzom_tevet 80, and WEDNESDAY 38.
       2.10.1 Unit tests
       \langle hebrewCalendarUnitTest.py 82 \rangle \equiv
82
         # \(\langle generated code warning 1 \rangle \)
          \langle import\ for\ testing\ 6 \rangle
         from appendixCUnitTest import AppendixCTable3TestCaseBase
          ⟨hebrew calendar unit test 81⟩
          \langle execute \ tests \ 5 \rangle
       Root chunk (not used in this document).
       Uses AppendixCTable3TestCaseBase 174.
```

2.11 Mayan Calendars

```
83
      \langle mayan \ calendars \ 83 \rangle \equiv
        ####################################
        # mayan calendars algorithms #
        # see lines 1989-1992 in calendrica-3.0.cl
        def mayan_long_count_date(baktun, katun, tun, uinal, kin):
            """Return a long count Mayan date data structure."""
            return [baktun, katun, tun, uinal, kin]
        # see lines 1994-1996 in calendrica-3.0.cl
        def mayan_haab_date(month, day):
            """Return a Haab Mayan date data structure."""
            return [month, day]
        # see lines 1998-2001 in calendrica-3.0.cl
        def mayan_tzolkin_date(number, name):
            """Return a Tzolkin Mayan date data structure."""
            return [number, name]
        # see lines 2003-2005 in calendrica-3.0.cl
        def mayan_baktun(date):
            """Return the baktun field of a long count Mayan
            date = [baktun, katun, tun, uinal, kin]."""
            return date[0]
        # see lines 2007-2009 in calendrica-3.0.cl
        def mayan_katun(date):
            """Return the katun field of a long count Mayan
            date = [baktun, katun, tun, uinal, kin]."""
            return date[1]
        # see lines 2011-2013 in calendrica-3.0.cl
        def mayan tun(date):
            """Return the tun field of a long count Mayan
            date = [baktun, katun, tun, uinal, kin]."""
            return date[2]
        # see lines 2015-2017 in calendrica-3.0.cl
        def mayan_uinal(date):
            """Return the uinal field of a long count Mayan
            date = [baktun, katun, tun, uinal, kin]."""
            return date[3]
        # see lines 2019-2021 in calendrica-3.0.cl
        def mayan_kin(date):
            """Return the kin field of a long count Mayan
            date = [baktun, katun, tun, uinal, kin]."""
            return date[4]
        # see lines 2023-2025 in calendrica-3.0.cl
        def mayan_haab_month(date):
            """Return the month field of Haab Mayan date = [month, day]."""
            return date[0]
        # see lines 2027-2029 in calendrica-3.0.cl
        def mayan_haab_day(date):
            """Return the day field of Haab Mayan date = [month, day]."""
            return date[1]
```

```
# see lines 2031-2033 in calendrica-3.0.cl
def mayan_tzolkin_number(date):
    """Return the number field of Tzolkin Mayan date = [number, name]."""
   return date[0]
# see lines 2035-2037 in calendrica-3.0.cl
def mayan_tzolkin_name(date):
    """Return the name field of Tzolkin Mayan date = [number, name]."""
   return date[1]
# see lines 2039-2044 in calendrica-3.0.cl
MAYAN_EPOCH = fixed_from_jd(584283)
# see lines 2046-2060 in calendrica-3.0.cl
def fixed_from_mayan_long_count(count):
    """Return fixed date corresponding to the Mayan long count count,
   which is a list [baktun, katun, tun, uinal, kin]."""
   baktun = mayan_baktun(count)
   katun = mayan_katun(count)
         = mayan_tun(count)
   tun
   uinal = mayan_uinal(count)
          = mayan_kin(count)
   return (MAYAN_EPOCH
            (baktun * 144000) +
            (katun * 7200) +
            (tun * 360)
            (uinal * 20)
           kin)
# see lines 2062-2074 in calendrica-3.0.cl
def mayan_long_count_from_fixed(date):
    """Return Mayan long count date of fixed date date."""
   long_count = date - MAYAN_EPOCH
   baktun, day_of_baktun = divmod(long_count, 144000)
   katun, day_of_katun = divmod(day_of_baktun, 7200)
                          = divmod(day_of_katun, 360)
   tun, day_of_tun
   uinal, kin
                          = divmod(day_of_tun, 20)
   return mayan_long_count_date(baktun, katun, tun, uinal, kin)
# see lines 2076-2081 in calendrica-3.0.cl
def mayan_haab_ordinal(h_date):
    """Return the number of days into cycle of Mayan haab date h_date."""
   day = mayan_haab_day(h_date)
   month = mayan_haab_month(h_date)
   return ((month - 1) * 20) + day
# see lines 2083-2087 in calendrica-3.0.cl
MAYAN_HAAB_EPOCH = MAYAN_EPOCH - mayan_haab_ordinal(mayan_haab_date(18, 8))
# see lines 2089-2096 in calendrica-3.0.cl
def mayan_haab_from_fixed(date):
    """Return Mayan haab date of fixed date date."""
   count = mod(date - MAYAN_HAAB_EPOCH, 365)
   day = mod(count, 20)
   month = quotient(count, 20) + 1
   return mayan_haab_date(month, day)
# see lines 2098-2105 in calendrica-3.0.cl
def mayan_haab_on_or_before(haab, date):
    """Return fixed date of latest date on or before fixed date date
   that is Mayan haab date haab."""
```

```
return date - mod(date - MAYAN_HAAB_EPOCH - mayan_haab_ordinal(haab), 365)
# see lines 2107-2114 in calendrica-3.0.cl
def mayan_tzolkin_ordinal(t_date):
    """Return number of days into Mayan tzolkin cycle of t_date."""
   number = mayan_tzolkin_number(t_date)
   name = mayan_tzolkin_name(t_date)
   return mod(number - 1 + (39 * (number - name)), 260)
# see lines 2116-2120 in calendrica-3.0.cl
MAYAN_TZOLKIN_EPOCH = (MAYAN_EPOCH -
                       mayan_tzolkin_ordinal(mayan_tzolkin_date(4, 20)))
# see lines 2122-2128 in calendrica-3.0.cl
def mayan_tzolkin_from_fixed(date):
    """Return Mayan tzolkin date of fixed date date."""
   count = date - MAYAN_TZOLKIN_EPOCH + 1
   number = amod(count, 13)
   name = amod(count, 20)
   return mayan_tzolkin_date(number, name)
# see lines 2130-2138 in calendrica-3.0.cl
def mayan_tzolkin_on_or_before(tzolkin, date):
    """Return fixed date of latest date on or before fixed date date
   that is Mayan tzolkin date tzolkin."""
   return (date -
           mod(date -
               MAYAN_TZOLKIN_EPOCH -
               mayan_tzolkin_ordinal(tzolkin), 260))
# see lines 2140-2150 in calendrica-3.0.cl
def mayan_year_bearer_from_fixed(date):
    """Return year bearer of year containing fixed date date.
   Returns BOGUS for uayeb."""
   x = mayan_haab_on_or_before(mayan_haab_date(1, 0), date + 364)
   return (BOGUS if (mayan_haab_month(mayan_haab_from_fixed(date)) == 19)
           else mayan_tzolkin_name(mayan_tzolkin_from_fixed(x)))
# see lines 2152-2168 in calendrica-3.0.cl
def mayan_calendar_round_on_or_before(haab, tzolkin, date):
    """Return fixed date of latest date on or before date, that is
   Mayan haab date haab and tzolkin date tzolkin.
   Returns BOGUS for impossible combinations."""
   haab_count = mayan_haab_ordinal(haab) + MAYAN_HAAB_EPOCH
   tzolkin_count = mayan_tzolkin_ordinal(tzolkin) + MAYAN_TZOLKIN_EPOCH
   diff = tzolkin_count - haab_count
   if mod(diff, 5) == 0:
       return date - mod(date - haab_count(365 * diff), 18980)
   else:
       return BOGUS
# see lines 2170-2173 in calendrica-3.0.cl
def aztec_xihuitl_date(month, day):
   """Return an Aztec xihuitl date data structure."""
   return [month, day]
# see lines 2175-2177 in calendrica-3.0.cl
def aztec_xihuitl_month(date):
    """Return the month field of an Aztec xihuitl date = [month, day]."""
   return date[0]
```

```
# see lines 2179-2181 in calendrica-3.0.cl
def aztec_xihuitl_day(date):
   """Return the day field of an Aztec xihuitl date = [month, day]."""
   return date[1]
# see lines 2183-2186 in calendrica-3.0.cl
def aztec_tonalpohualli_date(number, name):
    """Return an Aztec tonalpohualli date data structure."""
   return [number, name]
# see lines 2188-2191 in calendrica-3.0.cl
def aztec_tonalpohualli_number(date):
   """Return the number field of an Aztec tonalpohualli
   date = [number, name]."""
   return date[0]
# see lines 2193-2195 in calendrica-3.0.cl
def aztec_tonalpohualli_name(date):
    """Return the name field of an Aztec tonalpohualli
   date = [number, name]."""
   return date[1]
# see lines 2197-2200 in calendrica-3.0.cl
def aztec_xiuhmolpilli_designation(number, name):
    """Return an Aztec xiuhmolpilli date data structure."""
   return [number, name]
# see lines 2202-2205 in calendrica-3.0.cl
def aztec_xiuhmolpilli_number(date):
    """Return the number field of an Aztec xiuhmolpilli
   date = [number, name]."""
   return date[0]
# see lines 2207-2210 in calendrica-3.0.cl
def aztec_xiuhmolpilli_name(date):
    """Return the name field of an Aztec xiuhmolpilli
   date = [number, name]."""
   return date[1]
# see lines 2212-2215 in calendrica-3.0.cl
AZTEC_CORRELATION = fixed_from_julian(julian_date(1521, AUGUST, 13))
# see lines 2217-2223 in calendrica-3.0.cl
def aztec_xihuitl_ordinal(x_date):
   """Return the number of elapsed days into cycle of Aztec xihuitl
   date x_date."""
   day = aztec_xihuitl_day(x_date)
   month = aztec_xihuitl_month(x_date)
   return ((month - 1) * 20) + day - 1
# see lines 2225-2229 in calendrica-3.0.cl
AZTEC_XIHUITL_CORRELATION = (AZTEC_CORRELATION -
                              aztec_xihuitl_ordinal(aztec_xihuitl_date(11, 2)))
# see lines 2231-2237 in calendrica-3.0.cl
def aztec_xihuitl_from_fixed(date):
    """Return Aztec xihuitl date of fixed date date."""
   count = mod(date - AZTEC_XIHUITL_CORRELATION, 365)
   day = mod(count, 20) + 1
   month = quotient(count, 20) + 1
```

```
return aztec_xihuitl_date(month, day)
# see lines 2239-2246 in calendrica-3.0.cl
def aztec_xihuitl_on_or_before(xihuitl, date):
    """Return fixed date of latest date on or before fixed date date
   that is Aztec xihuitl date xihuitl."""
   return (date -
           mod(date -
                AZTEC_XIHUITL_CORRELATION -
                aztec_xihuitl_ordinal(xihuitl), 365))
# see lines 2248-2255 in calendrica-3.0.cl
def aztec_tonalpohualli_ordinal(t_date):
   """Return the number of days into Aztec tonalpohualli cycle of t_date."""
   number = aztec_tonalpohualli_number(t_date)
   name = aztec_tonalpohualli_name(t_date)
   return mod(number - 1 + 39 * (number - name), 260)
# see lines 2257-2262 in calendrica-3.0.cl
AZTEC_TONALPOHUALLI_CORRELATION = (AZTEC_CORRELATION -
                                    aztec_tonalpohualli_ordinal(
                                        aztec_tonalpohualli_date(1, 5)))
# see lines 2264-2270 in calendrica-3.0.cl
def aztec_tonalpohualli_from_fixed(date):
    """Return Aztec tonalpohualli date of fixed date date."""
   count = date - AZTEC_TONALPOHUALLI_CORRELATION + 1
   number = amod(count, 13)
   name = amod(count, 20)
   return aztec_tonalpohualli_date(number, name)
# see lines 2272-2280 in calendrica-3.0.cl
def aztec_tonalpohualli_on_or_before(tonalpohualli, date):
    """Return fixed date of latest date on or before fixed date date
   that is Aztec tonalpohualli date tonalpohualli."""
   return (date -
           mod(date -
                AZTEC_TONALPOHUALLI_CORRELATION -
               aztec_tonalpohualli_ordinal(tonalpohualli), 260))
# see lines 2282-2303 in calendrica-3.0.cl
def aztec_xihuitl_tonalpohualli_on_or_before(xihuitl, tonalpohualli, date):
   """Return fixed date of latest xihuitl_tonalpohualli combination
   on or before date date. That is the date on or before
   date date that is Aztec xihuitl date xihuitl and
   tonalpohualli date tonalpohualli.
   Returns BOGUS for impossible combinations."""
   xihuitl_count = aztec_xihuitl_ordinal(xihuitl) + AZTEC_XIHUITL_CORRELATION
   tonalpohualli_count = (aztec_tonalpohualli_ordinal(tonalpohualli) +
                           AZTEC_TONALPOHUALLI_CORRELATION)
   diff = tonalpohualli_count - xihuitl_count
    if mod(diff, 5) == 0:
       return date - mod(date - xihuitl_count - (365 * diff), 18980)
    else:
       return BOGUS
# see lines 2305-2316 in calendrica-3.0.cl
def aztec_xiuhmolpilli_from_fixed(date):
    """Return designation of year containing fixed date date.
   Returns BOGUS for nemontemi."""
   x = aztec_xihuitl_on_or_before(aztec_xihuitl_date(18, 20), date + 364)
```

```
month = aztec_xihuitl_month(aztec_xihuitl_from_fixed(date))
return BOGUS if (month == 19) else aztec_tonalpohualli_from_fixed(x)
```

```
This code is used in chunk 3.
Defines:
  AZTEC_CORRELATION, never used.
  AZTEC_TONALPOHUALLI_CORRELATION, never used.
  aztec_tonalpohualli_date, used in chunk 165.
  aztec_tonalpohualli_from_fixed, used in chunk 173.
  aztec_tonalpohualli_name, never used.
  aztec_tonalpohualli_number, never used.
  aztec_tonalpohualli_on_or_before, never used.
  aztec_tonalpohualli_ordinal, never used.
  AZTEC_XIHUITL_CORRELATION, never used.
  aztec_xihuitl_date, used in chunks 84 and 165.
  aztec_xihuitl_day, never used.
  aztec_xihuitl_from_fixed, used in chunks 84 and 173.
  aztec_xihuitl_month, never used.
  \verb"aztec_xihuitl_on_or_before", used in chunk § 4.
  aztec_xihuitl_ordinal, never used.
  {\tt aztec\_xihuitl\_tonalpohualli\_on\_or\_before,\ never\ used}.
  {\tt aztec\_xiuhmolpilli\_designation}, \ never \ used.
  aztec_xiuhmolpilli_from_fixed, never used.
  aztec_xiuhmolpilli_name, never used.
  aztec_xiuhmolpilli_number, never used.
  {\tt fixed\_from\_mayan\_long\_count}, \ {\tt used} \ {\tt in} \ {\tt chunks} \ {\tt 84} \ {\tt and} \ {\tt 173}.
  mayan_baktun, never used.
  mayan_calendar_round_on_or_before, never used.
  MAYAN_EPOCH, never used.
  mayan_haab_date, used in chunks 84 and 165.
  mayan_haab_day, never used.
  MAYAN_HAAB_EPOCH, never used.
  mayan_haab_from_fixed, used in chunks 84 and 173.
  mayan_haab_month, never used.
  \verb|mayan_haab_on_or_before|, used in chunk 84|.
  mayan_haab_ordinal, never used.
  mayan katun, never used.
  mayan_kin, never used.
  mayan_long_count_date, used in chunks 84 and 165.
  mayan_long_count_from_fixed, used in chunks 84 and 173.
  mayan_tun, never used.
  mayan_tzolkin_date, used in chunks 84 and 165.
  MAYAN_TZOLKIN_EPOCH, never used.
  mayan_tzolkin_from_fixed, used in chunks 84 and 173.
  mayan_tzolkin_name, never used.
  mayan_tzolkin_number, never used.
  mayan_tzolkin_on_or_before, used in chunk 84.
  mayan tzolkin ordinal, never used.
  mayan_uinal, never used.
  mayan_year_bearer_from_fixed, never used.
Uses amod 15, AUGUST 53, BOGUS 13, fixed_from_jd 48, fixed_from_julian 59, julian_date 59, mod 15,
  and quotient 14 14.
```

```
84
       \langle mayan \ calendars \ unit \ test \ 84 \rangle \equiv
         class MayanSmokeTestCase(unittest.TestCase):
             def setUp(self):
                 self.testvalue = 710347
             def testConversionFromFixed(self):
                 self.assertEqual(mayan_long_count_from_fixed(self.testvalue),
                                   mayan_long_count_date(12, 16, 11, 16, 9))
                 self.assertEqual(mayan_long_count_from_fixed(0),
                                   mayan_long_count_date(7, 17, 18, 13, 2))
                 self.assertEqual(mayan_haab_from_fixed(self.testvalue),
                                   mayan_haab_date(11, 7))
                 self.assertEqual(mayan_tzolkin_from_fixed(self.testvalue),
                                   mayan_tzolkin_date(11, 9))
             def testConversionToFixed(self):
                 self.assertEqual(
                     self.testvalue,
                     fixed_from_mayan_long_count(
                          mayan_long_count_date(12, 16, 11, 16, 9)))
                 self.assertEqual(
                     rd(0),
                      fixed_from_mayan_long_count(
                          mayan_long_count_date(7, 17, 18, 13, 2)))
                 self.assertEqual(
                     mayan_haab_on_or_before(mayan_haab_date(11, 7), self.testvalue),
                      self.testvalue)
                 self.assertEqual(
                     mayan_tzolkin_on_or_before(
                          mayan_tzolkin_date(11, 9), self.testvalue),
                      self.testvalue)
         class AztecSmokeTestCase(unittest.TestCase):
             def setUp(self):
                 self.testvalue = 710347
             def testConversionFromFixed(self):
                 self.assertEqual(
                     aztec_xihuitl_from_fixed(self.testvalue),
                     aztec_xihuitl_date(2, 1))
             def testConversionToFixed(self):
                 self.assertEqual(
                      aztec_xihuitl_on_or_before(
                          aztec_xihuitl_date(2, 1), self.testvalue),
                      self.testvalue)
       This definition is continued in chunk 172.
       This code is used in chunks 4 and 85.
       Defines:
         AztecSmokeTestCase, never used.
         MayanSmokeTestCase, never used.
       Uses aztec_xihuitl_date 83, aztec_xihuitl_from_fixed 83, aztec_xihuitl_on_or_before 83,
         fixed_from_mayan_long_count 83, mayan_haab_date 83, mayan_haab_from_fixed 83,
         mayan_haab_on_or_before 83, mayan_long_count_date 83, mayan_long_count_from_fixed 83,
         mayan_tzolkin_date 83, mayan_tzolkin_from_fixed 83, mayan_tzolkin_on_or_before 83, and rd 37.
```

2.11.1 Unit tests

85 $\langle mayanCalendarsUnitTest.py 85 \rangle \equiv$ # $\langle generated\ code\ warning\ 1 \rangle$ $\langle import\ for\ testing\ 6 \rangle$ from appendixCUnitTest import AppendixCTable2TestCaseBase $\langle mayan\ calendars\ unit\ test\ 84 \rangle$ $\langle execute\ tests\ 5 \rangle$

Root chunk (not used in this document). Uses AppendixCTable2TestCaseBase 165.

2.12 Old Hindu Calendars

```
⟨old hindu calendars 86⟩≡
86
        # old hindu calendars algorithms #
        # see lines 2321-2325 in calendrica-3.0.cl
        def old_hindu_lunar_date(year, month, leap, day):
            """Return an Old Hindu lunar date data structure."""
            return [year, month, leap, day]
        # see lines 2327-2329 in calendrica-3.0.cl
        def old_hindu_lunar_month(date):
            """Return the month field of an Old Hindu lunar
            date = [year, month, leap, day]."""
            return date[1]
        # see lines 2331-2333 in calendrica-3.0.cl
        def old_hindu_lunar_leap(date):
            """Return the leap field of an Old Hindu lunar
            date = [year, month, leap, day]."""
            return date[2]
        # see lines 2335-2337 in calendrica-3.0.cl
        def old_hindu_lunar_day(date):
            """Return the day field of an Old Hindu lunar
            date = [year, month, leap, day]."""
            return date[3]
        # see lines 2339-2341 in calendrica-3.0.cl
        def old_hindu_lunar_year(date):
            """Return the year field of an Old Hindu lunar
            date = [year, month, leap, day]."""
            return date[0]
        # see lines 2343-2346 in calendrica-3.0.cl
        def hindu_solar_date(year, month, day):
            """Return an Hindu solar date data structure."""
            return [year, month, day]
        # see lines 2348-2351 in calendrica-3.0.cl
        HINDU_EPOCH = fixed_from_julian(julian_date(bce(3102), FEBRUARY, 18))
        # see lines 2353-2356 in calendrica-3.0.cl
        def hindu_day_count(date):
            """Return elapsed days (Ahargana) to date date since Hindu epoch (KY)."""
            return date - HINDU_EPOCH
        # see lines 2358-2361 in calendrica-3.0.cl
        ARYA_SOLAR_YEAR = 1577917500/4320000
        # see lines 2363-2366 in calendrica-3.0.cl
        ARYA_SOLAR_MONTH = ARYA_SOLAR_YEAR / 12
        # see lines 2368-2378 in calendrica-3.0.cl
        def old_hindu_solar_from_fixed(date):
            """Return Old Hindu solar date equivalent to fixed date date."""
            sun = hindu_day_count(date) + days_from_hours(6)
            year = quotient(sun, ARYA_SOLAR_YEAR)
            month = mod(quotient(sun, ARYA_SOLAR_MONTH), 12) + 1
```

```
day = ifloor(mod(sun, ARYA_SOLAR_MONTH)) + 1
    return hindu_solar_date(year, month, day)
# see lines 2380-2390 in calendrica-3.0.cl
# The following
      from math import ceil as ceiling
\mbox{\tt\#} is not ok, the corresponding CL code
# uses CL ceiling which always returns and integer, while
# ceil from math module always returns a float...so I redefine it
def ceiling(n):
    """Return the integer rounded towards +infinitum of n."""
    from math import ceil
    return int(ceil(n))
def fixed_from_old_hindu_solar(s_date):
    """Return fixed date corresponding to Old Hindu solar date s_date."""
    month = standard_month(s_date)
    day = standard_day(s_date)
    year = standard_year(s_date)
    return ceiling(HINDU_EPOCH
                year * ARYA_SOLAR_YEAR
                (month - 1) * ARYA_SOLAR_MONTH +
                day + days_from_hours(-30))
# see lines 2392-2395 in calendrica-3.0.cl
ARYA_LUNAR_MONTH = 1577917500/53433336
# see lines 2397-2400 in calendrica-3.0.cl
ARYA_LUNAR_DAY = ARYA_LUNAR_MONTH / 30
# see lines 2402-2409 in calendrica-3.0.cl
def is_old_hindu_lunar_leap_year(l_year):
    """Return True if l_year is a leap year on the
    old Hindu calendar."""
    return mod(l_year * ARYA_SOLAR_YEAR - ARYA_SOLAR_MONTH,
               ARYA_LUNAR_MONTH) >= 23902504679/1282400064
# see lines 2411-2431 in calendrica-3.0.cl
def old_hindu_lunar_from_fixed(date):
    """Return Old Hindu lunar date equivalent to fixed date date."""
    sun = hindu_day_count(date) + days_from_hours(6)
    new_moon = sun - mod(sun, ARYA_LUNAR_MONTH)
    leap = (((ARYA_SOLAR_MONTH - ARYA_LUNAR_MONTH)
             >=
             mod(new_moon, ARYA_SOLAR_MONTH))
            (mod(new_moon, ARYA_SOLAR_MONTH) > 0))
    month = mod(ceiling(new_moon / ARYA_SOLAR_MONTH), 12) + 1
    day = mod(quotient(sun, ARYA_LUNAR_DAY), 30) + 1
    year = ceiling((new_moon + ARYA_SOLAR_MONTH) / ARYA_SOLAR_YEAR) - 1
    return old_hindu_lunar_date(year, month, leap, day)
# see lines 2433-2460 in calendrica-3.0.cl
def fixed_from_old_hindu_lunar(l_date):
    """Return fixed date corresponding to Old Hindu lunar date l_date."""
    year = old_hindu_lunar_year(l_date)
    month = old_hindu_lunar_month(l_date)
    leap = old_hindu_lunar_leap(l_date)
    day = old_hindu_lunar_day(l_date)
    mina = ((12 * year) - 1) * ARYA_SOLAR_MONTH
    lunar_new_year = ARYA_LUNAR_MONTH * (quotient(mina, ARYA_LUNAR_MONTH) + 1)
```

```
if ((not leap) and
            (ceiling((lunar_new_year - mina) / (ARYA_SOLAR_MONTH - ARYA_LUNAR_MONTH))
             <= month)):
            temp = month
       else:
           temp = month - 1
       temp = (HINDU_EPOCH
                lunar_new_year +
                 (ARYA_LUNAR_MONTH * temp) +
                 ((day - 1) * ARYA_LUNAR_DAY) +
                days_from_hours(-6))
       return ceiling(temp)
  # see lines 2462-2466 in calendrica-3.0.cl
  ARYA_JOVIAN_PERIOD = 1577917500/364224
  # see lines 2468-2473 in calendrica-3.0.cl
  def jovian_year(date):
       """Return year of Jupiter cycle at fixed date date."""
       return amod(quotient(hindu_day_count(date), ARYA_JOVIAN_PERIOD / 12) + 27,
This code is used in chunk 3.
Defines:
  ARYA_JOVIAN_PERIOD, never used.
  ARYA_LUNAR_DAY, never used.
  ARYA\_LUNAR\_MONTH, never used.
  ARYA_SOLAR_MONTH, never used.
  ARYA_SOLAR_YEAR, never used.
  ceiling, used in chunks 122, 133, 136, and 139.
  fixed_from_old_hindu_lunar, used in chunks 87 and 189.
  {\tt fixed\_from\_old\_hindu\_solar}, \ {\rm used} \ {\rm in} \ {\rm chunks} \ 87 \ {\rm and} \ 189.
  hindu_day_count, never used.
  HINDU_EPOCH, used in chunk 136.
  hindu_solar_date, used in chunks 87, 136, and 185.
  is_old_hindu_lunar_leap_year, never used.
  jovian_year, used in chunk 87.
  old_hindu_lunar_date, used in chunks 87 and 185.
  old_hindu_lunar_day, never used.
  {\tt old\_hindu\_lunar\_from\_fixed}, \, {\rm used} \, \, {\rm in} \, \, {\rm chunks} \, \, 87 \, \, {\rm and} \, \, 189.
  old_hindu_lunar_leap, never used.
  old_hindu_lunar_month, never used.
  old_hindu_lunar_year, never used.
  old_hindu_solar_from_fixed, used in chunks 87 and 189.
Uses amod 15, bce 59, days_from_hours 100, epoch 37, FEBRUARY 53, fixed_from_julian 59,
  ifloor 15, julian_date 59, mod 15, quotient 14 14, standard_day 39, standard_month 39,
  and standard_year 39.
```

```
\langle old\ hindu\ calendars\ unit\ test\ 87 \rangle \equiv
87
         class OldHinduSmokeTestCase(unittest.TestCase):
              def setUp(self):
                   self.testvalue = 710347
              def testConversionFromFixed(self):
                   self.assertEqual(
                       old_hindu_solar_from_fixed(self.testvalue),
                       hindu_solar_date(5046, 7, 29))
                   self.assertEqual(
                       old_hindu_lunar_from_fixed(self.testvalue),
                       old_hindu_lunar_date(5046, 8, False, 8))
                   # FIXME (not sure the check is correct)
                   self.assertEqual(jovian_year(self.testvalue), 32)
              def testConversionToFixed(self):
                   self.assertEqual(
                       self.testvalue,
                       fixed_from_old_hindu_solar(hindu_solar_date(5046, 7, 29)))
                   self.assertEqual(
                       self.testvalue,
                       fixed_from_old_hindu_lunar(
                            old_hindu_lunar_date(5046, 8, False, 8)))
       This definition is continued in chunk 188.
       This code is used in chunks 4 and 88.
       Defines:
         OldHinduSmokeTestCase, never used.
       Uses fixed_from_old_hindu_lunar 86, fixed_from_old_hindu_solar 86, hindu_solar_date
         86, jovian_year 86, old_hindu_lunar_date 86, old_hindu_lunar_from_fixed 86,
         and old_hindu_solar_from_fixed 86.
       2.12.1 Unit tests
       \langle oldHinduCalendarsUnitTest.py\ 88 \rangle \equiv
88
         # \(\langle generated code warning \mathbf{1}\rangle\)
         ⟨import for testing 6⟩
         from appendixCUnitTest import AppendixCTable4TestCaseBase
         ⟨old hindu calendars unit test 87⟩
         \langle execute \ tests \ 5 \rangle
       Root chunk (not used in this document).
```

Uses AppendixCTable4TestCaseBase 185.

2.13 Balinese Calendar

```
\langle balinese \ calendar \ 89 \rangle \equiv
89
        # balinese calendar algorithms #
        ###################################
        # see lines 2478-2481 in calendrica-3.0.cl
        def balinese_date(b1, b2, b3, b4, b5, b6, b7, b8, b9, b0):
             """Return a Balinese date data structure."""
            return [b1, b2, b3, b4, b5, b6, b7, b8, b9, b0]
        # see lines 2483-2485 in calendrica-3.0.cl
        def bali_luang(b_date):
            return b_date[0]
        # see lines 2487-2489 in calendrica-3.0.cl
        def bali_dwiwara(b_date):
            return b_date[1]
        # see lines 2491-2493 in calendrica-3.0.cl
        def bali_triwara(b_date):
            return b_date[2]
        # see lines 2495-2497 in calendrica-3.0.cl
        def bali_caturwara(b_date):
            return b_date[3]
        # see lines 2499-2501 in calendrica-3.0.cl
        def bali_pancawara(b_date):
            return b_date[4]
        # see lines 2503-2505 in calendrica-3.0.cl
        def bali_sadwara(b_date):
            return b_date[5]
        # see lines 2507-2509 in calendrica-3.0.cl
        def bali_saptawara(b_date):
            return b_date[6]
        # see lines 2511-2513 in calendrica-3.0.cl
        def bali_asatawara(b_date):
            return b_date[7]
        # see lines 2513-2517 in calendrica-3.0.cl
        def bali_sangawara(b_date):
            return b_date[8]
        # see lines 2519-2521 in calendrica-3.0.cl
        def bali_dasawara(b_date):
            return b_date[9]
        # see lines 2523-2526 in calendrica-3.0.cl
        BALI_EPOCH = fixed_from_jd(146)
        # see lines 2528-2531 in calendrica-3.0.cl
        def bali_day_from_fixed(date):
             """Return the position of date date in 210_day Pawukon cycle."""
            return mod(date - BALI_EPOCH, 210)
        def even(i):
            return mod(i, 2) == 0
```

```
def odd(i):
   return not even(i)
# see lines 2533-2536 in calendrica-3.0.cl
def bali_luang_from_fixed(date):
    """Check membership of date date in "1_day" Balinese cycle."""
   return even(bali_dasawara_from_fixed(date))
# see lines 2538-2541 in calendrica-3.0.cl
def bali_dwiwara_from_fixed(date):
   """Return the position of date date in 2_day Balinese cycle."""
   return amod(bali_dasawara_from_fixed(date), 2)
# see lines 2543-2546 in calendrica-3.0.cl
def bali_triwara_from_fixed(date):
    """Return the position of date date in 3_day Balinese cycle."""
   return mod(bali_day_from_fixed(date), 3) + 1
# see lines 2548-2551 in calendrica-3.0.cl
def bali_caturwara_from_fixed(date):
    """Return the position of date date in 4_day Balinese cycle."""
   return amod(bali_asatawara_from_fixed(date), 4)
# see lines 2553-2556 in calendrica-3.0.cl
def bali_pancawara_from_fixed(date):
    """Return the position of date date in 5_day Balinese cycle."""
   return amod(bali_day_from_fixed(date) + 2, 5)
# see lines 2558-2561 in calendrica-3.0.cl
def bali_sadwara_from_fixed(date):
    """Return the position of date date in 6_day Balinese cycle."""
   return mod(bali_day_from_fixed(date), 6) + 1
# see lines 2563-2566 in calendrica-3.0.cl
def bali_saptawara_from_fixed(date):
    """Return the position of date date in Balinese week."""
   return mod(bali_day_from_fixed(date), 7) + 1
# see lines 2568-2576 in calendrica-3.0.cl
def bali_asatawara_from_fixed(date):
    """Return the position of date date in 8_day Balinese cycle."""
   day = bali_day_from_fixed(date)
   return mod(max(6, 4 + mod(day - 70, 210)), 8) + 1
# see lines 2578-2583 in calendrica-3.0.cl
def bali_sangawara_from_fixed(date):
    """Return the position of date date in 9_day Balinese cycle."""
   return mod(max(0, bali_day_from_fixed(date) - 3), 9) + 1
# see lines 2585-2594 in calendrica-3.0.cl
def bali_dasawara_from_fixed(date):
   """Return the position of date date in 10_day Balinese cycle."""
   i = bali_pancawara_from_fixed(date) - 1
    j = bali_saptawara_from_fixed(date) - 1
   return mod(1 + [5, 9, 7, 4, 8][i] + [5, 4, 3, 7, 8, 6, 9][j], 10)
# see lines 2596-2609 in calendrica-3.0.cl
def bali_pawukon_from_fixed(date):
    """Return the positions of date date in ten cycles of Balinese Pawukon
   calendar."""
```

```
return balinese_date(bali_luang_from_fixed(date),
                           bali_dwiwara_from_fixed(date),
                            bali_triwara_from_fixed(date),
                            bali_caturwara_from_fixed(date),
                            bali_pancawara_from_fixed(date),
                            bali_sadwara_from_fixed(date),
                            bali_saptawara_from_fixed(date),
                            bali_asatawara_from_fixed(date),
                            bali_sangawara_from_fixed(date),
                            bali_dasawara_from_fixed(date))
  # see lines 2611-2614 in calendrica-3.0.cl
  def bali_week_from_fixed(date):
      """Return the week number of date date in Balinese cycle."""
      return quotient(bali_day_from_fixed(date), 7) + 1
  # see lines 2616-2630 in calendrica-3.0.cl
  def bali_on_or_before(b_date, date):
      """Return last fixed date on or before date with Pawukon date b_date."""
      a5 = bali_pancawara(b_date) - 1
      a6 = bali_sadwara(b_date)
                                 - 1
      b7 = bali_saptawara(b_date) - 1
      b35 = mod(a5 + 14 + (15 * (b7 - a5)), 35)
      days = a6 + (36 * (b35 - a6))
      cap_Delta = bali_day_from_fixed(0)
      return date - mod(date + cap_Delta - days, 210)
  # see lines 2632-2646 in calendrica-3.0.cl
  def positions_in_range(n, c, cap_Delta, range):
      """Return the list of occurrences of n-th day of c-day cycle
      in range.
      cap_Delta is the position in cycle of RD 0."""
      a = start(range)
      b = end(range)
      pos = a + mod(n - a - cap_Delta - 1, c)
      return ([] if (pos > b) else
              [pos].extend(
                  positions_in_range(n, c, cap_Delta, interval(pos + 1, b))))
  # see lines 2648-2654 in calendrica-3.0.cl
  def kajeng_keliwon(g_year):
      """Return the occurrences of Kajeng Keliwon (9th day of each
      15_day subcycle of Pawukon) in Gregorian year g_year."""
      year = gregorian_year_range(g_year)
      cap_Delta = bali_day_from_fixed(0)
      return positions_in_range(9, 15, cap_Delta, year)
  # see lines 2656-2662 in calendrica-3.0.cl
  def tumpek(g_year):
      """Return the occurrences of Tumpek (14th day of Pawukon and every
      35th subsequent day) within Gregorian year g_year."""
      year = gregorian_year_range(g_year)
      cap_Delta = bali_day_from_fixed(0)
      return positions_in_range(14, 35, cap_Delta, year)
This code is used in chunk 3.
Defines:
 bali asatawara, never used.
 {\tt bali\_asatawara\_from\_fixed}, \, {\tt never} \, \, {\tt used}.
 bali_caturwara, never used.
 bali_caturwara_from_fixed, never used.
  bali_dasawara, never used.
```

```
bali_dasawara_from_fixed, never used.
          bali_day_from_fixed, never used.
          bali_dwiwara, never used.
          bali_dwiwara_from_fixed, never used.
          BALI_EPOCH, never used.
          bali_luang, never used.
          bali_luang_from_fixed, never used.
          bali_on_or_before, used in chunk 90.
          bali_pancawara, never used.
          bali_pancawara_from_fixed, never used.
          bali_pawukon_from_fixed, used in chunks 90 and 180.
          bali_sadwara, never used.
          bali_sadwara_from_fixed, never used.
          bali_sangawara, never used.
          bali_sangawara_from_fixed, never used.
          bali_saptawara, never used.
          bali_saptawara_from_fixed, never used.
          bali_triwara, never used.
          bali_triwara_from_fixed, never used.
          bali_week_from_fixed, never used.
          balinese\_date, used in chunks 90 and 174.
          even, never used.
          kajeng_keliwon, never used.
          odd, used in chunk 133.
          positions_in_range, never used.
          tumpek, never used.
        Uses amod 15, end 47, fixed_from_jd 48, gregorian_year_range 56, interval 47, mod 15,
          quotient 14 14, and start 47.
90
        \langle balinese\ calendar\ unit\ test\ 90 \rangle \equiv
          class BalineseSmokeTestCase(unittest.TestCase):
               def setUp(self):
                    self.testvalue = 710347
               def testConversionFromFixed(self):
                    self.assertEqual(
                         bali_pawukon_from_fixed(self.testvalue),
                         balinese_date(True, 2, 1, 1, 3, 1, 2, 5, 7, 2))
               def testConversionToFixed(self):
                    self.assertEqual(
                         bali_on_or_before(
                              balinese_date(True, 2, 1, 1, 3, 1, 2, 5, 7, 2),
                              self.testvalue),
                         self.testvalue)
        This definition is continued in chunk 179.
        This code is used in chunks 4 and 91.
        Defines:
          BalineseSmokeTestCase, never used.
        Uses bali_on_or_before 89, bali_pawukon_from_fixed 89, and balinese_date 89.
        2.13.1
                   Unit tests
        \langle balineseCalendarUnitTest.py 91 \rangle \equiv
          # \(\langle generated code warning 1 \rangle \)
          \langle \mathit{import} \; \mathit{for} \; \mathit{testing} \; \textcolor{red}{6} \rangle
          from appendixCUnitTest import AppendixCTable3TestCaseBase
          \langle balinese\ calendar\ unit\ test\ 90 \rangle
          \langle execute \ tests \ 5 \rangle
        Root chunk (not used in this document).
        Uses AppendixCTable3TestCaseBase 174.
```

2.14 Time and Astronomy

The location of an object in the sky is determined by celestial coordinates, analogous to the latitude and longotude for the location of a position on Earth.

The "place of an object" concept is quite complicated. In fact in astronomy we speak of mean, apparent and true position.

apparent place is the position at which the object would actually be seen from the center of the Earth — if the Earth were transparent, nonrefracting, and massless — referred to the true equator and equinox. It is the position on the celestial sphere as seen from the center of the moving Earth and referred to the instantaneus equator, ecliptic and equinox.

mean place represents the direction of the object (a star or other celestial object outside the solar system) as it would hypothetically be observed from the solar system barycenter at the specified date, with respect to a fixed coordinate system if the masses of the Sun and other solar system bodies were negligible. It is the apparent position on the celestial sphere as it would be seen from the barycenter of the solar system and referred to the ecliptic and mean equinox of the date (or to the mean equator and mean equinox of the date.)

2.14.1 Alt - az Coordinate system

The alt-az is a topocentric (i.e. as seen from the observer's place on the Earth's surface) celestial coordinate system. It uses the horizon as its fundamental circle which divides the sky in two hemispheres. The pole of the upper hemisphere is called the zenith, while the one of the lower hemisphere is called nadir. These are defined by the local vertical (using a plumb-line or similar). The point of origin on the horizon is determined by the intersection of the vertical circle (i.e. trhough zenith and nadir) passing through north and south celestial pole.

The azimith (A) is the direction of a celestial object, measured clockwise around the observer's horizon from south.

Figure 2.1 displays the Earth and the alt-az (or horizontal) coordinate system.

Any coordinates given in the alt-az system depend on the place of observation (because the sky appears different from different points on Earth) and on the time of observation (because the Earth rotates, and each star appears to trace out a circle centred on North Celestial Pole).

2.14.2 HA - dec Coordinate system

A system of celestial coordinates which is fixed on the sky and independent of the observer's time and place can be defined by selecting the celestial equator as its fundamental circle

The North Celestial Pole (NCP) and the South Celestial Pole (SCP) lie directly above Earth's North and South Poles. The NCP and SCP form the poles of a great circle on the celestial sphere, analogous to the equator on Earth: it is called the celestial equator and it lies directly above the Earth's equator.

Any great circle between the NCP and the SCP is a meridian. The one which also passes through the zenith and the nadir is "the" celestial meridian, or the observer's meridian. (It is identical to the principal vertical.) This provides our new zero-point; in this case, we use the point where it crosses the southern half of the equator.

The Hour Angle (HA or H) of object X is the angular distance between the meridian of X and the celestial meridian. It is measured westwards in hours, 0h-24h, since the Earth rotates $360 \hat{A}^{\circ}$ in 24 hours.

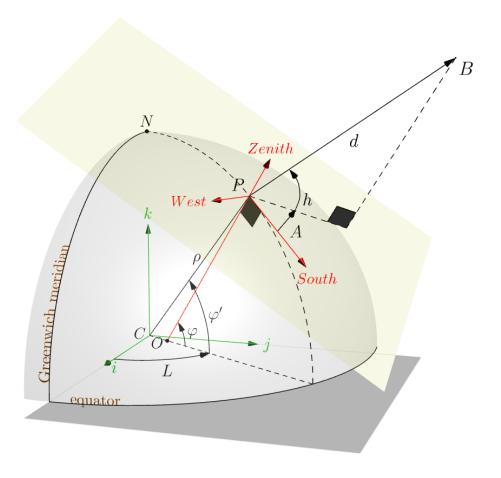


Figure 2.1: Alt-az coordinate system. N is the North (Celestial) Pole; i points at the intersection between Greenwich meridian and the equator; A is the azimuth of the celestial body B as seen from observer positioned in P (at geographical longitude L and geographical latitude φ ; φ' is the geocentric latitude [mesured from Earth's center])). The plane is tangent in P to the Earth's surface.

2.14.3 RA - dec Coordinate system

Figure 2.2 displays the celestial sphere and the RA-dec coordinate system (also named second equtorial).

Figure 2.3 displays ecliptic, lunar orbit (angle is exagerated), the lunar (ascending) node Ω and the origin Υ (at vernal equinox). It is intersting to note graphically what is later described algorithmically.

2.14.4 Galactic Coordinate system

2.14.5 Coordinates Transformation

Ecliptical from equatorial:

$$\tan \lambda = \frac{\sin \alpha \cos \varepsilon + \tan \delta \sin \varepsilon}{\cos \alpha} \tag{2.1}$$

$$\sin \beta = \sin \delta \, \cos \varepsilon - \cos \delta \, \sin \varepsilon \, \sin \alpha \tag{2.2}$$

where

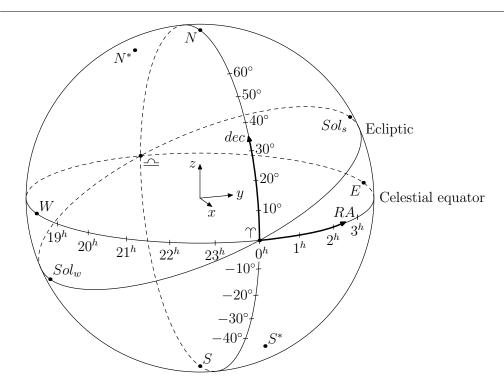


Figure 2.2: RA-dec coordinate system. N^* is the North pole of the ecliptic; N is the North Celestial Pole; Υ is the first point of Aries and the zero-point for this coordinate system. Right Ascension (RA or α) is measured in hours towards East (E); declination (dec or δ) is measured in degrees, positive if north (N) of the Celestial equator. Sol_w is the winter solstice point of 18^hRA and -23.5° dec; Sol_s is the summer solstice point of 6^hRA and 23.5° dec.

 λ is the ecliptical longitude, positive if north of the ecliptic, negative if south;

 β is the ecliptical latitude, positive if north of the ecliptic, negative if south;

 α is the right ascension;

 ε is the obliquity of the ecliptic, that is the angle between ecliptic and the celestial equator 1 ;

 δ is the declination, positive if north of the celestial equator, negative if south;

 $^{^{1}}$ if <u>apparent</u> right ascension and declination are used, i.e. affected by aberration and nutation), then the <u>true</u> obliquity should be used, see eq. ??; for <u>mean</u> RA and declination we can use mean obliquity from eq. 2.3

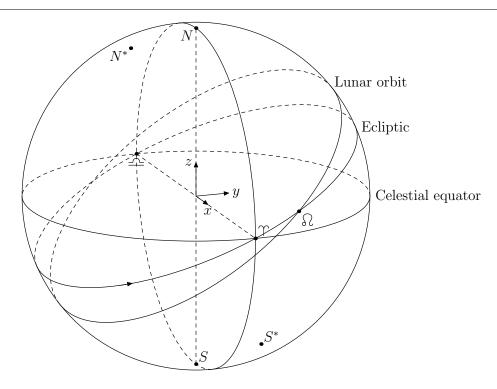


Figure 2.3: Celestial coordinate system. N^* is the North pole of the ecliptic; N is the North Celestial Pole; Υ is the first point of Aries or the ascending node of the mean ecliptic. Ω is the ascending node of the lunar orbit.

```
co = cos_degrees(obliquity)
              so = sin_degrees(obliquity)
              sa = sin_degrees(ra)
              lon = normalized_degrees_from_radians(
                  atan2(sa*co + tan_degrees(declination)*so, cos_degrees(ra)))
              lat = arcsin_degrees(
                       sin_degrees(declination)*co -
                       cos_degrees(declination)*so*sa)
              return [lon, lat]
       This definition is continued in chunks 94, 96, 98, and 100–102.
       This code is used in chunk 3.
         ecliptical_from_equatorial, used in chunk 95.
       Uses arcsin_degrees 100, declination 102, normalized_degrees_from_radians 100, obliquity 101,
         and sin_degrees 100.
       \langle \mathit{astronomical\ algorithms\ tests\ 93} \rangle {\equiv}
93
         def testEclipticalFromEquatorial(self):
              # from the values in the Ch 13 Astronomical Algorithms
              ra, de = equatorial_from_ecliptical(113.215630, 6.684170, 23.4392911)
              self.assertAlmostEqual(ra, 116.328942, 5)
              self.assertAlmostEqual(de, 28.026183, 6)
       This definition is continued in chunks 95, 97, 99, and 103.
       This code is used in chunk 104.
         testEclipticalFromEquatorial, never used.
       Uses equatorial_from_ecliptical 94.
```

```
94
       \langle time \ and \ astronomy \ 92 \rangle + \equiv
         def equatorial_from_ecliptical(longitude, latitude, obliquity):
              \hbox{\tt """}{\tt Convert} ecliptical coordinates (in degrees) to equatorial ones.
              'longitude' is the ecliptical longitude,
              'latitude' is the ecliptical latitude and
              'obliquity' is the obliquity of the ecliptic.
             NOTE: resuting 'ra' and 'declination' will be referred to the same equinox
                    as the one of input ecliptical longitude and latitude.
             co = cos_degrees(obliquity)
             so = sin_degrees(obliquity)
             sl = sin_degrees(longitude)
             ra = normalized_degrees_from_radians(
                  atan2(s1*co - tan_degrees(latitude)*so,
                  cos_degrees(longitude)))
             dec = arcsin_degrees(
                      sin_degrees(latitude)*co +
                      cos_degrees(latitude)*so*sl)
             return [ra, dec]
       This code is used in chunk 3.
       Defines:
         equatorial_from_ecliptical, used in chunk 93.
       Uses arcsin_degrees 100, latitude 100, longitude 100, normalized_degrees_from_radians 100,
         obliquity 101, and sin_degrees 100.
95
       \langle astronomical \ algorithms \ tests \ 93 \rangle + \equiv
         def testEquatorialFromEcliptical(self):
             # from the values in the Ch 13 Astronomical Algorithms
             lo, la = ecliptical_from_equatorial(116.328942, 28.026183, 23.4392911)
             self.assertAlmostEqual(lo, mpf(113.215630), 6)
             self.assertAlmostEqual(la, mpf(6.684170), 6)
       This code is used in chunk 104.
       Defines:
         testEquatorialFromEcliptical, never used.
       Uses ecliptical_from_equatorial 92.
```

```
96
       \langle time \ and \ astronomy \ 92 \rangle + \equiv
         def horizontal_from_equatorial(H, declination, latitude):
             """Convert equatorial coordinates (in degrees) to horizontal ones.
             Return 'azimuth' and 'altitude'.
                             is the local hour angle,
             'declination' is the declination,
             'latitude' is the observer's geographic latitude.
             NOTE: 'azimuth' is measured westward from the South.
             NOTE: This is not a good formula for using near the poles.
             ch = cos_degrees(H)
             sl = sin_degrees(latitude)
             cl = cos_degrees(latitude)
             A = normalized_degrees_from_radians(
                      atan2(sin_degrees(H),
                             ch * sl - tan_degrees(declination) * cl))
             h = arcsin_degrees(sl * sin_degrees(declination) +
                                  cl * cos_degrees(declination) * ch)
             return [A, h]
      This code is used in chunk 3.
       Defines:
         horizontal_from_equatorial, used in chunk 97.
       Uses angle 100, arcsin_degrees 100, declination 102, hour 39, latitude 100,
         normalized_degrees_from_radians 100, and sin_degrees 100.
97
       \langle astronomical \ algorithms \ tests \ 93 \rangle + \equiv
         def testHorizontalFromEquatorial(self):
             # from the values in the Ch 13 Astronomical Algorithms
             A, h = horizontal_from_equatorial(64.352133, -6.719892, angle(38, 55, 17))
             self.assertAlmostEqual(A, 68.0337, 4)
             self.assertAlmostEqual(h, 15.1249, 4)
       This code is used in chunk 104.
       Defines:
         testHorizontalFromEquatorial, never used.
       Uses angle 100 and horizontal_from_equatorial 96.
98
       \langle time \ and \ astronomy \ 92 \rangle + \equiv
         def equatorial_from_horizontal(A, h, phi):
             """Convert equatorial coordinates (in degrees) to horizontal ones.
             Return 'local hour angle' and 'declination'.
             'A' is the azimuth,
             'h' is the altitude,
             'phi' is the observer's geographical latitude.
             NOTE: 'azimuth' is measured westward from the South.
             H = normalized_degrees_from_radians(
                      atan2(sin_degrees(A),
                             (cos_degrees(A) * sin_degrees(phi) +
                              tan_degrees(h) * cos_degrees(phi))))
             delta = arcsin_degrees(sin_degrees(phi) * sin_degrees(h) -
                                      cos_degrees(phi) * cos_degrees(h) * cos_degrees(A))
             return [H, delta]
       This code is used in chunk 3.
       Defines:
         equatorial_from_horizontal, used in chunk 99.
       Uses arcsin_degrees 100, hour 39, latitude 100, normalized_degrees_from_radians 100,
         and sin_degrees 100.
```

```
100
       \langle time \ and \ astronomy \ 92 \rangle + \equiv
         # see lines 2667-2670 in calendrica-3.0.cl
         def days_from_hours(x):
             """Return the number of days given x hours."""
             return x / 24
         # see lines 2672-2675 in calendrica-3.0.cl
         def days_from_seconds(x):
             """Return the number of days given x seconds."""
             return x / 24 / 60 / 60
         # see lines 2677-2680 in calendrica-3.0.cl
         def mt(x):
             """Return x as meters."""
             return x
         # see lines 2682-2686 in calendrica-3.0.cl
         def deg(x):
             """Return the degrees in angle x."""
             return x
         # see lines 2688-2690 in calendrica-3.0.cl
         def secs(x):
              """Return the seconds in angle x."""
             return x / 3600
         # see lines 2692-2696 in calendrica-3.0.cl
         def angle(d, m, s):
              """Return an angle data structure
             from d degrees, m arcminutes and s arcseconds.
             This assumes that negative angles specifies negative d, m and s."""
             return d + ((m + (s / 60)) / 60)
         # see lines 2698-2701 in calendrica-3.0.cl
         def normalized_degrees(theta):
             """Return a normalize angle theta to range [0,360) degrees."""
             return mod(theta, 360)
         # see lines 2703-2706 in calendrica-3.0.cl
         def normalized_degrees_from_radians(theta):
             """Return normalized degrees from radians, theta.
             Function 'degrees' comes from mpmath."""
             return normalized_degrees(degrees(theta))
         # see lines 2708-2711 in calendrica-3.0.cl
         def radians_from_degrees(theta):
             pass
         from mpmath import radians as radians_from_degrees
         # see lines 2713-2716 in calendrica-3.0.cl
         def sin_degrees(theta):
             """Return sine of theta (given in degrees)."""
             #from math import sin
             return sin(radians_from_degrees(theta))
         # see lines 2718-2721 in calendrica-3.0.cl
         def cosine_degrees(theta):
             """Return cosine of theta (given in degrees)."""
             #from math import cos
             return cos(radians_from_degrees(theta))
```

```
# from errata20091230.pdf entry 112
cos_degrees=cosine_degrees
# see lines 2723-2726 in calendrica-3.0.cl
def tangent_degrees(theta):
    """Return tangent of theta (given in degrees)."""
   return tan(radians_from_degrees(theta))
# from errata20091230.pdf entry 112
tan_degrees=tangent_degrees
def signum(a):
   if a > 0:
       return 1
   elif a == 0:
       return 0
   else:
       return -1
#-----
# NOTE: arc[tan|sin|cos] casted with degrees given CL code
       returns angles [0, 360), see email from Dershowitz
       after my request for clarification
# see lines 2728-2739 in calendrica-3.0.cl
# def arctan_degrees(y, x):
      """ Arctangent of y/x in degrees."""
      from math import atan2
      return normalized_degrees_from_radians(atan2(x, y))
def arctan_degrees(y, x):
   """ Arctangent of y/x in degrees."""
   if (x == 0) and (y != 0):
      return mod(signum(y) * deg(mpf(90)), 360)
   else:
       alpha = normalized_degrees_from_radians(atan(y / x))
       if x \ge 0:
          return alpha
       else:
           return mod(alpha + deg(mpf(180)), 360)
# see lines 2741-2744 in calendrica-3.0.cl
def arcsin_degrees(x):
   """Return arcsine of x in degrees."""
   #from math import asin
   return normalized_degrees_from_radians(asin(x))
# see lines 2746-2749 in calendrica-3.0.cl
def arccos_degrees(x):
   """Return arccosine of x in degrees."""
   #from math import acos
   return normalized_degrees_from_radians(acos(x))
# see lines 2751-2753 in calendrica-3.0.cl
def location(latitude, longitude, elevation, zone):
    """Return a location data structure."""
   return [latitude, longitude, elevation, zone]
```

```
# see lines 2755-2757 in calendrica-3.0.cl
def latitude(location):
    """Return the latitude field of a location."""
   return location[0]
# see lines 2759-2761 in calendrica-3.0.cl
def longitude(location):
    """Return the longitude field of a location."""
   return location[1]
# see lines 2763-2765 in calendrica-3.0.cl
def elevation(location):
   """Return the elevation field of a location."""
   return location[2]
# see lines 2767-2769 in calendrica-3.0.cl
def zone(location):
    """Return the timezone field of a location."""
   return location[3]
# see lines 2771-2775 in calendrica-3.0.cl
MECCA = location(angle(21, 25, 24), angle(39, 49, 24), mt(298), days_from_hours(3))
# see lines 5898-5901 in calendrica-3.0.cl
JERUSALEM = location(31.8, 35.2, mt(800), days_from_hours(2))
BRUXELLES = location(angle(4, 21, 17), angle(50, 50, 47), mt(800), days_from_hours(1))
URBANA = location(40.1,
                  -88.2,
                  mt (225),
                  days_from_hours(-6))
GREENWHICH = location(51.4777815,
                      0,
                      mt(46.9),
                      days_from_hours(0))
# see lines 2777-2797 in calendrica-3.0.cl
def direction(location, focus):
   """Return the angle (clockwise from North) to face focus when
   standing in location, location. Subject to errors near focus and
   its antipode."""
   phi = latitude(location)
   phi_prime = latitude(focus)
   psi = longitude(location)
   psi_prime = longitude(focus)
   y = sin_degrees(psi_prime - psi)
   x = ((cosine_degrees(phi) * tangent_degrees(phi_prime)) -
         (sin_degrees(phi)
                            * cosine_degrees(psi - psi_prime)))
   if ((x == y == 0) \text{ or } (phi\_prime == deg(90))):
        return deg(0)
    elif (phi_prime == deg(-90)):
       return deg(180)
    else:
        return arctan_degrees(y, x)
# see lines 2799-2803 in calendrica-3.0.cl
def standard_from_universal(tee_rom_u, location):
```

```
"""Return standard time from tee_rom_u in universal time at location."""
   return tee_rom_u + zone(location)
# see lines 2805-2809 in calendrica-3.0.cl
def universal_from_standard(tee_rom_s, location):
    """Return universal time from tee_rom_s in standard time at location."""
   return tee_rom_s - zone(location)
# see lines 2811-2815 in calendrica-3.0.cl
def zone_from_longitude(phi):
    """Return the difference between UT and local mean time at longitude
    'phi' as a fraction of a day."""
   return phi / deg(360)
# see lines 2817-2820 in calendrica-3.0.cl
def local_from_universal(tee_rom_u, location):
    """Return local time from universal tee_rom_u at location, location."""
   return tee_rom_u + zone_from_longitude(longitude(location))
# see lines 2822-2825 in calendrica-3.0.cl
def universal_from_local(tee_ell, location):
    """Return universal time from local tee_ell at location, location."""
   return tee_ell - zone_from_longitude(longitude(location))
# see lines 2827-2832 in calendrica-3.0.cl
def standard_from_local(tee_ell, location):
    """Return standard time from local tee_ell at locale, location."""
   return standard_from_universal(universal_from_local(tee_ell, location),
                                   location)
# see lines 2834-2839 in calendrica-3.0.cl
def local_from_standard(tee_rom_s, location):
    """Return local time from standard tee_rom_s at location, location."""
   return local_from_universal(universal_from_standard(tee_rom_s, location),
                                location)
# see lines 2841-2844 in calendrica-3.0.cl
def apparent_from_local(tee, location):
    """Return sundial time at local time tee at location, location."""
   return tee + equation_of_time(universal_from_local(tee, location))
# see lines 2846-2849 in calendrica-3.0.cl
def local_from_apparent(tee, location):
    """Return local time from sundial time tee at location, location."""
   return tee - equation_of_time(universal_from_local(tee, location))
# see lines 2851-2857 in calendrica-3.0.cl
def midnight(date, location):
    """Return standard time on fixed date, date, of true (apparent)
   midnight at location, location."""
   return standard_from_local(local_from_apparent(date, location), location)
# see lines 2859-2864 in calendrica-3.0.cl
def midday(date, location):
   """Return standard time on fixed date, date, of midday
   at location, location."""
   return standard_from_local(local_from_apparent(date + days_from_hours(mpf(12)),
                                                   location), location)
# see lines 2866-2870 in calendrica-3.0.cl
def julian_centuries(tee):
```

```
"""Return Julian centuries since 2000 at moment tee."""
       return (dynamical_from_universal(tee) - J2000) / mpf(36525)
This code is used in chunk 3.
Defines:
  angle, used in chunks 30, 46, 96, 97, 99, 101, 102, 105, 107, 119, 120, 128, 133, 136, 142, and 196.
  apparent_from_local, used in chunk 142.
  arccos_degrees, used in chunks 102 and 142.
  arcsin_degrees, used in chunks 92, 94, 96, 98, 102, and 120.
  arctan_degrees, used in chunks 102, 105, and 109.
  BRUXELLES, never used.
  cosine_degrees, used in chunks 102, 107, 109, 120, and 142.
  days_from_hours, used in chunks 80, 86, 102, 105, 107, 122, 125, 128, 133, 136, and 142.
  days_from_seconds, used in chunk 102.
  deg, used in chunks 102, 104, 105, 107, 109, 111, 113, 115, 117, 119, 120, 122, 125, 133, 136, and 142.
  direction, never used.
  elevation, used in chunk 102.
  GREENWHICH, never used.
  JERUSALEM, used in chunk 196.
  julian_centuries, used in chunks 101, 102, 107, 109, 119, and 120.
  latitude, used in chunks 94, 96, 98, 102, 105, 107, 117, 119, 120, and 136.
  local_from_apparent, used in chunk 102.
  local_from_standard, never used.
  local_from_universal, used in chunk 142.
  location, used in chunks 102, 105, 120, 122, 125, 128, 133, 136, and 142.
  longitude, used in chunks 94, 102, 107, 109, 119, 120, 133, 136, and 194.
  MECCA, never used.
  midday, used in chunks 105 and 122.
  midnight, used in chunks 128, 133, and 136.
  mt, used in chunks 102, 120, 122, 125, 128, 133, 136, 142, 165, and 173.
  normalized_degrees, used in chunks 99, 109, 111, 113, 115, 117, and 119.
  normalized_degrees_from_radians, used in chunks 92, 94, 96, and 98.
  radians_from_degrees, never used.
  secs, used in chunks 102 and 109.
  signum, used in chunks 107 and 136.
  sin_degrees, used in chunks 92, 94, 96, 98, 102, 107, 109, 119, 120, and 136.
  standard_from_local, used in chunk 102.
  standard_from_universal, used in chunks 102 and 133.
  tangent_degrees, used in chunks 102, 105, and 107.
  universal_from_local, used in chunks 102 and 136.
  universal_from_standard, used in chunks 102, 105, 122, 125, 128, 133, and 142.
  URBANA, used in chunk 102.
  zone, used in chunk 133.
  zone_from_longitude, never used.
Uses dynamical_from_universal 105, equation_of_time 107, J2000 107, mod 15, and seconds 39.
Mean Obliquity
The mean obliquity is defined by the following formula [4, equ. 22.2]:
               \varepsilon_0 = 23^{\circ}26'21''.448 - 46''.8150T - 0''.00059T^2 + 0''.001813T^3
                                                                                             (2.3)
\langle time \ and \ astronomy \ 92 \rangle + \equiv
  # see lines 2872-2880 in calendrica-3.0.cl
  def obliquity(tee):
       """Return (mean) obliquity of ecliptic at moment tee."""
       c = julian_centuries(tee)
       return (angle(23, 26, mpf(21.448)) +
                poly(c, [mpf(0),
                           angle(0, 0, mpf(-46.8150)),
                            angle(0, 0, mpf(-0.00059)),
                            angle(0, 0, mpf(0.001813))]))
This code is used in chunk 3.
  obliquity, used in chunks 92, 94, 102, and 107.
```

Uses angle 100, julian_centuries 100, and poly 34.

101

A formula with better precision (0".01 after 1000 years and few seconds of arc after 10000 years around J2000.0) over a wider time (10000 years around J2000.0) span is given by [4, equ. 22.3]:

```
\varepsilon_0 = 23^{\circ}26'21''.448
                                                -4680''.93U
                                                -1''.55U^{2}
                                                +1999''25U^3
                                                -51''38U^4
                                                -249''.67U^5
                                                                                         (2.4)
                                                -39''.05U^6
                                                +7''12U^7
                                                +27''.87U^6
                                                +5.79U^{7}
                                                +2''45U^9
                                                                                         (2.5)
102
       \langle time \ and \ astronomy \ 92 \rangle + \equiv
         def precise_obliquity(tee):
              """Return precise (mean) obliquity of ecliptic at moment tee."""
              u = julian_centuries(tee)/100
              #assert(abs(u) < 1,</pre>
                       'Error! This formula is valid for +/-10000 years around J2000.0')
              return (poly(u, [angle(23, 26, mpf(21.448)),
                                angle(0, 0, mpf(-4680.93)),
                                angle(0, 0, mpf(- 1.55)),
                                angle(0, 0, mpf(+1999.25)),
                                angle(0, 0, mpf(- 51.38)),
                                angle(0, 0, mpf(- 249.67)),
                                angle(0, 0, mpf(- 39.05)),
                                angle(0, 0, mpf(+
                                                    7.12)),
                                angle(0, 0, mpf(+ 27.87)),
                                angle(0, 0, mpf(+
                                                     5.79)),
                                angle(0, 0, mpf(+
                                                     2.45))]))
         def true_obliquity(tee):
              """Return 'true' obliquity of ecliptic at moment tee.
              That is, where nutation is taken into accout."""
              pass
         # see lines 2882-2891 in calendrica-3.0.cl
         def declination(tee, beta, lam):
              """Return declination at moment UT tee of object at
              longitude 'lam' and latitude 'beta'.""
              varepsilon = obliquity(tee)
              return arcsin_degrees(
                  (sin_degrees(beta) * cosine_degrees(varepsilon)) +
                  (cosine_degrees(beta) * sin_degrees(varepsilon) * sin_degrees(lam)))
         # see lines 2893-2903 in calendrica-3.0.cl
         def right_ascension(tee, beta, lam):
              """Return right ascension at moment UT 'tee' of object at
              latitude 'lam' and longitude 'beta'."""
              varepsilon = obliquity(tee)
              return arctan_degrees(
                  (sin_degrees(lam) * cosine_degrees(varepsilon)) -
                  (tangent_degrees(beta) * sin_degrees(varepsilon)),
```

```
cosine_degrees(lam))
# see lines 2905-2920 in calendrica-3.0.cl
def sine_offset(tee, location, alpha):
    """Return sine of angle between position of sun at
   local time tee and when its depression is alpha at location, location.
   Out of range when it does not occur."""
   phi = latitude(location)
   tee_prime = universal_from_local(tee, location)
   delta = declination(tee_prime, deg(mpf(0)), solar_longitude(tee_prime))
   return ((tangent_degrees(phi) * tangent_degrees(delta)) +
            (sin_degrees(alpha) / (cosine_degrees(delta) *
                                   cosine_degrees(phi))))
# see lines 2922-2947 in calendrica-3.0.cl
def approx_moment_of_depression(tee, location, alpha, early):
    """Return the moment in local time near tee when depression angle
   of sun is alpha (negative if above horizon) at location;
   early is true when MORNING event is sought and false for EVENING.
   Returns BOGUS if depression angle is not reached."""
   ttry = sine_offset(tee, location, alpha)
   date = fixed_from_moment(tee)
   if (alpha >= 0):
        if early:
            alt = date
        else:
           alt = date + 1
        alt = date + days_from_hours(12)
   if (abs(ttry) > 1):
        value = sine_offset(alt, location, alpha)
    else:
        value = ttry
   if (abs(value) <= 1):</pre>
        temp = -1 if early else 1
        temp *= mod(days_from_hours(12) + arcsin_degrees(value) / deg(360), 1) - days_from_hours(6)
        temp += date + days_from_hours(12)
       return local_from_apparent(temp, location)
    else:
       return BOGUS
# see lines 2949-2963 in calendrica-3.0.cl
def moment_of_depression(approx, location, alpha, early):
    """Return the moment in local time near approx when depression
   angle of sun is alpha (negative if above horizon) at location;
    early is true when MORNING event is sought, and false for EVENING.
   Returns BOGUS if depression angle is not reached."""
   tee = approx_moment_of_depression(approx, location, alpha, early)
   if (tee == BOGUS):
        return BOGUS
    else:
        if (abs(approx - tee) < days_from_seconds(30)):</pre>
            return tee
        else:
            return moment_of_depression(tee, location, alpha, early)
# see lines 2965-2968 in calendrica-3.0.cl
```

```
MORNING = True
# see lines 2970-2973 in calendrica-3.0.cl
EVENING = False
# see lines 2975-2984 in calendrica-3.0.cl
def dawn(date, location, alpha):
    """Return standard time in morning on fixed date date at
    location location when depression angle of sun is alpha.
    Returns BOGUS if there is no dawn on date date."""
    result = moment_of_depression(date + days_from_hours(6), location, alpha, MORNING)
    if (result == BOGUS):
        return BOGUS
    else:
        return standard_from_local(result, location)
# see lines 2986-2995 in calendrica-3.0.cl
def dusk(date, location, alpha):
    """Return standard time in evening on fixed date 'date' at
    location 'location' when depression angle of sun is alpha.
    Return BOGUS if there is no dusk on date 'date'."""
    result = moment_of_depression(date + days_from_hours(18), location, alpha, EVENING)
    if (result == BOGUS):
       return BOGUS
    else:
        return standard_from_local(result, location)
# see lines 440-451 in calendrica-3.0.errata.cl
def refraction(tee, location):
    """Return refraction angle at location 'location' and time 'tee'."""
    from math import sqrt
          = max(mt(0), elevation(location))
    cap_R = mt(6.372E6)
    dip = arccos_degrees(cap_R / (cap_R + h))
    return angle(0, 50, 0) + dip + secs(19) * sqrt(h)
# see lines 2997-3007 in calendrica-3.0.cl
def sunrise(date, location):
    """Return Standard time of sunrise on fixed date 'date' at
    location 'location'."""
    alpha = refraction(date, location)
    return dawn(date, location, alpha)
# see lines 3009-3019 in calendrica-3.0.cl
def sunset(date, location):
    """Return standard time of sunset on fixed date 'date' at
    location 'location'.""
    alpha = refraction(date, location)
    return dusk(date, location, alpha)
# see lines 453-458 in calendrica-3.0.errata.cl
def observed_lunar_altitude(tee, location):
    """Return the observed altitude of moon at moment, tee, and
    at location, location, taking refraction into account."""
    return topocentric_lunar_altitude(tee, location) + refraction(tee, location)
# see lines 460-467 in calendrica-3.0.errata.cl
def moonrise(date, location):
    """Return the standard time of moonrise on fixed, date,
    and location, location."""
    t = universal_from_standard(date, location)
```

```
waning = (lunar_phase(t) > deg(180))
      alt = observed_lunar_altitude(t, location)
      offset = alt / 360
      if (waning and (offset > 0)):
           approx = t + 1 - offset
      elif waning:
           approx = t - offset
      else:
           approx = t + (1 / 2) + offset
      rise = binary_search(approx - days_from_hours(3),
                              approx + days_from_hours(3),
                              lambda u, l: ((u - 1) < \frac{days_from_hours}{(1 / 60)}),
                              lambda x: observed_lunar_altitude(x, location) > deg(0))
      return standard_from_universal(rise, location) if (rise < (t + 1)) else BOGUS
  def urbana_sunset(gdate):
       """Return sunset time in Urbana, Ill, on Gregorian date 'gdate'."""
      return time_from_moment(sunset(fixed_from_gregorian(gdate), URBANA))
  # from eq 13.38 pag. 191
  def urbana_winter(g_year):
       """Return standard time of the winter solstice in Urbana, Illinois, USA."""
      return standard_from_universal(
                   solar_longitude_after(
                        WINTER,
                       fixed_from_gregorian(gregorian_date(g_year, JANUARY, 1))),
                   URBANA)
This code is used in chunk 3.
  \verb"approx_moment_of_depression", never used.
  dawn, used in chunks 136, 194, and 196.
  declination, used in chunks 92, 96, 104, 105, and 120.
  dusk, used in chunks 104, 105, 136, and 142.
  EVENING, never used.
  moment_of_depression, never used.
  moonrise, never used.
  MORNING, never used.
  precise_obliquity, never used.
  refraction, used in chunk 120.
  right_ascension, used in chunks 104 and 120.
  sine_offset, never used.
  sunrise, used in chunks 105, 136, and 252.
  sunset, used in chunks 105, 125, 136, 142, 194, and 196.
  {\tt true\_obliquity}, \ {\rm never} \ {\rm used}.
  urbana_sunset, never used.
  urbana_winter, used in chunk 103.
Uses angle 100, arccos_degrees 100, arcsin_degrees 100, arctan_degrees 100 100, binary_search 25,
  BOGUS 13, cosine_degrees 100, days_from_hours 100, days_from_seconds 100, deg 100,
  elevation 100, fixed_from_gregorian 55, fixed_from_moment 40, gregorian_date 52,
  J2000 107, JANUARY 53, julian_centuries 100, latitude 100, local_from_apparent 100,
  location 100, longitude 100, lunar_phase 119, mod 15, mt 100, nutation 107, obliquity 101,
  poly 34, secs 100, sin_degrees 100, solar_longitude 107, solar_longitude_after 109,
  standard_from_local 100, standard_from_universal 100, tangent_degrees 100,
  {\tt time\_from\_moment~40,~topocentric\_lunar\_altitude~120,~universal\_from\_local~100,}
  universal_from_standard 100, URBANA 100, and WINTER 109.
```

```
103     ⟨astronomical algorithms tests 93⟩+≡
          def testUrbanaWinter(self):
          # from the values in the book pag 191
          self.assertAlmostEqual(
                urbana_winter(2000), 730475.31751, 5)

This code is used in chunk 104.
Defines:
```

 ${\tt testUrbanaWinter}, \ {\rm never} \ {\rm used}.$

Uses $urbana_winter 102$.

```
104
       \langle time \ and \ astronomy \ unit \ test \ 104 \rangle \equiv
         {\tt class} \  \, {\tt TimeAndAstronomySmokeTestCase} (unittest. {\tt TestCase}): \\
             def setUp(self):
                  self.rd = [-214193, -61387, 25469, 49217, 171307, 210155, 253427,
                              369740, 400085, 434355, 452605, 470160, 473837, 507850,
                              524156, 544676, 567118, 569477, 601716, 613424, 626596,
                              645554, 664224, 671401, 694799, 704424, 708842, 709409,
                              709580, 727274, 728714, 744313, 764652]
                  self.declinations = [341.009933681, 344.223866057, 344.349150723,
                                        343.080796014, 6.111045686, 23.282088850,
                                        11.054626067, 20.772095601, 350.530615797,
                                        26.524557874, 24.624220236, 341.329137381,
                                        22.952455871, 28.356788216, 11.708349719,
                                        17.836387256, 1.234462343, 342.613034686,
                                        339.494416096, 10.077195527, 356.273352051,
                                        10.933004147, 333.162727246, 12.857424363,
                                        342.981182734, 8.352097710, 342.717593219,
                                        359.480653210, 339.868605556, 6.747953072,
                                        15.403930316, 5.935073706, 6.502803786]
                  self.right_ascensions = [243.344057675, 204.985406451, 210.404938685,
                                            292.982801046, 157.347243474, 109.710580543,
                                            38.206587532, 99.237553669, 334.622772431,
                                            92.594013257, 77.002562902, 275.265641321,
                                            132.240141523, 89.495057657, 21.938682002,
                                            51.336108524, 189.141475514, 323.504045205,
                                            317.763636501, 146.668234288, 183.868193626,
                                            143.441024476, 251.771505962, 154.432825924,
                                            288.759213491, 24.368877399, 291.218608152,
                                            190.563965149, 285.912816020, 152.814362172,
                                            50.014265486, 26.456502208, 177.918419842]
                  self.lunar_altitudes = [-11.580406490, -13.996642398, -72.405467670,
                                            -26.949751162, 60.491536818, -32.333449636,
                                            43.325012802, -28.913935286, 20.844069354,
                                            -9.603298107, -13.290409748, 20.650429381,
                                            -9.068998404, -24.960604514, -34.865669400,
                                            -40.121041983, -50.193172697, -39.456259107,
                                            32.614203610, -46.078519304, -51.828340409,
                                            -42.577971851, -15.990046584, 28.658077283,
                                            22.718206310, 61.618573945, -26.504789606,
                                            32.371736207, -38.544325288, 31.594345546,
                                            -28.348377620, 30.478724056, -43.754783219]
                  self.dusks = [-214193.22, -61387.297, 25468.746, 49216.734,
                                 171306.7, 210154.78, 253426.7, 369739.78,
                                 400084.8, 434354.78, 452604.75, 470159.78,
                                 473836.78, 507849.8, 524155.75, 544675.7,
                                 567117.7, 569476.7, 601715.75, 613423.75,
                                 626595.75, 645553.75, 664223.75, 671400.7,
                                 694798.75, 704423.75, 708841.7, 709408.75,
                                 709579.7, 727273.7, 728713.7, 744312.7,
                                 764651.75]
             def testDeclination(self):
                  for i in range(len(self.rd)):
                      lamb = lunar_longitude(self.rd[i])
                      beta = lunar_latitude(self.rd[i])
                      alpha = declination(self.rd[i], beta, lamb)
```

```
self.assertAlmostEqual(alpha, self.declinations[i], 7)
      def testRightAscension(self):
           for i in range(len(self.rd)):
               lamb = lunar_longitude(self.rd[i])
               beta = lunar_latitude(self.rd[i])
               alpha = right_ascension(self.rd[i], beta, lamb)
               self.assertAlmostEqual(alpha, self.right_ascensions[i], 7)
      def testLunarAltitude(self):
           for i in range(len(self.rd)):
               alpha = lunar_altitude(self.rd[i], JAFFA)
               self.assertAlmostEqual(alpha, self.lunar_altitudes[i], 6)
      def testDusk(self):
           for i in range(len(self.rd)):
               du = dusk(self.rd[i] - 1, JAFFA, deg(mpf(4.5)))
               self.assertAlmostEqual(du, self.dusks[i], 0)
  class AstronomicalAlgorithmsTestCase(unittest.TestCase):
      \langle astronomical \ algorithms \ tests \ 93 \rangle
This definition is continued in chunk 195.
This code is used in chunks 4 and 121.
Defines:
  {\tt AstronomicalAlgorithmsTestCase}, \ never \ used.
  {\tt TimeAndAstronomySmokeTestCase}, \ never \ used.
Uses declination 102, deg 100, dusk 102, JAFFA 142, lunar_altitude 120, lunar_latitude 119,
  lunar_longitude 119, rd 37, and right_ascension 102.
```

```
105
       \langle astronomical\ lunar\ calendars\ 105 \rangle \equiv
         # astronomical lunar calendars algorithms #
         # see lines 3021-3025 in calendrica-3.0.cl
         def jewish_dusk(date, location):
             """Return standard time of Jewish dusk on fixed date, date,
            at location, location, (as per Vilna Gaon)."""
            return dusk(date, location, angle(4, 40, 0))
         # see lines 3027-3031 in calendrica-3.0.cl
         def jewish_sabbath_ends(date, location):
             """Return standard time of end of Jewish sabbath on fixed date, date,
             at location, location, (as per Berthold Cohn)."""
            return dusk(date, location, angle(7, 5, 0))
         # see lines 3033-3042 in calendrica-3.0.cl
         def daytime_temporal_hour(date, location):
             """Return the length of daytime temporal hour on fixed date, date
            at location, location.
            Return BOGUS if there no sunrise or sunset on date, date."""
             if (sunrise(date, location) == BOGUS) or (sunset(date, location) == BOGUS):
                return BOGUS
             else:
                return (sunset(date, location) - sunrise(date, location)) / 12
         # see lines 3044-3053 in calendrica-3.0.cl
         def nighttime_temporal_hour(date, location):
             """Return the length of nighttime temporal hour on fixed date, date,
            at location, location.
            Return BOGUS if there no sunrise or sunset on date, date."""
             if ((sunrise(date + 1, location) == BOGUS) or
                 (sunset(date, location) == BOGUS)):
                return BOGUS
             else:
                return (sunrise(date + 1, location) - sunset(date, location)) / 12
         # see lines 3055-3073 in calendrica-3.0.cl
         def standard_from_sundial(tee, location):
             """Return standard time of temporal moment, tee, at location, location.
            Return BOGUS if temporal hour is undefined that day."""
            date = fixed_from_moment(tee)
            hour = 24 * mod(tee, 1)
            if (6 <= hour <= 18):
                h = daytime_temporal_hour(date, location)
             elif (hour < 6):
                h = nighttime_temporal_hour(date - 1, location)
             else:
                h = nighttime_temporal_hour(date, location)
            # return
            if (h == BOGUS):
                return BOGUS
             elif (6 <= hour <= 18):
                return sunrise(date, location) + ((hour - 6) * h)
             elif (hour < 6):
                return sunset(date - 1, location) + ((hour + 6) * h)
             else:
                return sunset(date, location) + ((hour - 18) * h)
```

```
# see lines 3075-3079 in calendrica-3.0.cl
  def jewish_morning_end(date, location):
      """Return standard time on fixed date, date, at location, location,
      of \underline{\tt end} of morning according to Jewish ritual."""
      return standard_from_sundial(date + days_from_hours(10), location)
  # see lines 3081-3099 in calendrica-3.0.cl
  def asr(date, location):
      """Return standard time of asr on fixed date, date,
      at location, location."""
      noon = universal_from_standard(midday(date, location), location)
      phi = latitude(location)
      delta = declination(noon, deg(0), solar_longitude(noon))
      altitude = delta - phi - deg(90)
      h = arctan_degrees(tangent_degrees(altitude),
                           2 * tangent_degrees(altitude) + 1)
      # For Shafii use instead:
      # tangent_degrees(altitude) + 1)
      return dusk(date, location, -h)
  ######### here start the code inspired by Meeus
  # see lines 3101-3104 in calendrica-3.0.cl
  def universal_from_dynamical(tee):
      """Return Universal moment from Dynamical time, tee."""
      return tee - ephemeris_correction(tee)
  # see lines 3106-3109 in calendrica-3.0.cl
  def dynamical_from_universal(tee):
      """Return Dynamical time at Universal moment, tee."""
      return tee + ephemeris_correction(tee)
This definition is continued in chunks 107, 109, 111, 113, 115, 117, 119, 120, and 142.
This code is used in chunk 3.
Defines:
  asr, never used.
  daytime_temporal_hour, never used.
  dynamical_from_universal, used in chunks 100 and 106.
  jewish_dusk, never used.
  jewish_morning_end, never used.
  jewish_sabbath_ends, never used.
  nighttime_temporal_hour, never used.
  standard_from_sundial, used in chunk 136.
  universal_from_dynamical, used in chunks 106, 108, and 119.
Uses angle 100, arctan_degrees 100 100, BOGUS 13, days_from_hours 100, declination 102, deg 100,
  dusk 102, end 47, ephemeris_correction 107, fixed_from_moment 40, hour 39, latitude 100,
  location 100, midday 100, mod 15, solar_longitude 107, start 47, sunrise 102, sunset 102,
  tangent_degrees 100, and universal_from_standard 100.
```

```
106
       \langle astronomical\ lunar\ tests\ 106 \rangle \equiv
         def testUniversalFromDynamical(self):
             # from Meeus Example 10.a, pag 78
             date = gregorian_date(1977, FEBRUARY, 18)
             time = time_from_clock([3, 37, 40])
             td = fixed_from_gregorian(date) + time
             utc = universal_from_dynamical(td)
             clk = clock_from_moment(utc)
             self.assertEqual(hour(clk), 3)
             self.assertEqual(minute(clk), 36)
             self.assertEqual(iround(seconds(clk)), 52)
         def testDynamicalFromUniversal(self):
             # from Meeus Example 10.a, pag 78 (well, inverse of)
             date = gregorian_date(1977, FEBRUARY, 18)
             time = time_from_clock([3, 36, 52])
             utc = fixed_from_gregorian(date) + time
                 = dynamical_from_universal(utc)
             clk = clock_from_moment(td)
             self.assertEqual(hour(clk), 3)
             self.assertEqual(minute(clk), 37)
             self.assertEqual(iround(seconds(clk)), 40)
             # from Meeus Example 10.b, pag 79
             # I shoud get 7:42 but I get [7, 57, mpf('54.660540372133255')]
             # The equivalent CL
                   (load "calendrica-3.0.cl")
                   (in-package "CC3")
             #
                   (setq date (gregorian-date 333 february 6))
                   (setq time (time-from-clock '(6 0 0)))
                   (setq utc (+ (fixed-from-gregorian date) time))
                   (setq td (dynamical-from-universal utc))
                   (setq clk (clock-from-moment td))
             # gives (7 57 54.660540566742383817L0) on CLisp on PC
             # The reply from Prof Reingold and Dershowitz says:
             # From
                         Ed Reingold <reingold@emr.cs.iit.edu>
             # To
                         Enrico Spinielli <enrico.spinielli@googlemail.com>
             # Cc
                         nachumd@tau.ac.il
             # date
                         Thu, Aug 6, 2009 at 3:46 PM
             # subject Re: dynamical-from-universal values differ from Meeus
             # mailed-by emr.cs.iit.edu
             # hide details Aug 6
             # Our value of the ephemeris correction closely matches the value
             # given on the NASA web site
             # http://eclipse.gsfc.nasa.gov/SEhelp/deltat2004.html for 333
             # (interpolating between the years 300 and 400), namely,
             # their value is 7027 seconds, while ours is 7075 seconds.
             \mbox{\#} Meeus uses 6146 \mbox{seconds}, the difference amounts to about 14 minutes.
             # With Allegro Common Lisp, our functions
             # (clock-from-moment (dynamical-from-universal
                                     (+ (fixed-from-julian '(333 2 6)) 0.25L0)))
             # give
             #
                    (7 57 54.660540372133255d0)
             # while CLisp on my PC gives
                    (7 57 54.660540566742383817L0)
             # The difference in Delta-T explains Meeus's value of 7:42am.
```

```
# I then follow Calendrica Calculations (and NASA)
       date = gregorian_date(333, FEBRUARY, 6)
       time = time_from_clock([6, 0, 0])
      utc = fixed_from_gregorian(date) + time
       td = dynamical_from_universal(utc)
       clk = clock_from_moment(td)
       self.assertEqual(hour(clk), 7)
       self.assertEqual(minute(clk), 57)
       self.assertAlmostEqual(seconds(clk), 54.66054, 4)
This definition is continued in chunks 108, 110, 112, 114, 116, and 118.
This code is used in chunk 145.
Defines:
  {\tt testDynamicalFromUniversal}, \ {\rm never} \ {\rm used}.
  {\tt testUniversalFromDynamical}, \ {\rm never} \ {\rm used}.
Uses clock_from_moment 40, dynamical_from_universal 105, FEBRUARY 53, fixed_from_gregorian 55,
  gregorian_date 52, hour 39, iround 15, minute 39, seconds 39, time_from_clock 43,
  and universal_from_dynamical 105.
```

```
107
       \langle astronomical\ lunar\ calendars\ 105 \rangle + \equiv
         # see lines 3111-3114 in calendrica-3.0.cl
         J2000 = days_from_hours(mpf(12)) + gregorian_new_year(2000)
         # see lines 3116-3126 in calendrica-3.0.cl
         def sidereal_from_moment(tee):
             """Return the mean sidereal time of day from moment tee expressed
             as hour angle. Adapted from "Astronomical Algorithms"
             by Jean Meeus, Willmann_Bell, Inc., 1991."""
             c = (tee - J2000) / mpf(36525)
             return mod(poly(c, deg([mpf(280.46061837),
                                      mpf(36525) * mpf(360.98564736629),
                                      mpf(0.000387933),
                                      mpf(-1)/mpf(38710000)])),
                         360)
         # see lines 3128-3130 in calendrica-3.0.cl
         MEAN_TROPICAL_YEAR = mpf(365.242189)
         # see lines 3132-3134 in calendrica-3.0.cl
         MEAN_SIDEREAL_YEAR = mpf(365.25636)
         # see lines 93-97 in calendrica-3.0.errata.cl
         MEAN_SYNODIC_MONTH = mpf(29.530588861)
         # see lines 3140-3176 in calendrica-3.0.cl
         def ephemeris_correction(tee):
             """Return Dynamical Time minus Universal Time (in days) for
             moment, tee. Adapted from "Astronomical Algorithms"
             by Jean Meeus, Willmann_Bell, Inc., 1991."""
             year = gregorian_year_from_fixed(ifloor(tee))
             c = gregorian_date_difference(gregorian_date(1900, JANUARY, 1),
                                            gregorian_date(year, JULY, 1)) / mpf(36525)
             if (1988 <= year <= 2019):
                 return 1/86400 * (year - 1933)
             elif (1900 <= year <= 1987):
                 return poly(c, [mpf(-0.00002), mpf(0.000297), mpf(0.025184),
                                  mpf(-0.181133), mpf(0.553040), mpf(-0.861938),
                                  mpf(0.677066), mpf(-0.212591)])
             elif (1800 <= year <= 1899):
                 return poly(c, [mpf(-0.000009), mpf(0.003844), mpf(0.083563),
                                  mpf(0.865736), mpf(4.867575), mpf(15.845535),
                                  mpf(31.332267), mpf(38.291999), mpf(28.316289),
                                  mpf(11.636204), mpf(2.043794)])
             elif (1700 <= year <= 1799):
                 return (1/86400 *
                         poly(year - 1700, [8.118780842, -0.005092142,
                                             0.003336121, -0.0000266484]))
             elif (1620 <= year <= 1699):
                 return (1/86400 *
                         poly(year - 1600,
                               [mpf(196.58333), mpf(-4.0675), mpf(0.0219167)]))
             else:
                 x = (days_from_hours(mpf(12)) +
                       gregorian_date_difference(gregorian_date(1810, JANUARY, 1),
                                                 gregorian_date(year, JANUARY, 1)))
                 return 1/86400 * (((x * x) / mpf(41048480)) - 15)
         # see lines 3178-3207 in calendrica-3.0.cl
         def equation_of_time(tee):
             """Return the equation of time (as fraction of day) for moment, tee.
```

```
Adapted from "Astronomical Algorithms" by Jean Meeus,
   Willmann_Bell, Inc., 1991."""
   c = julian_centuries(tee)
   lamb = poly(c, deg([mpf(280.46645), mpf(36000.76983), mpf(0.0003032)]))
   anomaly = poly(c, deg([mpf(357.52910), mpf(35999.05030),
                               mpf(-0.0001559), mpf(-0.00000048)]))
    eccentricity = poly(c, [mpf(0.016708617),
                            mpf(-0.000042037)
                            mpf(-0.000001236)])
   varepsilon = obliquity(tee)
   y = pow(tangent_degrees(varepsilon / 2), 2)
    equation = ((1/2 / pi) *
                (y * sin_degrees(2 * lamb) +
                 -2 * eccentricity * sin_degrees(anomaly) +
                 (4 * eccentricity * y * sin_degrees(anomaly) *
                 cosine_degrees(2 * lamb)) +
                 -0.5 * y * y * sin_degrees(4 * lamb) +
                 -1.25 * eccentricity * eccentricity * sin_degrees(2 * anomaly)))
   return signum(equation) * min(abs(equation), days_from_hours(mpf(12)))
# see lines 3209-3259 in calendrica-3.0.cl
def solar_longitude(tee):
    """Return the longitude of sun at moment 'tee'.
   Adapted from 'Planetary Programs and Tables from -4000 to +2800'
   by Pierre Bretagnon and Jean_Louis Simon, Willmann_Bell, Inc., 1986.
   See also pag 166 of 'Astronomical Algorithms' by Jean Meeus, 2nd Ed 1998,
   with corrections Jun 2005."""
   c = julian_centuries(tee)
   coefficients = [403406, 195207, 119433, 112392, 3891, 2819, 1721,
                    660, 350, 334, 314, 268, 242, 234, 158, 132, 129, 114,
                    99, 93, 86, 78,72, 68, 64, 46, 38, 37, 32, 29, 28, 27, 27,
                    25, 24, 21, 21, 20, 18, 17, 14, 13, 13, 13, 12, 10, 10, 10,
   multipliers = [mpf(0.9287892), mpf(35999.1376958), mpf(35999.4089666),
                  mpf(35998.7287385), mpf(71998.20261), mpf(71998.4403),
                   mpf(36000.35726), mpf(71997.4812), mpf(32964.4678),
                  mpf(-19.4410), mpf(445267.1117), mpf(45036.8840), mpf(3.1008),
                  mpf(22518.4434), mpf(-19.9739), mpf(65928.9345),
                  mpf(9038.0293), mpf(3034.7684), mpf(33718.148), mpf(3034.448),
                  mpf(-2280.773), mpf(29929.992), mpf(31556.493), mpf(149.588),
                  mpf(9037.750), mpf(107997.405), mpf(-4444.176), mpf(151.771),
                   mpf(67555.316), mpf(31556.080), mpf(-4561.540),
                  mpf(107996.706), mpf(1221.655), mpf(62894.167),
                  mpf(31437.369), mpf(14578.298), mpf(-31931.757),
                  mpf(34777.243), mpf(1221.999), mpf(62894.511),
                  mpf(-4442.039), mpf(107997.909), mpf(119.066), mpf(16859.071),
                  mpf(-4.578), mpf(26895.292), mpf(-39.127), mpf(12297.536),
                  mpf(90073.778)]
    addends = [mpf(270.54861), mpf(340.19128), mpf(63.91854), mpf(331.26220),
              mpf(317.843), mpf(86.631), mpf(240.052), mpf(310.26), mpf(247.23),
              mpf(260.87), mpf(297.82), mpf(343.14), mpf(166.79), mpf(81.53),
              mpf(3.50), mpf(132.75), mpf(182.95), mpf(162.03), mpf(29.8),
              mpf(266.4), mpf(249.2), mpf(157.6), mpf(257.8), mpf(185.1),
              mpf(69.9), mpf(8.0), mpf(197.1), mpf(250.4), mpf(65.3),
              mpf(162.7), mpf(341.5), mpf(291.6), mpf(98.5), mpf(146.7),
              mpf(110.0), mpf(5.2), mpf(342.6), mpf(230.9), mpf(256.1),
              mpf(45.3), mpf(242.9), mpf(115.2), mpf(151.8), mpf(285.3),
              mpf(53.3), mpf(126.6), mpf(205.7), mpf(85.9), mpf(146.1)]
   lam = (deg(mpf(282.7771834)) +
           deg(mpf(36000.76953744)) * c +
           deg(mpf(0.000005729577951308232)) *
```

```
sigma([coefficients, addends, multipliers],
                     lambda x, y, z: x * sin_{degrees}(y + (z * c)))
      return mod(lam + aberration(tee) + nutation(tee), 360)
  def geometric_solar_mean_longitude(tee):
       """Return the geometric mean longitude of the Sun at moment, tee,
      referred to mean equinox of the date."""
      c = julian_centuries(tee)
      return poly(c, deg([mpf(280.46646), mpf(36000.76983), mpf(0.0003032)]))
  def solar_latitude(tee):
      """Return the latitude of Sun (in degrees) at moment, tee.
      Adapted from "Astronomical Algorithms" by Jean Meeus,
      Willmann_Bell, Inc., 1998."""
      pass
  def solar_distance(tee):
      """Return the distance of Sun (in degrees) at moment, tee.
      Adapted from "Astronomical Algorithms" by Jean Meeus,
      Willmann_Bell, Inc., 1998."""
      pass
  def solar_position(tee):
      """Return the position of the Sun (geocentric latitude and longitude [in degrees]
      and distance [in meters]) at moment, tee.
      Adapted from "Astronomical Algorithms" by Jean Meeus,
      Willmann_Bell, Inc., 2nd ed."""
      return (solar_latitude(tee), solar_longitude(tee), solar_distance(tee))
  # see lines 3261-3271 in calendrica-3.0.cl
  def nutation(tee):
      """Return the longitudinal nutation at moment, tee."""
      c = julian_centuries(tee)
      cap_A = poly(c, deg([mpf(124.90), mpf(-1934.134), mpf(0.002063)]))
      cap_B = poly(c, deg([mpf(201.11), mpf(72001.5377), mpf(0.00057)]))
      return (deg(mpf(-0.004778)) * sin_degrees(cap_A) +
               deg(mpf(-0.0003667)) * sin_degrees(cap_B))
This code is used in chunk 3.
Defines:
  {\tt ephemeris\_correction}, \, {\rm used} \, \, {\rm in} \, \, {\rm chunk} \, \, 105.
  equation_of_time, used in chunk 100.
  geometric_solar_mean_longitude, never used.
  J2000, used in chunks 100, 102, 109, and 119.
  MEAN_SIDEREAL_YEAR, used in chunk 136.
  MEAN_SYNODIC_MONTH, used in chunks 119, 133, and 142.
  MEAN_TROPICAL_YEAR, used in chunks 109, 122, 125, 130, and 133.
  nutation, used in chunks 102, 108, and 119.
  sidereal_from_moment, used in chunk 120.
  solar_distance, never used.
  solar_latitude, never used.
  solar_longitude, used in chunks 102, 105, 109, 119, 122, 125, 130, 133, 136, and 196.
  solar position, never used.
Uses aberration 109, angle 100, cosine_degrees 100, days_from_hours 100, deg 100, gregorian_date
  52, gregorian_date_difference 56, gregorian_new_year 56, gregorian_year_from_fixed 55,
  hour 39, ifloor 15, JANUARY 53, julian_centuries 100, JULY 53, latitude 100, longitude 100,
  mod 15, obliquity 101, poly 34, sigma 31, signum 100, sin_degrees 100, and tangent_degrees 100.
```

```
def testNutation(self):
    # from Meeus, pag 343
    TD = fixed_from_gregorian(gregorian_date(1992, APRIL, 12))
    tee = universal_from_dynamical(TD)
    self.assertAlmostEqual(nutation(tee), mpf(0.004610), 3)

This code is used in chunk 145.
Defines:
    testNutation, never used.
Uses APRIL 53, fixed_from_gregorian 55, gregorian_date 52, nutation 107, and universal_from_dynamical 105.
```

```
109
       \langle astronomical\ lunar\ calendars\ 105 \rangle + \equiv
         # see lines 3273-3281 in calendrica-3.0.cl
         def aberration(tee):
             """Return the aberration at moment, tee."""
             c = julian_centuries(tee)
             return ((deg(mpf(0.0000974)) *
                       cosine_degrees(deg(mpf(177.63)) + deg(mpf(35999.01848)) * c)) -
                     deg(mpf(0.005575)))
         # see lines 3283-3295 in calendrica-3.0.cl
         def solar_longitude_after(lam, tee):
             """Return the moment UT of the first time at or after moment, tee,
             when the solar longitude will be lam degrees."""
             rate = MEAN_TROPICAL_YEAR / deg(360)
             tau = tee + rate * mod(lam - solar_longitude(tee), 360)
             a = max(tee, tau - 5)
             b = tau + 5
             return invert_angular(solar_longitude, lam, a, b)
         # see lines 3297-3300 in calendrica-3.0.cl
         SPRING = deg(0)
         # see lines 3302-3305 in calendrica-3.0.cl
         SUMMER = deg(90)
         # see lines 3307-3310 in calendrica-3.0.cl
         AUTUMN = deg(180)
         # see lines 3312-3315 in calendrica-3.0.cl
         WINTER = deg(270)
         # see lines 3317-3339 in calendrica-3.0.cl
         def precession(tee):
             """Return the precession at moment tee using 0,0 as J2000 coordinates.
             Adapted from "Astronomical Algorithms" by Jean Meeus,
             Willmann-Bell, Inc., 1991."""
             c = julian_centuries(tee)
             eta = mod(poly(c, [0,
                                 secs(mpf(47.0029)),
                                 secs(mpf(-0.03302)),
                                 secs(mpf(0.000060))]),
                        360)
             cap_P = mod(poly(c, [deg(mpf(174.876384)),
                                   secs(mpf(-869.8089)),
                                   secs(mpf(0.03536))]),
                          360)
             p = mod(poly(c, [0,
                               secs(mpf(5029.0966)),
                               secs(mpf(1.11113)),
                               secs(mpf(0.000006))]),
                     360)
             cap_A = cosine_degrees(eta) * sin_degrees(cap_P)
             cap_B = cosine_degrees(cap_P)
             arg = arctan_degrees(cap_A, cap_B)
             return mod(p + cap_P - arg, 360)
         # see lines 3341-3347 in calendrica-3.0.cl
         def sidereal_solar_longitude(tee):
             """Return sidereal solar longitude at moment, tee."""
             return mod(solar_longitude(tee) - precession(tee) + SIDEREAL_START, 360)
```

```
# see lines 3349-3365 in calendrica-3.0.cl
          def estimate_prior_solar_longitude(lam, tee):
              """Return approximate moment at or before tee
              when solar longitude just exceeded lam degrees."""
              rate = MEAN_TROPICAL_YEAR / deg(360)
              tau = tee - (rate * mod(solar_longitude(tee) - lam, 360))
              cap_Delta = mod(solar_longitude(tau) - lam + deg(180), 360) - deg(180)
              return min(tee, tau - (rate * cap_Delta))
          # see lines 3367-3376 in calendrica-3.0.cl
          def mean_lunar_longitude(c):
              """Return mean longitude of moon (in degrees) at moment
              given in Julian centuries c (including the constant term of the
              effect of the light-time (-0".70).
              Adapted from eq. 47.1 in "Astronomical Algorithms" by Jean Meeus,
              Willmann_Bell, Inc., 2nd ed. with corrections, 2005."""
              return normalized_degrees(poly(c,deg([mpf(218.3164477), mpf(481267.88123421),
                                            mpf(-0.0015786), mpf(1/538841),
                                            mpf(-1/65194000)])))
        This code is used in chunk 3.
        Defines:
          aberration, used in chunk 107.
          AUTUMN, used in chunks 130 and 196.
          estimate_prior_solar_longitude, used in chunks 122, 125, 130, and 133.
          mean_lunar_longitude, used in chunks 110 and 119.
          precession, used in chunks 119 and 136.
          sidereal_solar_longitude, used in chunk 136.
          solar_longitude_after, used in chunks 102, 133, 142, and 196.
          SPRING, used in chunks 122, 125, 142, and 196.
          SUMMER, used in chunk 196.
          WINTER, used in chunks 102, 133, and 196.
        Uses arctan_degrees 100 100, cosine_degrees 100, deg 100, invert_angular 28 28, J2000 107,
          julian_centuries 100, longitude 100, MEAN_TROPICAL_YEAR 107, mod 15, normalized_degrees 100,
          poly 34, secs 100, SIDEREAL_START 136, sin_degrees 100, and solar_longitude 107.
110
        \langle astronomical\ lunar\ tests\ 106 \rangle + \equiv
          def testMeanLunarLongitude(self):
              # from Example 47.a in Jan Meeus "Astronomical Algorithms" pag 342
              self.assertAlmostEqual(mean_lunar_longitude(-0.077221081451), 134.290182, 6)
        This code is used in chunk 145.
        Defines:
          testMeanLunarLongitude, never used.
        Uses mean_lunar_longitude 109.
111
        \langle astronomical\ lunar\ calendars\ 105 \rangle + \equiv
          # see lines 3378-3387 in calendrica-3.0.cl
          def lunar_elongation(c):
               """Return elongation of moon (in degrees) at moment
              given in Julian centuries c.
              Adapted from eq. 47.2 in "Astronomical Algorithms" by Jean Meeus,
              Willmann_Bell, Inc., 2nd ed. with corrections, 2005."""
              return normalized_degrees(poly(c, deg([mpf(297.8501921), mpf(445267.1114034),
                                             mpf(-0.0018819), mpf(1/545868),
                                             mpf(-1/113065000)])))
        This code is used in chunk 3.
        Defines:
          lunar_elongation, used in chunks 112, 119, and 120.
        Uses deg 100, normalized_degrees 100, and poly 34.
```

```
112
        \langle astronomical\ lunar\ tests\ 106 \rangle + \equiv
          def testLunarElongation(self):
               # from Example 47.a in Jan Meeus "Astronomical Algorithms" pag 342
               self.assertAlmostEqual(lunar_elongation(-0.077221081451), 113.842304, 6)
        This code is used in chunk 145.
        Defines:
          testLunarElongation, never used.
        Uses lunar_elongation 111.
        \langle astronomical\ lunar\ calendars\ 105 \rangle + \equiv
113
          # see lines 3389-3398 in calendrica-3.0.cl
          def solar_anomaly(c):
               """Return mean anomaly of sun (in degrees) at moment
               given in Julian centuries c.
               Adapted from eq. 47.3 in "Astronomical Algorithms" by Jean Meeus,
               Willmann_Bell, Inc., 2nd ed. with corrections, 2005."""
               return normalized_degrees(poly(c,deg([mpf(357.5291092), mpf(35999.0502909),
                                             mpf(-0.0001536), mpf(1/24490000)])))
        This code is used in chunk 3.
        Defines:
          solar_anomaly, used in chunks 114, 119, 120, and 139.
        Uses deg 100, normalized_degrees 100, and poly 34.
114
        \langle astronomical\ lunar\ tests\ 106 \rangle + \equiv
          def testSolarAnomaly(self):
               # from Example 47.a in Jan Meeus "Astronomical Algorithms" pag 342
               self.assertAlmostEqual(solar_anomaly(-0.077221081451), 97.643514, 6)
        This code is used in chunk 145.
        Defines:
          testSolarAnomaly, never used.
        Uses solar_anomaly 113.
        \langle astronomical\ lunar\ calendars\ 105 \rangle + \equiv
115
          # see lines 3400-3409 in calendrica-3.0.cl
          def lunar_anomaly(c):
               """Return mean anomaly of moon (in degrees) at moment
               given in Julian centuries c.
               Adapted from eq. 47.4 in "Astronomical Algorithms" by Jean Meeus,
               Willmann_Bell, Inc., 2nd ed. with corrections, 2005."""
               return normalized_degrees(poly(c, deg([mpf(134.9633964), mpf(477198.8675055),
                                              mpf(0.0087414), mpf(1/69699),
                                              mpf(-1/14712000)])))
        This code is used in chunk 3.
        Defines:
          lunar_anomaly, used in chunks 116, 119, 120, and 139.
        Uses deg 100, normalized_degrees 100, and poly 34.
116
        \langle astronomical\ lunar\ tests\ 106 \rangle + \equiv
          def testLunarAnomaly(self):
               # from Example 47.a in Jan Meeus "Astronomical Algorithms" pag 342
               self.assertAlmostEqual(lunar_anomaly(-0.077221081451), 5.150833, 6)
        This code is used in chunk 145.
          testLunarAnomaly, never used.
        Uses lunar_anomaly 115.
```

```
\langle astronomical\ lunar\ calendars\ 105 \rangle + \equiv
117
                                  # see lines 3411-3420 in calendrica-3.0.cl
                                  def moon_node(c):
                                                """Return Moon's argument of <a href="latitude">latitude</a> (in degrees) at moment
                                                given in Julian centuries 'c'.
                                                Adapted from eq. 47.5 in "Astronomical Algorithms" by Jean Meeus,
                                                Willmann_Bell, Inc., 2nd ed. with corrections, 2005."""
                                                \texttt{return normalized\_degrees(poly(c, deg([mpf(93.2720950), mpf(483202.0175233), mpf(483202.01752333), mpf(483202.0175233), mpf(483202.0175233), mpf(483202.0175233), mpf(483202.0175233), mpf(483202.0175233), mpf(483202.0175233), mpf(483202.0175233), mpf(483202.01752333), mpf(483202.01752333), mpf(483202.01752333), mpf(483202.0175233330), mpf(483202.017523333), mpf(483200.01752333), mpf(483200.01752333), mpf(483200.01752333),
                                                                                                                                                     mpf(-0.0036539), mpf(-1/3526000),
                                                                                                                                                     mpf(1/863310000)])))
                          This code is used in chunk 3.
                          Defines:
                                 moon_node, used in chunks 118-20.
                          Uses deg 100, latitude 100, normalized_degrees 100, and poly 34.
118
                          \langle astronomical\ lunar\ tests\ 106 \rangle + \equiv
                                  def testMoonNode(self):
                                                # from Example 47.a in Jan Meeus "Astronomical Algorithms" pag 342
                                                self.assertAlmostEqual(moon_node(-0.077221081451), 219.889721, 6)
                           This code is used in chunk 145.
                          Defines:
                                  {\tt testMoonNode}, \ {\rm never} \ {\rm used}.
                           Uses moon_node 117.
```

```
119
       \langle astronomical\ lunar\ calendars\ 105 \rangle + \equiv
         # see lines 3422-3485 in calendrica-3.0.cl
         def lunar_longitude(tee):
             """Return longitude of moon (in degrees) at moment tee.
             Adapted from "Astronomical Algorithms" by Jean Meeus,
             Willmann_Bell, Inc., 2nd ed., 1998."""
             c = julian_centuries(tee)
             cap_L_prime = mean_lunar_longitude(c)
             cap_D = lunar_elongation(c)
             cap_M = solar_anomaly(c)
             cap_M_prime = lunar_anomaly(c)
             cap_F = moon_node(c)
             # see eq. 47.6 in Meeus
             cap_E = poly(c, [1, mpf(-0.002516), mpf(-0.0000074)])
             args_lunar_elongation = \
                     [0, 2, 2, 0, 0, 0, 2, 2, 2, 2, 0, 1, 0, 2, 0, 0, 4, 0, 4, 2, 2, 1,
                      1, 2, 2, 4, 2, 0, 2, 2, 1, 2, 0, 0, 2, 2, 2, 4, 0, 3, 2, 4, 0, 2,
                      2, 2, 4, 0, 4, 1, 2, 0, 1, 3, 4, 2, 0, 1, 2]
             args_solar_anomaly = \
                     [0, 0, 0, 0, 1, 0, 0, -1, 0, -1, 1, 0, 1, 0, 0, 0, 0, 0, 0, 1, 1,
                      0, 1, -1, 0, 0, 0, 1, 0, -1, 0, -2, 1, 2, -2, 0, 0, -1, 0, 0, 1,
                      -1, 2, 2, 1, -1, 0, 0, -1, 0, 1, 0, 1, 0, 0, -1, 2, 1, 0]
             args_lunar_anomaly = \
                     [1, -1, 0, 2, 0, 0, -2, -1, 1, 0, -1, 0, 1, 0, 1, 1, -1, 3, -2,
                      -1, 0, -1, 0, 1, 2, 0, -3, -2, -1, -2, 1, 0, 2, 0, -1, 1, 0,
                      -1, 2, -1, 1, -2, -1, -1, -2, 0, 1, 4, 0, -2, 0, 2, 1, -2, -3,
                      2, 1, -1, 3]
             args_moon_node = \
                     0, 0, 0, 0, 0, 0, 2, 0, 0, 0, 0, 0, -2, 2, 0, 2, 0, 0, 0,
                      0, 0, -2, 0, 0, 0, -2, -2, 0, 0, 0, 0, 0, 0]
             sine_coefficients = \
                     [6288774,1274027,658314,213618,-185116,-114332,
                      58793,57066,53322,45758,-40923,-34720,-30383,
                      15327,-12528,10980,10675,10034,8548,-7888,
                      -6766, -5163, 4987, 4036, 3994, 3861, 3665, -2689,
                      -2602, 2390, -2348, 2236, -2120, -2069, 2048, -1773,
                      -1595,1215,-1110,-892,-810,759,-713,-700,691,
                      596,549,537,520,-487,-399,-381,351,-340,330,
                      327, -323, 299, 294]
             correction = (deg(1/1000000) *
                           sigma([sine_coefficients, args_lunar_elongation,
                                  args_solar_anomaly, args_lunar_anomaly,
                                  args_moon_node],
                                 lambda v, w, x, y, z:
                                 v * pow(cap_E, abs(x)) *
                                 sin_degrees((w * cap_D) +
                                             (x * cap_M) +
                                             (y * cap_M_prime) +
                                             (z * cap_F))))
             A1 = deg(mpf(119.75)) + (c * deg(mpf(131.849)))
             venus = (deg(3958/1000000) * sin_degrees(A1))
             A2 = deg(mpf(53.09)) + c * deg(mpf(479264.29))
             jupiter = (deg(318/1000000) * sin_degrees(A2))
             flat_earth = (deg(1962/1000000) * sin_degrees(cap_L_prime - cap_F))
             return mod(cap_L_prime + correction + venus +
                        jupiter + flat_earth + nutation(tee), 360)
         # see lines 3663-3732 in calendrica-3.0.cl
         def lunar_latitude(tee):
```

```
"""Return the latitude of moon (in degrees) at moment, tee.
   Adapted from "Astronomical Algorithms" by Jean Meeus,
   Willmann_Bell, Inc., 1998."""
   c = julian_centuries(tee)
   cap_L_prime = mean_lunar_longitude(c)
   cap_D = lunar_elongation(c)
   cap_M = solar_anomaly(c)
   cap_M_prime = lunar_anomaly(c)
   cap_F = moon_node(c)
   cap_E = poly(c, [1, mpf(-0.002516), mpf(-0.0000074)])
   args_lunar_elongation = \
            [0, 0, 0, 2, 2, 2, 2, 0, 2, 0, 2, 2, 2, 2, 2, 2, 2, 2, 0, 4, 0, 0, 0, 0]
            1, 0, 0, 0, 1, 0, 4, 4, 0, 4, 2, 2, 2, 2, 0, 2, 2, 2, 2, 4, 2, 2,
            0, 2, 1, 1, 0, 2, 1, 2, 0, 4, 4, 1, 4, 1, 4, 2]
   args_solar_anomaly = \
            [0, 0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 0, 0, 1, -1, -1, -1, 1, 0, 1,
            0, 1, 0, 1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, -1, 0, 0, 0, 1, 1,
            0, -1, -2, 0, 1, 1, 1, 1, 1, 0, -1, 1, 0, -1, 0, 0, 0, -1, -2]
   args_lunar_anomaly = \
            [0, 1, 1, 0, -1, -1, 0, 2, 1, 2, 0, -2, 1, 0, -1, 0, -1, -1, -1,
            0, 0, -1, 0, 1, 1, 0, 0, 3, 0, -1, 1, -2, 0, 2, 1, -2, 3, 2, -3,
            -1, 0, 0, 1, 0, 1, 1, 0, 0, -2, -1, 1, -2, 2, -2, -1, 1, 1, -2,
            0, 0]
   args_moon_node = \
           -1, 1, 3, 1, 1, 1, -1, -1, 1, -1, 1, -3, 1, -3, -1, -1, 1,
            -1, 1, -1, 1, 1, 1, -1, 3, -1, -1, 1, -1, -1, 1, -1, 1, -1,
            -1, -1, -1, -1, -1, 1]
   sine_coefficients = \
            [5128122, 280602, 277693, 173237, 55413, 46271, 32573,
            17198, 9266, 8822, 8216, 4324, 4200, -3359, 2463, 2211,
            2065, -1870, 1828, -1794, -1749, -1565, -1491, -1475,
            -1410, -1344, -1335, 1107, 1021, 833, 777, 671, 607,
            596, 491, -451, 439, 422, 421, -366, -351, 331, 315,
            302, -283, -229, 223, 223, -220, -220, -185, 181,
            -177, 176, 166, -164, 132, -119, 115, 107]
   beta = (deg(1/1000000) *
           sigma([sine_coefficients,
                  args_lunar_elongation,
                  args_solar_anomaly,
                  args_lunar_anomaly,
                  args_moon_node],
                 lambda v, w, x, y, z: (v *
                                        pow(cap_E, abs(x)) *
                                        sin_degrees((w * cap_D) +
                                                    (x * cap_M) +
                                                    (y * cap_M_prime) +
                                                    (z * cap_F)))))
   venus = (deg(175/1000000) *
            (\sin_{\deg(mpf(119.75))} + c * \deg(mpf(131.849)) + cap_F) +
             sin_degrees(deg(mpf(119.75)) + c * deg(mpf(131.849)) - cap_F)))
   flat_earth = (deg(-2235/1000000) * sin_degrees(cap_L_prime) +
                 deg(127/1000000) * sin_degrees(cap_L_prime - cap_M_prime) +
                 deg(-115/1000000) * sin_degrees(cap_L_prime + cap_M_prime))
   extra = (deg(382/1000000) *
            sin_degrees(deg(mpf(313.45)) + c * deg(mpf(481266.484))))
   return beta + venus + flat_earth + extra
# see lines 192-197 in calendrica-3.0.errata.cl
def lunar_node(tee):
```

```
"""Return Angular distance of the node from the equinoctal point
   at fixed moment, tee.
   Adapted from eq. 47.7 in "Astronomical Algorithms"
   by Jean Meeus, Willmann_Bell, Inc., 2nd ed., 1998
   with corrections June 2005."""
   return mod(moon_node(julian_centuries(tee)) + deg(90), 180) - 90
def alt_lunar_node(tee):
    """Return Angular distance of the node from the equinoctal point
   at fixed moment, tee.
   Adapted from eq. 47.7 in "Astronomical Algorithms"
   by Jean Meeus, Willmann_Bell, Inc., 2nd ed., 1998
   with corrections June 2005."""
   return normalized_degrees(poly(julian_centuries(tee), deg([mpf(125.0445479),
                                                     mpf(-1934.1362891),
                                                     mpf(0.0020754),
                                                     mpf(1/467441),
                                                     mpf(-1/60616000)])))
def lunar_true_node(tee):
    """Return Angular distance of the true node (the node of the instantaneus
   lunar orbit) from the equinoctal point at moment, tee.
   Adapted from eq. 47.7 and pag. 344 in "Astronomical Algorithms"
   by Jean Meeus, Willmann_Bell, Inc., 2nd ed., 1998
   with corrections June 2005."""
   c = julian_centuries(tee)
   cap_D = lunar_elongation(c)
   cap_M = solar_anomaly(c)
   cap_M_prime = lunar_anomaly(c)
   cap_F = moon_node(c)
   periodic_terms = (deg(-1.4979) * sin_degrees(2 * (cap_D - cap_F)) +
                      deg(-0.1500) * sin_degrees(cap_M) +
                      deg(-0.1226) * sin_degrees(2 * cap_D) +
                      deg(0.1176) * sin_degrees(2 * cap_F) +
                      deg(-0.0801) * sin_degrees(2 * (cap_M_prime - cap_F)))
   return alt_lunar_node(tee) + periodic_terms
def lunar_perigee(tee):
    """Return Angular distance of the perigee from the equinoctal point
   at moment, tee.
   Adapted from eq. 47.7 in "Astronomical Algorithms"
   by Jean Meeus, Willmann_Bell, Inc., 2nd ed., 1998
   with corrections June 2005."""
   return normalized_degrees(poly(julian_centuries(tee), deg([mpf(83.3532465),
                                                     mpf(4069.0137287),
                                                     mpf(-0.0103200),
                                                     mpf(-1/80053),
                                                     mpf(1/18999000)])))
# see lines 199-206 in calendrica-3.0.errata.cl
def sidereal_lunar_longitude(tee):
    """Return sidereal lunar longitude at moment, tee."""
   return mod(lunar_longitude(tee) - precession(tee) + SIDEREAL_START, 360)
# see lines 99-190 in calendrica-3.0.errata.cl
def nth_new_moon(n):
   """Return the moment of n-th new moon after (or before) the new moon
   of January 11, 1. Adapted from "Astronomical Algorithms"
   by Jean Meeus, Willmann_Bell, Inc., 2nd ed., 1998."""
```

```
n0 = 24724
k = n - n0
c = k / mpf(1236.85)
approx = (J2000 +
         poly(c, [mpf(5.09766),
                  MEAN_SYNODIC_MONTH * mpf(1236.85),
                  mpf(0.0001437),
                  mpf(-0.00000150),
                  mpf(0.0000000073)]))
cap_E = poly(c, [1, mpf(-0.002516), mpf(-0.0000074)])
solar_anomaly = poly(c, deg([mpf(2.5534),
                            (mpf(1236.85) * mpf(29.10535669)),
                            mpf(-0.0000014), mpf(-0.00000011)]))
lunar_anomaly = poly(c, deg([mpf(201.5643),
                            (mpf(385.81693528) * mpf(1236.85)),
                            {\tt mpf(0.0107582), mpf(0.00001238),}
                            mpf(-0.000000058)]))
moon_argument = poly(c, deg([mpf(160.7108),
                            (mpf(390.67050284) * mpf(1236.85)),
                            mpf(-0.0016118), mpf(-0.00000227),
                            mpf(0.00000011)]))
cap\_omega = poly(c, [mpf(124.7746),
                    (mpf(-1.56375588) * mpf(1236.85)),
                    mpf(0.0020672), mpf(0.00000215)])
0, 0, 0, 0, 0, 0]
solar_coeff = [0, 1, 0, 0, -1, 1, 2, 0, 0, 1, 0, 1, 1, -1, 2,
              0, 3, 1, 0, 1, -1, -1, 1, 0]
lunar_coeff = [1, 0, 2, 0, 1, 1, 0, 1, 1, 2, 3, 0, 0, 2, 1, 2,
              0, 1, 2, 1, 1, 1, 3, 4]
moon_coeff = [0, 0, 0, 2, 0, 0, 0, -2, 2, 0, 0, 2, -2, 0, 0,
              -2, 0, -2, 2, 2, 2, -2, 0, 0]
sine\_coeff = [mpf(-0.40720), mpf(0.17241), mpf(0.01608),
             mpf(0.01039), mpf(0.00739), mpf(-0.00514),
             mpf(0.00208), mpf(-0.00111), mpf(-0.00057),
             mpf(0.00056), mpf(-0.00042), mpf(0.00042),
             mpf(0.00038), mpf(-0.00024), mpf(-0.00007),
             mpf(0.00004), mpf(0.00004), mpf(0.00003),
             mpf(0.00003), mpf(-0.00003), mpf(0.00003),
             mpf(-0.00002), mpf(-0.00002), mpf(0.00002)]
correction = ((deg(mpf(-0.00017)) * sin_degrees(cap_omega)) +
              sigma([sine_coeff, E_factor, solar_coeff,
                    lunar_coeff, moon_coeff],
                   lambda v, w, x, y, z: (v *
                               pow(cap_E, w) *
                               sin_degrees((x * solar_anomaly) +
                                           (y * lunar_anomaly) +
                                           (z * moon_argument)))))
add_const = [mpf(251.88), mpf(251.83), mpf(349.42), mpf(84.66),
            mpf(141.74), mpf(207.14), mpf(154.84), mpf(34.52),
            mpf(207.19), mpf(291.34), mpf(161.72), mpf(239.56),
            mpf(331.55)]
add_coeff = [mpf(0.016321), mpf(26.651886), mpf(36.412478),
            mpf(18.206239), mpf(53.303771), mpf(2.453732),
            mpf(7.306860), mpf(27.261239), mpf(0.121824),
            mpf(1.844379), mpf(24.198154), mpf(25.513099),
            mpf(3.592518)]
add_factor = [mpf(0.000165), mpf(0.000164), mpf(0.000126),
             mpf(0.000110), mpf(0.000062), mpf(0.000060),
             mpf(0.000056), mpf(0.000047), mpf(0.000042),
             mpf(0.000040), mpf(0.000037), mpf(0.000035),
```

```
mpf(0.000023)]
    extra = (deg(mpf(0.000325)) *
             sin_degrees(poly(c, deg([mpf(299.77), mpf(132.8475848),
                                      mpf(-0.009173)]))))
   additional = sigma([add_const, add_coeff, add_factor],
                       lambda i, j, 1: 1 * sin_degrees(i + j * k))
   return universal_from_dynamical(approx + correction + extra + additional)
# see lines 3578-3585 in calendrica-3.0.cl
def new_moon_before(tee):
   """Return the moment UT of last new moon before moment tee."""
   t0 = nth_new_moon(0)
   phi = lunar_phase(tee)
   n = iround(((tee - t0) / MEAN_SYNODIC_MONTH) - (phi / deg(360)))
   return nth_new_moon(final(n - 1, lambda k: nth_new_moon(k) < tee))</pre>
# see lines 3587-3594 in calendrica-3.0.cl
def new_moon_at_or_after(tee):
    """Return the moment UT of first new moon at or after moment, tee."""
   t0 = nth_new_moon(0)
   phi = lunar_phase(tee)
   n = iround((tee - t0) / MEAN_SYNODIC_MONTH - phi / deg(360))
   return nth_new_moon(next(n, lambda k: nth_new_moon(k) >= tee))
# see lines 3596-3613 in calendrica-3.0.cl
def lunar_phase(tee):
    """Return the lunar phase, as an angle in degrees, at moment tee.
   An angle of 0 means a new moon, 90 degrees means the
   first quarter, 180 means a full moon, and 270 degrees
   means the last quarter."""
   phi = mod(lunar_longitude(tee) - solar_longitude(tee), 360)
   t0 = nth_new_moon(0)
   n = iround((tee - t0) / MEAN_SYNODIC_MONTH)
   phi_prime = (deg(360) *
                mod((tee - nth_new_moon(n)) / MEAN_SYNODIC_MONTH, 1))
   if abs(phi - phi_prime) > deg(180):
       return phi_prime
   else:
       return phi
# see lines 3615-3625 in calendrica-3.0.cl
def lunar_phase_at_or_before(phi, tee):
    """Return the moment UT of the last time at or before moment, tee,
   when the lunar_phase was phi degrees."""
   tau = (tee -
           (MEAN_SYNODIC_MONTH *
            (1/\deg(360)) *
            mod(lunar_phase(tee) - phi, 360)))
   a = tau - 2
   b = min(tee, tau +2)
   return invert_angular(lunar_phase, phi, a, b)
# see lines 3627-3631 in calendrica-3.0.cl
NEW = deg(0)
```

```
# see lines 3633-3637 in calendrica-3.0.cl
  FIRST_QUARTER = deg(90)
  # see lines 3639-3643 in calendrica-3.0.cl
  FULL = deg(180)
  # see lines 3645-3649 in calendrica-3.0.cl
  LAST_QUARTER = deg(270)
  # see lines 3651-3661 in calendrica-3.0.cl
  def lunar_phase_at_or_after(phi, tee):
       """Return the moment UT of the next time at or after moment, tee,
       when the lunar_phase is phi degrees."""
       tau = (tee +
                (MEAN_SYNODIC_MONTH
                 (1/\deg(360)) *
                 mod(phi - lunar_phase(tee), 360)))
       a = max(tee, tau - 2)
       b = tau + 2
       return invert_angular(lunar_phase, phi, a, b)
This code is used in chunk 3.
Defines:
  alt_lunar_node, never used.
  FIRST_QUARTER, used in chunk 142.
  FULL, used in chunk 142.
  LAST_QUARTER, never used.
  lunar_latitude, used in chunks 104, 120, and 142.
  lunar_longitude, used in chunks 104, 120, and 196.
  lunar_node, never used.
  lunar_perigee, never used.
  lunar_phase, used in chunks 102, 136, and 142.
  lunar_phase_at_or_after, used in chunk 142.
  {\tt lunar\_phase\_at\_or\_before}, \ {\tt never} \ {\tt used}.
  lunar_true_node, never used.
  NEW, used in chunk 142.
  new_moon_at_or_after, used in chunks 133, 136, and 196.
  new_moon_before, used in chunks 133 and 136.
  {\tt nth\_new\_moon}, \ {\rm never} \ {\rm used}.
  sidereal_lunar_longitude, never used.
Uses angle \frac{100}{100}, deg \frac{100}{100}, final \frac{19}{100}, invert_angular \frac{28}{200}, iround \frac{15}{100}, \frac{12000}{100}, julian_centuries \frac{100}{100},
  latitude 100, longitude 100, lunar_anomaly 115, lunar_elongation 111, mean_lunar_longitude 109,
  MEAN_SYNODIC_MONTH 107, mod 15, moon_node 117, next 16, normalized_degrees 100, nutation 107,
  poly 34, precession 109, SIDEREAL_START 136, sigma 31, sin_degrees 100, solar_anomaly 113,
  solar_longitude 107, and universal_from_dynamical 105.
```

```
120
       \langle astronomical\ lunar\ calendars\ 105 \rangle + \equiv
         # see lines 3734-3762 in calendrica-3.0.cl
         def lunar_altitude(tee, location):
             """Return the geocentric altitude of moon at moment, tee,
             at location, location, as a small positive/negative angle in degrees,
             ignoring parallax and refraction. Adapted from 'Astronomical
             Algorithms' by Jean Meeus, Willmann_Bell, Inc., 1998."""
             phi = latitude(location)
             psi = longitude(location)
             lamb = lunar_longitude(tee)
             beta = lunar_latitude(tee)
             alpha = right_ascension(tee, beta, lamb)
             delta = declination(tee, beta, lamb)
             theta0 = sidereal_from_moment(tee)
             cap_H = mod(theta0 + psi - alpha, 360)
             altitude = arcsin_degrees(
                 (sin_degrees(phi) * sin_degrees(delta)) +
                 (cosine_degrees(phi) * cosine_degrees(delta) * cosine_degrees(cap_H)))
             return mod(altitude + deg(180), 360) - deg(180)
         # see lines 3764-3813 in calendrica-3.0.cl
         def lunar_distance(tee):
             """Return the distance to moon (in meters) at moment, tee.
             Adapted from "Astronomical Algorithms" by Jean Meeus,
             Willmann_Bell, Inc., 2nd ed."""
             c = julian_centuries(tee)
             cap_D = lunar_elongation(c)
             cap_M = solar_anomaly(c)
             cap_M_prime = lunar_anomaly(c)
             cap_F = moon_node(c)
             cap_E = poly(c, [1, mpf(-0.002516), mpf(-0.0000074)])
             args_lunar_elongation = \
                 [0, 2, 2, 0, 0, 0, 2, 2, 2, 2, 0, 1, 0, 2, 0, 0, 4, 0, 4, 2, 2, 1,
                  1, 2, 2, 4, 2, 0, 2, 2, 1, 2, 0, 0, 2, 2, 2, 4, 0, 3, 2, 4, 0, 2,
                  2, 2, 4, 0, 4, 1, 2, 0, 1, 3, 4, 2, 0, 1, 2, 2,]
             args_solar_anomaly = \
                 [0,\ 0,\ 0,\ 0,\ 1,\ 0,\ 0,\ -1,\ 0,\ -1,\ 1,\ 0,\ 1,\ 0,\ 0,\ 0,\ 0,\ 0,\ 0,\ 1,\ 1,
                  0, 1, -1, 0, 0, 0, 1, 0, -1, 0, -2, 1, 2, -2, 0, 0, -1, 0, 0, 1,
                  -1, 2, 2, 1, -1, 0, 0, -1, 0, 1, 0, 1, 0, 0, -1, 2, 1, 0, 0]
             args_lunar_anomaly = \
                 [1, -1, 0, 2, 0, 0, -2, -1, 1, 0, -1, 0, 1, 0, 1, 1, -1, 3, -2,
                  -1, 0, -1, 0, 1, 2, 0, -3, -2, -1, -2, 1, 0, 2, 0, -1, 1, 0,
                  -1, 2, -1, 1, -2, -1, -1, -2, 0, 1, 4, 0, -2, 0, 2, 1, -2, -3,
                  2, 1, -1, 3, -1]
             args_moon_node = \
                 0, 0, 0, 0, 0, 0, 0, 2, 0, 0, 0, 0, 0, 0, -2, 2, 0, 2, 0, 0, 0, 0,
                  0, 0, -2, 0, 0, 0, 0, -2, -2, 0, 0, 0, 0, 0, 0, 0, -2]
             cosine_coefficients = \
                 [-20905355, -3699111, -2955968, -569925, 48888, -3149,
                  246158, -152138, -170733, -204586, -129620, 108743,
                  104755, 10321, 0, 79661, -34782, -23210, -21636, 24208,
                  30824, -8379, -16675, -12831, -10445, -11650, 14403,
                  -7003, 0, 10056, 6322, -9884, 5751, 0, -4950, 4130, 0,
                  -3958, 0, 3258, 2616, -1897, -2117, 2354, 0, 0, -1423,
                  -1117, -1571, -1739, 0, -4421, 0, 0, 0, 0, 1165, 0, 0,
                  87521
             correction = sigma ([cosine_coefficients,
                                  args_lunar_elongation,
                                  args_solar_anomaly,
```

```
args_lunar_anomaly,
                            args_moon_node],
                           lambda v, w, x, y, z: (v *
                                        pow(cap_E, abs(x)) *
                                        cosine_degrees((w * cap_D) +
                                                        (x * cap_M) +
                                                        (y * cap_M_prime) +
                                                        (z * cap_F))))
      return mt(385000560) + correction
  def lunar_position(tee):
      """Return the moon position (geocentric latitude and longitude [in degrees]
      and distance [in meters]) at moment, tee.
      Adapted from "Astronomical Algorithms" by Jean Meeus,
      Willmann_Bell, Inc., 2nd ed."""
      return (lunar_latitude(tee), lunar_longitude(tee), lunar_distance(tee))
  # see lines 3815-3824 in calendrica-3.0.cl
  def lunar_parallax(tee, location):
      """Return the parallax of moon at moment, tee, at location, location.
      Adapted from "Astronomical Algorithms" by Jean Meeus,
      Willmann_Bell, Inc., 1998."""
      geo = lunar_altitude(tee, location)
      Delta = lunar_distance(tee)
      alt = mt(6378140) / Delta
      arg = alt * cosine_degrees(geo)
      return arcsin_degrees(arg)
  # see lines 3826-3832 in calendrica-3.0.cl
  def topocentric_lunar_altitude(tee, location):
      """Return the topocentric altitude of moon at moment, tee,
      at location, location, as a small positive/negative angle in degrees,
      ignoring refraction."""
      return lunar_altitude(tee, location) - lunar_parallax(tee, location)
  # see lines 3834-3839 in calendrica-3.0.cl
  def lunar_diameter(tee):
      """Return the geocentric apparent lunar diameter of the moon (in
      degrees) at moment, tee. Adapted from 'Astronomical
      Algorithms' by Jean Meeus, Willmann_Bell, Inc., 2nd ed."""
      return deg(1792367000/9) / lunar_distance(tee)
This code is used in chunk 3.
Defines:
  lunar_altitude, used in chunks 104 and 142.
  lunar_diameter, never used.
  lunar_distance, never used.
  lunar_parallax, never used.
  lunar_position, never used.
  topocentric_lunar_altitude, used in chunk 102.
Uses angle 100, arcsin_degrees 100, cosine_degrees 100, declination 102, deg 100,
  julian_centuries 100, latitude 100, location 100, longitude 100, lunar_anomaly 115,
  lunar_elongation 111, lunar_latitude 119, lunar_longitude 119, mod 15, moon_node 117,
  mt 100, poly 34, refraction 102, right_ascension 102, sidereal_from_moment 107, sigma 31,
  sin_degrees 100, and solar_anomaly 113.
```

2.14.6 Unit tests

```
121 ⟨timeAndAstronomyUnitTest.py 121⟩≡

# ⟨generated code warning 1⟩

⟨import for testing 6⟩

from appendixCUnitTest import AppendixCTable5TestCaseBase
⟨time and astronomy unit test 104⟩

⟨execute tests 5⟩

Root chunk (not used in this document).

Uses AppendixCTable5TestCaseBase 194.
```

2.15 Persian Calendar

```
\langle persian \ calendar \ 122 \rangle \equiv
122
         # persian calendar algorithms #
         # see lines 3844-3847 in calendrica-3.0.cl
         def persian_date(year, month, day):
             """Return a Persian date data structure."""
             return [year, month, day]
         # see lines 3849-3852 in calendrica-3.0.cl
         PERSIAN_EPOCH = fixed_from_julian(julian_date(ce(622), MARCH, 19))
         # see lines 3854-3858 in calendrica-3.0.cl
         TEHRAN = location(deg(mpf(35.68)),
                           deg(mpf(51.42)),
                           mt(1100),
                           days_from_hours(3 + 1/2))
         # see lines 3860-3865 in calendrica-3.0.cl
         def midday_in_tehran(date):
             """Return Universal time of midday on fixed date, date, in Tehran."""
             return universal_from_standard(midday(date, TEHRAN), TEHRAN)
         # see lines 3867-3876 in calendrica-3.0.cl
         def persian_new_year_on_or_before(date):
             """Return the fixed date of Astronomical Persian New Year on or
             before fixed date, date."""
             approx = estimate_prior_solar_longitude(SPRING, midday_in_tehran(date))
             return next(ifloor(approx) - 1,
                         lambda day: (solar_longitude(midday_in_tehran(day)) <=</pre>
                                      (SPRING + deg(2))))
         # see lines 3880-3898 in calendrica-3.0.cl
         def fixed_from_persian(p_date):
             """Return fixed date of Astronomical Persian date, p_date."""
             month = standard_month(p_date)
             day = standard_day(p_date)
             year = standard_year(p_date)
             temp = (year - 1) if (0 < year) else year
             new_year = persian_new_year_on_or_before(PERSIAN_EPOCH + 180 +
                                                      ifloor(MEAN_TROPICAL_YEAR * temp))
             return ((new_year - 1) +
                     ((31 * (month - 1)) if (month <= 7) else (30 * (month - 1) + 6)) +
                     day)
         # see lines 3898-3918 in calendrica-3.0.cl
         def persian_from_fixed(date):
             """Return Astronomical Persian date (year month day)
             corresponding to fixed date, date."""
             new_year = persian_new_year_on_or_before(date)
             y = iround((new_year - PERSIAN_EPOCH) / MEAN_TROPICAL_YEAR) + 1
             year = y if (0 < y) else (y - 1)
             day_of_year = date - fixed_from_persian(persian_date(year, 1, 1)) + 1
             month = (ceiling(day_of_year / 31)
                      if (day_of_year <= 186)</pre>
                      else ceiling((day_of_year - 6) / 30))
             day = date - (fixed_from_persian(persian_date(year, month, 1)) - 1)
             return persian_date(year, month, day)
```

```
# see lines 3920-3932 in calendrica-3.0.cl
  def is_arithmetic_persian_leap_year(p_year):
      """Return True if p_year is a leap year on the Persian calendar."""
      y = (p_year - 474) if (0 < p_year) else (p_year - 473)
      year = mod(y, 2820) + 474
      return mod((year + 38) * 31, 128) < 31
  # see lines 3934-3958 in calendrica-3.0.cl
  def fixed_from_arithmetic_persian(p_date):
      """Return fixed date equivalent to Persian date p_date."""
      day
           = standard_day(p_date)
      month = standard_month(p_date)
      p_year = standard_year(p_date)
             = (p_year - 474) if (0 < p_year) else (p_year - 473)
           = mod(y, 2820) + 474
      year
           = (31 * (month - 1)) if (month <= 7) else ((30 * (month - 1)) + 6)
      temp
      return ((PERSIAN_EPOCH - 1)
              + (1029983 * quotient(y, 2820))
              + (365 * (year - 1))
              + quotient((31 * year) - 5, 128)
              + temp
              + day)
  # see lines 3960-3986 in calendrica-3.0.cl
  def arithmetic_persian_year_from_fixed(date):
      """Return Persian year corresponding to the fixed date, date."""
           = date - fixed_from_arithmetic_persian(persian_date(475, 1, 1))
      n2820 = quotient(d0, 1029983)
          = mod(d0, 1029983)
      y2820 = 2820 if (d1 == 1029982) else (quotient((128 * d1) + 46878, 46751))
      year = 474 + (2820 * n2820) + y2820
      return year if (0 < year) else (year - 1)
  # see lines 3988-4001 in calendrica-3.0.cl
  def arithmetic_persian_from_fixed(date):
      """Return the Persian date corresponding to fixed date, date."""
                 = arithmetic_persian_year_from_fixed(date)
      day_of_year = 1 + date - fixed_from_arithmetic_persian(
                                    persian_date(year, 1, 1))
                  = (ceiling(day_of_year / 31)
      month
                     if (day_of_year <= 186)
                     else ceiling((day_of_year - 6) / 30))
      day = date - fixed_from_arithmetic_persian(persian_date(year, month, 1)) +1
      return persian_date(year, month, day)
  # see lines 4003-4015 in calendrica-3.0.cl
  def naw_ruz(g_year):
      """Return the Fixed date of Persian New Year (Naw-Ruz) in Gregorian
         year g_year."""
      persian_year = g_year - gregorian_year_from_fixed(PERSIAN_EPOCH) + 1
      y = (persian_year - 1) if (persian_year <= 0) else persian_year</pre>
      return fixed_from_persian(persian_date(y, 1, 1))
This code is used in chunk 3.
Defines:
  arithmetic_persian_from_fixed, used in chunk 182.
  \verb"arithmetic_persian_year_from_fixed", never used.
  fixed_from_arithmetic_persian, used in chunk 182.
  fixed_from_persian, used in chunk 182.
  is_arithmetic_persian_leap_year, never used.
```

```
midday_in_tehran, never used.
            naw_ruz, never used.
            persian_date, never used.
            PERSIAN_EPOCH, never used.
            persian_from_fixed, used in chunk 182.
            persian_new_year_on_or_before, never used.
            TEHRAN, never used.
          Uses ce 59, ceiling 86 86, days_from_hours 100, deg 100, estimate_prior_solar_longitude 109,
            fixed_from_julian 59, gregorian_year_from_fixed 55, ifloor 15, iround 15, julian_date 59,
            location 100, MARCH 53, MEAN_TROPICAL_YEAR 107, midday 100, mod 15, mt 100, next 16,
            quotient 14 14, solar_longitude 107, SPRING 109, standard_day 39, standard_month 39,
            standard_year 39, and universal_from_standard 100.
123
          \langle persian\ calendar\ unit\ test\ {\color{red}123}\rangle \equiv
          This definition is continued in chunk 181.
         This code is used in chunks 4 and 124.
         2.15.1
                      Unit tests
124
          \langle persianCalendarUnitTest.py 124 \rangle \equiv
            # \(\langle generated code warning 1 \rangle \)
            \langle import\ for\ testing\ {\color{red}6} \rangle
            from \ appendix CUnitTest \ import \ \underline{AppendixCTable3TestCaseBase}
            \langle persian\ calendar\ unit\ test\ 123 \rangle
            \langle execute\ tests\ {\color{red}5}\rangle
          Root chunk (not used in this document).
```

Uses AppendixCTable3TestCaseBase 174.

2.16 Bahai Calendar

```
\langle bahai \ calendar \ 125 \rangle \equiv
125
         # bahai calendar algorithms #
         # see lines 4020-4023 in calendrica-3.0.cl
         def bahai_date(major, cycle, year, month, day):
             """Return a Bahai date data structure."""
             return [major, cycle, year, month, day]
         # see lines 4025-4027 in calendrica-3.0.cl
         def bahai_major(date):
             """Return 'major' element of a Bahai date, date."""
             return date[0]
         # see lines 4029-4031 in calendrica-3.0.cl
         def bahai_cycle(date):
             """Return 'cycle' element of a Bahai date, date."""
             return date[1]
         # see lines 4033-4035 in calendrica-3.0.cl
         def bahai_year(date):
             """Return 'year' element of a Bahai date, date."""
             return date[2]
         # see lines 4037-4039 in calendrica-3.0.cl
         def bahai_month(date):
             """Return 'month' element of a Bahai date, date."""
             return date[3]
         # see lines 4041-4043 in calendrica-3.0.cl
         def bahai_day(date):
             """Return 'day' element of a Bahai date, date."""
             return date[4]
         # see lines 4045-4048 in calendrica-3.0.cl
         BAHAI_EPOCH = fixed_from_gregorian(gregorian_date(1844, MARCH, 21))
         # see lines 4050-4053 in calendrica-3.0.cl
         AYYAM_I_HA = 0
         # see lines 4055-4076 in calendrica-3.0.cl
         def fixed_from_bahai(b_date):
             """Return fixed date equivalent to the Bahai date, b_date."""
             major = bahai_major(b_date)
             cycle = bahai_cycle(b_date)
             year = bahai_year(b_date)
             month = bahai_month(b_date)
             day = bahai_day(b_date)
             g_{year} = (361 * (major - 1) +
                       19 * (cycle - 1) +
                       year - 1 +
                       gregorian_year_from_fixed(BAHAI_EPOCH))
             if (month == AYYAM_I_HA):
                 elapsed_months = 342
             elif (month == 19):
                 if (is_gregorian_leap_year(g_year + 1)):
                     elapsed_months = 347
                 else:
                     elapsed_months = 346
```

```
else:
        elapsed_months = 19 * (month - 1)
   return (fixed_from_gregorian(gregorian_date(g_year, MARCH, 20)) +
            elapsed_months +
           day)
# see lines 4078-4111 in calendrica-3.0.cl
def bahai_from_fixed(date):
    """Return Bahai date [major, cycle, year, month, day] corresponding
   to fixed date, date."""
   g_year = gregorian_year_from_fixed(date)
   start = gregorian_year_from_fixed(BAHAI_EPOCH)
   years = (g_year - start -
              (1 if (date <= fixed_from_gregorian())</pre>
                  gregorian_date(g_year, MARCH, 20))) else 0))
   major = 1 + quotient(years, 361)
   cycle = 1 + quotient(mod(years, 361), 19)
         = 1 + mod(years, 19)
   vear
         = date - fixed_from_bahai(bahai_date(major, cycle, year, 1, 1))
   # month
   if (date >= fixed_from_bahai(bahai_date(major, cycle, year, 19, 1))):
       month = 19
   elif (date >= fixed_from_bahai(
        bahai_date(major, cycle, year, AYYAM_I_HA, 1))):
       month = AYYAM_I_HA
   else:
       month = 1 + quotient(days, 19)
   day = date + 1 - fixed_from_bahai(bahai_date(major, cycle, year, month, 1))
   return bahai_date(major, cycle, year, month, day)
# see lines 4113-4117 in calendrica-3.0.cl
def bahai_new_year(g_year):
    """Return fixed date of Bahai New Year in Gregorian year, g_year."""
   return fixed_from_gregorian(gregorian_date(g_year, MARCH, 21))
# see lines 4119-4122 in calendrica-3.0.cl
HAIFA = location(deg(mpf(32.82)), deg(35), mt(0), days_from_hours(2))
# see lines 4124-4130 in calendrica-3.0.cl
def sunset_in_haifa(date):
    """Return universal time of sunset of evening
   before fixed date, date in Haifa."""
   return universal_from_standard(sunset(date, HAIFA), HAIFA)
# see lines 4132-4141 in calendrica-3.0.cl
def future_bahai_new_year_on_or_before(date):
    """Return fixed date of Future Bahai New Year on or
   before fixed date, date."""
   approx = estimate_prior_solar_longitude(SPRING, sunset_in_haifa(date))
   return next(ifloor(approx) - 1,
                lambda day: (solar_longitude(sunset_in_haifa(day)) <=</pre>
                             (SPRING + deg(2)))
# see lines 4143-4173 in calendrica-3.0.cl
def fixed_from_future_bahai(b_date):
```

```
"""Return fixed date of Bahai date, b_date."""
      major = bahai_major(b_date)
      cycle = bahai_cycle(b_date)
      year = bahai_year(b_date)
      month = bahai_month(b_date)
      day = bahai_day(b_date)
      years = (361 * (major - 1)) + (19 * (cycle - 1)) + year
      if (month == 19):
          return (future_bahai_new_year_on_or_before(
              BAHAI_EPOCH +
              ifloor(MEAN_TROPICAL_YEAR * (years + 1/2))) -
                  20 + day
      elif (month == AYYAM_I_HA):
          return (future_bahai_new_year_on_or_before(
              BAHAI_EPOCH +
              ifloor(MEAN_TROPICAL_YEAR * (years - 1/2))) +
                  341 + day)
      else:
          return (future_bahai_new_year_on_or_before(
              BAHAI_EPOCH +
              ifloor(MEAN_TROPICAL_YEAR * (years - 1/2))) +
                  (19 * (month - 1)) + day - 1)
  # see lines 4175-4201 in calendrica-3.0.cl
  def future_bahai_from_fixed(date):
      """Return Future Bahai date corresponding to fixed date, date."""
      new_year = future_bahai_new_year_on_or_before(date)
      years
              = iround((new_year - BAHAI_EPOCH) / MEAN_TROPICAL_YEAR)
      major
              = 1 + quotient(years, 361)
      cycle
              = 1 + quotient(mod(years, 361), 19)
              = 1 + mod(years, 19)
      year
      days
              = date - new_year
      if (date >= fixed_from_future_bahai(bahai_date(major, cycle, year, 19, 1))):
          month = 19
      elif(date >= fixed_from_future_bahai(
          bahai_date(major, cycle, year, AYYAM_I_HA, 1))):
          month = AYYAM_I_HA
      else:
          month = 1 + quotient(days, 19)
      day = date + 1 - fixed_from_future_bahai(
          bahai_date(major, cycle, year, month, 1))
      return bahai_date(major, cycle, year, month, day)
  # see lines 4203-4213 in calendrica-3.0.cl
  def feast_of_ridvan(g_year):
      """Return Fixed date of Feast of Ridvan in Gregorian year year, g_year."""
      years = g_year - gregorian_year_from_fixed(BAHAI_EPOCH)
      major = 1 + quotient(years, 361)
      cycle = 1 + quotient(mod(years, 361), 19)
      year = 1 + mod(years, 19)
      return fixed_from_future_bahai(bahai_date(major, cycle, year, 2, 13))
This code is used in chunk 3.
Defines:
  AYYAM_I_HA, never used.
```

```
bahai_cycle, never used.
  bahai_date, used in chunk 165.
  bahai_day, never used.
  BAHAI_EPOCH, never used.
  bahai_from_fixed, used in chunk 171.
  bahai_major, never used.
  bahai_month, never used.
  bahai_new_year, never used.
  bahai_year, never used.
  feast_of_ridvan, never used.
  {\tt fixed\_from\_bahai, used in \ chunk \ 171}.
  fixed_from_future_bahai, used in chunk 171.
  future_bahai_from_fixed, used in chunk 171.
  future_bahai_new_year_on_or_before, never used.
  HAIFA, never used.
  {\tt sunset\_in\_haifa}, \, {\tt never} \, \, {\tt used}.
Uses days_from_hours 100, deg 100, estimate_prior_solar_longitude 109, fixed_from_gregorian 55,
  gregorian_date 52, gregorian_year_from_fixed 55, ifloor 15, iround 15, is_gregorian_leap_year
  54, location 100, MARCH 53, MEAN_TROPICAL_YEAR 107, mod 15, mt 100, next 16, quotient 14 14,
  solar_longitude 107, SPRING 109, start 47, sunset 102, and universal_from_standard 100.
\langle bahai \ calendar \ unit \ test \ 126 \rangle \equiv
This definition is continued in chunk 170.
This code is used in chunks 4 and 127.
```

2.16.1 Unit tests

126

```
127 \langle bahaiCalendarUnitTest.py\ 127 \rangle \equiv
# \langle generated\ code\ warning\ 1 \rangle
\langle import\ for\ testing\ 6 \rangle
from appendixCUnitTest import AppendixCTable2TestCaseBase \langle bahai\ calendar\ unit\ test\ 126 \rangle
\langle execute\ tests\ 5 \rangle
```

Root chunk (not used in this document). Uses AppendixCTable2TestCaseBase 165.

2.17 French Revolutionary Calendar

```
128
       \langle french \ revolutionary \ calendar \ 128 \rangle \equiv
          # french revolutionary calendar algorithms #
          # see lines 4218-4220 in calendrica-3.0.cl
          def french_date(year, month, day):
              """Return a French Revolutionary date data structure."""
              return [year, month, day]
          # see lines 4222-4226 in calendrica-3.0.cl
          #"""Fixed date of start of the French Revolutionary calendar."""
          FRENCH_EPOCH = fixed_from_gregorian(gregorian_date(1792, SEPTEMBER, 22))
          # see lines 4228-4233 in calendrica-3.0.cl
          PARIS = location(angle(48, 50, 11),
                             angle(2, 20, 15),
                             mt(27),
                             days_from_hours(1))
          # see lines 4235-4241 in calendrica-3.0.cl
          def midnight_in_paris(date):
              """Return Universal Time of true midnight at the end of
                 fixed date, date."""
              # tricky bug: I was using midDAY!!! So French Revolutionary was failing...
              return universal_from_standard(midnight(date + 1, PARIS), PARIS)
       This definition is continued in chunk 130.
       This code is used in chunk 3.
       Defines:
          french_date, used in chunks 130 and 174.
          FRENCH_EPOCH, used in chunk 130.
         midnight_in_paris, used in chunks 129 and 130.
          PARIS, used in chunk 196.
       Uses angle 100, days_from_hours 100, end 47, fixed_from_gregorian 55, gregorian_date 52,
          location 100, midnight 100, mt 100, SEPTEMBER 53, start 47, and universal_from_standard 100.
       I add a test for midnight_in_paris: it took me a lot of time to spot that the Python
       implementation was using midday instaed of midnight!
129
       \langle french \ revolutionary \ calendar \ unit \ test \ 129 \rangle \equiv
          def testMidnightInParis(self):
              d = fixed_from_gregorian(gregorian_date(1992,OCTOBER, 13))
              self.assertEqual(midnight_in_paris(d), d+1)
       This definition is continued in chunks 131 and 183.
       This code is used in chunks 4 and 132.
       Uses fixed_from_gregorian 55, gregorian_date 52, midnight_in_paris 128, and OCTOBER 53.
```

```
# see lines 4243-4252 in calendrica-3.0.cl
def french_new_year_on_or_before(date):
    """Return fixed date of French Revolutionary New Year on or
      before fixed date, date."""
   approx = estimate_prior_solar_longitude(AUTUMN, midnight_in_paris(date))
   return next(ifloor(approx) - 1,
               lambda day: AUTUMN <= solar_longitude(midnight_in_paris(day)))</pre>
# see lines 4254-4267 in calendrica-3.0.cl
def fixed_from_french(f_date):
   """Return fixed date of French Revolutionary date, f_date"""
   month = standard_month(f_date)
   day = standard_day(f_date)
   year = standard_year(f_date)
   new_year = french_new_year_on_or_before(
                  ifloor(FRENCH_EPOCH +
                        180 +
                        MEAN_TROPICAL_YEAR * (year - 1)))
   return new_year - 1 + 30 * (month - 1) + day
# see lines 4269-4278 in calendrica-3.0.cl
def french_from_fixed(date):
    """Return French Revolutionary date of fixed date, date."""
   new_year = french_new_year_on_or_before(date)
   year = iround((new_year - FRENCH_EPOCH) / MEAN_TROPICAL_YEAR) + 1
   month = quotient(date - new_year, 30) + 1
   day = mod(date - new_year, 30) + 1
   return french_date(year, month, day)
# see lines 4280-4286 in calendrica-3.0.cl
def is_arithmetic_french_leap_year(f_year):
    """Return True if year, f_year, is a leap year on the French
       Revolutionary calendar."""
   return ((mod(f_year, 4) == 0)
            (mod(f_year, 400) not in [100, 200, 300]) and
            (mod(f_year, 4000) != 0))
# see lines 4288-4302 in calendrica-3.0.cl
def fixed_from_arithmetic_french(f_date):
   """Return fixed date of French Revolutionary date, f_date."""
   month = standard_month(f_date)
   day = standard_day(f_date)
   year = standard_year(f_date)
   return (FRENCH_EPOCH - 1
           365 * (year - 1)
            quotient(year - 1, 4)
            quotient(year - 1, 100) +
            quotient(year - 1, 400)
            quotient(year - 1, 4000) +
            30 * (month - 1)
           day)
# see lines 4304-4325 in calendrica-3.0.cl
def arithmetic_french_from_fixed(date):
    """Return French Revolutionary date [year, month, day] of fixed
       date, date."""
    approx = quotient(date - FRENCH_EPOCH + 2, 1460969/4000) + 1
```

```
= ((approx - 1)
       year
                   if (date <
                        fixed_from_arithmetic_french(french_date(approx, 1, 1)))
                   else approx)
       month = 1 + quotient(date -
                            fixed_from_arithmetic_french(french_date(year, 1, 1)), 30)
                = date - fixed_from_arithmetic_french(
       day
                                   french_date(year, month, 1)) + 1
       return french_date(year, month, day)
This code is used in chunk 3.
Defines:
  arithmetic_french_from_fixed, used in chunk 184.
  fixed_from_arithmetic_french, used in chunk 184.
  fixed_from_french, used in chunk 184.
  french_from_fixed, used in chunk 184.
  french_new_year_on_or_before, never used.
  is_arithmetic_french_leap_year, never used.
Uses AUTUMN 109, estimate_prior_solar_longitude 109, french_date 128, FRENCH_EPOCH 128,
  ifloor 15, iround 15, MEAN_TROPICAL_YEAR 107, midnight_in_paris 128, mod 15, next 16,
  quotient 14 14, solar_longitude 107, standard_day 39, standard_month 39, and standard_year 39.
\langle french \ revolutionary \ calendar \ unit \ test \ 129 \rangle + \equiv
This code is used in chunks 4 and 132.
2.17.1
           Unit tests
\langle frenchRevolutionaryCalendarUnitTest.py 132 \rangle \equiv
  # \(\langle generated code warning \mathbf{1}\rangle\)
  (import for testing 6)
  {\tt from\ appendixCUnitTest\ import\ {\tt AppendixCTable3TestCaseBase}}
  \langle french \ revolutionary \ calendar \ unit \ test \ 129 \rangle
  \langle execute \ tests \ 5 \rangle
Root chunk (not used in this document).
Uses AppendixCTable3TestCaseBase 174.
```

131

132

2.18 Chinese Calendar

```
\langle chinese\ calendar\ 133 \rangle \equiv
133
         # chinese calendar algorithms #
         # see lines 4330-4333 in calendrica-3.0.cl
         def chinese_date(cycle, year, month, leap, day):
             """Return a Chinese date data structure."""
             return [cycle, year, month, leap, day]
         # see lines 4335-4337 in calendrica-3.0.cl
         def chinese_cycle(date):
             """Return 'cycle' element of a Chinese date, date."""
             return date[0]
         # see lines 4339-4341 in calendrica-3.0.cl
         def chinese_year(date):
             """Return 'year' element of a Chinese date, date."""
             return date[1]
         # see lines 4343-4345 in calendrica-3.0.cl
         def chinese month(date):
             """Return 'month' element of a Chinese date, date."""
             return date[2]
         # see lines 4347-4349 in calendrica-3.0.cl
         def chinese_leap(date):
             """Return 'leap' element of a Chinese date, date."""
             return date[3]
         # see lines 4351-4353 in calendrica-3.0.cl
         def chinese_day(date):
             """Return 'day' element of a Chinese date, date."""
             return date[4]
         # see lines 4355-4363 in calendrica-3.0.cl
         def chinese_location(tee):
             """Return location of Beijing; time zone varies with time, tee."""
             year = gregorian_year_from_fixed(ifloor(tee))
             if (year < 1929):
                 return location(angle(39, 55, 0), angle(116, 25, 0),
                                mt(43.5), days_from_hours(1397/180))
             else:
                 return location(angle(39, 55, 0), angle(116, 25, 0),
                                 mt(43.5), days_from_hours(8))
         # see lines 4365-4377 in calendrica-3.0.cl
         def chinese_solar_longitude_on_or_after(lam, date):
             """Return moment (Beijing time) of the first date on or after
             fixed date, date, (Beijing time) when the solar longitude
             will be 'lam' degrees."""
             tee = solar_longitude_after(lam,
                                         universal_from_standard(date,
                                                                 chinese_location(date)))
             return standard_from_universal(tee, chinese_location(tee))
         # see lines 4379-4387 in calendrica-3.0.cl
         def current_major_solar_term(date):
             """Return last Chinese major solar term (zhongqi) before
```

```
fixed date, date."""
    s = solar_longitude(universal_from_standard(date,
                                                chinese_location(date)))
   return amod(2 + quotient(int(s), deg(30)), 12)
# see lines 4389-4397 in calendrica-3.0.cl
def major_solar_term_on_or_after(date):
    """Return moment (in Beijing) of the first Chinese major
   solar term (zhongqi) on or after fixed date, date. The
   major terms begin when the sun's longitude is a
   multiple of 30 degrees."""
   s = solar_longitude(midnight_in_china(date))
   1 = mod(30 * ceiling(s / 30), 360)
   return chinese_solar_longitude_on_or_after(1, date)
# see lines 4399-4407 in calendrica-3.0.cl
def current_minor_solar_term(date):
    """Return last Chinese minor solar term (jieqi) before date, date."""
   s = solar_longitude(universal_from_standard(date,
                                                chinese_location(date)))
   return amod(3 + quotient(s - deg(15), deg(30)), 12)
# see lines 4409-4422 in calendrica-3.0.cl
def minor_solar_term_on_or_after(date):
    """Return moment (in Beijing) of the first Chinese minor solar
   term (jieqi) on or after fixed date, date. The minor terms
   begin when the sun's longitude is an odd multiple of 15 degrees."""
   s = solar_longitude(midnight_in_china(date))
   1 = mod(30 * ceiling((s - deg(15)) / 30) + deg(15), 360)
   return chinese_solar_longitude_on_or_after(1, date)
# see lines 4424-4433 in calendrica-3.0.cl
def chinese_new_moon_before(date):
    """Return fixed date (Beijing) of first new moon before fixed date, date."""
   tee = new_moon_before(midnight_in_china(date))
   return ifloor(standard_from_universal(tee, chinese_location(tee)))
# see lines 4435-4444 in calendrica-3.0.cl
def chinese_new_moon_on_or_after(date):
    """Return fixed date (Beijing) of first new moon on or after
   fixed date, date."""
   tee = new_moon_at_or_after(midnight_in_china(date))
   return ifloor(standard_from_universal(tee, chinese_location(tee)))
# see lines 4446-4449 in calendrica-3.0.cl
CHINESE_EPOCH = fixed_from_gregorian(gregorian_date(-2636, FEBRUARY, 15))
# see lines 4451-4457 in calendrica-3.0.cl
def is_chinese_no_major_solar_term(date):
    """Return True if Chinese lunar month starting on date, date,
   has no major solar term."""
   return (current_major_solar_term(date) ==
           current_major_solar_term(chinese_new_moon_on_or_after(date + 1)))
# see lines 4459-4463 in calendrica-3.0.cl
def midnight_in_china(date):
    """Return Universal time of (clock) midnight at start of fixed
   date, date, in China."""
   return universal_from_standard(date, chinese_location(date))
# see lines 4465-4474 in calendrica-3.0.cl
```

```
def chinese_winter_solstice_on_or_before(date):
    """Return fixed date, in the Chinese zone, of winter solstice
   on or before fixed date, date."""
   approx = estimate_prior_solar_longitude(WINTER,
                                            midnight_in_china(date + 1))
   return next(ifloor(approx) - 1,
               lambda day: WINTER < solar_longitude(</pre>
                   midnight_in_china(1 + day)))
# see lines 4476-4500 in calendrica-3.0.cl
def chinese_new_year_in_sui(date):
    """Return fixed date of Chinese New Year in sui (period from
   solstice to solstice) containing date, date."""
   s1 = chinese_winter_solstice_on_or_before(date)
   s2 = chinese_winter_solstice_on_or_before(s1 + 370)
   next_m11 = chinese_new_moon_before(1 + s2)
   m12 = chinese_new_moon_or_after(1 + s1)
   m13 = chinese_new_moon_or_after(1 + m12)
   leap_year = iround((next_m11 - m12) / MEAN_SYNODIC_MONTH) == 12
   if (leap_year and
        (is_chinese_no_major_solar_term(m12) or is_chinese_no_major_solar_term(m13))):
        return chinese_new_moon_on_or_after(1 + m13)
    else:
        return m13
# see lines 4502-4511 in calendrica-3.0.cl
def chinese_new_year_on_or_before(date):
    """Return fixed date of Chinese New Year on or before fixed date, date."""
   new_year = chinese_new_year_in_sui(date)
   if (date >= new_year):
        return new_year
    else:
       return chinese_new_year_in_sui(date - 180)
# see lines 4513-4518 in calendrica-3.0.cl
def chinese_new_year(g_year):
    """Return fixed date of Chinese New Year in Gregorian year, g_year."""
   return chinese_new_year_on_or_before(
        fixed_from_gregorian(gregorian_date(g_year, JULY, 1)))
# see lines 4520-4565 in calendrica-3.0.cl
def chinese_from_fixed(date):
   """Return Chinese date (cycle year month leap day) of fixed date, date."""
   s1 = chinese_winter_solstice_on_or_before(date)
   s2 = chinese_winter_solstice_on_or_before(s1 + 370)
   next_m11 = chinese_new_moon_before(1 + s2)
   m12 = chinese_new_moon_or_after(1 + s1)
   leap_year = iround((next_m11 - m12) / MEAN_SYNODIC_MONTH) == 12
   m = chinese_new_moon_before(1 + date)
   month = amod(iround((m - m12) / MEAN_SYNODIC_MONTH) -
                  (1 if (leap_year and
                         is_chinese_prior_leap_month(m12, m)) else 0),
                  12)
   leap_month = (leap_year and
                  is_chinese_no_major_solar_term(m) and
                  (not is_chinese_prior_leap_month(m12,
                                                chinese_new_moon_before(m))))
    elapsed_years = (ifloor(mpf(1.5) -
```

```
(month / 12) +
                           ((date - CHINESE_EPOCH) / MEAN_TROPICAL_YEAR)))
   cycle = 1 + quotient(elapsed_years - 1, 60)
   year = amod(elapsed_years, 60)
   day = 1 + (date - m)
   return chinese_date(cycle, year, month, leap_month, day)
# see lines 4567-4596 in calendrica-3.0.cl
def fixed_from_chinese(c_date):
   """Return fixed date of Chinese date, c_date."""
   cycle = chinese_cycle(c_date)
   year = chinese_year(c_date)
   month = chinese_month(c_date)
   leap = chinese_leap(c_date)
   day = chinese_day(c_date)
   mid_year = ifloor(CHINESE_EPOCH +
                      ((((cycle - 1) * 60) + (year - 1) + 1/2) *
                      MEAN_TROPICAL_YEAR))
   new_year = chinese_new_year_on_or_before(mid_year)
   p = chinese_new_moon_or_after(new_year + ((month - 1) * 29))
   d = chinese_from_fixed(p)
   prior_new_moon = (p if ((month == chinese_month(d)) and
                            (leap == chinese_leap(d)))
                        else chinese_new_moon_or_after(1 + p))
   return prior_new_moon + day - 1
# see lines 4598-4607 in calendrica-3.0.cl
def is_chinese_prior_leap_month(m_prime, m):
    """Return True if there is a Chinese leap month on or after lunar
   month starting on fixed day, m_prime and at or before
   lunar month starting at fixed date, m."""
   return ((m >= m_prime) and
            (is_chinese_no_major_solar_term(m) or
             is_chinese_prior_leap_month(m_prime, chinese_new_moon_before(m))))
# see lines 4609-4615 in calendrica-3.0.cl
def chinese_name(stem, branch):
    """Return BOGUS if stem/branch combination is impossible."""
   if (mod(stem, 2) == mod(branch, 2)):
       return [stem, branch]
   else:
       return BOGUS
# see lines 4617-4619 in calendrica-3.0.cl
def chinese_stem(name):
   return name[0]
# see lines 4621-4623 in calendrica-3.0.cl
def chinese_branch(name):
   return name[1]
# see lines 4625-4629 in calendrica-3.0.cl
def chinese_sexagesimal_name(n):
    """Return the n_th name of the Chinese sexagesimal cycle."""
   return chinese_name(amod(n, 10), amod(n, 12))
```

```
# see lines 4631-4644 in calendrica-3.0.cl
def chinese_name_difference(c_name1, c_name2):
    """Return the number of names from Chinese name c_name1 to the
   next occurrence of Chinese name c_name2."""
   stem1 = chinese_stem(c_name1)
   stem2 = chinese_stem(c_name2)
   branch1 = chinese_branch(c_name1)
   branch2 = chinese_branch(c_name2)
   stem_difference = stem2 - stem1
   branch_difference = branch2 - branch1
   return 1 + mod(stem_difference - 1 +
                   25 * (branch_difference - stem_difference), 60)
# see lines 4646-4649 in calendrica-3.0.cl
# see lines 214-215 in calendrica-3.0.errata.cl
def chinese_year_name(year):
    """Return sexagesimal name for Chinese year, year, of any cycle."""
   return chinese_sexagesimal_name(year)
# see lines 4651-4655 in calendrica-3.0.cl
CHINESE_MONTH_NAME_EPOCH = 57
# see lines 4657-4664 in calendrica-3.0.cl
# see lines 211-212 in calendrica-3.0.errata.cl
def chinese_month_name(month, year):
    """Return sexagesimal name for month, month, of Chinese year, year."""
   elapsed_months = (12 * (year - 1)) + (month - 1)
   return chinese_sexagesimal_name(elapsed_months - CHINESE_MONTH_NAME_EPOCH)
# see lines 4666-4669 in calendrica-3.0.cl
CHINESE_DAY_NAME_EPOCH = rd(45)
# see lines 4671-4675 in calendrica-3.0.cl
# see lines 208-209 in calendrica-3.0.errata.cl
def chinese_day_name(date):
    """Return Chinese sexagesimal name for date, date."""
   return chinese_sexagesimal_name(date - CHINESE_DAY_NAME_EPOCH)
# see lines 4677-4687 in calendrica-3.0.cl
def chinese_day_name_on_or_before(name, date):
    """Return fixed date of latest date on or before fixed date, date, that
   has Chinese name, name."""
   return (date -
           mod(date +
                chinese_name_difference(name,
                            chinese_sexagesimal_name(CHINESE_DAY_NAME_EPOCH)),
                60))
# see lines 4689-4699 in calendrica-3.0.cl
def dragon_festival(g_year):
    """Return fixed date of the Dragon Festival occurring in Gregorian
   year g_year."""
   elapsed_years = 1 + g_year - gregorian_year_from_fixed(CHINESE_EPOCH)
   cycle = 1 + quotient(elapsed_years - 1, 60)
   year = amod(elapsed_years, 60)
```

```
return fixed_from_chinese(chinese_date(cycle, year, 5, False, 5))
# see lines 4701-4708 in calendrica-3.0.cl
def qing_ming(g_year):
    """Return fixed date of Qingming occurring in Gregorian year, g_year."""
   return ifloor(minor_solar_term_on_or_after(
        fixed_from_gregorian(gregorian_date(g_year, MARCH, 30))))
# see lines 4710-4722 in calendrica-3.0.cl
def chinese_age(birthdate, date):
    """Return the age at fixed date, date, given Chinese birthdate, birthdate,
   according to the Chinese custom.
   Returns BOGUS if date is before birthdate."""
   today = chinese_from_fixed(date)
   if (date >= fixed_from_chinese(birthdate)):
       return (60 * (chinese_cycle(today) - chinese_cycle(birthdate)) +
                (chinese_year(today) - chinese_year(birthdate)) + 1)
   else:
        return BOGUS
# see lines 4724-4758 in calendrica-3.0.cl
def chinese_year_marriage_augury(cycle, year):
    """Return the marriage augury type of Chinese year, year in cycle, cycle.
   O means lichun does not occur (widow or double-blind years),
   1 means it occurs once at the end (blind),
   2 means it occurs once at the start (bright), and
   3 means it occurs twice (double-bright or double-happiness)."""
   new_year = fixed_from_chinese(chinese_date(cycle, year, 1, False, 1))
   c = (cycle + 1) if (year == 60) else cycle
   y = 1 if (year == 60) else (year + 1)
   next_new_year = fixed_from_chinese(chinese_date(c, y, 1, False, 1))
   first_minor_term = current_minor_solar_term(new_year)
   next_first_minor_term = current_minor_solar_term(next_new_year)
   if ((first_minor_term == 1) and (next_first_minor_term == 12)):
       res = 0
   elif ((first_minor_term == 1) and (next_first_minor_term != 12)):
   elif ((first_minor_term != 1) and (next_first_minor_term == 12)):
       res = 2
    else:
       res = 3
   return res
# see lines 4760-4769 in calendrica-3.0.cl
def japanese_location(tee):
    """Return the location for Japanese calendar; varies with moment, tee."""
   year = gregorian_year_from_fixed(ifloor(tee))
    if (year < 1888):
        # Tokyo (139 deg 46 min east) local time
        loc = location(deg(mpf(35.7)), angle(139, 46, 0),
                           mt(24), days_from_hours(9 + 143/450))
    else:
        # Longitude 135 time zone
        loc = location(deg(35), deg(135), mt(0), days_from_hours(9))
   return loc
```

```
# see lines 4771-4795 in calendrica-3.0.cl
  def korean_location(tee):
       """Return the location for Korean calendar; varies with moment, tee."""
      # Seoul city hall at a varying time zone.
      if (tee < fixed_from_gregorian(gregorian_date(1908, APRIL, 1))):</pre>
           #local mean time for longitude 126 deg 58 min
           z = 3809/450
      elif (tee < fixed_from_gregorian(gregorian_date(1912, JANUARY, 1))):</pre>
      elif (tee < fixed_from_gregorian(gregorian_date(1954, MARCH, 21))):</pre>
       elif (tee < fixed_from_gregorian(gregorian_date(1961, AUGUST, 10))):</pre>
           z = 8.5
       else:
           z = 9
      return location(angle(37, 34, 0), angle(126, 58, 0),
                         mt(0), days_from_hours(z))
  # see lines 4797-4800 in calendrica-3.0.cl
  def korean_year(cycle, year):
       """Return equivalent Korean year to Chinese cycle, cycle, and year, year."""
      return (60 * cycle) + year - 364
  # see lines 4802-4811 in calendrica-3.0.cl
  def vietnamese_location(tee):
       """Return the location for Vietnamese calendar is Hanoi;
      varies with moment, tee. Time zone has changed over the years."""
      if (tee < gregorian_new_year(1968)):</pre>
           z = 8
       else:
           z = 7
           return location(angle(21, 2, 0), angle(105, 51, 0),
                              mt(12), days_from_hours(z))
This code is used in chunk 3.
Defines:
  chinese_age, never used.
  chinese_branch, never used.
  chinese_cycle, never used.
  chinese\_date, used in chunk 185.
  chinese_day, never used.
  chinese_day_name, used in chunk 187.
  CHINESE_DAY_NAME_EPOCH, never used.
  chinese_day_name_on_or_before, never used.
  CHINESE EPOCH, never used.
  chinese_from_fixed, used in chunk 187.
  chinese_leap, never used.
  chinese_location, never used.
  chinese_month, never used.
  chinese_month_name, never used.
  {\tt CHINESE\_MONTH\_NAME\_EPOCH,\ never\ used}.
  chinese_name, never used.
  {\tt chinese\_name\_difference}, \ {\rm never} \ {\rm used}.
  chinese_new_moon_before, never used.
  chinese new moon on or after, never used.
  chinese_new_year, never used.
  chinese_new_year_in_sui, never used.
  {\tt chinese\_new\_year\_on\_or\_before}, \ {\tt never} \ {\tt used}.
  {\tt chinese\_sexagesimal\_name}, \ {\tt never} \ {\tt used}.
  {\tt chinese\_solar\_longitude\_on\_or\_after}, \ {\tt never} \ {\tt used}.
  chinese stem, never used.
  {\tt chinese\_winter\_solstice\_on\_or\_before, \, never \, used.}
```

```
chinese_year, never used.
  {\tt chinese\_year\_marriage\_augury}, \ {\tt never} \ {\tt used}.
  chinese_year_name, never used.
  current_major_solar_term, never used.
  {\tt current\_minor\_solar\_term}, \ {\rm never} \ {\rm used}.
  dragon_festival, never used.
  fixed_from_chinese, used in chunk 187.
  \verb"is_chinese_no_major_solar_term", never used.
  is_chinese_prior_leap_month, never used.
  japanese_location, never used.
  korean_location, never used.
  korean_year, never used.
  major_solar_term_on_or_after, used in chunk 187.
  midnight_in_china, never used.
  minor_solar_term_on_or_after, never used.
  qing_ming, never used.
  vietnamese_location, never used.
Uses amod 15, angle 100, APRIL 53, AUGUST 53, BOGUS 13, ceiling 86 86, days_from_hours 100,
  deg 100, end 47, estimate_prior_solar_longitude 109, FEBRUARY 53, fixed_from_gregorian 55,
  gregorian_date 52, gregorian_new_year 56, gregorian_year_from_fixed 55, ifloor 15,
  iround 15, JANUARY 53, JULY 53, location 100, longitude 100, MARCH 53, MEAN_SYNODIC_MONTH 107,
  MEAN_TROPICAL_YEAR 107, midnight 100, mod 15, mt 100, new_moon_at_or_after 119, new_moon_before
  119, next 16, odd 89, quotient 14 14, rd 37, solar_longitude 107, solar_longitude_after 109,
  \mathtt{standard\_from\_universal\ 100},\ \mathtt{start\ 47},\ \mathtt{universal\_from\_standard\ 100},\ \mathtt{WINTER\ 109},\ \mathtt{and\ zone\ 100}.
\langle chinese\ calendar\ unit\ test\ 134 \rangle \equiv
  # Tests other than the ones from Appendix C #
```

This definition is continued in chunk 186. This code is used in chunks 4 and 135.

2.18.1 Unit tests

134

135 $\langle chineseCalendarUnitTest.py\ 135 \rangle \equiv$ # $\langle generated\ code\ warning\ 1 \rangle$ $\langle import\ for\ testing\ 6 \rangle$ from appendixCUnitTest import AppendixCTable4TestCaseBase $\langle chinese\ calendar\ unit\ test\ 134 \rangle$ $\langle execute\ tests\ 5 \rangle$

Root chunk (not used in this document). Uses AppendixCTable4TestCaseBase 185.

2.19 Modern Hindu Calendars

```
\langle modern\ hindu\ calendars\ 136 \rangle \equiv
136
         # modern hindu calendars algorithms #
         # see lines 4816-4820 in calendrica-3.0.cl
         def hindu_lunar_date(year, month, leap_month, day, leap_day):
             """Return a lunar Hindu date data structure."""
             return [year, month, leap_month, day, leap_day]
         # see lines 4822-4824 in calendrica-3.0.cl
         def hindu lunar month(date):
             """Return 'month' element of a lunar Hindu date, date."""
             return date[1]
         # see lines 4826-4828 in calendrica-3.0.cl
         def hindu_lunar_leap_month(date):
             """Return 'leap_month' element of a lunar Hindu date, date."""
             return date[2]
         # see lines 4830-4832 in calendrica-3.0.cl
         def hindu_lunar_day(date):
             """Return 'day' element of a lunar Hindu date, date."""
             return date[3]
         # see lines 4834-4836 in calendrica-3.0.cl
         def hindu_lunar_leap_day(date):
             """Return 'leap_day' element of a lunar Hindu date, date."""
             return date[4]
         # see lines 4838-4840 in calendrica-3.0.cl
         def hindu_lunar_year(date):
             """Return 'year' element of a lunar Hindu date, date."""
             return date[0]
         # see lines 4842-4850 in calendrica-3.0.cl
         def hindu_sine_table(entry):
             """Return the value for entry in the Hindu sine table.
             Entry, entry, is an \[ \text{angle given as a multiplier of } 225'.""" \]
             exact = 3438 * sin_degrees(entry * angle(0, 225, 0))
             error = 0.215 * signum(exact) * signum(abs(exact) - 1716)
             return iround(exact + error) / 3438
         # see lines 4852-4861 in calendrica-3.0.cl
         def hindu_sine(theta):
             """Return the linear interpolation for angle, theta, in Hindu table."""
                    = theta / angle(0, 225, 0)
             fraction = mod(entry, 1)
             return ((fraction * hindu_sine_table(ceiling(entry))) +
                     ((1 - fraction) * hindu_sine_table(ifloor(entry))))
         # see lines 4863-4873 in calendrica-3.0.cl
         def hindu_arcsin(amp):
             """Return the inverse of Hindu sine function of amp."""
             if (amp < 0):
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return -hindu_arcsin(-amp)
    else:
       pos = next(0, lambda k: amp <= hindu_sine_table(k))</pre>
        below = hindu_sine_table(pos - 1)
       return (angle(0, 225, 0) *
                (pos - 1 + ((amp - below) / (hindu_sine_table(pos) - below))))
# see lines 4875-4878 in calendrica-3.0.cl
HINDU_SIDEREAL_YEAR = 365 + 279457/1080000
# see lines 4880-4883 in calendrica-3.0.cl
HINDU_CREATION = HINDU_EPOCH - 1955880000 * HINDU_SIDEREAL_YEAR
# see lines 4885-4889 in calendrica-3.0.cl
def hindu_mean_position(tee, period):
   """Return the position in degrees at moment, tee, in uniform circular
   orbit of period days."""
   return deg(360) * mod((tee - HINDU_CREATION) / period, 1)
# see lines 4891-4894 in calendrica-3.0.cl
HINDU_SIDEREAL_MONTH = 27 + 4644439/14438334
# see lines 4896-4899 in calendrica-3.0.cl
HINDU_SYNODIC_MONTH = 29 + 7087771/13358334
# see lines 4901-4904 in calendrica-3.0.cl
HINDU_ANOMALISTIC_YEAR = 1577917828000/(4320000000 - 387)
# see lines 4906-4909 in calendrica-3.0.cl
HINDU_ANOMALISTIC_MONTH = mpf(1577917828)/(57753336 - 488199)
# see lines 4911-4926 in calendrica-3.0.cl
def hindu_true_position(tee, period, size, anomalistic, change):
    """Return the longitudinal position at moment, tee.
   period is the period of mean motion in days.
   size is ratio of radii of epicycle and deferent.
   anomalistic is the period of retrograde revolution about epicycle.
   change is maximum decrease in epicycle size."""
               = hindu_mean_position(tee, period)
   lam
              = hindu_sine(hindu_mean_position(tee, anomalistic))
   contraction = abs(offset) * change * size
              = hindu_arcsin(offset * (size - contraction))
   return mod(lam - equation, 360)
# see lines 4928-4932 in calendrica-3.0.cl
def hindu_solar_longitude(tee):
   """Return the solar longitude at moment, tee."""
   return hindu_true_position(tee,
                               HINDU_SIDEREAL_YEAR,
                               14/360,
                               HINDU_ANOMALISTIC_YEAR,
                               1/42)
# see lines 4934-4938 in calendrica-3.0.cl
def hindu_zodiac(tee):
   """Return the zodiacal sign of the sun, as integer in range 1..12,
   at moment tee."""
   return quotient(float(hindu_solar_longitude(tee)), deg(30)) + 1
```

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# see lines 4940-4944 in calendrica-3.0.cl
def hindu_lunar_longitude(tee):
    """Return the lunar longitude at moment, tee."""
   return hindu_true_position(tee,
                               HINDU_SIDEREAL_MONTH,
                               32/360,
                               HINDU_ANOMALISTIC_MONTH,
# see lines 4946-4952 in calendrica-3.0.cl
def hindu_lunar_phase(tee):
   """Return the longitudinal distance between the sun and moon
   at moment, tee.""
   return mod(hindu_lunar_longitude(tee) - hindu_solar_longitude(tee), 360)
# see lines 4954-4958 in calendrica-3.0.cl
def hindu_lunar_day_from_moment(tee):
    """Return the phase of moon (tithi) at moment, tee, as an integer in
   the range 1..30."""
   return quotient(hindu_lunar_phase(tee), deg(12)) + 1
# see lines 4960-4973 in calendrica-3.0.cl
def hindu_new_moon_before(tee):
    """Return the approximate moment of last new moon preceding moment, tee,
   close enough to determine zodiacal sign."""
   varepsilon = pow(2, -1000)
   tau = tee - ((1/deg(360))
                 hindu_lunar_phase(tee) *
                 HINDU_SYNODIC_MONTH)
   return binary_search(tau - 1, min(tee, tau + 1),
                         lambda 1, u: ((hindu_zodiac(1) == hindu_zodiac(u)) or
                                       ((u - 1) < varepsilon)),
                         lambda x: hindu_lunar_phase(x) < deg(180))</pre>
# see lines 4975-4988 in calendrica-3.0.cl
def hindu_lunar_day_at_or_after(k, tee):
   """Return the time lunar_day (tithi) number, k, begins at or after
   moment, tee. k can be fractional (for karanas)."""
   phase = (k - 1) * deg(12)
   tau = tee + ((1/\deg(360)) *
                   mod(phase - hindu_lunar_phase(tee), 360) *
                   HINDU_SYNODIC_MONTH)
   a = max(tee, tau - 2)
   b = tau + 2
   return invert_angular(hindu_lunar_phase, phase, a, b)
# see lines 4990-4996 in calendrica-3.0.cl
def hindu_calendar_year(tee):
   """Return the solar year at given moment, tee."""
   return iround(((tee - HINDU_EPOCH) / HINDU_SIDEREAL_YEAR) -
                 (hindu_solar_longitude(tee) / deg(360)))
# see lines 4998-5001 in calendrica-3.0.cl
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HINDU_SOLAR_ERA = 3179
# see lines 5003-5020 in calendrica-3.0.cl
def hindu_solar_from_fixed(date):
    """Return the Hindu (Orissa) solar date equivalent to fixed date, date."""
   critical = hindu_sunrise(date + 1)
           = hindu_zodiac(critical)
   month
   year
            = hindu_calendar_year(critical) - HINDU_SOLAR_ERA
   approx = date - 3 - mod(ifloor(hindu_solar_longitude(critical)), deg(30))
   begin
            = next(approx,
                    lambda i: (hindu_zodiac(hindu_sunrise(i + 1)) == month))
   day
            = date - begin + 1
   return hindu_solar_date(year, month, day)
# see lines 5022-5039 in calendrica-3.0.cl
def fixed_from_hindu_solar(s_date):
    """Return the fixed date corresponding to Hindu solar date, s_date,
    (Saka era; Orissa rule.)"""
   month = standard_month(s_date)
   day = standard_day(s_date)
   year = standard_year(s_date)
   begin = ifloor((year + HINDU_SOLAR_ERA + ((month - 1)/12)) *
                 HINDU_SIDEREAL_YEAR + HINDU_EPOCH)
   return (day - 1 +
           next(begin - 3,
                lambda d: (hindu_zodiac(hindu_sunrise(d + 1)) == month)))
# see lines 5041-5044 in calendrica-3.0.cl
HINDU_LUNAR_ERA = 3044
# see lines 5046-5074 in calendrica-3.0.cl
def hindu_lunar_from_fixed(date):
    """Return the Hindu lunar date, new_moon scheme,
   equivalent to fixed date, date."""
   critical = hindu_sunrise(date)
            = hindu_lunar_day_from_moment(critical)
   leap_day = (day == hindu_lunar_day_from_moment(hindu_sunrise(date - 1)))
   last_new_moon = hindu_new_moon_before(critical)
   next_new_moon = hindu_new_moon_before(ifloor(last_new_moon) + 35)
   solar_month = hindu_zodiac(last_new_moon)
                 = (solar_month == hindu_zodiac(next_new_moon))
            = amod(solar_month + 1, 12)
            = (hindu_calendar_year((date + 180) if (month <= 2) else date) -
               HINDU_LUNAR_ERA)
   return hindu_lunar_date(year, month, leap_month, day, leap_day)
# see lines 5076-5123 in calendrica-3.0.cl
def fixed_from_hindu_lunar(l_date):
    """Return the Fixed date corresponding to Hindu lunar date, l_date."""
              = hindu_lunar_year(1_date)
              = hindu_lunar_month(1_date)
   leap_month = hindu_lunar_leap_month(l_date)
             = hindu_lunar_day(1_date)
   leap_day = hindu_lunar_leap_day(l_date)
   approx = HINDU_EPOCH + (HINDU_SIDEREAL_YEAR *
                           (year + HINDU_LUNAR_ERA + ((month - 1) / 12)))
   s = ifloor(approx - ((1/deg(360)) *
                       HINDU_SIDEREAL_YEAR *
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mod(hindu_solar_longitude(approx) -
                            ((month - 1) * deg(30)) +
                            deg(180), 360) -
                        deg(180)))
   k = hindu_lunar_day_from_moment(s + days_from_hours(6))
   if (3 < k < 27):
        temp = k
   else:
        mid = hindu_lunar_from_fixed(s - 15)
        if ((hindu_lunar_month(mid) != month) or
            (hindu_lunar_leap_month(mid) and not leap_month)):
            temp = mod(k + 15, 30) - 15
        else:
            temp = mod(k - 15, 30) + 15
    est = s + day - temp
   tau = (est -
          mod(hindu_lunar_day_from_moment(est + days_from_hours(6)) - day + 15, 30) +
   date = next(tau - 1,
                lambda d: (hindu_lunar_day_from_moment(hindu_sunrise(d)) in
                           [day, amod(day + 1, 30)]))
   return (date + 1) if leap_day else date
# see lines 5125-5139 in calendrica-3.0.cl
def hindu_equation_of_time(date):
    """Return the time from true to mean midnight of date, date."""
   offset = hindu_sine(hindu_mean_position(date, HINDU_ANOMALISTIC_YEAR))
   equation_sun = (offset *
                    angle(57, 18, 0) *
                    (14/360 - (abs(offset) / 1080)))
   return ((hindu_daily_motion(date) / deg(360)) *
            (equation_sun / deg(360)) *
           HINDU_SIDEREAL_YEAR)
# see lines 5141-5155 in calendrica-3.0.cl
def hindu_ascensional_difference(date, location):
    """Return the difference between right and oblique ascension
   of sun on date, date, at location, location."""
   sin_delta = (1397/3438) * hindu_sine(hindu_tropical_longitude(date))
   phi = latitude(location)
   diurnal_radius = hindu_sine(deg(90) + hindu_arcsin(sin_delta))
   tan_phi = hindu_sine(phi) / hindu_sine(deg(90) + phi)
   earth_sine = sin_delta * tan_phi
   return hindu_arcsin(-earth_sine / diurnal_radius)
# see lines 5157-5172 in calendrica-3.0.cl
def hindu_tropical_longitude(date):
    """Return the Hindu tropical longitude on fixed date, date.
   Assumes precession with maximum of 27 degrees
   and period of 7200 sidereal years (= 1577917828/600 days)."""
   days = ifloor(date - HINDU_EPOCH)
   precession = (deg(27) -
                  (abs(deg(54) -
                       mod(deg(27) +
                           (deg(108) * 600/1577917828 * days),
                           108))))
   return mod(hindu_solar_longitude(date) - precession, 360)
```

```
# see lines 5174-5183 in calendrica-3.0.cl
def hindu_rising_sign(date):
   """Return the tabulated speed of rising of current zodiacal sign on
   date, date."""
   i = quotient(float(hindu_tropical_longitude(date)), deg(30))
   return [1670/1800, 1795/1800, 1935/1800, 1935/1800,
            1795/1800, 1670/1800][mod(i, 6)]
# see lines 5185-5200 in calendrica-3.0.cl
def hindu_daily_motion(date):
   """Return the sidereal daily motion of sun on date, date."""
   mean_motion = deg(360) / HINDU_SIDEREAL_YEAR
              = hindu_mean_position(date, HINDU_ANOMALISTIC_YEAR)
   anomaly
             = 14/360 - abs(hindu_sine(anomaly)) / 1080
   epicycle
               = quotient(float(anomaly), angle(0, 225, 0))
   entry
   sine_table_step = hindu_sine_table(entry + 1) - hindu_sine_table(entry)
   factor = -3438/225 * sine_table_step * epicycle
   return mean_motion * (factor + 1)
# see lines 5202-5205 in calendrica-3.0.cl
def hindu_solar_sidereal_difference(date):
    """Return the difference between solar and sidereal day on date, date."""
   return hindu_daily_motion(date) * hindu_rising_sign(date)
# see lines 5207-5211 in calendrica-3.0.cl
UJJAIN = location(angle(23, 9, 0), angle(75, 46, 6),
                 mt(0), days_from_hours(5 + 461/9000))
# see lines 5213-5216 in calendrica-3.0.cl
# see lines 217-218 in calendrica-3.0.errata.cl
HINDU_LOCATION = UJJAIN
# see lines 5218-5228 in calendrica-3.0.cl
def hindu_sunrise(date):
    """Return the sunrise at hindu_location on date, date."""
   return (date + days_from_hours(6) +
            ((longitude(UJJAIN) - longitude(HINDU_LOCATION)) / deg(360)) -
           hindu_equation_of_time(date) +
            ((1577917828/1582237828 / deg(360)) *
             (hindu_ascensional_difference(date, HINDU_LOCATION) +
             (1/4 * hindu_solar_sidereal_difference(date)))))
# see lines 5230-5244 in calendrica-3.0.cl
def hindu_fullmoon_from_fixed(date):
    """Return the Hindu lunar date, full_moon scheme,
   equivalent to fixed date, date."""
   1_date
              = hindu_lunar_from_fixed(date)
              = hindu_lunar_year(1_date)
   year
              = hindu_lunar_month(l_date)
   leap_month = hindu_lunar_leap_month(l_date)
           = hindu_lunar_day(l_date)
   leap_day = hindu_lunar_leap_day(l_date)
   m = (hindu_lunar_month(hindu_lunar_from_fixed(date + 20))
        if (day >= 16)
        else month)
   return hindu_lunar_date(year, m, leap_month, day, leap_day)
```

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# see lines 5246-5255 in calendrica-3.0.cl
def is_hindu_expunged(l_month, l_year):
    """Return True if Hindu lunar month l_month in year, l_year
   is expunged."""
   return (1_month !=
           hindu_lunar_month(
                hindu_lunar_from_fixed(
                    fixed_from_hindu_lunar(
                        [l_year, l_month, False, 15, False]))))
# see lines 5257-5272 in calendrica-3.0.cl
def fixed_from_hindu_fullmoon(l_date):
    """Return the fixed date equivalent to Hindu lunar date, l_{date},
   in full_moon scheme."""
   year
              = hindu_lunar_year(l_date)
              = hindu_lunar_month(l_date)
   month
   leap_month = hindu_lunar_leap_month(l_date)
             = hindu_lunar_day(l_date)
   leap_day = hindu_lunar_leap_day(l_date)
   if (leap_month or (day <= 15)):</pre>
       m = month
   elif (is_hindu_expunged(amod(month - 1, 12), year)):
       m = amod(month - 2, 12)
   else:
       m = amod(month - 1, 12)
   return fixed_from_hindu_lunar(
        hindu_lunar_date(year, m, leap_month, day, leap_day))
# see lines 5274-5280 in calendrica-3.0.cl
def alt_hindu_sunrise(date):
    """Return the astronomical sunrise at Hindu location on date, date,
   per Lahiri, rounded to nearest minute, as a rational number."""
   rise = dawn(date, HINDU_LOCATION, angle(0, 47, 0))
   return 1/24 * 1/60 * iround(rise * 24 * 60)
# see lines 5282-5292 in calendrica-3.0.cl
def hindu_sunset(date):
   """Return sunset at HINDU_LOCATION on date, date."""
   return (date + days_from_hours(18) +
            ((longitude(UJJAIN) - longitude(HINDU_LOCATION)) / deg(360)) -
           hindu_equation_of_time(date) +
            (((1577917828/1582237828) / deg(360)) *
             (- hindu_ascensional_difference(date, HINDU_LOCATION) +
              (3/4 * hindu_solar_sidereal_difference(date)))))
# see lines 5294-5313 in calendrica-3.0.cl
def hindu_sundial_time(tee):
   """Return Hindu local time of temporal moment, tee."""
   date = fixed_from_moment(tee)
   time = mod(tee, 1)
      = ifloor(4 * time)
   if (q == 0):
       a = hindu_sunset(date - 1)
       b = hindu_sunrise(date)
       t = days_from_hours(-6)
```

```
elif (q == 3):
       a = hindu_sunset(date)
       b = hindu_sunrise(date + 1)
       t = days_from_hours(18)
    else:
       a = hindu_sunrise(date)
       b = hindu_sunset(date)
       t = days_from_hours(6)
   return a + (2 * (b - a) * (time - t))
# see lines 5315-5318 in calendrica-3.0.cl
def ayanamsha(tee):
    """Return the difference between tropical and sidereal solar longitude."""
   return solar_longitude(tee) - sidereal_solar_longitude(tee)
# see lines 5320-5323 in calendrica-3.0.cl
def astro_hindu_sunset(date):
    """Return the geometrical sunset at Hindu location on date, date."""
   return dusk(date, HINDU_LOCATION, deg(0))
# see lines 5325-5329 in calendrica-3.0.cl
def sidereal_zodiac(tee):
    """Return the sidereal zodiacal sign of the sun, as integer in range
   1..12, at moment, tee."""
   return quotient(int(sidereal_solar_longitude(tee)), deg(30)) + 1
# see lines 5331-5337 in calendrica-3.0.cl
def astro_hindu_calendar_year(tee):
    """Return the astronomical Hindu solar year KY at given moment, tee."""
   return iround(((tee - HINDU_EPOCH) / MEAN_SIDEREAL_YEAR) -
                 (sidereal_solar_longitude(tee) / deg(360)))
# see lines 5339-5357 in calendrica-3.0.cl
def astro_hindu_solar_from_fixed(date):
    """Return the Astronomical Hindu (Tamil) solar date equivalent to
   fixed date, date."""
   critical = astro_hindu_sunset(date)
            = sidereal_zodiac(critical)
            = astro_hindu_calendar_year(critical) - HINDU_SOLAR_ERA
   approx = (date - 3 -
               mod(ifloor(sidereal_solar_longitude( critical)), deg(30)))
   begin
            = next(approx,
                   lambda i: (sidereal_zodiac(astro_hindu_sunset(i)) == month))
            = date - begin + 1
   day
   return hindu_solar_date(year, month, day)
# see lines 5359-5375 in calendrica-3.0.cl
def fixed_from_astro_hindu_solar(s_date):
   """Return the fixed date corresponding to Astronomical
   Hindu solar date (Tamil rule; Saka era)."""
   month = standard_month(s_date)
   day = standard_day(s_date)
   year = standard_year(s_date)
   approx = (HINDU_EPOCH - 3 +
              ifloor(((year + HINDU_SOLAR_ERA) + ((month - 1) / 12)) *
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MEAN_SIDEREAL_YEAR))
   begin = next(approx,
                 lambda i: (sidereal_zodiac(astro_hindu_sunset(i)) == month))
   return begin + day - 1
# see lines 5377-5381 in calendrica-3.0.cl
def astro_lunar_day_from_moment(tee):
    """Return the phase of moon (tithi) at moment, tee, as an integer in
   the range 1..30."""
   return quotient(lunar_phase(tee), deg(12)) + 1
# see lines 5383-5410 in calendrica-3.0.cl
def astro_hindu_lunar_from_fixed(date):
    """Return the astronomical Hindu lunar date equivalent to
   fixed date, date."""
   critical = alt_hindu_sunrise(date)
           = astro_lunar_day_from_moment(critical)
   leap_day = (day == astro_lunar_day_from_moment(
       alt_hindu_sunrise(date - 1)))
   last_new_moon = new_moon_before(critical)
   next_new_moon = new_moon_at_or_after(critical)
   solar_month = sidereal_zodiac(last_new_moon)
   leap_month
                 = solar_month == sidereal_zodiac(next_new_moon)
   month
           = amod(solar_month + 1, 12)
            = astro_hindu_calendar_year((date + 180)
   year
                                         if (month <= 2)
                                         else date) - HINDU_LUNAR_ERA
   return hindu_lunar_date(year, month, leap_month, day, leap_day)
# see lines 5412-5460 in calendrica-3.0.cl
def fixed_from_astro_hindu_lunar(l_date):
    """Return the fixed date corresponding to Hindu lunar date, l_date."""
   year = hindu_lunar_year(l_date)
   month = hindu_lunar_month(1_date)
   leap_month = hindu_lunar_leap_month(l_date)
   day = hindu_lunar_day(l_date)
   leap_day = hindu_lunar_leap_day(l_date)
   approx = (HINDU_EPOCH +
              MEAN_SIDEREAL_YEAR *
              (year + HINDU_LUNAR_ERA + ((month - 1) / 12)))
   s = ifloor(approx -
              1/deg(360) * MEAN_SIDEREAL_YEAR *
              (mod(sidereal_solar_longitude(approx) -
                 (month - 1) * deg(30) + deg(180), 360) - deg(180)))
   k = astro_lunar_day_from_moment(s + days_from_hours(6))
   if (3 < k < 27):
        temp = k
   else:
        mid = astro_hindu_lunar_from_fixed(s - 15)
        if ((hindu_lunar_month(mid) != month) or
            (hindu_lunar_leap_month(mid) and not leap_month)):
            temp = mod(k + 15, 30) - 15
        else:
            temp = mod(k - 15, 30) + 15
   est = s + day - temp
   tau = (est -
          mod(astro_lunar_day_from_moment(est + days_from_hours(6)) - day + 15, 30) +
```

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date = next(tau - 1,
                lambda d: (astro_lunar_day_from_moment(alt_hindu_sunrise(d)) in
                           [day, amod(day + 1, 30)]))
   return (date + 1) if leap_day else date
# see lines 5462-5467 in calendrica-3.0.cl
def hindu_lunar_station(date):
    """Return the Hindu lunar station (nakshatra) at sunrise on date, date."""
   critical = hindu_sunrise(date)
   return quotient(hindu_lunar_longitude(critical), angle(0, 800, 0)) + 1
# see lines 5469-5480 in calendrica-3.0.cl
def hindu_solar_longitude_at_or_after(lam, tee):
    """Return the moment of the first time at or after moment, tee
   when Hindu solar longitude will be lam degrees."""
   tau = tee + (HINDU_SIDEREAL_YEAR *
                 (1 / deg(360)) *
                 mod(lam - hindu_solar_longitude(tee), 360))
   a = max(tee, tau - 5)
   b = tau +5
   return invert_angular(hindu_solar_longitude, lam, a, b)
# see lines 5482-5487 in calendrica-3.0.cl
def mesha_samkranti(g_year):
    """Return the fixed moment of Mesha samkranti (Vernal equinox)
   in Gregorian year, g_year."""
   jan1 = gregorian_new_year(g_year)
   return hindu_solar_longitude_at_or_after(deg(0), jan1)
# see lines 5489-5493 in calendrica-3.0.cl
SIDEREAL_START = precession(universal_from_local(mesha_samkranti(ce(285)),
                                                 HINDU_LOCATION))
# see lines 5495-5513 in calendrica-3.0.cl
def hindu_lunar_new_year(g_year):
    """Return the fixed date of Hindu lunisolar new year in
   Gregorian year, g_year."""
            = gregorian_new_year(g_year)
   jan1
            = hindu_solar_longitude_at_or_after(deg(330), jan1)
   new_moon = hindu_lunar_day_at_or_after(1, mina)
           = ifloor(new_moon)
   critical = hindu_sunrise(h_day)
   return (h_day +
            (0 if ((new_moon < critical) or
                   (hindu_lunar_day_from_moment(hindu_sunrise(h_day + 1)) == 2))
             else 1))
# see lines 5515-5539 in calendrica-3.0.cl
def is_hindu_lunar_on_or_before(l_date1, l_date2):
    """Return True if Hindu lunar date, l_date1 is on or before
   Hindu lunar date, l_date2."""
   month1 = hindu_lunar_month(l_date1)
   month2 = hindu_lunar_month(1_date2)
   leap1 = hindu_lunar_leap_month(l_date1)
   leap2 = hindu_lunar_leap_month(1_date2)
   day1 = hindu_lunar_day(l_date1)
```

```
= hindu_lunar_day(1_date2)
   leap_day1 = hindu_lunar_leap_day(l_date1)
   leap_day2 = hindu_lunar_leap_day(1_date2)
   year1 = hindu_lunar_year(l_date1)
   year2 = hindu_lunar_year(1_date2)
   return ((year1 < year2) or</pre>
            ((year1 == year2) and
             ((month1 < month2) or
              ((month1 == month2) and
               ((leap1 and not leap2) or
                ((leap1 == leap2) and
                 ((day1 < day2) or
                  ((day1 == day2) and
                   ((not leap_day1) or
                    leap_day2)))))))))
# see lines 5941-5967 in calendrica-3.0.cl
def hindu_date_occur(l_month, l_day, l_year):
    """Return the fixed date of occurrence of Hindu lunar month, l_month,
   day, l_day, in Hindu lunar year, l_year, taking leap and
    expunged days into account. When the month is
    expunged, then the following month is used."""
   lunar = hindu_lunar_date(l_year, l_month, False, l_day, False)
   ttry = fixed_from_hindu_lunar(lunar)
   mid = hindu_lunar_from_fixed((ttry - 5) if (l_day > 15) else ttry)
   expunged = l_month != hindu_lunar_month(mid)
   1_date = hindu_lunar_date(hindu_lunar_year(mid),
                              hindu_lunar_month(mid),
                              hindu_lunar_leap_month(mid),
                              l_day,
                              False)
   if (expunged):
        return next(ttry,
                    lambda d: (not is_hindu_lunar_on_or_before(
                        hindu_lunar_from_fixed(d),
                        l_date))) - 1
    elif (l_day != hindu_lunar_day(hindu_lunar_from_fixed(ttry))):
       return ttry - 1
   else:
       return ttry
# see lines 5969-5980 in calendrica-3.0.cl
def hindu_lunar_holiday(l_month, l_day, g_year):
    """Return the list of fixed dates of occurrences of Hindu lunar
   month, month, day, day, in Gregorian year, g_year."""
   l_year = hindu_lunar_year(
       hindu_lunar_from_fixed(gregorian_new_year(g_year)))
   date1 = hindu_date_occur(l_month, l_day, l_year)
   date2 = hindu_date_occur(l_month, l_day, l_year + 1)
   return list_range([date1, date2], gregorian_year_range(g_year))
# see lines 5582-5586 in calendrica-3.0.cl
def diwali(g_year):
    """Return the list of fixed date(s) of Diwali in Gregorian year, g_year."""
   return hindu_lunar_holiday(8, 1, g_year)
# see lines 5588-5605 in calendrica-3.0.cl
```

```
def hindu_tithi_occur(l_month, tithi, tee, l_year):
   """Return the fixed date of occurrence of Hindu lunar tithi prior
   to sundial time, tee, in Hindu lunar month, l_month, and
   year, l_year."""
   approx = hindu_date_occur(l_month, ifloor(tithi), l_year)
   lunar = hindu_lunar_day_at_or_after(tithi, approx - 2)
           = fixed_from_moment(lunar)
   tee_h = standard_from_sundial(ttry + tee, UJJAIN)
   if ((lunar <= tee_h) or</pre>
        (hindu_lunar_phase(standard_from_sundial(ttry + 1 + tee, UJJAIN)) >
         (12 * tithi))):
        return ttry
   else:
        return ttry + 1
# see lines 5607-5620 in calendrica-3.0.cl
def hindu_lunar_event(l_month, tithi, tee, g_year):
    """Return the list of fixed dates of occurrences of Hindu lunar tithi
   prior to sundial time, tee, in Hindu lunar month, l_month,
   in Gregorian year, g_year."""
   l_year = hindu_lunar_year(
       hindu_lunar_from_fixed(gregorian_new_year(g_year)))
   date1 = hindu_tithi_occur(l_month, tithi, tee, l_year)
   date2 = hindu_tithi_occur(l_month, tithi, tee, l_year + 1)
   return list_range([date1, date2],
                      gregorian_year_range(g_year))
# see lines 5622-5626 in calendrica-3.0.cl
def shiva(g_year):
    """Return the list of fixed date(s) of Night of Shiva in Gregorian
   year, g_year."""
   return hindu_lunar_event(11, 29, days_from_hours(24), g_year)
# see lines 5628-5632 in calendrica-3.0.cl
def rama(g_year):
    """Return the list of fixed date(s) of Rama's Birthday in Gregorian
   year, g_year."""
   return hindu_lunar_event(1, 9, days_from_hours(12), g_year)
# see lines 5634-5640 in calendrica-3.0.cl
def karana(n):
   """Return the number (0-10) of the name of the n-th (1-60) Hindu
   karana."""
   if (n == 1):
       return 0
    elif (n > 57):
       return n - 50
   else:
       return amod(n - 1, 7)
# see lines 5642-5648 in calendrica-3.0.cl
def yoga(date):
    """Return the Hindu yoga on date, date."""
   return ifloor(mod((hindu_solar_longitude(date) +
                 hindu_lunar_longitude(date)) / angle(0, 800, 0), 27)) + 1
```

```
# see lines 5650-5655 in calendrica-3.0.cl
  def sacred_wednesdays(g_year):
      """Return the list of Wednesdays in Gregorian year, g_year,
      that are day 8 of Hindu lunar months.""
      return sacred_wednesdays_in_range(gregorian_year_range(g_year))
  # see lines 5657-5672 in calendrica-3.0.cl
  def sacred_wednesdays_in_range(range):
      """Return the list of Wednesdays within range of dates
      that are day 8 of Hindu lunar months."""
              = start(range)
              = end(range)
      b
              = kday_on_or_after(WEDNESDAY, a)
      wed
      h_date = hindu_lunar_from_fixed(wed)
      ell = [wed] if (hindu_lunar_day(h_date) == 8) else []
      if is_in_range(wed, range):
           ell[:0] = sacred_wednesdays_in_range(interval(wed + 1, b))
           return ell
      else:
           return []
This code is used in chunk 3.
Defines:
  alt_hindu_sunrise, never used.
  astro_hindu_calendar_year, never used.
  astro_hindu_lunar_from_fixed, used in chunk 191.
  astro_hindu_solar_from_fixed, used in chunk 191.
  astro_hindu_sunset, never used.
  astro_lunar_day_from_moment, never used.
  ayanamsha, never used.
  diwali, never used.
  fixed_from_astro_hindu_lunar, used in chunk 191.
  fixed_from_astro_hindu_solar, used in chunk 191.
  fixed_from_hindu_fullmoon, never used.
  fixed_from_hindu_lunar, used in chunk 191.
  fixed_from_hindu_solar, used in chunk 191.
  HINDU_ANOMALISTIC_MONTH, never used.
  HINDU_ANOMALISTIC_YEAR, never used.
  hindu_arcsin, never used.
  hindu_ascensional_difference, never used.
  hindu_calendar_year, never used.
  HINDU_CREATION, never used.
  hindu_daily_motion, never used.
  hindu_date_occur, never used.
  hindu_equation_of_time, never used.
  hindu_fullmoon_from_fixed, never used.
  HINDU_LOCATION, never used.
  hindu_lunar_date, used in chunk 185.
  hindu_lunar_day, never used.
  hindu_lunar_day_at_or_after, never used.
  hindu_lunar_day_from_moment, never used.
  HINDU_LUNAR_ERA, never used.
  hindu_lunar_event, never used.
  hindu_lunar_from_fixed, used in chunk 191.
  hindu_lunar_holiday, never used.
  hindu_lunar_leap_day, never used.
  hindu_lunar_leap_month, never used.
  hindu_lunar_longitude, never used.
  hindu_lunar_month, never used.
  hindu_lunar_new_year, never used.
  hindu_lunar_phase, never used.
  hindu_lunar_station, never used.
  hindu_lunar_year, never used.
  hindu_mean_position, never used.
  hindu_new_moon_before, never used.
```

```
hindu_rising_sign, never used.
  HINDU_SIDEREAL_MONTH, never used.
  HINDU_SIDEREAL_YEAR, never used.
  hindu_sine, never used.
  hindu_sine_table, never used.
  HINDU_SOLAR_ERA, never used.
  hindu_solar_from_fixed, used in chunk 191.
  hindu_solar_longitude, never used.
  hindu_solar_longitude_at_or_after, never used.
  hindu_solar_sidereal_difference, never used.
  hindu_sundial_time, never used.
  hindu_sunrise, never used.
  hindu sunset, never used.
  HINDU_SYNODIC_MONTH, never used.
  hindu_tithi_occur, never used.
  hindu_tropical_longitude, never used.
  hindu_true_position, never used.
  hindu_zodiac, never used.
  is_hindu_expunged, never used.
  is_hindu_lunar_on_or_before, never used.
  karana, never used.
  mesha_samkranti, never used.
  rama, never used.
  sacred_wednesdays, never used.
  sacred_wednesdays_in_range, never used.
  shiva, never used.
  SIDEREAL_START, used in chunks 109 and 119.
  sidereal_zodiac, never used.
  UJJAIN, never used.
  yoga, never used.
Uses amod 15, angle 100, binary_search 25, ce 59, ceiling 86 86, dawn 102, days_from_hours 100,
  deg 100, dusk 102, end 47, fixed_from_moment 40, gregorian_new_year 56, gregorian_year_range 56,
  HINDU_EPOCH 86, hindu_solar_date 86, ifloor 15, interval 47, invert_angular 28 28, iround 15,
  is_in_range 47, kday_on_or_after 56, latitude 100, list_range 47, location 100, longitude 100,
  lunar_phase 119, MEAN_SIDEREAL_YEAR 107, midnight 100, minute 39, mod 15, mt 100,
  new_moon_at_or_after 119, new_moon_before 119, next 16, precession 109, quotient 14 14,
  sidereal_solar_longitude 109, signum 100, sin_degrees 100, solar_longitude 107,
  standard_day 39, standard_from_sundial 105, standard_month 39, standard_year 39, start 47,
  sunrise 102, sunset 102, universal_from_local 100, and WEDNESDAY 38.
\langle modern\ hindu\ calendars\ unit\ test\ 137 \rangle \equiv
This definition is continued in chunk 190.
This code is used in chunks 4 and 138.
2.19.1
           Unit tests
\langle modernHinduCalendarsUnitTest.py 138 \rangle \equiv
  # \(\langle generated code warning \)
  \langle import\ for\ testing\ 6 \rangle
  from appendixCUnitTest import AppendixCTable4TestCaseBase
  ⟨modern hindu calendars unit test 137⟩
  \langle execute \ tests \ 5 \rangle
```

137

138

Root chunk (not used in this document). Uses AppendixCTable4TestCaseBase 185.

2.20 Tibetan Calendar

```
\langle tibetan\ calendar\ 139 \rangle \equiv
139
         # tibetan calendar algorithms #
         # see lines 5677-5681 in calendrica-3.0.cl
         def tibetan_date(year, month, leap_month, day, leap_day):
             """Return a Tibetan date data structure."""
             return [year, month, leap_month, day, leap_day]
         # see lines 5683-5685 in calendrica-3.0.cl
         def tibetan month(date):
             """Return 'month' element of a Tibetan date, date."""
             return date[1]
         # see lines 5687-5689 in calendrica-3.0.cl
         def tibetan_leap_month(date):
             """Return 'leap month' element of a Tibetan date, date."""
             return date[2]
         # see lines 5691-5693 in calendrica-3.0.cl
         def tibetan day(date):
             """Return 'day' element of a Tibetan date, date."""
             return date[3]
         # see lines 5695-5697 in calendrica-3.0.cl
         def tibetan_leap_day(date):
             """Return 'leap day' element of a Tibetan date, date."""
             return date[4]
         # see lines 5699-5701 in calendrica-3.0.cl
         def tibetan_year(date):
             """Return 'year' element of a Tibetan date, date."""
             return date[0]
         # see lines 5703-5705 in calendrica-3.0.cl
         TIBETAN_EPOCH = fixed_from_gregorian(gregorian_date(-127, DECEMBER, 7))
         # see lines 5707-5717 in calendrica-3.0.cl
         def tibetan_sun_equation(alpha):
             """Return the interpolated tabular sine of solar anomaly, alpha."""
             if (alpha > 6):
                 return -tibetan_sun_equation(alpha - 6)
             elif (alpha > 3):
                 return tibetan_sun_equation(6 - alpha)
             elif isinstance(alpha, int):
                 return [0, 6/60, 10/60, 11/60][alpha]
             else:
                 return ((mod(alpha, 1) * tibetan_sun_equation(ceiling(alpha))) +
                         (mod(-alpha, 1) * tibetan_sun_equation(ifloor(alpha))))
         # see lines 5719-5731 in calendrica-3.0.cl
         def tibetan_moon_equation(alpha):
             """Return the interpolated tabular sine of lunar anomaly, alpha."""
             if (alpha > 14):
                 return -tibetan_moon_equation(alpha - 14)
             elif (alpha > 7):
```

```
return tibetan_moon_equation(14 -alpha)
    elif isinstance(alpha, int):
        return [0, 5/60, 10/60, 15/60,
                19/60, 22/60, 24/60, 25/60][alpha]
   else:
       return ((mod(alpha, 1) * tibetan_moon_equation(ceiling(alpha))) +
                (mod(-alpha, 1) * tibetan_moon_equation(ifloor(alpha))))
# see lines 5733-5755 in calendrica-3.0.cl
def fixed_from_tibetan(t_date):
   """Return the fixed date corresponding to Tibetan lunar date, t_date."""
              = tibetan_year(t_date)
   month
              = tibetan_month(t_date)
   leap_month = tibetan_leap_month(t_date)
             = tibetan_day(t_date)
   day
   leap_day = tibetan_leap_day(t_date)
   months = ifloor((804/65 * (year - 1)) +
                   (67/65 * month) +
                   (-1 if leap_month else 0) +
                   64/65)
   days = (30 * months) + day
   mean = ((days * 11135/11312) -30 +
            (0 if leap_day else -1) +
            1071/1616)
   solar_anomaly = mod((days * 13/4824) + 2117/4824, 1)
   lunar_anomaly = mod((days * 3781/105840) +
                        2837/15120, 1)
   sun = -tibetan_sun_equation(12 * solar_anomaly)
   moon = tibetan_moon_equation(28 * lunar_anomaly)
   return ifloor(TIBETAN_EPOCH + mean + sun + moon)
# see lines 5757-5796 in calendrica-3.0.cl
def tibetan_from_fixed(date):
    """Return the Tibetan lunar date corresponding to fixed date, date."""
   cap_Y = 365 + 4975/18382
   years = ceiling((date - TIBETAN_EPOCH) / cap_Y)
   year0 = final(years,
                  lambda y:(date >=
                            fixed_from_tibetan(
                                tibetan_date(y, 1, False, 1, False))))
   month0 = final(1,
                   lambda m: (date >=
                              fixed_from_tibetan(
                                  tibetan_date(year0, m, False, 1, False))))
   est = date - fixed_from_tibetan(
       tibetan_date(year0, month0, False, 1, False))
   day0 = final(est -2,
                 lambda d: (date >=
                            fixed_from_tibetan(
                                tibetan_date(year0, month0, False, d, False))))
   leap_month = (day0 > 30)
   day = amod(day0, 30)
   if (day > day0):
        temp = month0 - 1
    elif leap_month:
        temp = month0 + 1
    else:
       temp = month0
   month = amod(temp, 12)
```

```
if ((day > day0) \text{ and } (month0 == 1)):
          year = year0 - 1
      elif (leap_month and (month0 == 12)):
          year = year0 + 1
      else:
          year = year0
      leap_day = date == fixed_from_tibetan(
          tibetan_date(year, month, leap_month, day, True))
      return tibetan_date(year, month, leap_month, day, leap_day)
  # see lines 5798-5805 in calendrica-3.0.cl
  def is_tibetan_leap_month(t_month, t_year):
      """Return True if t_month is leap in Tibetan year, t_year."""
      return (t_month ==
               tibetan_month(tibetan_from_fixed(
                   fixed_from_tibetan(
                        tibetan_date(t_year, t_month, True, 2, False)))))
  # see lines 5807-5813 in calendrica-3.0.cl
  def losar(t_year):
      """Return the fixed date of Tibetan New Year (Losar)
      in Tibetan year, t_year."""
      t_leap = is_tibetan_leap_month(1, t_year)
      return fixed_from_tibetan(tibetan_date(t_year, 1, t_leap, 1, False))
  # see lines 5815-5824 in calendrica-3.0.cl
  def tibetan_new_year(g_year):
      """Return the list of fixed dates of Tibetan New Year in
      Gregorian year, g_year.""
      dec31 = gregorian_year_end(g_year)
      t_year = tibetan_year(tibetan_from_fixed(dec31))
      return list_range([losar(t_year - 1), losar(t_year)],
                          gregorian_year_range(g_year))
This code is used in chunk 3.
Defines:
  fixed_from_tibetan, used in chunk 193.
  is_tibetan_leap_month, never used.
  losar, never used.
  tibetan_date, used in chunk 185.
  tibetan_day, never used.
  tibetan_from_fixed, used in chunk 193.
  tibetan_leap_day, never used.
  tibetan_leap_month, never used.
  tibetan_month, never used.
  tibetan_moon_equation, never used.
  tibetan_new_year, never used.
  tibetan_sun_equation, never used.
  tibetan_year, never used.
Uses amod 15, ceiling 86 86, DECEMBER 53, final 19, fixed_from_gregorian 55, gregorian_date 52,
  gregorian_year_end 56, gregorian_year_range 56, ifloor 15, list_range 47, lunar_anomaly 115,
  mod 15, and solar_anomaly 113.
\langle tibetan\ calendar\ unit\ test\ 140 \rangle \equiv
This definition is continued in chunk 192.
This code is used in chunks 4 and 141.
```

140

2.20.1 Unit tests

```
| \( \text{\text{tibetanCalendarUnitTest.py 141}} \) \( \text{\text{\text{\text{$}}}} \) \( \text{\text{\text{$}}} \) \( \text{\text{\text{$}}} \) \( \text{\text{$}} \) \( \te
```

2.21 Astronomical Lunar Calendars

```
\langle astronomical\ lunar\ calendars\ 105 \rangle + \equiv
142
         # astronomical lunar calendars algorithms #
         # see lines 5829-5845 in calendrica-3.0.cl
         def visible_crescent(date, location):
             """Return S. K. Shaukat's criterion for likely
             visibility of crescent moon on eve of date 'date',
             at location 'location'."""
             tee = universal_from_standard(dusk(date - 1, location, deg(mpf(4.5))),
                                          location)
             phase = lunar_phase(tee)
             altitude = lunar_altitude(tee, location)
             arc_of_light = arccos_degrees(cosine_degrees(lunar_latitude(tee)) *
                                           cosine_degrees(phase))
             return ((NEW < phase < FIRST_QUARTER) and
                     (deg(mpf(10.6)) \le arc_of_light \le deg(90)) and
                     (altitude > deg(mpf(4.1))))
         # see lines 5847-5860 in calendrica-3.0.cl
         def phasis_on_or_before(date, location):
             """Return the closest fixed date on or before date 'date', when crescent
             moon first became visible at location 'location'."""
             mean = date - ifloor(lunar_phase(date + 1) / deg(360) *
                                 MEAN_SYNODIC_MONTH)
             tau = ((mean - 30)
                    if (((date - mean) <= 3) and (not visible_crescent(date, location)))</pre>
                    else (mean - 2))
             return next(tau, lambda d: visible_crescent(d, location))
         # see lines 5862-5866 in calendrica-3.0.cl
         # see lines 220-221 in calendrica-3.0.errata.cl
         # Sample location for Observational Islamic calendar
         # (Cairo, Egypt).
         ISLAMIC_LOCATION = location(deg(mpf(30.1)), deg(mpf(31.3)), mt(200), days_from_hours(2))
         # see lines 5868-5882 in calendrica-3.0.cl
         def fixed_from_observational_islamic(i_date):
             """Return fixed date equivalent to Observational Islamic date, i_date."""
                     = standard_month(i_date)
             day
                      = standard_day(i_date)
                     = standard_year(i_date)
             year
             midmonth = ISLAMIC_EPOCH + ifloor((((year - 1) * 12) + month - 0.5) *
                                              MEAN SYNODIC MONTH)
             return (phasis_on_or_before(midmonth, ISLAMIC_LOCATION) +
                     day - 1)
         # see lines 5884-5896 in calendrica-3.0.cl
         def observational_islamic_from_fixed(date):
             """Return Observational Islamic date (year month day)
             corresponding to fixed date, date."""
             crescent = phasis_on_or_before(date, ISLAMIC_LOCATION)
             elapsed_months = iround((crescent - ISLAMIC_EPOCH) / MEAN_SYNODIC_MONTH)
             year = quotient(elapsed months, 12) + 1
             month = mod(elapsed_months, 12) + 1
             day = (date - crescent) + 1
             return islamic_date(year, month, day)
         # see lines 5898-5901 in calendrica-3.0.cl
```

```
JERUSALEM = location(deg(mpf(31.8)), deg(mpf(35.2)), mt(800), days_from_hours(2))
# see lines 5903-5918 in calendrica-3.0.cl
def astronomical_easter(g_year):
    """Return date of (proposed) astronomical Easter in Gregorian
   year, g_year."""
    jan1 = gregorian_new_year(g_year)
   equinox = solar_longitude_after(SPRING, jan1)
   paschal_moon = ifloor(apparent_from_local(
                             local_from_universal(
                                lunar_phase_at_or_after(FULL, equinox),
                                JERUSALEM),
                             JERUSALEM))
   # Return the Sunday following the Paschal moon.
   return kday_after(SUNDAY, paschal_moon)
# see lines 5920-5923 in calendrica-3.0.cl
JAFFA = location(angle(32, 1, 60), angle(34, 45, 0), mt(0), days_from_hours(2))
# see lines 5925-5938 in calendrica-3.0.cl
def phasis_on_or_after(date, location):
    """Return closest fixed date on or after date, date, on the eve
   of which crescent moon first became visible at location, location."""
   mean = date - ifloor(lunar_phase(date + 1) / deg(mpf(360)) *
                        MEAN_SYNODIC_MONTH)
   tau = (date if (((date - mean) \le 3) and
                    (not visible_crescent(date - 1, location)))
           else (mean + 29))
   return next(tau, lambda d: visible_crescent(d, location))
# see lines 5940-5955 in calendrica-3.0.cl
def observational_hebrew_new_year(g_year):
    """Return fixed date of Observational (classical)
   Nisan 1 occurring in Gregorian year, g_year."""
   jan1 = gregorian_new_year(g_year)
   equinox = solar_longitude_after(SPRING, jan1)
   sset = universal_from_standard(sunset(ifloor(equinox), JAFFA), JAFFA)
   return phasis_on_or_after(ifloor(equinox) - (14 if (equinox < sset) else 13),</pre>
# see lines 5957-5973 in calendrica-3.0.cl
def fixed_from_observational_hebrew(h_date):
   """Return fixed date equivalent to Observational Hebrew date."""
   month = standard_month(h_date)
   day = standard_day(h_date)
   year = standard_year(h_date)
   year1 = (year - 1) if (month >= TISHRI) else year
   start = fixed_from_hebrew(hebrew_date(year1, NISAN, 1))
   g_year = gregorian_year_from_fixed(start + 60)
   new_year = observational_hebrew_new_year(g_year)
   midmonth = new_year + iround(29.5 * (month - 1)) + 15
   return phasis_on_or_before(midmonth, JAFFA) + day - 1
# see lines 5975-5991 in calendrica-3.0.cl
def observational_hebrew_from_fixed(date):
   """Return Observational Hebrew date (year month day)
   corresponding to fixed date, date."""
   crescent = phasis_on_or_before(date, JAFFA)
   g_year = gregorian_year_from_fixed(date)
   ny = observational_hebrew_new_year(g_year)
   new_year = observational_hebrew_new_year(g_year - 1) if (date < ny) else ny</pre>
```

```
year = (standard_year(hebrew_from_fixed(new_year)) +
                          (1 if (month >= TISHRI) else 0))
                day = date - crescent + 1
                return hebrew_date(year, month, day)
           # see lines 5993-5997 in calendrica-3.0.cl
           def classical_passover_eve(g_year):
                """Return fixed date of Classical (observational) Passover Eve
                (Nisan 14) occurring in Gregorian year, g_year."""
                return observational_hebrew_new_year(g_year) + 13
         This code is used in chunk 3.
         Defines:
           astronomical_easter, used in chunk 178.
           classical_passover_eve, never used.
           fixed_from_observational_hebrew, used in chunks 176 and 253.
           fixed_from_observational_islamic, used in chunk 169.
           ISLAMIC_LOCATION, never used.
           JAFFA, used in chunk 104.
           JERUSALEM, used in chunk 196.
           observational\_hebrew\_from\_fixed, used in chunks 176 and 253.
           observational_hebrew_new_year, never used.
           observational_islamic_from_fixed, used in chunk 169.
           phasis_on_or_after, never used.
           phasis_on_or_before, never used.
           visible crescent, never used.
         Uses angle 100, apparent_from_local 100, arccos_degrees 100, cosine_degrees 100,
           days_from_hours 100, deg 100, dusk 102, FIRST_QUARTER 119, fixed_from_hebrew 80,
           FULL 119, gregorian_new_year 56, gregorian_year_from_fixed 55, hebrew_date 80,
           hebrew_from_fixed 80, ifloor 15, iround 15, islamic_date 77, ISLAMIC_EPOCH 77, kday_after 56,
           local_from_universal 100, location 100, lunar_altitude 120, lunar_latitude 119,
           lunar_phase 119, lunar_phase_at_or_after 119, MEAN_SYNODIC_MONTH 107, mod 15, mt 100,
           NEW 119, next 16, NISAN 80, quotient 14 14, solar_longitude_after 109, SPRING 109,
           standard_day 39, standard_month 39, standard_year 39, start 47, SUNDAY 38, sunset 102,
           TISHRI 80, and universal_from_standard 100.
         \langle \mathit{coda} \ 143 \rangle \equiv
143
           # That's all folks!
         This code is used in chunk 3.
                    Unit tests
         2.21.1
144
         \langle astronomicalLunarCalendarsUnitTest.py 144 \rangle \equiv
           # \(\langle generated code warning 1 \rangle \)
           ⟨import for testing 6⟩
           from appendixCUnitTest import AppendixCTable5TestCaseBase
           ⟨astronomical lunar calendars unit test 145⟩
           \langle execute \ tests \ 5 \rangle
         Root chunk (not used in this document).
         Uses \ {\tt AppendixCTable5TestCaseBase} \ {\tt 194}.
         \langle astronomical\ lunar\ calendars\ unit\ test\ 145 \rangle \equiv
145
           {\tt class} \  \, {\tt AstronomicalLunarCalendarsTestCase} \  \, ({\tt unittest.TestCase}) : \\
                \langle astronomical\ lunar\ tests\ 106 \rangle
         This code is used in chunks 4 and 144.
         Defines:
           AstronomicalLunarCalendarsTestCase, never used.
```

month = iround((crescent - new_year) / 29.5) + 1

2.22 Appendix C test data and unit tests

Prof. Reingold kindly provided me with an electronic version of Appendix C test data [1, see pag xxx]. In order to verify the alignment of my implementation in PYTHON with the one of the book, I designed the following tools and tests:

```
\langle trasformLatexDates2Cvs \ 146 \rangle \equiv
146
         #/bin/sh
         # transform "Calendrical Calculations" Appendix C test data
         # from LaTeX table to comma-separated-values
         sed -e 's/\$//g' -e 's/\\/g' \
    -e's/[ ][ ]*\&[ ][
                                                 ]*/,/g'\
              -e 's/multicolumn{4}{c}{fun{bogus}}/bogus,bogus,bogus,bogus/g'
       Root chunk (not used in this document).
147
       \langle appendixCUnitTest.py 147 \rangle \equiv
         # \langle generated \ code \ warning \ 1 \rangle
         ⟨import for testing 6⟩
          ⟨appendix c unit test 148⟩
          ⟨execute tests 5⟩
       Root chunk (not used in this document).
148
       \langle appendix \ c \ unit \ test \ 148 \rangle \equiv
         # The idea is to use the Appendix C in "Calendrical Calculations", 3rd Ed
         # values to check the correctness (or the same erroneusness !-) of the
         # Python implementation.
         # read each row and transform the first cell in the various calendar and the
         # check the result
         import csv
         ⟨appendixCTable1Tests 149⟩
          \langle appendixCTable2Tests 165 \rangle
          \langle appendixCTable3Tests 174 \rangle
          ⟨appendixCTable₄Tests 185⟩
          \langle appendixCTable5Tests 194 \rangle
```

This code is used in chunk 147.

The test data are for five areas. The first one is about weekdays, Julian day, modified Julian day, Gregorian date, ISO date, Julian date, Roman name of Julian date, Egyptian date, Armenian date and Coptic date.

```
\langle appendixCTable1Tests 149 \rangle \equiv
149
         class AppendixCTable1TestCaseBase():
             """This class provides methods to load the relevant test data and helpers."""
             def _dayOfWeek(self, d):
                 return self._wdDict[d]
             def _romanLeap(self, c):
                 return False if c == 'f' else True
             def setUp(self):
                 self._wdDict = {'Sunday': SUNDAY,
                                  'Monday': MONDAY,
                                  'Tuesday': TUESDAY,
                                  'Wednesday': WEDNESDAY,
                                  'Thursday': THURSDAY,
                                  'Friday': FRIDAY,
                                  'Saturday': SATURDAY}
                 reader = csv.reader(open("dates1.csv", "rU"),
                                      delimiter=',',
                                      quoting=csv.QUOTE_NONE)
                 self.rd
                            = [] # Rata Die
                 self.wd
                            = [] # WeekDay
                 self.jd
                            = [] # Julian Day
                 self.mjd = [] # Madified Julian Day
                            = [] # Gregorian Date
                 self.gd
                 self.isod = [] # ISO Date
                 self.jdt = [] # Julian DaTe
                 self.jrn = [] # Julian Roman Name
                 self.ed
                            = [] # Egyptian Date
                 self.ad
                            = [] # Armenian Date
                 self.cd
                            = [] # Coptic Date
                 for row in reader:
                     self.rd.append(int(row[0]))
                     self.wd.append(self._dayOfWeek(row[1]))
                     self.jd.append(float(row[2]))
                     self.mjd.append(int(row[3]))
                     self.gd.append(
                          gregorian_date(int(row[4]), int(row[5]), int(row[6])))
                     self.isod.append(
                          iso_date(int(row[7]), int(row[8]), int(row[9])))
                     self.jdt.append(
                          julian_date(int(row[10]), int(row[11]), int(row[12])))
                     self.jrn.append(roman_date(int(row[13]),
                                                 int(row[14]),
                                                 int(row[15]),
                                                 int(row[16]),
                                                 self._romanLeap(row[17])))
                     self.ed.append(
                          egyptian_date(int(row[18]), int(row[19]), int(row[20])))
                     self.ad.append(
                          armenian_date(int(row[21]), int(row[22]), int(row[23])))
                     self.cd.append(
                          coptic_date(int(row[24]), int(row[25]), int(row[26])))
```

```
class AppendixCTable1TestCase(AppendixCTable1TestCaseBase, unittest.TestCase):
                 \langle test\ basic\ appendix\ c\ 151 \rangle
                 ⟨test julian appendix c 158⟩
                 \langle test\ gregorian\ appendix\ c\ 155 \rangle
                 \langle test \ iso \ appendix \ c \ 157 \rangle
                 \langle test \ julian \ appendix \ c \ 158 \rangle
                 \langle test\ egyptian\ appendix\ c\ 160 \rangle
                 \langle test \ armenian \ appendix \ c \ 161 \rangle
                 \langle test\ coptic\ appendix\ c\ 164 \rangle
         This code is used in chunk 148.
         Defines:
            AppendixCTable1TestCase, never used.
            AppendixCTable1TestCaseBase, used in chunks 4, 49, 58, 64, 67, 70, 73, 150, 152, 154, 156, 159, 162,
         Uses armenian_date 65, coptic_date 71, egyptian_date 65, FRIDAY 38, gregorian_date 52,
            iso_date 68, julian_date 59, MONDAY 38, rd 37, roman_date 61, SATURDAY 38, SUNDAY 38, THURSDAY 38,
            TUESDAY 38, and WEDNESDAY 38.
150
         \langle basic\ code\ unit\ test\ 50\rangle + \equiv
            class BasicAppendixCTestCase(AppendixCTable1TestCaseBase, unittest.TestCase):
                 \langle test\ basic\ appendix\ c\ 151 \rangle
         This code is used in chunks 4 and 49.
         Defines:
            {\tt BasicAppendixCTestCase}, \ never \ used.
         Uses AppendixCTable1TestCaseBase 149.
151
         \langle test\ basic\ appendix\ c\ {\color{red}151}\rangle {\color{red}\equiv}
            def testWeekdays(self):
                 for i in range(len(self.rd)):
                      # weekdays
                      self.assertEqual(day_of_week_from_fixed(self.rd[i]), self.wd[i])
         This code is used in chunks 149 and 150.
         Defines:
            testWeekdays, never used.
         Uses day_of_week_from_fixed 38 and rd 37.
152
         \langle julian\ calendar\ unit\ test\ 60\rangle + \equiv
            class JulianDayAppendixCTestCase(AppendixCTable1TestCaseBase,
                                                         unittest.TestCase):
                 \langle test \ julian \ day \ appendix \ c \ 153 \rangle
         This code is used in chunks 4 and 64.
         Defines:
            JulianDayAppendixCTestCase, never used.
         Uses AppendixCTable1TestCaseBase 149.
         \langle test \ julian \ day \ appendix \ c \ 153 \rangle \equiv
153
            def testJulianDay(self):
                 for i in range(len(self.rd)):
                      # julian day
                      self.assertEqual(jd_from_fixed(self.rd[i]), self.jd[i])
                      self.assertEqual(fixed_from_jd(self.jd[i]), self.rd[i])
                      # modified julian day
                      self.assertEqual(mjd_from_fixed(self.rd[i]), self.mjd[i])
                      self.assertEqual(fixed_from_mjd(self.mjd[i]), self.rd[i])
         This code is used in chunk 152.
            testJulianDay, never used.
         Uses fixed_from_jd 48, fixed_from_mjd 48, jd_from_fixed 48, mjd_from_fixed 48, and rd 37.
```

```
154
        \langle gregorian\ calendar\ unit\ test\ 57 \rangle + \equiv
           {\tt class~GregorianAppendixCTestCase(AppendixCTable1TestCaseBase,}
                                                    unittest.TestCase):
                \langle test\ gregorian\ appendix\ c\ 155 \rangle
        This code is used in chunks 4 and 58.
        Defines:
           GregorianAppendixCTestCase, never used.
        Uses AppendixCTable1TestCaseBase 149.
155
        \langle test\ gregorian\ appendix\ c\ 155 \rangle \equiv
           def testGregorian(self):
               for i in range(len(self.rd)):
                    self.assertEqual(gregorian_from_fixed(self.rd[i]), self.gd[i])
                    self.assertEqual(fixed_from_gregorian(self.gd[i]), self.rd[i])
                    self.assertEqual(
                         gregorian_year_from_fixed(self.rd[i]), standard_year(self.gd[i]))
           def testAltGregorian(self):
               for i in range(len(self.rd)):
                    self.assertEqual(alt_gregorian_from_fixed(self.rd[i]), self.gd[i])
                    {\tt self.assertEqual(alt\_fixed\_from\_gregorian(self.gd[i]), self.rd[i])}
                    self.assertEqual(
                         alt_gregorian_year_from_fixed(self.rd[i]),
                         standard_year(self.gd[i]))
        This code is used in chunks 149 and 154.
        Defines:
           testAltGregorian, never used.
           testGregorian, never used.
        Uses alt_fixed_from_gregorian_56, alt_gregorian_from_fixed 56, alt_gregorian_year_from_fixed
           56, fixed_from_gregorian 55, gregorian_from_fixed 56, gregorian_year_from_fixed 55, rd 37,
           and standard_year 39.
156
        \langle iso\ calendar\ unit\ test\ 69 \rangle + \equiv
           {\tt class~IsoAppendixCTestCase(AppendixCTable1TestCaseBase,~unittest.TestCase):}
                \langle test \ iso \ appendix \ c \ 157 \rangle
        This code is used in chunks 4 and 70.
        Defines:
           IsoAppendixCTestCase, never used.
        Uses AppendixCTable1TestCaseBase 149.
157
        \langle test \ iso \ appendix \ c \ 157 \rangle \equiv
           def testIso(self):
               for i in range(len(self.rd)):
                    self.assertEqual(iso_from_fixed(self.rd[i]), self.isod[i])
                    self.assertEqual(fixed_from_iso(self.isod[i]), self.rd[i])
        This code is used in chunks 149 and 156.
        Defines:
           testIso, never used.
        Uses fixed_from_iso 68, iso_from_fixed 68, and rd 37.
```

```
158
         \langle test \ julian \ appendix \ c \ 158 \rangle \equiv
           def testJulian(self):
                for i in range(len(self.rd)):
                     # julian date
                     self.assertEqual(julian_from_fixed(self.rd[i]), self.jdt[i])
                     self.assertEqual(fixed_from_julian(self.jdt[i]), self.rd[i])
                     # julian date, roman name
                     self.assertEqual(roman_from_fixed(self.rd[i]), self.jrn[i])
                     self.assertEqual(fixed_from_roman(self.jrn[i]), self.rd[i])
         This code is used in chunks 149 and 159.
         Defines:
           testJulian, never used.
         Uses fixed_from_julian 59, fixed_from_roman 61, julian_from_fixed 59, rd 37,
           and roman_from_fixed 61.
159
         \langle julian\ calendar\ unit\ test\ 60\rangle + \equiv
           class JulianAppendixCTestCase(AppendixCTable1TestCaseBase):
                ⟨test julian appendix c 158⟩
         This code is used in chunks 4 and 64.
         Defines:
           {\tt JulianAppendixCTestCase}, \ {\tt never} \ {\tt used}.
         Uses AppendixCTable1TestCaseBase 149.
160
         \langle test\ egyptian\ appendix\ c\ 160 \rangle \equiv
           def testEgyptian(self):
                for i in range(len(self.rd)):
                     self.assertEqual(egyptian_from_fixed(self.rd[i]), self.ed[i])
                     self.assertEqual(fixed_from_egyptian(self.ed[i]), self.rd[i])
         This code is used in chunks 149 and 162.
         Defines:
           testEgyptian, never used.
         Uses egyptian_from_fixed 65, fixed_from_egyptian 65, and rd 37.
161
         \langle test \ armenian \ appendix \ c \ 161 \rangle \equiv
           def testArmenian(self):
                for i in range(len(self.rd)):
                     self.assertEqual(armenian_from_fixed(self.rd[i]), self.ad[i])
                     self.assertEqual(fixed_from_armenian(self.ad[i]), self.rd[i])
         This code is used in chunks 149 and 162.
         Defines:
           testArmenian, never used.
         Uses armenian_from_fixed 65, fixed_from_armenian 65, and rd 37.
         \langle egyptian \ and \ armenian \ calendars \ unit \ test \ 66 \rangle + \equiv
162
           class ArmeniamAppendixCTestCase(AppendixCTable1TestCaseBase):
               \langle test \ armenian \ appendix \ c \ 161 \rangle
           \verb|class EgyptianAppendixCTestCase(AppendixCTable1TestCaseBase)|:
               \langle test\ egyptian\ appendix\ c\ 160 \rangle
         This code is used in chunks 4 and 67.
         Defines:
           ArmeniamAppendixCTestCase, never used.
           {\tt EgyptianAppendixCTestCase}, \ {\tt never} \ {\tt used}.
         Uses AppendixCTable1TestCaseBase 149.
```

```
163
         \langle coptic\ and\ ethiopic\ calendars\ unit\ test\ 72 \rangle + \equiv
            class CopticAppendixCTestCase(AppendixCTable1TestCaseBase):
                 \langle test\ coptic\ appendix\ c\ 164 \rangle
         This code is used in chunks 4 and 73.
         Defines:
            {\tt CopticAppendixCTestCase}, \ {\tt never} \ {\tt used}.
         Uses AppendixCTable1TestCaseBase 149.
164
         \langle \mathit{test\ coptic\ appendix\ c\ 164} \rangle \equiv
            def testCoptic(self):
                 for i in range(len(self.rd)):
                      self.assertEqual(coptic_from_fixed(self.rd[i]), self.cd[i])
                      self.assertEqual(fixed_from_coptic(self.cd[i]), self.rd[i])
         This code is used in chunks 149 and 163.
         Defines:
            testCoptic, never used.
         Uses coptic_from_fixed 71, fixed_from_coptic 71, and rd 37.
```

The second is for Ethiopic, Islamic (Arithmetic and Observational), Bahai, Future Bahai, Mayan (Long count, Haab and Tzolkin), Aztec (Xihuitl and Tonalpohualli).

```
\langle appendixCTable2Tests 165 \rangle \equiv
165
          class AppendixCTable2TestCaseBase():
              def setUp(self):
                  reader = csv.reader(open("dates2.csv", "rU"),
                                        delimiter=',',
                                        quoting=csv.QUOTE_NONE)
                  self.rd
                              = [] # Rata Die
                  self.ed
                              = [] # Ethiopic Date
                  self.id
                              = [] # Islamic Date
                  self.io
                              = [] # Islamic Observational date
                  self.bd
                             = [] # Bahai Date
                              = [] # Bahai Future date
                  self.bf
                  self.mlc = [] # Mayan Long Count
                  self.mh
                             = [] # Mayan Haab
                  self.mt = [] # Mayan Tzolkin
                  self.ax = [] # Aztec Xihuitl
                  self.at
                              = [] # Aztec Tonalpohualli
                  for row in reader:
                       self.rd.append(int(row[0]))
                       self.ed.append(
                           ethiopic_date(int(row[1]), int(row[2]), int(row[3])))
                       self.id.append(
                           islamic_date(int(row[4]), int(row[5]), int(row[6])))
                       self.io.append(
                           islamic_date(int(row[7]), int(row[8]), int(row[9])))
                       self.bd.append(
                           bahai_date(int(row[10]), int(row[11]), int(row[12]),
                                       int(row[13]), int(row[14])))
                       self.bf.append(
                           bahai_date(int(row[15]), int(row[16]), int(row[17]),
                                       int(row[18]), int(row[19])))
                       self.mlc.append(
                           mayan_long_count_date(int(row[20]), int(row[21]),
                                                   int(row[22]), int(row[23]),
                                                                int(row[24])))
                       self.mh.append(
                           mayan_haab_date(int(row[25]), int(row[26])))
                       self.mt.append(
                           mayan_tzolkin_date(int(row[27]), int(row[28])))
                       self.ax.append(
                           aztec_xihuitl_date(int(row[29]), int(row[30])))
                       self.at.append(
                           aztec_tonalpohualli_date(int(row[31]), int(row[32])))
          class AppendixCTable2TestCase(AppendixCTable2TestCaseBase,
                                            unittest.TestCase):
              \langle test\ ethiopic\ appendix\ c\ 167 \rangle
              \langle test \ islamic \ appendix \ c \ 169 \rangle
              \langle test \ bahai \ appendix \ c \ 171 \rangle
              \langle test \ mayan \ appendix \ c \ 173 \rangle
        This code is used in chunk 148.
```

Defines:

```
AppendixCTable2TestCase, never used.
           {\tt AppendixCTable2TestCaseBase, used in chunks 4, 73, 79, 85, 127, 166, 168, 170, and 172.}
         Uses aztec_tonalpohualli_date 83, aztec_xihuitl_date 83, bahai_date 125, ethiopic_date 71,
           islamic_date 77, mayan_haab_date 83, mayan_long_count_date 83, mayan_tzolkin_date 83, mt 100,
           and rd 37.
         \langle coptic \ and \ ethiopic \ calendars \ unit \ test \ 72 \rangle + \equiv
166
           {\tt class\ Ethiopic Appendix CTest Case (Appendix CTable 2 Test Case Base,}
                                                    unittest.TestCase):
                \langle test\ ethiopic\ appendix\ c\ 167 \rangle
         This code is used in chunks 4 and 73.
         Defines:
           EthiopicAppendixCTestCase, never used.
         Uses AppendixCTable2TestCaseBase 165.
167
         \langle test\ ethiopic\ appendix\ c\ 167 \rangle \equiv
           def testEthiopic(self):
                for i in range(len(self.rd)):
                     # ethiopic day
                     self.assertEqual(ethiopic_from_fixed(self.rd[i]), self.ed[i])
                     self.assertEqual(fixed_from_ethiopic(self.ed[i]), self.rd[i])
         This code is used in chunks 165 and 166.
         Defines:
           testEthiopic, never used.
         Uses ethiopic_from_fixed 71, fixed_from_ethiopic 71, and rd 37.
168
         \langle islamic\ calendar\ unit\ test\ 78 \rangle + \equiv
           class IslamicAppendixCTestCase(AppendixCTable2TestCaseBase,
                                                   unittest.TestCase):
                \langle test \ islamic \ appendix \ c \ 169 \rangle
         This code is used in chunks 4 and 79.
         Defines:
           IslamicAppendixCTestCase, never used.
         Uses AppendixCTable2TestCaseBase 165.
         \langle test \ islamic \ appendix \ c \ 169 \rangle \equiv
169
           def testIslamic(self):
                for i in range(len(self.rd)):
                     # islamic
                     self.assertEqual(islamic_from_fixed(self.rd[i]), self.id[i])
                     self.assertEqual(fixed_from_islamic(self.id[i]), self.rd[i])
                     # islamic (observational)
                     self.assertEqual(
                          fixed_from_observational_islamic(self.io[i]), self.rd[i])
                     self.assertEqual(
                          observational_islamic_from_fixed(self.rd[i]), self.io[i])
         This code is used in chunks 165 and 168.
         Defines:
           testIslamic, never used.
         Uses fixed_from_islamic 77, fixed_from_observational_islamic 142, islamic_from_fixed 77,
           observational_islamic_from_fixed 142, and rd 37.
170
         \langle bahai\ calendar\ unit\ test\ 126 \rangle + \equiv
           class BahaiAppendixCTestCase(AppendixCTable2TestCaseBase,
                                                 unittest.TestCase):
                \langle test \ bahai \ appendix \ c \ 171 \rangle
         This code is used in chunks 4 and 127.
           BahaiAppendixCTestCase, never used.
         Uses AppendixCTable2TestCaseBase 165.
```

```
171
        \langle test \ bahai \ appendix \ c \ 171 \rangle \equiv
          def testBahai(self):
               for i in range(len(self.rd)):
                    # bahai
                    self.assertEqual(bahai_from_fixed(self.rd[i]), self.bd[i])
                    self.assertEqual(fixed_from_bahai(self.bd[i]), self.rd[i])
                    # bahai future
                    self.assertEqual(future_bahai_from_fixed(self.rd[i]), self.bf[i])
                    self.assertEqual(fixed_from_future_bahai(self.bf[i]), self.rd[i])
        This code is used in chunks 165 and 170.
        Defines:
          testBahai, never used.
        Uses bahai_from_fixed 125, fixed_from_bahai 125, fixed_from_future_bahai 125,
          future_bahai_from_fixed 125, and rd 37.
172
        \langle mayan \ calendars \ unit \ test \ 84 \rangle + \equiv
          class MayanAppendixCTestCase(AppendixCTable2TestCaseBase,
                                             unittest.TestCase):
               \langle test \ may an \ appendix \ c \ 173 \rangle
        This code is used in chunks 4 and 85.
        Defines:
          MayanAppendixCTestCase, never used.
        Uses AppendixCTable2TestCaseBase 165.
173
        \langle test \ may an \ appendix \ c \ 173 \rangle \equiv
          def testMayan(self):
               for i in range(len(self.rd)):
                    # mayan (long count)
                    self.assertEqual(
                        mayan_long_count_from_fixed(self.rd[i]), self.mlc[i])
                    self.assertEqual(
                        fixed_from_mayan_long_count(self.mlc[i]), self.rd[i])
                    # mayan (haab)
                    self.assertEqual(mayan_haab_from_fixed(self.rd[i]), self.mh[i])
                    # mayan (tzolkin)
                    self.assertEqual(mayan_tzolkin_from_fixed(self.rd[i]), self.mt[i])
          def testAztec(self):
               for i in range(len(self.rd)):
                    # aztec xihuitl
                    self.assertEqual(aztec_xihuitl_from_fixed(self.rd[i]), self.ax[i])
                    # aztec tonalpohualli
                    self.assertEqual(
                        aztec_tonalpohualli_from_fixed(self.rd[i]), self.at[i])
        This code is used in chunks 165 and 172.
        Defines:
          testAztec, never used.
          testMayan, never used.
        Uses aztec_tonalpohualli_from_fixed 83, aztec_xihuitl_from_fixed 83, fixed_from_mayan_long_count
          83, mayan_haab_from_fixed 83, mayan_long_count_from_fixed 83, mayan_tzolkin_from_fixed 83,
          mt 100, and rd 37.
```

The third is for Hebrew (Standard and observational), Easter (Julian, Gregorian, Astronomical), Balinese Pawukon, Persian (Astronomical and arithmetic) and French Revolutionary (original and modified).

```
\langle appendixCTable3Tests 174 \rangle \equiv
174
         class AppendixCTable3TestCaseBase():
             def _toBoolean(self, c):
                 return False if c == 'f' else True
             def setUp(self):
                 reader = csv.reader(open("dates3.csv", "rU"),
                                      delimiter=',',
                                      quoting=csv.QUOTE_NONE)
                 self.rd
                             = []
                 self.hd
                             = [] # hebrew standard
                 self.ho
                            = [] # hebrew observational
                 self.je
                            = [] # julian easter
                 self.ge
                            = [] # gregorian easter
                 self.ae
                            = [] # astronomical easter
                 self.bd
                            = [] # balinese pawukon
                 self.pas = [] # persian astronomical
                 self.par = [] # persian arithmetic
                 self.fr
                             = [] # french original
                 self.frm = [] # french modified
                 for row in reader:
                      self.rd.append(int(row[0]))
                      self.hd.append(hebrew_date(int(row[1]), int(row[2]), int(row[3])))
                      self.ho.append(hebrew_date(int(row[4]), int(row[5]), int(row[6])))
                      self.je.append(julian_date(int(row[7]), int(row[8]), int(row[9])))
                      self.ge.append(gregorian_date(int(row[10]),
                                                     int(row[11]),
                                                     int(row[12])))
                      self.ae.append(gregorian_date(int(row[13]),
                                                     int(row[14]),
                                                     int(row[15])))
                      self.bd.append(balinese_date(self._toBoolean(row[16]),
                                                     int(row[17]),
                                                     int(row[18]),
                                                     int(row[19]),
                                                     int(row[20]),
                                                     int(row[21]),
                                                     int(row[22]),
                                                     int(row[23]),
                                                     int(row[24]),
                                                     int(row[25])))
                      self.pas.append(gregorian_date(int(row[26]),
                                                     int(row[27]),
                                                     int(row[28])))
                      self.par.append(gregorian_date(int(row[29]),
                                                     int(row[30]),
                                                     int(row[31])))
                      self.fr.append(french_date(int(row[32]),
                                                  int(row[33]),
                                                 int(row[34])))
                      self.frm.append(french_date(int(row[35]),
                                                   int(row[36]),
                                                   int(row[37])))
```

class AppendixCTable3TestCase(AppendixCTable3TestCaseBase,

```
unittest.TestCase):
                 \langle test\ hebrew\ appendix\ c\ 176 \rangle
                 \langle test \ easter \ appendix \ c \ 178 \rangle
                 \langle test \ balinese \ appendix \ c \ 180 \rangle
                 \langle test \ persian \ appendix \ c \ 182 \rangle
                 ⟨test french appendix c 184⟩
         This code is used in chunk 148.
         Defines:
            AppendixCTable3TestCase, never used.
            AppendixCTable3TestCaseBase, used in chunks 4, 76, 82, 91, 124, 132, 175, 177, 179, 181, and 183.
         Uses balinese_date 89, easter 74, french_date 128, gregorian_date 52, hebrew_date 80,
            julian_date 59, and rd 37.
175
         \langle hebrew\ calendar\ unit\ test\ 81 \rangle + \equiv
            class HebrewAppendixCTestCase(AppendixCTable3TestCaseBase,
                                                    unittest.TestCase):
                 \langle test\ hebrew\ appendix\ c\ 176 \rangle
         This code is used in chunks 4 and 82.
         Defines:
            {\tt HebrewAppendixCTestCase}, \ {\tt never} \ {\tt used}.
         Uses AppendixCTable3TestCaseBase 174.
176
         \langle test\ hebrew\ appendix\ c\ 176 \rangle \equiv
            def testHebrew(self):
                 for i in range(len(self.rd)):
                      self.assertEqual(fixed_from_hebrew(self.hd[i]), self.rd[i])
                      self.assertEqual(hebrew_from_fixed(self.rd[i]), self.hd[i])
                      # observational
                      self.assertEqual(
                           observational_hebrew_from_fixed(self.rd[i]), self.ho[i])
                      self.assertEqual(
                           fixed_from_observational_hebrew(self.ho[i]), self.rd[i])
         This code is used in chunks 174 and 175.
         Defines:
            testHebrew, never used.
         Uses fixed_from_hebrew 80, fixed_from_observational_hebrew 142, hebrew_from_fixed 80,
            observational_hebrew_from_fixed 142, and rd 37.
177
         \langle ecclesiastical\ calendars\ unit\ test\ 75 \rangle + \equiv
            class EasterAppendixCTestCase(AppendixCTable3TestCaseBase,
                                                    unittest.TestCase):
                 \langle test \ easter \ appendix \ c \ 178 \rangle
         This code is used in chunks 4 and 76.
         Defines:
            EasterAppendixCTestCase, never used.
         Uses AppendixCTable3TestCaseBase 174.
```

```
178
         \langle test \ easter \ appendix \ c \ 178 \rangle \equiv
           def testEaster(self):
                for i in range(len(self.rd)):
                     self.assertEqual(
                            gregorian_from_fixed(orthodox_easter(
                                   gregorian_year_from_fixed(self.rd[i]))),
                            self.je[i])
                     self.assertEqual(
                            gregorian_from_fixed(alt_orthodox_easter(
                                   gregorian_year_from_fixed(self.rd[i]))),
                            self.je[i])
                     self.assertEqual(
                            gregorian_from_fixed(easter(
                                   gregorian_year_from_fixed(self.rd[i]))),
                            self.ge[i])
                     self.assertEqual(
                            gregorian_from_fixed(astronomical_easter(
                                   gregorian_year_from_fixed(self.rd[i]))),
                            self.ae[i])
         This code is used in chunks 174 and 177.
         Defines:
           testEaster, never used.
         Uses alt_orthodox_easter 74, astronomical_easter 142, easter 74, gregorian_from_fixed 56,
           gregorian_year_from_fixed 55, orthodox_easter 74, and rd 37.
179
         \langle balinese\ calendar\ unit\ test\ 90 \rangle + \equiv
           class BalineseAppendixCTestCase(AppendixCTable3TestCaseBase):
                 \langle test \ balinese \ appendix \ c \ 180 \rangle
         This code is used in chunks 4 and 91.
         Defines:
           {\tt BalineseAppendixCTestCase}, \ {\tt never} \ {\tt used}.
         Uses AppendixCTable3TestCaseBase 174.
180
         \langle test \ balinese \ appendix \ c \ 180 \rangle \equiv
           def testBalinese(self):
                for i in range(len(self.rd)):
                     self.assertEqual(bali_pawukon_from_fixed(self.rd[i]), self.bd[i])
         This code is used in chunks 174 and 179.
         Defines:
           testBalinese, never used.
         Uses bali_pawukon_from_fixed 89 \ \mathrm{and} \ \mathrm{rd} \ 37.
181
         \langle persian\ calendar\ unit\ test\ 123 \rangle + \equiv
           {\tt class\ Persian Appendix CTest Case} ({\tt Appendix CTable 3Test Case Base},
                                                    unittest.TestCase):
                 \langle test \ persian \ appendix \ c \ 182 \rangle
         This code is used in chunks 4 and 124.
         Defines:
           PersianAppendixCTestCase, never used.
         Uses AppendixCTable3TestCaseBase 174.
```

```
182
        \langle test\ persian\ appendix\ c\ 182 \rangle \equiv
          def testPersian(self):
               for i in range(len(self.rd)):
                   # persian arithmetic
                   self.assertEqual(
                        fixed_from_arithmetic_persian(self.par[i]), self.rd[i])
                   self.assertEqual(
                        arithmetic_persian_from_fixed(self.rd[i]), self.par[i])
                   # persian astronomical
                   self.assertEqual(persian_from_fixed(self.rd[i]), self.pas[i])
                   self.assertEqual(fixed_from_persian(self.pas[i]), self.rd[i])
        This code is used in chunks 174 and 181.
        Defines:
          testPersian, never used.
        Uses arithmetic_persian_from_fixed 122, fixed_from_arithmetic_persian 122, fixed_from_persian
          122, persian_from_fixed 122, and rd 37.
183
        \langle french \ revolutionary \ calendar \ unit \ test \ 129 \rangle + \equiv
          class FrenchRevolutionaryAppendixCTestCase(AppendixCTable3TestCaseBase,
                                                            unittest.TestCase):
               ⟨test french appendix c 184⟩
        This code is used in chunks 4 and 132.
        Defines:
          FrenchRevolutionaryAppendixCTestCase, never used.
        Uses AppendixCTable3TestCaseBase 174.
184
        \langle test \ french \ appendix \ c \ 184 \rangle \equiv
          #def assertEqual(one, two, msg=""):
                print one, two
          def testFrenchRevolutionary(self):
               for i in range(len(self.rd)):
                   # french revolutionary original
                   self.assertEqual(fixed_from_french(self.fr[i]), self.rd[i])
                   self.assertEqual(french_from_fixed(self.rd[i]), self.fr[i])
                   # french revolutionary modified
                   self.assertEqual(fixed from arithmetic french(self.frm[i]), self.rd[i])
                   self.assertEqual(arithmetic_french_from_fixed(self.rd[i]), self.frm[i])
        This code is used in chunks 174 and 183.
        Defines:
          testFrenchRevolutionary, never used.
        Uses arithmetic_french_from_fixed 130, fixed_from_arithmetic_french 130, fixed_from_french 130,
          french_from_fixed 130, and rd 37.
```

```
The fourth is for Chinese ...
185
       \langle appendixCTable4Tests 185 \rangle \equiv
         class AppendixCTable4TestCaseBase():
             def _toBoolean(self, c):
                 return False if c == 'f' else True
             def setUp(self):
                 reader = csv.reader(open("dates4.csv", "rU"),
                                      delimiter=',',
                                      quoting=csv.QUOTE_NONE)
                            = []
                 self.rd
                 self.cd
                            = [] # chinese date
                          = [] # chinese day name
                 self.cn
                 self.ms = [] # major solar term
                 self.ohs = [] # old hindu solar date
                 self.mhs = [] # modern hindu solar date
                 self.ahs = [] # astronomical hindu solar date
                 self.ohl = [] # old hindu lunar date
                 self.mhl = [] # modern hindu lunar date
                 self.ahl = [] # astronomical hindu lunar date
                 self.td = [] # tibetan date
                 for row in reader:
                      self.rd.append(int(row[0]))
                     self.cd.append(chinese_date(int(row[1]), int(row[2]), int(row[3]),
                                                  self._toBoolean(row[4]), int(row[5])))
                     self.cn.append([int(row[6]), int(row[7])])
                     self.ms.append(float(row[8]))
                     self.ohs.append(hindu_solar_date(int(row[9]),
                                                       int(row[10]),
                                                       int(row[11])))
                     self.mhs.append(hindu_solar_date(int(row[12]),
                                                       int(row[13]),
                                                       int(row[14])))
                     self.ahs.append(hindu_solar_date(int(row[15]),
                                                       int(row[16]),
                                                       int(row[17])))
                     self.ohl.append(old_hindu_lunar_date(int(row[18]),
                                                       int(row[19]),
                                                       self._toBoolean(row[20]),
                                                       int(row[21])))
                     self.mhl.append(hindu_lunar_date(int(row[22]),
                                                       int(row[23]),
                                                       self._toBoolean(row[24]),
                                                       int(row[25]),
                                                       self._toBoolean(row[26])))
                      self.ahl.append(hindu_lunar_date(int(row[27]),
                                                       int(row[28]),
                                                       self._toBoolean(row[29]),
                                                       int(row[30]),
                                                       self._toBoolean(row[31])))
                     self.td.append(tibetan_date(int(row[32]),
                                                  int(row[33]),
                                                  self._toBoolean(row[34]),
                                                  int(row[35]),
                                                  self._toBoolean(row[36])))
```

class AppendixCTable4TestCase(AppendixCTable4TestCaseBase,

```
unittest.TestCase):
                \langle test\ chinese\ appendix\ c\ 187 \rangle
                \langle test \ old \ hindu \ appendix \ c \ 189 \rangle
                \langle test \ modern \ hindu \ appendix \ c \ 191 \rangle
                \langle test\ tibetan\ appendix\ c\ 193 \rangle
         This code is used in chunk 148.
         Defines:
           AppendixCTable4TestCase, never used.
           AppendixCTable4TestCaseBase, used in chunks 4, 88, 135, 138, 141, 186, 188, 190, and 192.
         Uses chinese_date 133, hindu_lunar_date 136, hindu_solar_date 86, old_hindu_lunar_date 86,
           rd 37, and tibetan_date 139.
186
         \langle \mathit{chinese\ calendar\ unit\ test\ 134} \rangle + \equiv
           class ChineseAppendixCTestCase(AppendixCTable4TestCaseBase,
                                                   unittest.TestCase):
                \langle test\ chinese\ appendix\ c\ 187 \rangle
         This code is used in chunks 4 and 135.
         Defines:
           ChineseAppendixCTestCase, never used.
         Uses AppendixCTable4TestCaseBase 185.
187
         \langle test\ chinese\ appendix\ c\ 187 \rangle \equiv
           def testChinese(self):
                for i in range(len(self.rd)):
                     self.assertEqual(fixed_from_chinese(self.cd[i]), self.rd[i])
                     self.assertEqual(chinese_from_fixed(self.rd[i]), self.cd[i])
                     self.assertEqual(chinese_day_name(self.rd[i]), self.cn[i])
                     self.assertAlmostEqual(
                          major_solar_term_on_or_after(self.rd[i]), self.ms[i], 6)
         This code is used in chunks 185 and 186.
         Defines:
           testChinese, never used.
         Uses chinese_day_name 133, chinese_from_fixed 133, fixed_from_chinese 133,
           major_solar_term_on_or_after 133, and rd 37.
188
         \langle old\ hindu\ calendars\ unit\ test\ 87 \rangle + \equiv
           class OldHinduAppendixCTestCase(AppendixCTable4TestCaseBase,
                                                    unittest.TestCase):
                \langle test \ old \ hindu \ appendix \ c \ 189 \rangle
         This code is used in chunks 4 and 88.
         Defines:
           OldHinduAppendixCTestCase, never used.
         Uses AppendixCTable4TestCaseBase 185.
189
         \langle test \ old \ hindu \ appendix \ c \ 189 \rangle \equiv
           def testOldHindu(self):
                for i in range(len(self.rd)):
                     # solar
                     self.assertEqual(fixed_from_old_hindu_solar(self.ohs[i]), self.rd[i])
                     self.assertEqual(old_hindu_solar_from_fixed(self.rd[i]), self.ohs[i])
                     # lunisolar
                     self.assertEqual(fixed_from_old_hindu_lunar(self.ohl[i]), self.rd[i])
                     self.assertEqual(old_hindu_lunar_from_fixed(self.rd[i]), self.ohl[i])
         This code is used in chunks 185 and 188.
         Defines:
           testOldHindu, never used.
         Uses fixed_from_old_hindu_lunar 86, fixed_from_old_hindu_solar 86, old_hindu_lunar_from_fixed
           86, old_hindu_solar_from_fixed 86, and rd 37.
```

```
\( \lambda modern \text{ hindu calendars unit test 137} \rightarrow \equiv \text{class ModernHinduAppendixCTestCase(AppendixCTable4TestCaseBase, unittest.TestCase): \( \lambda test modern \text{ hindu appendix c 191} \rightarrow \equiv \text{class of test modern hindu appendix c 191} \rightarrow \equiv \text{class of test modern hindu appendix c 191} \rightarrow \equiv \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern hindu appendix c 191} \rightarrow \text{class of test modern
```

```
191
        \langle test \ modern \ hindu \ appendix \ c \ 191 \rangle \equiv
          def testHinduSolarModernToFixed(self):
              for i in range(len(self.rd)):
                  # hindu solar
                        modern
                  self.assertEqual(fixed_from_hindu_solar(self.mhs[i]), self.rd[i])
          def testHinduSolarModernFromFixed(self):
              for i in range(len(self.rd)):
                  # hindu solar
                        modern
                  self.assertEqual(hindu_solar_from_fixed(self.rd[i]), self.mhs[i])
          def testHinduSolarAstronomicalToFixed(self):
              for i in range(len(self.rd)):
                  # astronomical
                  self.assertEqual(fixed_from_astro_hindu_solar(self.ahs[i]), self.rd[i])
          def testHinduSolarAstronomicalFromFixed(self):
              for i in range(len(self.rd)):
                        astronomical
                  self.assertEqual(astro_hindu_solar_from_fixed(self.rd[i]), self.ahs[i])
          def testHinduLunisolarModernToFixed(self):
              for i in range(len(self.rd)):
                  # hindu lunisolar
                        modern
                  self.assertEqual(fixed_from_hindu_lunar(self.mhl[i]), self.rd[i])
          def testHinduLunisolarModernFromFixed(self):
              for i in range(len(self.rd)):
                  # hindu lunisolar
                        modern
                  self.assertEqual(hindu_lunar_from_fixed(self.rd[i]), self.mhl[i])
          def testHinduLunisolarAstronomicalToFixed(self):
              for i in range(len(self.rd)):
                  # hindu lunisolar
                        astronomical
                  self.assertEqual(fixed_from_astro_hindu_lunar(self.ahl[i]), self.rd[i])
          def testHinduLunisolarAstronomicalFromFixed(self):
              for i in range(len(self.rd)):
                  # hindu lunisolar
                        {\tt astronomical}
                  self.assertEqual(astro_hindu_lunar_from_fixed(self.rd[i]), self.ahl[i])
       This code is used in chunks 185 and 190.
        Defines:
          {\tt testHinduLunisolarAstronomicalFromFixed}, \ {\tt never} \ {\tt used}.
          testHinduLunisolarAstronomicalToFixed, never used.
          testHinduLunisolarModernFromFixed, never used.
          testHinduLunisolarModernToFixed, never used.
          testHinduSolarAstronomicalFromFixed, never used.
          testHinduSolarAstronomicalToFixed, never used.
          testHinduSolarModernFromFixed, never used.
          testHinduSolarModernToFixed, never used.
        Uses astro_hindu_lunar_from_fixed 136, astro_hindu_solar_from_fixed 136,
          fixed_from_astro_hindu_lunar 136, fixed_from_astro_hindu_solar 136, fixed_from_hindu_lunar
          136, fixed_from_hindu_solar 136, hindu_lunar_from_fixed 136, hindu_solar_from_fixed 136,
          and rd 37.
```

```
192
         \langle tibetan\ calendar\ unit\ test\ 140 \rangle + \equiv
            {\tt class} \ \ {\tt TibetanAppendixCTestCase} ( {\tt AppendixCTable4TestCaseBase}, \ unittest. {\tt TestCase}): \\
                 \langle test\ tibetan\ appendix\ c\ 193 \rangle
         This code is used in chunks 4 and 141.
         Defines:
            {\tt TibetanAppendixCTestCase}, \ {\tt never} \ {\tt used}.
         Uses AppendixCTable4TestCaseBase 185.
193
         \langle test\ tibetan\ appendix\ c\ 193 \rangle \equiv
            def testTibetan(self):
                 for i in range(len(self.rd)):
                       self.assertEqual(fixed_from_tibetan(self.td[i]), self.rd[i])
                       self.assertEqual(tibetan_from_fixed(self.rd[i]), self.td[i])
         This code is used in chunks 185 and 192.
         Defines:
            testTibetan, never used.
         Uses fixed_from_tibetan 139, rd 37, and tibetan_from_fixed 139.
```

```
The fifth is for Astronomical calculations
        \langle \mathit{appendixCTable5Tests} \ \textcolor{red}{\textbf{194}} \rangle \equiv
194
          class AppendixCTable5TestCaseBase():
               def _toBoolean(self, c):
                    return False if c == 'f' else True
               def setUp(self):
                    reader = csv.reader(open("dates5.csv", "rU"),
                                           delimiter=',',
                                           quoting=csv.QUOTE_NONE)
                    self.rd
                                = []
                    self.sl
                                = [] # solar longitude
                    self.nse = [] # next solstice/equinox
                    self.ll
                                = [] # lunar longitude
                    self.nnm = [] # next new moon
                    self.dip = [] # dawn in Paris
                    self.sij = [] # sunset in Jerusalem
                    for row in reader:
                        self.rd.append(int(row[0]))
                        self.sl.append(float(row[1]))
                        self.nse.append(float(row[2]))
                        self.ll.append(float(row[3]))
                        #self.nnm.append(float(row[4])) # read from errata file
                        self.dip.append(row[5])
                        self.sij.append(row[9])
                    reader1 = csv.reader(open("dates5.errata.csv", "rU"),
                                           delimiter=',',
                                           quoting=csv.QUOTE_NONE)
                    for row in reader1:
                        self.nnm.append(float(row[1]))
          class AppendixCTable5TestCase(AppendixCTable5TestCaseBase,
                                               unittest.TestCase):
               \langle test \ astronomy \ appendix \ c \ 196 \rangle
        This code is used in chunk 148.
          AppendixCTable5TestCase, never used.
          AppendixCTable5TestCaseBase, used in chunks 4, 121, 144, and 195.
        Uses dawn 102, longitude 100, next 16, rd 37, and sunset 102.
195
        \langle time \ and \ astronomy \ unit \ test \ 104 \rangle + \equiv
          {\tt class\ AstronomyAppendixCTestCase(AppendixCTable5TestCaseBase,}
                                                  unittest.TestCase):
               \langle test \ astronomy \ appendix \ c \ 196 \rangle
        This code is used in chunks 4 and 121.
        Defines:
          AstronomyAppendixCTestCase, never used.
        Uses AppendixCTable5TestCaseBase 194.
```

```
196
       \langle test \ astronomy \ appendix \ c \ 196 \rangle \equiv
          def testSolarLongitude(self):
              for i in range(len(self.rd)):
                  \# +0.5 takes into account that the value has to be
                  # calculated at 12:00 UTC
                  self.assertAlmostEqual(solar_longitude(self.rd[i] + 0.5),
                                           self.sl[i],
          def testNextSolsticeEquinox(self):
              # I run some tests for Gregorian year 1995 about new Moon and
              # start of season against data from HM Observatory...and they
              # are ok
              for i in range(len(self.rd)):
                  t = [solar_longitude_after(SPRING, self.rd[i]),
                        solar_longitude_after(SUMMER, self.rd[i]),
                        solar_longitude_after(AUTUMN, self.rd[i]),
                        solar_longitude_after(WINTER, self.rd[i])]
                  self.assertAlmostEqual(min(t), self.nse[i], 6)
          def testLunarLongitude(self):
              for i in range(len(self.rd)):
                  self.assertAlmostEqual(lunar_longitude(self.rd[i]),
                                           self.ll[i],
                                           6)
          def testNextNewMoon(self):
              for i in range(len(self.rd)):
                  self.assertAlmostEqual(new_moon_at_or_after(self.rd[i]),
                                           self.nnm[i],
          def testDawnInParis(self):
              # as clarified by Prof. Reingold in CL it is:
                    (dawn day paris 18d0)
              \mbox{\tt\#} note that d0 stands for double float precision and in
              # the Python routines we use mpf with 52 digits for dawn()
              alpha = angle(18, 0, 0)
              for i in range(len(self.rd)):
                  if (self.dip[i] == BOGUS):
                       self.assertEqual(dawn(self.rd[i], PARIS, alpha), self.dip[i])
                  else:
                       self.assertAlmostEqual(
                                   mod(dawn(self.rd[i], PARIS, alpha), 1),
                                   mpf(self.dip[i]),
                                   6)
          def testSunsetInJerusalem(self):
              for i in range(len(self.rd)):
                  self.assertAlmostEqual(
                        mod(sunset(self.rd[i], JERUSALEM), 1),
                        float(self.sij[i]),
       This code is used in chunks 194 and 195.
       Defines:
          testDawnInParis, never used.
          {\tt testLunarLongitude}, \ {\rm never} \ {\rm used}.
          testNextNewMoon, never used.
          testNextSolsticeEquinox, never used.
          testSolarLongitude, never used.
          testSunsetInJerusalem, never used.
```

```
Uses angle 100, AUTUMN 109, BOGUS 13, dawn 102, JERUSALEM 100 142, lunar_longitude 119, mod 15, new_moon_at_or_after 119, PARIS 128, rd 37, solar_longitude 107, solar_longitude_after 109, SPRING 109, start 47, SUMMER 109, sunset 102, and WINTER 109.
```

2.23 Test Coverage

I want to understand what I am covering with my tests. This is have a quantitative evaluation of the amount of lines of code of my software I am traversing with my tests. This does not give me any confidence about the correctness of my code, but at least it says what is lacking a test.

I found a nice, simple tool written in Python, coverage [10]. I defined a new target in Makefile to produce an HTML report

```
\(\lambda Makefile: coverage target \frac{197}{\equiv } = \\ .PHONY : coverage \\
\text{coverage: pycalcaltests.py appendixCUnitTest.py testdata} \\
\text{coverage -e -x pycalcaltests.py # -e drop previous} \\
\text{coverage -b -i -d html pycalcal.py # HTML report for pycalcal.py}
```

This code is used in chunk 220.

2.24 Cross checking

The following scripts have been used to generate and check the initial set of function signatures for the project.

2.24.1 Generating all function signatures

The follwing command will generate all Python function signatures from Common LISP counterparts:

Root chunk (not used in this document).

and here is the one to get the ones from pycalcal.py:

```
\langle extractcalcalsignatures 199 \rangle \equiv cat pycalcal.py | grep '^def '
```

199

Root chunk (not used in this document).

The idea is to extract all functions defined in calendrica-3.0.cl using extractcc3signatures and compare them with the ones in pycalcal.py like:

```
prompt> cat calendrica-3.0.cl | extractcc3signatures | sort > allcc3
prompt> cat pycalcal.py | extractcalcalsignatures | sort > allcalcal
prompt> diff allcc3 allcalcal
```

There is also the need to check all constants, i.e. defconstant. TODO.

2.24.2 Checking the function signatures

This code is used in chunk 218.

Chapter 3

Tutorial

This chapter goes into some practical examples of using PyCalCal.

Using dates and times

```
Convert 30<sup>th</sup> Jan 1967 11:20:00 UT to RD
>>> d=gregorian_date(1967, JANUARY, 30)
>>> t=time_from_clock([11, 20, 00])
>>> r=fixed_from_gregorian(d) + t
718096.47222222225
    Print a RD in human readable format
>>> clock_from_moment(r)
[11, 20, 2.2351741790771484e-06]
>>> gregorian_from_fixed(fixed_from_moment(r))
[1967, 1, 30]
```

Chapter 4

Future evolutions

I would like to define an OO version of these calendrical algorithms. This can be implemented on top of existing functional implementation, i.e. GregorianCalendar will have relevant fields like, day, month and year and methods like isEaster() or so.

Validation of astonomical algorithm could be performed using data service for astronomical applications as made available by the US Naval Observatory web services [13] or the IMCCE [6].

I created a google app for PYCALCAL, accessible at http://calendrica.appspot.com.

Here is what I did to make it (sort of) work.

In a directory named 'calendrica' I did put calendrica.py and app.yaml. I also create a 'lib' directory where I copied the whole mpmath distribution. You can run in web app in your development environment using

```
dev_appserver.py calendrica/
and browsing it at
    http://localhost:8080/
Once ready you can deploy it using
```

appcfg.py update calendrica/

201

```
\langle calendrica.py 201 \rangle \equiv
 # \(\langle generated code warning 1 \rangle \)
 # This is a Google App that converts a date from/to a limited #
 # set (gregorian, hebrew, islamic) calendars using pycalcal
 # It assumes the app has a lib dir with the following pkgs:
      * pycalcal.py
      * mpmath package <a href="http://code.google.com/p/mpmath/">http://code.google.com/p/mpmath/>
        (the full 'mpmath' dir of the installation under
         .../Python25/Lib/site-packages/mpmath)
 # This file, calendrica.py, and its companion configuration
 # app.yaml are contained in a directory named calendrica.
 from google.appengine.ext import webapp
 from google.appengine.ext.webapp.util import run_wsgi_app
 import cgi
 # PyCalCal imports
 import os
 import sys
 sys.path.reverse()
 sys.path.append(os.path.abspath('./lib'))
```

```
sys.path.reverse()
import pycalcal as cal
class MainPage(webapp.RequestHandler):
 def get(self):
   self.response.out.write("""
     <html>
       <body>
         <div>This is a simple web app which allows to
         convert dates between calendars.<br />
         This is just the backbone using
         <a href="http://code.google.com/p/pycalcal">pycalcal</a>.<br />
         Try it out with input like <code>[2009, 10, 25]</code>
         for a Gregorian date.
         </div>
         <form action="/convert" method="get">
           <div><input type="text" name="date" /></div>
             <select name="fromCalendar">
               <option value="gregorian" selected="selected">
               Gregorian date (year, month, day) [int, int, int] </option>
               <option value="islamic">
               Islamic date (year, month, day) [int, int, int]
               <option value="observational_islamic">
               Observational Islamic date (year, month, day) [int, int, int]
               </option>
               <option value="hebrew">
               Hebrew date (year, month, day) [int, int, int]
               <option value="observational_hebrew">
               Observational Hebrew date (year, month, day) [int, int, int]
               </option>
               <option value="egyptian">
               Egyptian date (year, month, day) [int, int, int] </option>
               <option value="armenian">
               Armenian date (year, month, day) [int, int, int] </option>
               <option value="iso">
               ISO date (year, week, day) [int, int, int] </ option>
               <option value="coptic">
               Coptic date (year, month, day) [int, int, int]
               <option value="ethiopic">
               Ethiopic date (year, month, day) [int, int, int] </option>
               <option value="mayan_long_count">
               Mayan Long Count date (baktun, katun, tun, uinal, kin)
               [int, int, int, int]
               <option value="old_hindu_solar">
               Old Hindu solar date (year, month, day) [int, int, int]</option>
               <option value="hindu_solar">
               Hindu solar date (year, month, day) [int, int, int]
               <option value="astro_hindu_solar">
               Astro Hindu solar date (year, month, day) [int, int, int]
               </option>
               <option value="old_hindu_lunar">
               Old Hindu lunar date (year, month, leap, day)
               [int, int, bool, int]
               <option value="hindu_lunar">
               Hindu lunar date (year, month, leap_month, day, leap_day)
               [int, int, bool, int, bool]
               <option value="astro_hindu_lunar">
               Astro Hindu lunar date (year, month, leap_month, day, leap_day)
               [int, int, bool, int, bool]
```

```
<option value="tibetan">Tibetan date
   (year, month, leap_month, day, leap_day)
   [int, int, bool, int, bool]
   <option value="persian">
   Persian date (year, month, day) [int, int, int] </option>
   <option value="arithmetic_persian">
   Arithmetic Persian date (year, month, day)
   [int, int, int]
   <option value="bahai">
   Bahai date (major, cycle, year, month, day)
   [int, int, int, int]
   <option value="future_bahai">
   Future Bahai date (major, cycle, year, month, day)
   [int, int, int, int]
   <option value="french">
   French date (year, month, day) [int, int, int]</option>
   <option value="arithmetic_french">
   Arithmetic French date (year, month, day) [int, int, int]
   </option>
   <option value="chinese">
   Chinese date (cycle, year, month, leap_month, day)
   [int, int, int, bool, int]
   <option value="julian">
   Julian date (year, month, day) [int, int, int]
   <option value="roman">
   Roman date (year, month, event, count, leap)
   [int, int, int, bool]
   <option value="jd">Julian Day int</option>
   <option value="mjd">Modified Julian Day int</option>
   <option value="moment">Moment float</option>
 </select>
</div>
<div>
 <select name="toCalendar">
   <option value="gregorian">
   Gregorian date (year, month, day) [int, int, int] </option>
   <option value="islamic">
   Islamic date (year, month, day) [int, int, int]
   <option value="observational_islamic">
   Observational Islamic date (year, month, day)
   [int, int, int]
   <option value="hebrew">
   Hebrew date (year, month, day) [int, int, int]
   <option value="observational_hebrew">
   Observational Hebrew date (year, month, day)
   [int, int, int]
   <option value="egyptian">
   Egyptian date (year, month, day) [int, int, int] </option>
   <option value="armenian">
   Armenian date (year, month, day) [int, int, int] </option>
   <option value="iso" selected="selected">
   ISO date (year, week, day) [int, int, int] </option>
   <option value="coptic">
   Coptic date (year, month, day) [int, int, int]</option>
   <option value="ethiopic">
   Ethiopic date (year, month, day) [int, int, int] </option>
   <option value="mayan_long_count">
   Mayan Long Count date (baktun, katun, tun, uinal, kin)
   [int, int, int, int]
   <option value="old_hindu_solar">
   Old Hindu solar date (year, month, day)
```

```
<option value="hindu_solar">
               Hindu solar date (year, month, day) [int, int, int]
               <option value="astro_hindu_solar">
               Astro Hindu solar date (year, month, day)
               [int, int, int]
               <option value="old_hindu_lunar">
               Old Hindu lunar date (year, month, leap, day)
               [int, int, bool, int]
               <option value="hindu_lunar">
               Hindu lunar date (year, month, leap_month, day, leap_day)
               [int, int, bool, int, bool]
               <option value="astro_hindu_lunar">
               Astro Hindu lunar date (year, month, leap_month, day, leap_day)
               [int, int, bool, int, bool]
               <option value="tibetan">
               Tibetan date (year, month, leap_month, day, leap_day)
               [int, int, bool, int, bool]
               <option value="persian">
               Persian date (year, month, day) [int, int, int] </option>
               <option value="arithmetic_persian">
               Arithmetic Persian date (year, month, day)
               [int, int, int]
               <option value="bahai">
               Bahai date (major, cycle, year, month, day)
               [int, int, int, int]
               <option value="future_bahai">
               Future Bahai date (major, cycle, year, month, day)
               [int, int, int, int]
               <option value="french">
               French date (year, month, day) [int, int, int] </ option>
               <option value="arithmetic_french">
               Arithmetic French date (year, month, day)
               [int, int, int]
               <option value="chinese">
               Chinese date (cycle, year, month, leap_month, day)
               [int, int, int, bool, int]
               <option value="julian">
               Julian date (year, month, day) [int, int, int]
               <option value="roman">
               Roman date (year, month, event, count, leap)
               [int, int, int, bool]
               <option value="jd">Julian Day int</option>
               <option value="mjd">Modified Julian Day int</option>
               <option value="moment">Moment float</option>
             </select>
           </div>
           <div><input type="submit" value="Convert"></div>
         </form>
       </body>
     </html>""")
class Converter(webapp.RequestHandler):
 def get(self):
   values = dict((k, cgi.escape(self.request.get(k))) for k in (
       'fromCalendar',
       'toCalendar',
       'date'))
   fixed_from_FROM_name = 'fixed_from_' + values['fromCalendar']
```

[int, int, int]

```
TO_from_fixed_name
                                                                                             = values['toCalendar'] + '_from_fixed'
               from_method = cal.__dict__[fixed_from_FROM_name]
               to_method = cal.__dict__[TO_from_fixed_name]
               date = eval(values['date'])
               result = to_method(from_method(date))
               self.response.out.write('<html><body>You converted ' +
                                                                                                              values['fromCalendar'] +
                                                                                                                 , date , +
                                                                                                               values['date'] +
                                                                                                                 , to , +
                                                                                                               values['toCalendar'] +
                                                                                                                 ' date ' +
                                                                                                               repr(result)
               self.response.out.write('<br />
               <a href="/">Try again!</a></body></html>')
application = webapp.WSGIApplication(
                                                                                                                                                     [('/', MainPage),
                                                                                                                                                        ('/convert', Converter)],
                                                                                                                                                   debug=True)
# the code to randomly generate from/to functions could come handy some day
# class OldMainPage(webapp.RequestHandler):
                        def get(self):
#
                                        self.response.headers['Content-Type'] = 'text/plain'
#
                                        self.response.out.write(self.doUsefulComputation())
#
                        def doUsefulComputation(self):
                                        """Convert from a Gregorian date to a random calendar from the ones % \left( 1\right) =\left( 1\right) \left( 1\right) +\left( 1\right) \left( 1\right) \left( 1\right) +\left( 1\right) \left( 1
#
                                       available in pycalcal"""
#
                                       b = cal.fixed_from_gregorian(cal.gregorian_date(1967, 1, 30))
                                       ############################
                                       # pick a random calendar
#
                                       ##########################
#
                                      from random import choice
#
                                      import re
#
                                      # here is the 'xyz_from_fixed' string
#
                                      f = choice(self.fromFixed())
#
                                       # invoke the conversion to destination calendar
#
                                      d = cal.__dict__[f](b)
#
                                      # get the calendar name: 'xyz'
                                       r = re.compile('(.+)(_from_fixed)')
                                      n = r.match(f).group(1)
#
                                      res = 'gergorian=1967, 1, 30; %s=%s' % (n, d)
#
                                       return res
                        def fromFixed(self):
#
#
                                      import re
#
                                       m2 = re.compile('.+_from_fixed$')
                                       m3 = re.compile('.+(year|week|day|year_bearer)_from_fixed$')
```

```
l_fromFixed = []
          #
                     for i in dir(cal):
          #
                          if re.match(m2, i) and not re.match(m3, i):
          #
                              1_fromFixed.append(i)
          #
                     return l_fromFixed
          #
                 def toFixed(self):
          #
                     import re
          #
                     m1 = re.compile('^fixed_from_')
          #
                     1_toFixed = []
                     for i in dir(cal):
          #
          #
                          if re.match(m1, i):
          #
                              l_toFixed.append(i)
                     return l_toFixed
          def main():
              run_wsgi_app(application)
          if __name__ == "__main__":
              main()
        Root chunk (not used in this document).
        Uses fixed_from_gregorian 55\ \mathrm{and}\ \mathrm{gregorian\_date}\ 52.
        This is the config file
202
        \langle app.yaml \ 202 \rangle \equiv
          application: calendrica
          version: 1
          runtime: python
          api_version: 1
          handlers:
          - url: /.*
            script: calendrica.py
        Root chunk (not used in this document).
```

Chapter 5

Technicalities

Root chunk (not used in this document).

Uses next 16.

By definition of *Calendrical Calculations*'s authors, the only authoritative document is their Common LISP code. For this reason I want to keep track of the relevant Common LISP code when defining my Python counterpart and the following sections explain how I make sure I implement all the algorithms and how I pair Common LISP code and Python code..

5.1 Inserting snippets of Common LISP code

I would like to be able to prepend the relevant snippet of (PYTHON-commented) COMMON LISP code from calendrica-3.0.cl to the relevant PYTHON counterpart.

I created a sort of pre-processor for NOWEB: it allows to write a code chunck reference like # see lines x-y in file and to obtain the insertion of a portion of a file. Its semantic is: "Insert the content of file 'file' from line 'x' to line 'y'".

The preprocessor is called premarkup and is defined as follows:

```
⟨premarkup 203⟩≡
203
          #! /bin/awk -f
          # \langle generated \ code \ warning \ 1 \rangle
          #-*- mode: awk -*-
          # substitute chunks of the form 'see lines <x>-<y> in <file>'
          # with the contents of file 'file' from line 'x' to line 'y' inclusive
          # eventually prefixed
          /# see lines [0-9][0-9]*-[0-9][0-9]* in .*$/ {
                  # extract x and y
                  # (file -> substr($1,3))
                  split($4, a, "-")
                  # the command 'excerpt 10 20 file'
                  # prints the contents of file 'file' from line 10 till 20
                  system("excerpt " a[1] " " a[2] " " $6 " | prefix")
                  # move to next line
                  next}
          # match and print all the rest
```

Note that it uses other two scripts, prefix and excerpt, to insert and comment out the relevant snippet of code.

```
204
        \langle prefix 204 \rangle \equiv
          #!/bin/sh
          # \(\langle generated code warning \mathbf{1}\rangle\)
          # -*- mode: shell -*-
          scriptname=$0
          function usage () {
               cat «EOF
          Usage: ${scriptname} [-p prefix] [prepend]
                            define new prefix string (default is '# ')
              -p prefix
                            displays basic help
          Prepend <prefix> to each line.
          EOF
               exit 0
          }
          pref='#'
          while getopts hp: name
               case $name in
               p)
                      pref="$OPTARG";;
               h)
                      usage;;
               esac
           done
          shift $(($OPTIND - 1))
          if (( $# > 1 ))
          then
               return 1
          blanks="$*"
           sed -e "s,[^.],${blanks}${pref}&,"
        Root chunk (not used in this document).
        And here are the targets for Makefile:
205
        \langle Makefile: premarkup 205 \rangle \equiv
          premarkup: prefix excerpt
                    notangle -Rpremarkup $(NW_MAIN) $(CPIF) premarkup
                    -chmod ug+x premarkup
        This code is used in chunk 242.
        \langle Makefile: prefix 206 \rangle \equiv
206
          prefix:
                    notangle -Rprefix $(NW_MAIN) $(CPIF) prefix
                    -chmod ug+x prefix
```

This code is used in chunk 242.

```
Excerpt, a simple invokation of sed:
        \langle excerpt \ 207 \rangle \equiv
207
           #!/bin/sh
           # \langle generated \ code \ warning \ 1 \rangle
           # excerpt b e f
           # print contents of file 'f' from line 'b' till 'e'
           sed -n $1,$2p $3
           #$ this is to fake emacs in nw source
        Root chunk (not used in this document).
            An example of use of premarkup is as follows:
        prompt> premarkup pycalcal.nw | noweave -n -delay - | cpif pycalcal.tex
            The target for Makefile is
        \langle Makefile: excerpt \ 208 \rangle \equiv
208
           excerpt:
                    notangle -Rexcerpt $(NW_MAIN) $(CPIF) excerpt
                    -chmod ug+x excerpt
```

This code is used in chunk 242.

5.2 How to avoid Noweb from indexing comments: HACK?

The problem with NOWEB indexing is that comments are parsed as well and I do not like to get index entries in Common LISP code. One possible hack is to create indexing info from a copy of the LATEX doc where Common LISP code is blanked out. So blankecerpt will try to accomplish this:

Root chunk (not used in this document).

```
Still I am not sure how to use this...but we probably need something like:
        \langle blankpremarkup \ 210 \rangle \equiv
210
          #! /bin/awk -f
          # substitute chunks of the form '# see lines <x>-<y> in <file>'
          # with the contents of file 'file' from line 'x' to line 'y' inclusive
          # eventually prefixed
          /# see lines [0-9][0-9]*-[0-9][0-9]* in .*$/ {
                   # extract x and y
                   # (file -> substr($1,3))
                   split($4, a, "-")
                   # the command 'blankexcerpt 10 20 file'
                   # prints the contents of file 'file' from line 10 till 20
                   system("blankexcerpt " a[1] " " a[2] " " $6 " | prefix")
                   # move to next line
                   next}
          #$ this is to fake emacs in nw source
          # match and print all the rest
        Root chunk (not used in this document).
        Uses next 16.
           The relevant Makefile targets are:
211
        \langle Makefile: blankpremarkup 211 \rangle \equiv
          blankpremarkup: prefix blankexcerpt
                   notangle -Rblankpremarkup $(NW_MAIN) $(CPIF) blankpremarkup
                   -chmod ug+x blankpremarkup
        This code is used in chunk 242.
212
        \langle Makefile: blankexcerpt 212 \rangle \equiv
          blankexcerpt:
                   notangle -Rblankexcerpt $(NW_MAIN) $(CPIF) blankexcerpt
                   -chmod ug+x blankexcerpt
        This code is used in chunk 242.
```

5.3 Make It Work

The Makefile I defined is minimalistically simple.

```
213 \langle Makefile\ 213 \rangle \equiv
# \langle generated\ code\ warning\ 1 \rangle
\langle Makefile:\ heading\ comment\ 214 \rangle
VERSION = \langle project\ version\ 10 \rangle
\langle Makefile:\ files\ declarations\ 215 \rangle
\langle Makefile:\ commands\ 216 \rangle
\langle Makefile:\ suffixes\ 217 \rangle
\langle Makefile:\ targets\ 218 \rangle
```

Root chunk (not used in this document).

```
\langle Makefile: heading comment 214 \rangle \equiv
214
        # Author: Enrico Spinielli
        # Makefile for my noweb project on calendrical calculations in Python.
        # Got hints from Makefile in Noweb distibution
        This code is used in chunk 213.
215
      \langle Makefile: files \ declarations \ 215 \rangle \equiv
        NW_MAIN=pycalcal.nw
        NW_SRC=
        TOOLS=prefix excerpt premarkup blankexcerpt blankpremarkup sconstruct
        PYTHON_SITE_PACKAGES=/Library/Python/2.6/site-packages
        UNIT_TEST_FILES=basicCodeUnitTest.py \
                       egyptianAndArmenianCalendarsUnitTest.py \
                       gregorianCalendarUnitTest.py \
                       isoCalendarUnitTest.py \
                       julianCalendarUnitTest.py \
                       copticAndEthiopicCalendarsUnitTest.py \
                       ecclesiasticalCalendarsUnitTest.py \
                       islamicCalendarUnitTest.py \
                       hebrewCalendarUnitTest.py \
                       mayanCalendarsUnitTest.py \
                       oldHinduCalendarsUnitTest.py \
                       balineseCalendarUnitTest.py \
                       timeAndAstronomyUnitTest.py \
                       persianCalendarUnitTest.py \
                       bahaiCalendarUnitTest.py \
                       frenchRevolutionaryCalendarUnitTest.py \
                       chineseCalendarUnitTest.py \
                       modernHinduCalendarsUnitTest.py \
                       tibetanCalendarUnitTest.py \
                       astronomicalLunarCalendarsUnitTest.py
```

This code is used in chunk 213.

```
216
        \langle \mathit{Makefile: commands 216} \rangle \equiv
          # We can use:
          # PREMARKUP=./premarkup $(NW_MAIN)
          # PREMARKUP=./blankpremarkup $(NW_MAIN)
          PREMARKUP=cat $(NW_MAIN)
          NOTANGLE_PURE=cat $(NW_MAIN) | notangle
          NOTANGLE=$(PREMARKUP) | notangle
          NOWEAVE=$(PREMARKUP) | noweave -n -delay NODEFS=$(PREMARKUP) | nodefs
          #LATEX=pdflatex -include-directory=$$(cygpath -w /usr/local/noweb/texmf)
          LATEX=latex
          PDFLATEX=pdflatex
          BIBTEX=bibtex
          EPSTOPSF=epstopdf
          # to be used only when there are multiple .nw files
          NOINDEX=noindex
          # change to ">" to ensure all sources are always made
          CPIF=| cpif
          NW_ALL=$(NW_MAIN) $(NW_SRC)
```

This code is used in chunk 213.

```
\langle \mathit{Makefile: suffixes 217} \rangle \equiv
217
          .SUFFIXES:
          .SUFFIXES: .nw .tex .py .dvi .defs .html .pdf .mp .asy .mps .gv .png .cl
          .nw.py:
                  $(NOTANGLE) -filter btdefn -R$*.py - $(CPIF) $*.py
          .nw.cl:
                  $(NOTANGLE) -filter btdefn -R$*.cl - $(CPIF) $*.cl
          .nw.html:
                  $(NOWEAVE) -filter 12h -filter btdefn -index -html $*.nw $(CPIF) $*.html
          .nw.defs:
                  $(NODEFS) - $(CPIF) $*.defs
          .nw.tex:
                  $(NOWEAVE) -filter btdefn -index - $(CPIF) $*.tex
          .tex.dvi:
                  $(LATEX) $*; \
                  $(NOINDEX) $*;\
                  if grep -s 'There were undefined references' $*.log;\
                  then $(BIBTEX) $*; fi;\
                  while grep -s 'Rerun to get cross-references right' $*.log;\
                  do $(LATEX) $*;\
                  done; \
          .tex.pdf:
                  $(PDFLATEX) $*; \
                  $(NOINDEX) $*; \
                  if grep -s 'There were undefined references' $*.log;\
                  then $(BIBTEX) $*; fi;
                  while grep -s 'Rerun to get cross-references right' *.\log;\
                  do $(PDFLATEX) $*;\
                  done; \
          .mp.mps:
                  mpost -tex=pdflatex $*.mp
          .mp.pdf:
                  mptopdf -latex $*.mp
          .asy.pdf:
                  asy -epsdriver=ps2write $*.asy
                  $(EPSTOPDF) $*.eps -hires -o=$*.pdf
          .nw.gv:
                  $(NOTANGLE) -filter btdefn -R$*.gv - $(CPIF) $*.gv
          .gv.png:
                  dot -Tpng $*.gv > $*.png
```

This code is used in chunk 213.

```
\langle \mathit{Makefile: targets 218} \rangle \equiv
218
         # %.chk (this is a check for latex)
         # Do not delete the following targets:
         .PRECIOUS: %.aux %.bbl
         .PHONY : all
         all: tools code tests doc
         .PHONY : tools
         tools:
                if [[ ! -x "prefix" ]]; \
                then \
                        $(MAKE) $(TOOLS); \
                fi;
         .PHONY : code
         code: pycalcal.py pycalcaltests.py
         .PHONY : tests
         tests: testSunset.cl
                $(MAKE) testdata
                $(MAKE) $(UNIT_TEST_FILES)
         .PHONY : doc
         doc:
                -$(MAKE) figures
                -$(MAKE) index
                $(MAKE) pycalcal.pdf
         .PHONY : index
         index: pycalcal.defs
         pycalcal.defs: $(NW_MAIN) premarkup
                $(NODEFS) - $(CPIF) $*.defs
         #all.defs: pycalcal.defs
                cat pycalcal.defs ${CPIF} all.defs
                sort -u $(NW_ALL:.nw=.defs) $(CPIF) all.defs
         .PHONY : figures
         figures: fig_ra-dec.pdf fig_ecliptic.pdf fig_alt-az.pdf
         ⟨Makefile: distro 219⟩
         (Makefile: unit tests and targets 220)
         ⟨Makefile: cross checks 200⟩
         (Makefile: tools 242)
         \langle Makefile: clean 243 \rangle
         .PHONY : webapp
         webapp: calendrica.py
                -mkdir -p calendrica/lib
                -cp pycalcal.py calendrica/lib
                -cp -fR $(PYTHON_SITE_PACKAGES)/mpmath calendrica/lib
```

```
calendrica.py: $(NW_MAIN:.nw=.py)
                 -mkdir calendrica
                 $(NOTANGLE) -filter btdefn -R$*.py - $(CPIF) calendrica/calendrica.py
                 $(NOTANGLE) -filter btdefn -Rapp.yaml - $(CPIF) calendrica/app.yaml
       This code is used in chunk 213.
       \langle Makefile: distro 219 \rangle \equiv
219
         ####################################
         DISTRO_FILES=$(NW_MAIN) $(NW_MAIN:.nw=.py) $(NW_MAIN:.nw=.pdf) \
                         README INSTALL STATUS COPYRIGHT_DERSHOWITZ_REINGOLD \
                         makemake.sh \
                         Makefile \
                         calendrica-3.0.cl \
                          calendrica-3.0.errata.cl \
                          $(NW_MAIN:.nw=.tex) \
                          $(NW_MAIN:.nw=.bib) \
                          figure.mp \
                          astro.mp \
                         alt-az.asy \
                         testSunset.cl
         .PHONY : distro
         distro: all
                 tar -czf pycalcal_$$(date +"%Y%m%d%H%M").tar.gz $(DISTRO_FILES)
```

This code is used in chunk 218.

```
Unit test and target
        \langle Makefile: unit tests and targets 220 \rangle \equiv
220
          pycalcaltests.py:
                   $(NOTANGLE) -filter btdefn -R$*.py - $(CPIF) $*.py
          testSunset.cl:
                   $(NOTANGLE) -filter btdefn -R$*.cl - $(CPIF) $*.cl
          .PHONY : check
          check: code tests
                  python pycalcaltests.py 2>&1 | tee testResult.txt
          .PHONY : check1by1
          check1by1: code tests
                  for t in $$(cat Makefile | grep -e '^[^
                                                                       ]*UnitTest.py:' | \
                           cut -f1 -d':' | grep -v appendix); \
                   do \
                           $(MAKE) $$t; \
                   done
          # create all unit test files
          .PHONY : 11t.
          ut:
                   $(MAKE) $$(cat pycalcal.nw | grep -e '^«.*UnitTest.py»=' | \
                            grep -v appendix | sed -e 's/\ll//g' -e 's/\gg=//g')
                   $(MAKE) $(UNIT_TEST_FILES)
          (Makefile: basics unit tests and target 221)
          (Makefile: egyptian and armenian unit tests and target 222)
          (Makefile: gregorian unit tests and target 223)
          (Makefile: iso unit tests and target 224)
          (Makefile: julian unit tests and target 225)
          (Makefile: coptic and ethiopic unit tests and target 226)
          (Makefile: ecclesiastical unit tests and target 227)
          (Makefile: islamic unit tests and target 228)
          (Makefile: hebrew unit tests and target 229)
          (Makefile: mayan unit tests and target 230)
          (Makefile: old hindu unit tests and target 231)
          (Makefile: balinese unit tests and target 232)
          (Makefile: time and astronomy unit tests and target 233)
          (Makefile: persian unit tests and target 234)
          (Makefile: bahai unit tests and target 235)
          (Makefile: french unit tests and target 236)
          ⟨Makefile: chinese unit tests and target 237⟩
          (Makefile: modern hindu unit tests and target 238)
          (Makefile: tibetan unit tests and target 239)
          (Makefile: astronomical lunar unit tests and target 240)
          ⟨Makefile: appendix c unit tests and target 241⟩
          ⟨Makefile: coverage target 197⟩
          trasformLatexDates2Cvs:
                   notangle -RtrasformLatexDates2Cvs $(NW_MAIN) $(CPIF) trasformLatexDates2Cvs
                   -chmod ug+x trasformLatexDates2Cvs
```

This code is used in chunk 218.

```
221
        \langle Makefile: basics unit tests and target 221 \rangle \equiv
           basicCodeUnitTest.py: appendixCUnitTest.py
                    $(NOTANGLE) -filter btdefn -R$*.py - > $*.py
           .PHONY : basicCodeUnitTest
           basicCodeUnitTest: basicCodeUnitTest.py
                    python $0.py 2>&1 | tee $0_result.txt
        This code is used in chunk 220.
222
        \langle Makefile: egyptian \ and \ armenian \ unit \ tests \ and \ target \ 222 \rangle \equiv
           egyptianAndArmenianCalendarsUnitTest.py: appendixCUnitTest.py
                    $(NOTANGLE) -filter btdefn -R$*.py - > $*.py
           . \verb|PHONY| : egyptianAndArmenianCalendarsUnitTest|
           \verb| egyptianAndArmenianCalendarsUnitTest: egyptianAndArmenianCalendarsUnitTest.py| \\
                    python $0.py 2>&1 | tee $0_result.txt
        This code is used in chunk 220.
223
        \langle Makefile: gregorian unit tests and target 223 \rangle \equiv
           gregorianCalendarUnitTest.py: appendixCUnitTest.py
                    $(NOTANGLE) -filter btdefn -R$*.py - > $*.py
           .PHONY : gregorianCalendarUnitTest
           gregorianCalendarUnitTest: gregorianCalendarUnitTest.py
                    python $0.py 2>&1 | tee $0_result.txt
        This code is used in chunk 220.
224
        \langle Makefile: iso unit tests and target 224 \rangle \equiv
           isoCalendarUnitTest.py: appendixCUnitTest.py
                    $(NOTANGLE) -filter btdefn -R$*.py - > $*.py
           .PHONY : isoCalendarUnitTest
           isoCalendarUnitTest: isoCalendarUnitTest.py
                    python $0.py 2>&1 | tee $0_result.txt
        This code is used in chunk 220.
225
        \langle Makefile: julian unit tests and target 225 \rangle \equiv
           julianCalendarUnitTest.py: appendixCUnitTest.py
                    $(NOTANGLE) -filter btdefn -R$*.py - > $*.py
           .PHONY : julianCalendarUnitTest
           julianCalendarUnitTest: julianCalendarUnitTest.py
                    python $0.py 2>&1 | tee $0_result.txt
        This code is used in chunk 220.
226
        \langle Makefile: coptic \ and \ ethiopic \ unit \ tests \ and \ target \ 226 \rangle \equiv
           copticAndEthiopicCalendarsUnitTest.py: appendixCUnitTest.py
                    $(NOTANGLE) -filter btdefn -R$*.py - > $*.py
           .PHONY : copticAndEthiopicCalendarsUnitTest
           \verb|copticAndEthiopicCalendarsUnitTest: copticAndEthiopicCalendarsUnitTest.py| \\
                    python $0.py 2>&1 | tee $0_result.txt
```

This code is used in chunk 220.

```
227
        \langle Makefile: ecclesiastical unit tests and target 227 \rangle \equiv
           ecclesiasticalCalendarsUnitTest.py: appendixCUnitTest.py
                    $(NOTANGLE) -filter btdefn -R$*.py - > $*.py
           .PHONY : ecclesiasticalCalendarsUnitTest
           \verb|ecclesiasticalCalendarsUnitTest: ecclesiasticalCalendarsUnitTest.py|\\
                    python $0.py 2>&1 | tee $0_result.txt
        This code is used in chunk 220.
        \langle Makefile: islamic unit tests and target 228 \rangle \equiv
228
           \verb|islam| icCalendar UnitTest.py: appendix CUnitTest.py|
                    NOTANGLE -filter btdefn -R$*.py - > $*.py
           .PHONY : islamicCalendarUnitTest
           islamicCalendarUnitTest: islamicCalendarUnitTest.py
                    python $0.py 2>&1 | tee $0_result.txt
        This code is used in chunk 220.
229
        \langle Makefile: hebrew unit tests and target 229 \rangle \equiv
          hebrewCalendarUnitTest.py: appendixCUnitTest.py
                    $(NOTANGLE) -filter btdefn -R$*.py - > $*.py
           .PHONY : hebrewCalendarUnitTest
           hebrewCalendarUnitTest: hebrewCalendarUnitTest.py
                    python $0.py 2>&1 | tee $0_result.txt
        This code is used in chunk 220.
        \langle \mathit{Makefile: mayan unit tests and target 230} \rangle \equiv
230
          mayanCalendarsUnitTest.py: appendixCUnitTest.py
                    $(NOTANGLE) -filter btdefn -R$*.py - > $*.py
           .PHONY : mayanCalendarsUnitTest
           mayanCalendarsUnitTest: mayanCalendarsUnitTest.py
                    python $0.py 2>&1 | tee $0_result.txt
        This code is used in chunk 220.
231
        \langle Makefile: old hindu unit tests and target 231 \rangle \equiv
           oldHinduCalendarsUnitTest.py: appendixCUnitTest.py
                    $(NOTANGLE) -filter btdefn -R$*.py - > $*.py
           .PHONY : oldHinduCalendarsUnitTest
           \verb|oldHinduCalendarsUnitTest|: oldHinduCalendarsUnitTest.py|
                    python $0.py 2>&1 | tee $0_result.txt
        This code is used in chunk 220.
232
        \langle Makefile: balinese unit tests and target 232 \rangle \equiv
           balineseCalendarUnitTest.py: appendixCUnitTest.py
                    (NOTANGLE) -filter btdefn -R**.py - > **.py
           .PHONY : balineseCalendarUnitTest
           balineseCalendarUnitTest: balineseCalendarUnitTest.py
                    python $0.py 2>&1 | tee $0_result.txt
```

This code is used in chunk 220.

```
233
        \langle Makefile: time \ and \ astronomy \ unit \ tests \ and \ target \ 233 \rangle \equiv
           timeAndAstronomyUnitTest.py: appendixCUnitTest.py
                    $(NOTANGLE) -filter btdefn -R$*.py - > $*.py
           . \verb"PHONY": timeAndAstronomyUnitTest"
           \verb|timeAndAstronomyUnitTest: timeAndAstronomyUnitTest.py|\\
                   python $0.py 2>&1 | tee $0_result.txt
        This code is used in chunk 220.
234
        \langle Makefile: persian unit tests and target 234 \rangle \equiv
           persianCalendarUnitTest.py: appendixCUnitTest.py
                    $(NOTANGLE) -filter btdefn -R$*.py - > $*.py
           .PHONY : persianCalendarUnitTest
           persianCalendarUnitTest: persianCalendarUnitTest.py
                    python $0.py 2>&1 | tee $0_result.txt
        This code is used in chunk 220.
        \langle Makefile: bahai unit tests and target 235 \rangle \equiv
235
           bahaiCalendarUnitTest.py: appendixCUnitTest.py
                    $(NOTANGLE) -filter btdefn -R$*.py - > $*.py
           .PHONY : bahaiCalendarUnitTest
           bahaiCalendarUnitTest: bahaiCalendarUnitTest.py
                    python $0.py 2>&1 | tee $0_result.txt
        This code is used in chunk 220.
        \langle Makefile: french unit tests and target 236 \rangle \equiv
236
           frenchRevolutionaryCalendarUnitTest.py: appendixCUnitTest.py
                    $(NOTANGLE) -filter btdefn -R$*.py - > $*.py
           .PHONY : frenchRevolutionaryCalendarUnitTest
           french Revolution ary Calendar Unit Test: french Revolution ary Calendar Unit Test.py \\
                    python $0.py 2>&1 | tee $0_result.txt
        This code is used in chunk 220.
        \langle Makefile: chinese unit tests and target 237 \rangle \equiv
237
           chineseCalendarUnitTest.py: appendixCUnitTest.py
                    $(NOTANGLE) -filter btdefn -R$*.py - > $*.py
           .PHONY : chineseCalendarUnitTest
           chineseCalendarUnitTest: chineseCalendarUnitTest.py
                    python $0.py 2>&1 | tee $0_result.txt
        This code is used in chunk 220.
238
        \langle Makefile: modern \ hindu \ unit \ tests \ and \ target \ 238 \rangle \equiv
           modernHinduCalendarsUnitTest.py: appendixCUnitTest.py
                    $(NOTANGLE) -filter btdefn -R$*.py - > $*.py
           .PHONY : modernHinduCalendarsUnitTest
           modernHinduCalendarsUnitTest: modernHinduCalendarsUnitTest.py
                    python $0.py 2>&1 | tee $0_result.txt
```

This code is used in chunk 220.

```
239
        \langle Makefile: tibetan unit tests and target 239 \rangle \equiv
          tibetanCalendarUnitTest.py: appendixCUnitTest.py
                    $(NOTANGLE) -filter btdefn -R$*.py - > $*.py
           .PHONY : tibetanCalendarUnitTest
          tibetanCalendarUnitTest: tibetanCalendarUnitTest.py
                   python $0.py 2>&1 | tee $0_result.txt
        This code is used in chunk 220.
        \langle Makefile: astronomical lunar unit tests and target 240 \rangle \equiv
240
          {\tt astronomicalLunarCalendarsUnitTest.py: appendixCUnitTest.py}
                    $(NOTANGLE) -filter btdefn -R$*.py - > $*.py
           . \verb|PHONY| : astronomical Lunar Calendars Unit Test|
          astronomicalLunarCalendarsUnitTest: astronomicalLunarCalendarsUnitTest.py
                   python $0.py 2>&1 | tee $0_result.txt
        This code is used in chunk 220.
241
        \langle Makefile: appendix \ c \ unit \ tests \ and \ target \ 241 \rangle \equiv
          appendixCUnitTest.py: $(NW_MAIN:.nw=.py)
                    $(NOTANGLE) -filter btdefn -R$*.py - > $*.py
           .PHONY : appendixCUnitTest
          appendixCUnitTest: appendixCUnitTest.py
                   python $0.py 2>&1 | tee $0_result.txt
           .PHONY : testdata
          testdata: trasformLatexDates2Cvs
                   cat dates1.tex | ./trasformLatexDates2Cvs > dates1.csv
                    cat dates2.tex | ./trasformLatexDates2Cvs > dates2.csv
                    cat dates3.tex | ./trasformLatexDates2Cvs > dates3.csv
                    cat dates4.tex | ./trasformLatexDates2Cvs > dates4.csv
                    cat dates5.tex | ./trasformLatexDates2Cvs > dates5.csv
        This code is used in chunk 220.
242
        \langle Makefile: tools 242 \rangle \equiv
          ⟨Makefile: premarkup 205⟩
          (Makefile: prefix 206)
          (Makefile: excerpt 208)
           ⟨Makefile: blankpremarkup 211⟩
          ⟨Makefile: blankexcerpt 212⟩
          sconstruct:
                   notangle -RSConstruct $(NW_MAIN) $(CPIF) SConstruct
```

This code is used in chunk 218.

```
\langle Makefile: clean 243 \rangle \equiv
243
          .PHONY : clean clobber xclean
          clobber: clean
          clean:
                  rm -fR pycalcal.tex NW_MAIN:.nw=.py pycalcaltests.py *.dvi *.aux *.log \
                           *.blg *.toc *.bbl *~ *.pyc *.defs *.nwi premarkup prefix \
                           excerpt dates?.csv blankexcerpt blankpremarkup \
                           trasformLatexDates2Cvs pycalcal.pdf extractcc3signatures \
                           extractcalcalsignatures pycalcal.ind pycalcal.out pycalcal.ilg \
                          pycalcal.idx *UnitTest.py *UnitTest_result.txt \
                          html/ calendrica/ pycalcal*.gz figure.mpx \
                          $$(ls \mid grep "figure.[0-9][0-9]*") figure-*.pdf fig_*.pdf \
                           *.mps *mpx fig_*.0 SConstruct testSunset.cl fig_alt-az.eps
          # ask to remove all files not recognized by hg
          xclean: clean
                  for f in \$(git status -s \mid grep -e '^??' \mid sed -e 's/^??' //g'); \
                rm -i $$f; \
             done
```

This code is used in chunk 218.

5.4 SConstruct It

I installed scons via the usual \$ sudo python setup.py install from the SCons distribution directory.

Here is my experiment with SCons

```
\langle SConstruct \ 244 \rangle \equiv
244
              # (generated code warning 1)
              \langle scons \ preamble \ 245 \rangle
              \langle scons \ not angle \ 246 \rangle
              \langle scons\ noweave\ 247 \rangle
              \langle scons\ noindex\ 248 \rangle
              \langle scons \ pycalcal \ preamble \ 249 \rangle
              \langle scons \ pycalcal \ tools \ 250 \rangle
              \langle scons \ pycalcal \ targets \ 251 \rangle
           Root chunk (not used in this document).
245
           \langle scons\ preamble\ 245 \rangle \equiv
              import os
              dbg = Environment()
              env = Environment(ENV = os.environ)
              env.PrependENVPath('PATH', '.')
              EnsurePythonVersion(2,5)
                            = 'cat $SOURCE'
              spitsrc
                            = 'premarkup'
              pre
                            = , | ,
              pipe
              # noweb install dir
              noweb_home = '/usr/local/noweb/bin/'
```

This code is used in chunk 244.

```
\langle scons \ not angle \ 246 \rangle \equiv
246
          # notangle consts
                    = noweb_home + 'notangle'
          ntfile
          ntflags = '-filter btdefn -R$TARGET'
          ntcmd
                    = ntfile + ' ' + ntflags + ' - > $TARGET'
          prent
                     = spitsrc + pipe + \
                       pre
                                 + pipe + \
                       ntcmd
                     = spitsrc + pipe + \
          nt
                       ntcmd
          env.Append(BUILDERS={'NoTangle': Builder(action = nt)})
          dbg.Append(BUILDERS={'NoTangle': Builder(action = prent)})
        This code is used in chunk 244.
247
        \langle scons\ noweave\ {\color{red} 247} \rangle \equiv
          # noweave consts
          nwfile = noweb_home + 'noweave'
          nwflags = ' -n -delay -filter btdefn -index'
          nwcmd = nwfile + ' ' + nwflags + ' - > $TARGET'
          prenw
                   = spitsrc + pipe + \
                     pre
                              + pipe + \
                     nwcmd
                   = spitsrc + pipe + \
          nw
                     nwcmd
          env.Append(BUILDERS={'NoWeave': Builder(action = nw)})
          dbg.Append(BUILDERS={'NoWeave': Builder(action = prenw)})
        This code is used in chunk 244.
248
        \langle scons\ noindex\ 248 \rangle \equiv
          # noindex
          nifile = noweb_home + 'noindex'
          niflags = "
                  = nifile + ' ' + niflags + ' $SOURCE'
          nicmd
          ni
                   = nicmd
          env.Append(BUILDERS={'NoIndex': Builder(action = ni)})
          dbg.Append(BUILDERS={'NoIndex': Builder(action = ni)})
```

This code is used in chunk 244.

```
249
       \langle scons\ pycalcal\ preamble\ 249 \rangle \equiv
          # pycalcal specific
          builder=env
          unit_test_files="""basicCodeUnitTest.py
                          \verb"egyptianAndArmenianCalendarsUnitTest.py"
                          gregorianCalendarUnitTest.py
                          isoCalendarUnitTest.py
                          julianCalendarUnitTest.py
                          copticAndEthiopicCalendarsUnitTest.py
                          ecclesiasticalCalendarsUnitTest.py
                          islamicCalendarUnitTest.py
                          hebrewCalendarUnitTest.py
                          mayanCalendarsUnitTest.py
                          oldHinduCalendarsUnitTest.py
                          balineseCalendarUnitTest.py
                          timeAndAstronomyUnitTest.py
                          persianCalendarUnitTest.py
                          bahaiCalendarUnitTest.py
                          frenchRevolutionaryCalendarUnitTest.py
                          chineseCalendarUnitTest.py
                          modernHinduCalendarsUnitTest.py
                          tibetanCalendarUnitTest.py
                          astronomicalLunarCalendarsUnitTest.py"""
       This code is used in chunk 244.
250
       \langle scons\ pycalcal\ tools\ 250 \rangle \equiv
          # tools
         prefix = builder.NoTangle('prefix', 'pycalcal.nw')
          excerpt = builder.NoTangle('excerpt', 'pycalcal.nw')
          premarkup = builder.NoTangle('premarkup', 'pycalcal.nw')
          Requires(premarkup, [excerpt, prefix])
       This code is used in chunk 244.
       \langle \mathit{scons}\ \mathit{pycalcal}\ \mathit{targets}\ \underline{^{251}}\rangle {\equiv}
251
         pycalcal_code = dbg.NoTangle('pycalcal.py', 'pycalcal.nw',)
          # Requires(pycalcal_code, premarkup)
          Clean(pycalcal_code, Split('pycalcal.pyo pycalcal.pyc'))
          pycalcal_tests = builder.NoTangle('pycalcaltests.py', 'pycalcal.nw',)
          Requires(pycalcal_tests, [premarkup, pycalcal_code])
          Clean(pycalcal_tests, Split('pycalcaltests.pyo pycalcaltestst.pyc'))
          pycalcal_latex = builder.NoWeave('pycalcal.tex', 'pycalcal.nw')
          Requires(pycalcal_latex, premarkup)
          Clean(pycalcal_latex, 'pycalcal.out')
          pycalcal_noindex = builder.NoIndex('pycalcal.nwi', 'pycalcal.tex')
          Depends(pycalcal_noindex, pycalcal_latex)
          pycalcal_pdf = builder.PDF(target = 'pycalcal.pdf',
                               source = 'pycalcal.tex')
          Depends(pycalcal_pdf, Split('pycalcal.tex pycalcal.bib'))
          Default(pycalcal_pdf, pycalcal_code, pycalcal_tests)
```

This code is used in chunk 244.

5.5 Floating-point nuances

In oder to check numerical results, I compared Common LISP output with Python. (I used both CLisp [on PC and Linux] and SBCL [this is easier to install on OS X]). A snippet of Common LISP code from Prof. Reingold.

```
\langle testSunset.cl \ 252 \rangle \equiv
252
          #!/usr/bin/env sbcl
          ;; -*- Mode: Lisp -*-
          (load "calendrica-3.0.cl")
          ;;(in-package "CC3")
          ;;(use-package "CC3")
          (defun format-time (p)
            (if (equal p CC3:bogus)
                "\\multicolumn{4}{c}{\\fun{bogus}}"
                   ;;; add 1/2 second...
              (let ((time (CC3:clock-from-moment (+ (/ 0.5 24 60 60) p))))
                (list (mod p 1)
                       (format nil "~2,'0D" (first time))
                       (format nil "~2,'0D" (second time))
                       ;;; ....and truncate
                       (format nil "~2,'0D" (floor (third time)))))))
          (defvar *moment*
            (and (= 1 (length *args*))
                 (ignore-errors
                    (with-input-from-string (strm (first *args*))
                      (read strm)))))
          (if (integerp *moment*)
              (format-time (CC3:sunrise *moment* CC3:paris))
            (format t "~&error on the command line~&"))
        Root chunk (not used in this document).
        Uses mod 15 and sunrise 102.
```

5.6 Small differences or errors?

This is a python script to output values from "Calendrical Calculations" and the ones from my library.

```
253
        \langle printObservationalHebrewFromFixed.py 253 \rangle \equiv
          from pycalcal import *
          import csv
          rd = []
          ho = []
          reader = csv.reader(open("dates3.csv", "rU"),
                                delimiter=',',
                                quoting=csv.QUOTE_NONE)
          for row in reader:
              rd.append(int(row[0]))
              ho.append(hebrew_date(int(row[4]), int(row[5]), int(row[6])))
          for i in range(len(rd)):
              # observational
              print 'R.D.= %d; oh_from_fxd=%s; fxd_from_oh=%d; book=%s' % (rd[i],
                                         observational_hebrew_from_fixed(rd[i]),
                                         fixed_from_observational_hebrew(ho[i]),
                                                             ho[i])
        Root chunk (not used in this document).
        Uses fixed_from_observational_hebrew 142, hebrew_date 80, observational_hebrew_from_fixed 142,
          and rd 37.
```

5.7 Floating-point nuances

While investigating the differences from my results and COMMON LISP ones, I got a nice email exchange with Prof. Reingold. I was pointing out that COMMON LISP on my machine was not returning the same numbers as in the Appendix C' last table. He ran it on SPARC and on Intel x86 . . . and bang!

On the Python side, my tests fail for "Dawn in Paris" if I force 6 digits of precision, otherwise they all pass but one (on RD 601716) when 4 digits are taken: this last paragraph is not true. I found this was due to the wrong implementation of angle: division was with integers and not floating point numbers!

5.8 Chasing bugs

Observational Hebrew convertion tests fail for (almost all) Appendix C dates. I try to find what's wrong in observational_hebrew_from_fixed: gregorian_year_from_fixed seems to be ok; observational_hebrew_new_year is not; gregorian_new_year is ok.

```
[1] (load "calendrica-3.0.cl")
[4]> (CC3:observational-hebrew-new-year (CC3:gregorian-year-from-fixed -214193))
-214319
[5] > (CC3:observational-hebrew-new-year (CC3:gregorian-year-from-fixed -61387))
-61647
[6] > (CC3:gregorian-year-from-fixed -214193)
-586
[7] > (CC3:gregorian-year-from-fixed -61387)
-168
[8] > (CC3:gregorian-year-from-fixed 25469)
[9] > (CC3:gregorian-year-from-fixed 613424)
1680
[10] > (CC3:gregorian-year-from-fixed 744313)
2038
[11] > (CC3:solar-longitude-after CC3:spring (CC3:gregorian-new-year 764652))
2.7928327878524209297L8
and python:
>>> p.solar_longitude_after(p.SPRING, p.gregorian_new_year(764652))
p.solar_longitude_after(p.SPRING, p.gregorian_new_year(764652))
mpf('279283278.7852416')
```

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Appendix A

Version control

My code is now at http://espinielli.github.com/pycalcal. As you can guess from the URL, it is on GitHub and I use git.

Appendix B

Old Version control

I used to store my code in google code repo, http://code.google.com/p/pycalcal/, based on Mercurial version control system. For an introduction to Mercurial read the excellent tutorial from Joel Spolsky at http://hginit.com/index.html.

Usual commands I used:

```
$ cd <my repo>
$ hg status  # to see what has changed
$ hg add file1 # to add a new element in the repo
$ hg update  # to retrieve changes from the repo
$ hg commit  # to commit changes to the repo
```

Appendix C

Chunks

C.1 Chunks Index

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