

# A database of molecular and reaction properties integrated in the Materials Project

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## Abstract

Advanced chemical research is increasingly reliant on large datasets of molecule and reaction properties to discover new functional molecules, understand chemical trends, train machine learning models, and more. To be of greatest use to the scientific community, such datasets should follow FAIR principles (i.e. be findable, accessible, interoperable, and reusable). In this work, we present a FAIR expansion of the Materials Project database (“MPcules”) that adds more than 170,000 molecules studied using density functional theory (DFT) to the existing data, which comprises crystalline solids. MPcules is a diverse collection of DFT-calculated molecular properties, with an emphasis on reactive, open-shell, and charged species - relevant for studying reaction pathways - and a wide array of structural, electronic, vibrational, and thermodynamic properties. This database can be queried through an OpenAPI-compliant application programming interface and a featureful web application. We continue to expand the data available on MPcules and encourage contributions from the community.

## Introduction

With advances in scientific workflow automation and high-performance computing, it has become increasingly facile to generate large datasets of molecules,<sup>1</sup> materials,<sup>2</sup> and reactions,<sup>3,4</sup> as well as their computed and predicted properties. Such datasets, which commonly rely on atomistic simulations using some combination of classical or *ab initio* molecular dynamics, semi-empirical quantum chemistry, density functional theory (DFT), and wavefunction methods, have ushered in a new paradigm of data-driven chemical research, enabling in-depth understanding of complex chemical domains<sup>5–7</sup> and the discovery and design of new materials and molecules with desirable properties in diverse applications.<sup>8–12</sup> Well-designed, systematic, and diverse datasets are also essential for virtually all machine learning (ML) tasks in chemistry and materials science.<sup>13–22</sup>

While the wealth of data available to researchers is a boon, not all data is created equal.

It is increasingly recognized that for datasets to maximally benefit the scientific community, the underlying data should follow **FAIR** principles:<sup>23</sup> they should be **Findable** (the data can be easily searched using rich metadata and unique identifiers or IDs); **Accessible** (the data are as open to the public as possible and can be reached using standard communication protocols); **Interoperable** (the data can be readily combined with other data or used with a wide range of tools); and **Reusable** (the data contain many useful attributes relevant to the domain of interest, have provenance allowing for verification of their accuracy, and are licensed in such a way as to allow others to employ them in their own work).

Since the advent of the Materials Genome Initiative in the United States,<sup>24,25</sup> a number of databases of materials and their computed properties have been developed. Many of these databases, including the Open Quantum Materials Database (OQMD),<sup>26,27</sup> Novel Materials Discovery (NOMAD) repository,<sup>28</sup> and the Materials Project,<sup>29</sup> aspire to follow FAIR principles. Though they vary in scale, the types of materials contained, and the properties reported, these repositories are all alike in that they have web interfaces where users can easily search and visualize data as well as application programming interfaces (APIs) that allow programmatic access to a wide range of data and metadata - enabling individual users with knowledge of computer programming to more easily access large collections of materials properties and allowing these databases to be integrated into other applications.

In contrast, few FAIR databases of calculated molecular properties exist. It remains common for computational chemistry data to be presented as a single unit (for instance, a zipped file that cannot be easily searched), or worse, not be publicly shared at all. The Molecular Sciences Software Institute's QCArchive,<sup>30</sup> which hosts large collections of user-submitted data, including the popular QM9<sup>31</sup> and ANI-1 datasets,<sup>32</sup> is a noteworthy and laudable example of quantum chemical data approaching FAIR standards. The data on QCArchive can be downloaded in HDF5 format from their web site or can be accessed through a representational state transfer (REST) API, making it accessible and interoperable. QCArchive data is also reasonably findable and reusable. Molecules in QCArchive are given unique IDs.

However, at the time of writing, it is not possible to search for specific molecules in the datasets listed on the web interface. Moreover, data visualization tools are either limited or nonexistent, making it difficult for users to discover or digest the data without downloading and sifting through large collections. In terms of reusability, QCArchive boasts an enormous collection of molecules and datapoints with provenance based on over 10 million calculations, but the available data is often limited in scope and applicability. Many of the datasets included in QCArchive contain relatively few properties (for instance, only structures and electronic energies), meaning that the data can only easily be applied to very specific tasks, e.g. training ML force-fields for molecular dynamics.

In order to continue the advancement of data-driven chemical research, new platforms are needed that emphasize ease of access and diversity of data and data attributes. Here, in an effort to fill this need and support computational chemistry and chemical ML research, we report an extension of the Materials Project for calculated molecular data which we call the “Materials Project for Molecules”, or “MPcules” for short. We have developed a database schema and modular data processing pipeline that allows molecular DFT calculations to be converted into rich molecule and molecular property documents with unique, robust, and chemically meaningful IDs. This data pipeline can be used to add data to MPcules or to develop bespoke datasets. As a means to access the data in MPcules, we have expanded the Materials Project API and associated Python API client. Further, we have developed and released a new application (app) on the Materials Project web site allowing users to visualize the data in MPcules without any programming knowledge. MPcules currently contains more than 170,000 molecules assembled from more than half a million DFT calculations. It is envisioned as a dynamic database that will continue to grow both in terms of the number of molecules as well as the number and types of properties included. In this paper, we describe the methods used to construct MPcules and report on the current status of the database.

## Quantum Chemical Methods

All data currently included in MPcules are directly calculated or derived from DFT calculations. Specifically, all calculations were performed with the Q-Chem electronic structure code, using either version 5 or 6.<sup>33</sup> Calculation automation and initial processing of DFT inputs and outputs relied on the `fireworks`,<sup>34</sup> `custodian`,<sup>35,36</sup> and `atomate`<sup>37</sup> Python libraries.

At present, the calculations that make up MPcules use a small set of DFT methods. Specifically, calculations have been performed using three exchange-correlation functionals - the range-separated hybrid generalized gradient approximation (GGA) functionals  $\omega$ B97X-D<sup>38</sup> and  $\omega$ B97X-V<sup>39</sup> and the range-separated hybrid meta-generalized gradient approximation (meta-GGA) functional  $\omega$ B97M-V<sup>40</sup> - as well as three basis sets from the def2 family with polarization and diffuse functions added - def2-SVPD, def2-TZVPPD, and def2-QZVPPD.<sup>41</sup> Many calculations were performed in vacuum, but calculations using the polarizable continuum model (PCM)<sup>42</sup> and the solvent model with density (SMD)<sup>43</sup> implicit solvent methods are also included. We note that while these calculation methods reflect the data currently in MPcules, the database can easily accept calculations applying any functional and basis set included in Q-Chem.

## Database Construction

The MPcules database is constructed using the `emmet` Python packages. `emmet-core` defines “data models” or “documents” (using the `pydantic` data validation framework) that represent everything from the output of a Q-Chem calculation, to a molecule or a specific property; `emmet-builders` describes how raw calculation outputs can be converted into molecule and molecule property documents (defined in `emmet-core`) and how these documents should be inserted as entries in a database (MPcules, like most of the Materials Project, uses a MongoDB NoSQL architecture). Lastly, `emmet-api` defines how MPcules can be queried to

obtain the data that has been built. Here, we elaborate on the structure of MPcules and how the database is constructed.

## Assigning Priority to Calculations

As discussed above (“Quantum chemical methods”), MPcules can accommodate calculations that use many different levels of theory, where we define “level of theory” as the combination of a density functional, basis set, and solvent method. Therefore, when a particular property has been calculated using multiple levels of theory, we must rank them in order to retain and report only the “best” property available.

Each component of the level of theory – the functional, basis set, and solvent method – is assigned a score. Because the accuracy and appropriateness of computational methods depends sensitively on the property of interest and the types of molecules being considered, these scores are inherently heuristic in nature but are based on e.g. previous benchmark studies and simple rules. Further details regarding the scoring of the components of level of theory are provided in the Supplementary Information.

While one solvent method may be considered more accurate or reliable than another, the same cannot be true of solvents themselves. That is, a calculation using PCM parameterized with  $\epsilon = 80$  (roughly approximating an aqueous medium) is no more or less accurate than one parameterized with  $\epsilon = 7$  (approximating the dielectric of e.g. tetrahydrofuran). Rather, calculations performed with different solvent media are better or worse suited for particular applications. When tabulating molecular properties, we therefore select the best level of theory available *for each solvent medium*. We note that calculations conducted in vacuum are ranked below those performed using implicit solvent methods, but vacuum properties are still reported when available, as we treat vacuum as a distinct solvent medium.

## Tasks

A single DFT workflow may correspond to one calculation (e.g. a single-point energy calculation or geometry optimization) or may be a collection of related calculations (e.g. a geometry optimization followed by a vibrational frequency analysis to confirm that the optimized structure is a local minimum of the potential energy surface or PES). In either case, the metadata, input parameters, and results of the calculation(s) are parsed by `atomate` and stored in a MongoDB database in a single “task document” (represented in `emmet-core` as a `TaskDocument` object). Tasks/`TaskDocuments` are the most fundamental collections of data used to construct MPcules, corresponding almost directly to the parameters and raw outputs of DFT calculations.

## Molecules

“Molecules” are central to MPcules. Most data in MPcules is conceptually organized and grouped by molecule. How we define the term “molecule” therefore affects how users will access and interact with data. Although chemists and physicists have intuitive understandings of what a molecule is, we must be careful in defining the term and consider how best to represent a molecule in a database.

### What Is a Molecule?

Conventionally, a molecule is defined as a group of two or more atoms that are bound together. We expand the term to include single atoms (e.g.  $H^0$ ) and monatomic ions (e.g.  $F^{-1}$ ), as such species can be important for the calculation of molecular and reaction properties. For instance, single metal ions like  $Li^{+1}$  are necessary to compute the binding energies of those ions to coordinating molecules.

A molecule can be minimally described by its chemical composition, charge, and spin multiplicity. This definition is in line with common written nomenclature for molecules and ions. As a small example, diatomic oxygen in the triplet ground state ( ${}^3O_2$ ) is differentiated

by composition from the oxygen atom ( $O_1$ ), by charge from a peroxide anion ( $O_2^{-2}$ ), and by spin from the singlet excited state ( $^1O_2$ ). To specify beyond this starting point, there are two natural definitions: one, more physically inspired, based on PES, and another, more chemically inspired, based on the idea of chemical bonding (Figure 1).

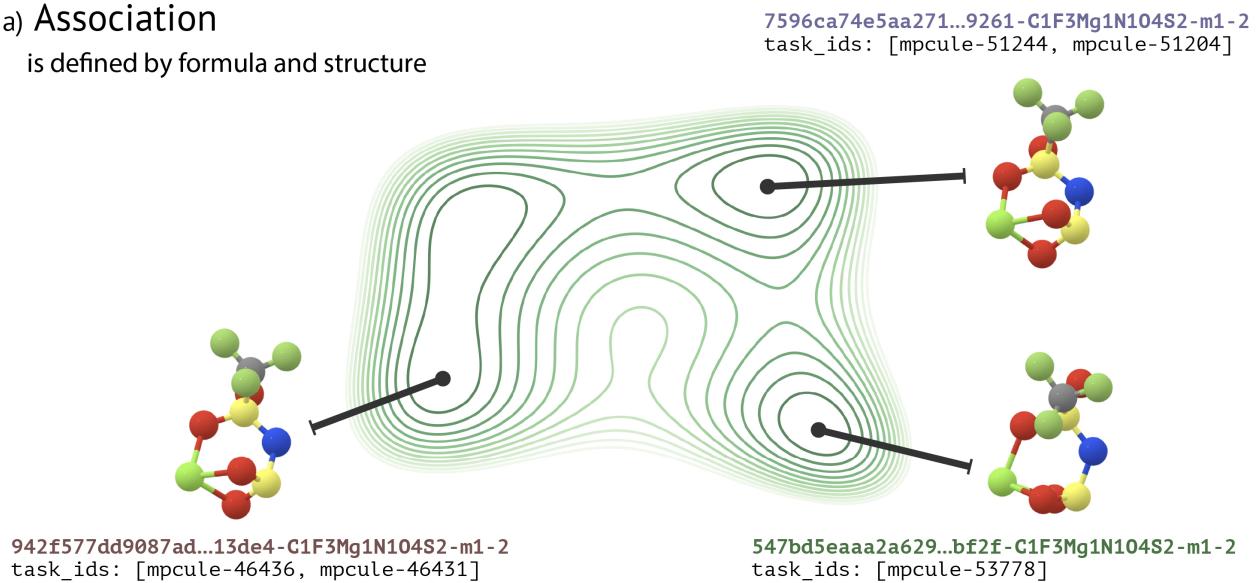
The physical definition says that a molecule is defined as a local minimum on a PES. The PES, in turn, is defined by the chemical composition, total number of electrons, number of *unpaired* electrons, and the DFT methods (level of theory and other calculation parameters) employed. In this definition, every unique atomic structure (in terms of interatomic distances and angles) corresponding to a local PES minimum obtained via a geometry optimization calculation is a different molecule. It is worth noting that this physical definition is used within the Materials Project’s data for crystalline solids to define a unique “material”.

In contrast, the chemical definition says that it is the *connectivity* of a molecule - the way that atoms are linked to each other through chemical bonds and other interatomic interactions - that distinguishes molecules. Different local minima on a PES may correspond to structures with different bonds, but they may also simply be different conformational isomers (conformers). This chemical definition is somewhat more complex than the physical picture, as it requires additional definitions and decisions. For instance, this definition relies on the idea of a “bond” and associated criteria determining when two or more atoms are or are not bonded.

In MPcules, we use both the physical and the chemical definitions to construct molecules, as described below (“Building molecules”). However, as most chemical observables of interest – including various spectra, electrochemical properties, and reaction properties like thermodynamics or kinetics – are averaged over different interconverting conformers,<sup>44</sup> we rely in most cases on the chemical definition based on bonding.

## a) Association

is defined by formula and structure



## b) Collection

is defined by formula, charge, spin & connectivity

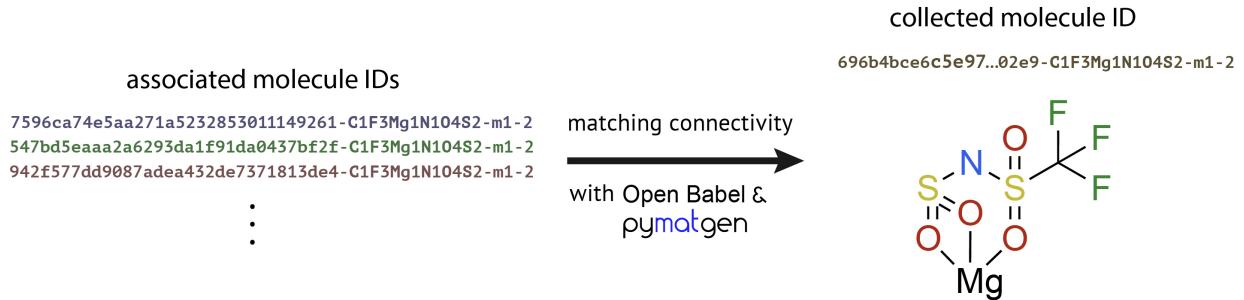


Figure 1: Conceptual guide to molecule definition and construction in MPcules. a) In the physical definition, a molecule is a unique minimum of a potential energy surface, defined by some composition and structure (e.g. interatomic distances and angles). This definition is used in the first (association) stage of molecule building. b) In the chemical definition, a molecule is defined by its composition, charge, spin multiplicity, and connectivity. Different conformers (species with distinct structures but the same connectivity) can all be thought of as the same molecule. This definition is used for the second (collection) stage of molecule building, where we use OpenBabel and `pymatgen` to determine bonding.

## Building Molecules

Molecules (`MoleculeDocs` in `emmet-core`) are constructed in two stages: association and collection. In the first (association) stage (Figure 1a), tasks are grouped according to the physical definition of a molecule (i.e., each structure corresponding to a unique local minimum of a PES is a unique molecule). When tasks are initially grouped together, charge and spin multiplicity are not considered, because calculations could be performed which use structures optimized at one charge/spin state but compute the electronic structure at a different charge or spin state; for instance, this is necessary to compute the vertical electron affinity or ionization energy of a molecule.<sup>45</sup> The structures associated with each task (represented by `pymatgen Molecule` objects) are then compared, and tasks with structures that are identical within a tight tolerance (by default, the root-mean-squared displacement or RMSD  $\leq 10^{-6}$ ) are grouped together. If no task in a group corresponds to a geometry optimization and the structure in question is not a single atom (for which geometry optimization is not meaningful), then we cannot confirm if the structure is a local minimum of a PES, and so the group is discarded. For groups that remain, a single representative structure is chosen by ranking the geometry optimization calculations by level of theory (see “Assigning priority” above) and electronic energy, and the charge and spin of the associated `MoleculeDoc` are determined based on this “best” structure.

In the second (collection) stage (Figure 1b), the structures of associated `MoleculeDocs` are compared on the basis of connectivity. Though we can define bonding using several methods informed by quantum chemistry (see “Molecular properties” below), for the purpose of collecting `MoleculeDocs` we need to choose a definition of bonding such that the connectivity of every molecule in MPcules can be determined regardless of what calculations have been performed. We use the bond detection algorithm included in the OpenBabel cheminformatics toolkit<sup>46</sup> and then identify missing coordinate bonds to metals with the `metal_edge_extender` defined in `pymatgen`.<sup>35</sup> This method is entirely based on heuristics and does not depend on any electronic structure calculations. Upon detecting bonds, we

construct a molecular graph representation using the `pymatgen MoleculeGraph` functionality. If there are multiple associated `MoleculeDocs` with the same formula, charge, spin, and connectivity, then we rank the different documents (again in terms of the level of theory used to optimize the best structure and the associated electronic energy) and choose the best to represent the group. All other associated `MoleculeDocs` with the same formula, charge, spin, and connectivity are linked to this representative as “similar molecules”.

Molecules are assigned unique identifiers (“`MPculeIDs`”) based on their chemical formulas, charges, spin multiplicities, and connectivity; further details regarding the `MPculeID` format are provided in the Supplementary Information. Likewise, tasks are given unique IDs defined by an (optional) prefix and some integer. `MoleculeDocs` store a list of the IDs of all tasks performed on the same geometry. Collected `MoleculeDocs` additionally store the IDs of the tasks that produced the “best” structure for each implicit solvent medium (including vacuum) for that molecule and the `MPculeIDs` of the “similar” associated `MoleculeDocs` (documents with the same connectivity, but with geometries representing different PES minima). This allows users to collect the properties of various conformers of a given molecule.

## Molecular Properties

`MoleculeDocs` and their underlying `TaskDocuments` contain all of the information about a molecule that is stored in `MPcules`. To aid in accessibility and reusability, we further process task- and molecule-level data to generate property documents. Typically, property documents are uniquely defined by the combination of `MPculeID` and solvent. In some cases, a property can be calculated or determined using multiple different methods; for instance, atomic partial spins can be defined using Mulliken population analysis<sup>47</sup> or the natural atomic populations determined by the natural bonding orbital (NBO) program.<sup>48,49</sup> For such properties, a property document is uniquely defined by `MPculeID`, solvent, and method. Though one could search for a property document using these defining characteristics, for convenience, we also define IDs for property documents. These IDs are generated by con-

structing a string with the identifying information for the document (including MPculeID, solvent, and - where relevant - method, as well as potentially other information used to generate the document); this string is then hashed using the BLAKE2 algorithm,<sup>50</sup> as implemented in the Python standard library. The uniqueness of a hash can in general not be guaranteed, but because there are other ways to access a desired property document using data that are essentially guaranteed to be unique, the relatively remote possibility of hash collisions is acceptable in the case of property documents.

At present, we generate property documents for the following properties: natural atomic and molecular orbitals (based on NBO); atomic partial charges; atomic partial spins; bonding; thermodynamics; vibrational properties; redox and electrochemical properties; and coordination or binding of metals. Basic details for these different properties are provided below, and a schematic of how collections of tasks, molecules, and properties are connected is shown in Figure 2.

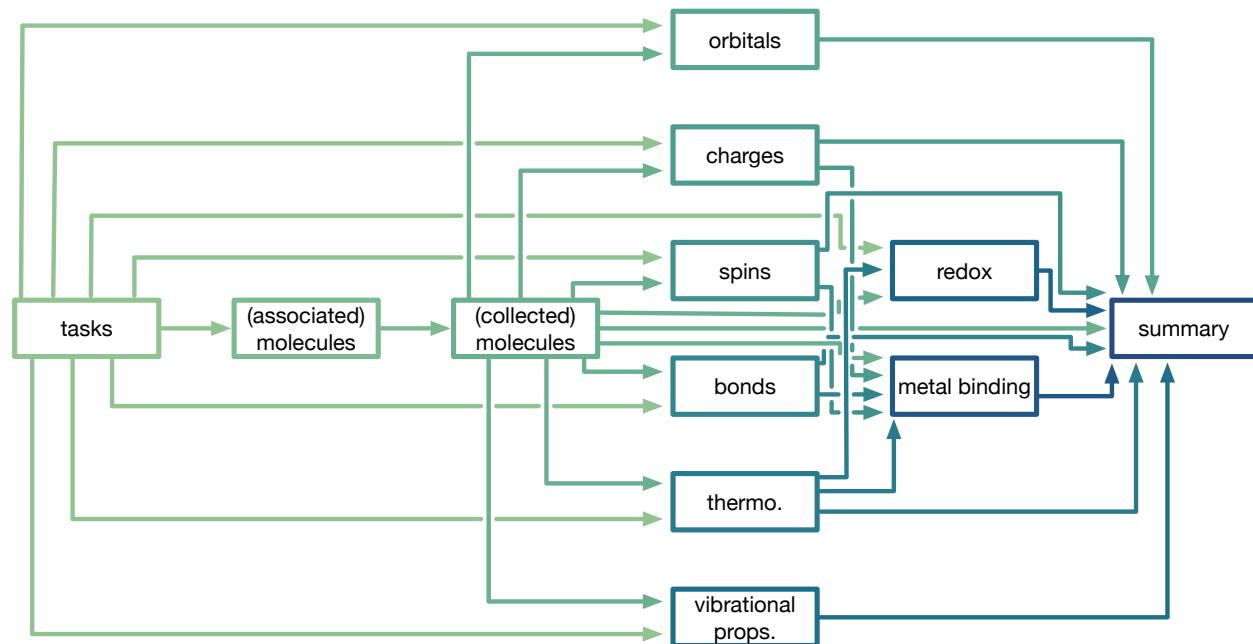


Figure 2: Diagram showing how different collections of tasks, (associated) molecules, and properties are linked together in MPcules. An arrow from a source collection (box) to another destination collection indicates that documents in the source are used to construct documents in the destination.

For molecules with multiple optimized structures for a given solvent medium (i.e., for cases where multiple associated `MoleculeDocs` were collapsed into a single `MoleculeDoc` during the collection stage), we only calculate properties based on the “best” structure. This ensures that comparable properties for the same molecule always refer to the same structure. We further note that, for atomic properties (e.g. atomic partial charges, atomic partial spins) or properties with atomic components (e.g. normal modes of vibration), we consistently use the same atomic indices as the `pymatgen Molecule` object for the “best” structure.

## Natural Atomic and Molecular Orbitals

NBO processes the optimized multi-electron wavefunction produced during a DFT self-consistent field (SCF) calculation. After first converting the atom-centered orbital basis into sets of natural atomic orbitals, natural hybrid orbitals, natural bond orbitals, and natural localized molecular orbitals, the NBO program can perform detailed atomic population analysis, analysis of lone pairs and bonds (including hyperbonds and 3-center bonds), and perform second-order perturbation theory analysis of donor-acceptor type orbital interactions.<sup>48</sup>

For each atom, we store the number of core, valence, and Rydberg electrons, as well as the total number of electrons assigned to that atom. Lone pair information includes the orbital character of the lone pair (fraction of the lone pair made up of s, p, d, and f natural atomic orbitals), as well as its total occupancy. Similarly, for bonds we include the orbital character of each atom’s contribution and the total occupancy, as well as information regarding the bond polarization. We also store information regarding orbital interactions, including the perturbation energy, the energy difference between the donor and acceptor orbitals, and the Fock matrix element for the interaction. For each type of hybrid orbital (e.g. long pair or bond) or orbital interaction, we retain information regarding the atoms involved in the hybrid orbital(s) as well as the orbital type(s), using the codes from NBO

outputs. For instance, lone pair orbitals are labeled “LP”, while antibonding orbitals are labeled as “BD\*”.

For molecules with unpaired electrons, NBO separates its analysis for  $\alpha$  and  $\beta$  electrons. Accordingly, the orbital data on MPcules is structured differently for open-shell and closed-shell molecules. Closed-shell molecules have singular collections of populations, lone pairs, bonds, and interactions, while open-shell molecules have one collection of each type of property for  $\alpha$  electrons and one for  $\beta$  electrons.

NBO version 7 significantly improved the bond-detection algorithm over version 5.<sup>49</sup> As a result, we currently only allow NBO 7 calculations to be included in MPcules. Users wishing to adopt our methodology should note that Q-Chem is packaged with NBO version 5 and uses this version by default, meaning that configuration of an external NBO application is necessary to benefit from the improvements and produce data that can be incorporated into MPcules.

## Atomic Partial Charges

Atomic partial charges are determined from DFT calculations following SCF convergence. They can be obtained by assessing the population of orbitals in an electronic wavefunction, by partitioning the total electron density, by calculating the electrostatic potential, or by other means.<sup>51</sup> In MPcules, we currently calculate atomic partial charges using four methods: Mulliken population analysis,<sup>47</sup> the restrained electrostatic potential (RESP),<sup>52</sup> Bader charges<sup>53</sup> (obtained using the `critic2` program),<sup>54</sup> and natural atomic populations via NBO. When other methods are available, we recommend against Mulliken population analysis, as the Mulliken method is known to depend strongly on basis set and produce in some cases unphysical partial charges.<sup>55</sup> We include Mulliken partial charges because they remain widely used in computational chemistry and because Mulliken population analysis is performed by default in Q-Chem DFT calculations. We provide a comparison of Mulliken and NBO atomic partial charges in the Supplementary Information.

## Atomic Partial Spins

For molecules with unpaired electrons, atomic partial spins can be calculated in a manner analogous to atomic partial charges (for closed-shell molecules without unpaired electrons, the net spin on all atoms is always 0). Atomic partial spins are currently calculated using two methods: Mulliken population analysis and NBO natural atomic populations. We note (Supplementary Information Figures S1-S5) that Mulliken atomic partial spins are more well-behaved than Mulliken atomic partial charges and are qualitatively similar to NBO-based partial spins.

## Bonding

Bonds are a key molecular property, as we have already discussed (“Building Molecules”). Bonding documents (`MoleculeBondingDocs` in `emmet-core`) include a list of bonds (using indices to represent what atoms are bonded), bond lengths organized by bond type (e.g. “C-O” for bonds between carbon and oxygen), and a graph representation of the molecule, with bonds included as edges (using `MoleculeGraph` in `pymatgen`).

In addition to the heuristic method of defining bonds using OpenBabel and `pymatgen`, we can determine bonding in two ways: 1) with the method of Spotte-Smith, Blau, et al.,<sup>56</sup> in which OpenBabel/`pymatgen` heuristic bonding is augmented with bonds identified by analyzing the critical points of the total electron density (using `critic2`) and 2) via natural bonding orbitals identified with NBO.

NBO reports bonds that form hybrid orbitals based on the sharing of electrons between atoms - in other words, covalent bonds. Ionic bonds, coordinate bonds, and other electrostatic interatomic interactions are not captured directly as bonds in the NBO output. However, such non-covalent bonds and interactions can be inferred from other NBO-reported quantities. Specifically, to identify metal coordinate bonds, we examine NBO’s second-order perturbation theory analysis of the Fock matrix. If there is an interaction between a lone pair (“LP”) orbital on a nonmetal (donor) and a lone vacant (“LV”) or anti-Rydberg orbital

(“RY\*”) on a metal (acceptor) where the metal is within 3.0 Å of the nonmetal and the perturbation energy is greater than or equal to 3.0 kcal/mol, then we determine the metal and nonmetal to be electrostatically bonded. These cutoff values were determined by manual inspection of set of metal-containing complexes and are, like most definitions of bonding, somewhat arbitrary.

## Molecular Thermodynamics

Typical DFT calculations produce as output an electronic energy, which can be used to determine the relative stability of different structures or calculate reaction energies. If a vibrational frequency analysis has been performed, the zero-point energy, as well as the enthalpy, entropy, and their components (vibrational, rotational, and translational), can be obtained; from this, one can calculate the molecular Gibbs free energy, which is often a more natural thermodynamic potential, particularly for comparison to experiments at constant temperature and pressure.

In order to obtain optimized geometries and calculate free energies at reduced cost, it is common for computational chemists to optimize structures at a relatively inexpensive level of theory (e.g. using a small basis set, or ignoring solvent effects) and then re-calculate the electronic energy with a single-point calculation using a more accurate and expensive level of theory (e.g. using a larger basis set or including an implicit solvent model). There are therefore two natural ways to calculate molecular thermodynamics: one in which all thermodynamic quantities of interest (electronic energy, enthalpy, entropy, etc.) are calculated from a single vibrational frequency analysis calculation, and another in which most properties are obtained from a vibrational frequency analysis but the electronic energy is instead obtained from a single-point energy calculation performed on the same structure at a higher level of theory.

We construct thermodynamic property documents (`MoleculeThermoDocs` in `emmet-core`) using both methods. If, for a given solvent, one can produce a `MoleculeThermoDoc` both

with and without a single-point energy correction, then the scores for the “best” uncorrected document (based on the level of theory used and the electronic energy) and “best” corrected document (based on the average of the scores of the levels of theory used for the vibrational frequency analysis and the single-point energy calculation, and the electronic energy) are compared, and the document with the better (lower) score is selected.

## Vibrational Properties

Vibrational frequency analyses produce molecular vibrational frequencies (related to the eigenvalues of the Hessian matrix) and associated normal modes (related to the Hessian eigenvectors). At present, we report these frequencies and normal modes, as well as the calculated infrared (IR) activities and intensities. From these quantities, it is possible to obtain a calculated IR spectrum of a molecule.

## Redox and Electrochemical Properties

We calculate properties related to molecular reduction and oxidation using both the vertical and adiabatic approximations (Figure 3).<sup>45</sup> In the vertical approximation, one does not allow the molecular atomic structure to relax upon accepting or donating an electron, under the assumption that electron attachment or detachment occurs much more rapidly than atomic rearrangement. Calculating a vertical electron affinity (EA) or ionization energy (IE) therefore requires only a single-point energy calculation on an optimized geometry with the charge shifted by -1 (for EA) or +1 (for IE). Since vertical EA and IE calculations involve only a single molecular structure, they can be calculated using a single **MoleculeDoc** and its associated tasks.

In the adiabatic approximation, one allows a reduced or oxidized molecule to fully relax. Calculating an adiabatic reduction or oxidation (free) energy therefore requires two optimized structures (and therefore two **MoleculeDocs**) at two different charge states. Because it can be challenging to predict *a priori* how a molecule may decompose upon charge transfer, we

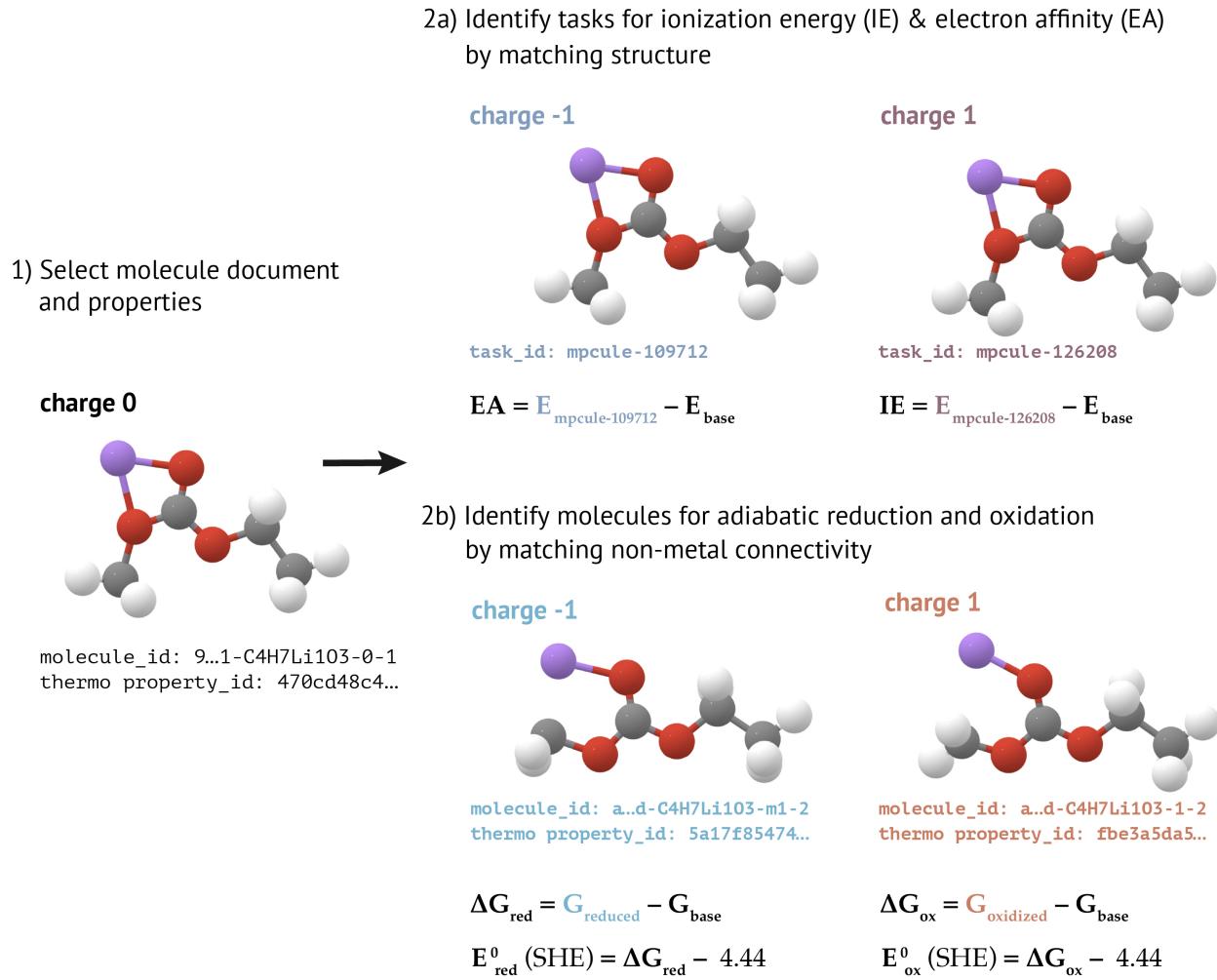


Figure 3: Calculation of redox and electrochemical properties in MPcules. 1) For a given molecule, the molecule document and related thermodynamics properties are needed. 2a) Vertical ionization energy (IE) and electron affinity (EA) can be calculated by identifying tasks with the same structure as the molecule of interest, but with charge shifted by +1 (for ionization energy) or -1 (for electron affinity). 2b) Adiabatic reduction and oxidation properties can be calculated by identifying molecules with the same connectivity (ignoring metal coordination) but with charge shifted by -1 (for reduction) or +1 (for oxidation). For clarity, the charge of each molecule and task is shown next to its structure.

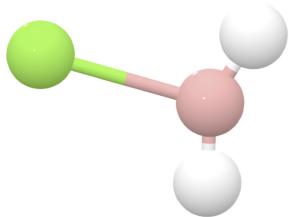
neglect the possibility of dissociative redox reactions. Instead, when calculating adiabatic redox properties for a given molecule, we search for **MoleculeDocs** that have the same connectivity as that molecule (not including bonds involving metals), but with charge shifted by -1 (for reduction) or +1 (for oxidation). Reaction free energies are calculated using previously-constructed **MoleculeThermoDocs** (see “Molecular Thermodynamics”). If the oxidized and/or reduced **MoleculeDocs** can be identified, we also calculate reduction or oxidation potentials, referenced to the standard hydrogen electrode (SHE) using the relative potentials reported by Trasatti.<sup>57</sup>

## Metal Coordination and Binding

Metal coordination is important in a range of applications, including chemical separation,<sup>58</sup> organometallic chemistry,<sup>59</sup> and the design of electrolytes for energy storage and other applications.<sup>60</sup> We therefore collect information regarding the binding properties of metals in molecules, including the number, type, and length of coordinating bonds, as well as the thermodynamics of metal binding for the reaction A–M → A + M, where M is a metal and A is a coordinating molecule.

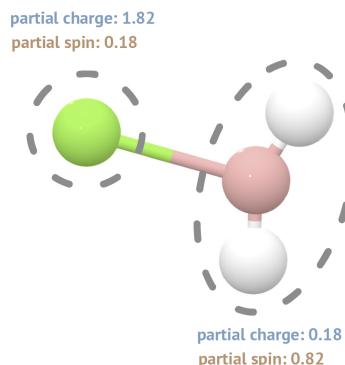
To determine metal binding properties (Figure 4), we must first ascertain the charge and spin state of each metal in a given molecule. To do this, we round the atomic partial charge and the atomic partial spin of the metal atom in the molecule to the nearest whole number. These atomic partial charges and spins are obtained from previously-constructed collections in MPcules (see “Atomic Partial Charges” and “Atomic Partial Spins” above). If the rounded charge and spin are incompatible - for instance, if a Mg atom were assigned a charge of +1 and a spin multiplicity of 1 (spin 0) - then the charge is shifted by +1 or -1 (whichever produces a charge which is closer to the calculated atomic partial charge). We shift the charge, rather than the spin multiplicity, because we have found that the spin state of metals is more often well described by DFT than metal charge states (see “Comparison of Atomic Partial Charges and Spin” in the Supplementary Information).

1) Select molecule document and properties



```
molecule_id: 71c4935465d926a4474b7b26a547205d-B1H2Mg1-2-2
charges property_id: 6fac9975b97af8b8134a7457379d7426690de...
spins property_id: 1e58643b8e3dcc5390a32f48b6bcf30335c7fc8...
bonding property_id: f6443125f7c8d3947e6e6dd9962728d1b3825...
thermo property_id: a510f90b085d90e9dd4c3893d69212c58fb210...
```

2) Determine metal oxidation state



3) Identify documents for metal and molecule with no metal

```
molecule_id: 4fb7c39e64f4e72e59f87c77c6047584-Mg1-2-1
thermo property_id: 198119afbb81aa3b428c13085c545cdv...
```

Mg: charge 2, spin multiplicity 1



BH<sub>2</sub>: charge 0, spin multiplicity 2

```
molecule_id: 933339117efcfcc2c48f94b4d8f6e81c-B1H2-0-2
thermo property_id: e09b691eae49f9ee01e06fca8ef27850..
```

4) Calculate binding properties

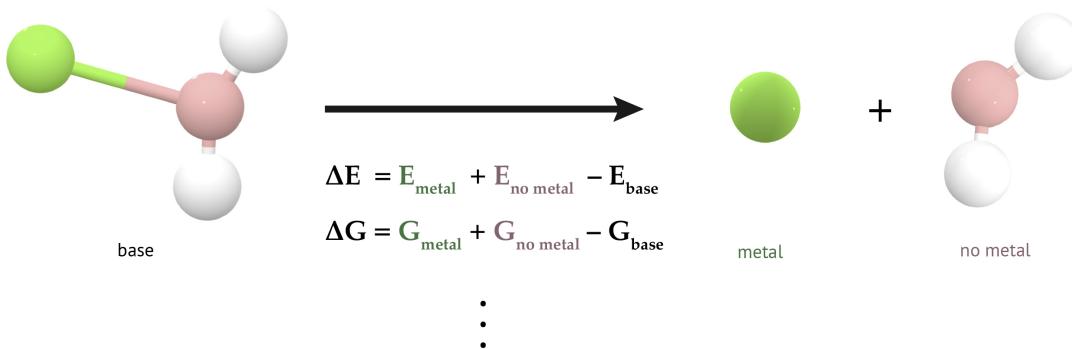


Figure 4: Calculation of metal binding properties in MPCules. 1) For a given molecule, the molecule document, along with atomic partial charge, atomic partial spin (if the molecule is open-shell), bonding, and thermodynamics information, must be available. 2) For each metal in the molecule, the atomic partial charges and spins (if applicable) are used to determine the metal's oxidation state. This specifies what non-bound species will be searched for. 3) Documents for the unbound metal and the molecule without that metal attached (no metal), along with their thermodynamic information, are sought. 4) Metal binding properties can be calculated using the thermodynamics of the base molecule, metal, and no metal.

After the oxidation and spin state of each metal have been determined, the bonding environment around the metal atoms are characterized using previously calculated bonding information (see “Bonding”). For each metal, we then construct a `MoleculeGraph` of the molecule with that metal removed. Using this graph, we search for molecules with the same connectivity and the appropriate charge and spin multiplicity. If appropriate `MoleculeDocs` can be located for both the metal (M in the previous chemical equation) and the molecule without the metal (A), then we calculate the reaction thermodynamics using previously-constructed `MoleculeThermoDocs` (see “Molecular Thermodynamics”).

Atomic partial charges, atomic partial spins, and bonding can all be determined in multiple ways, which means that there are numerous possible combinations that could determine the metal-binding properties of a molecule. However, with the aim of ensuring that the various methods used are as consistent as possible, we currently only allow two combinations of methods to be used. In the first, atomic partial charges, atomic partial spins, and binding are all determined using NBO. In the second, the atomic partial charges and atomic partial spins are both calculated using the Mulliken method, and the bonding is determined using the default method combining OpenBabel with `pymatgen`.

We would like to point out that DFT can struggle to accurately predict the thermochemical properties of single atoms and ions, whether in vacuum or in implicit solvent. This may affect the accuracy of computed binding (free) energies.

## Summary Documents

After all property documents have been constructed, we compile a subset of calculated properties into a single document called a `MoleculeSummaryDoc`. Whereas property documents are uniquely defined by `MPculeID`, solvent medium, and sometimes method, the summary document is uniquely defined only by the `MPculeID`. Properties in the summary document that are not method-dependent are represented as key-value pairs, where the keys are the names of solvents used to calculate the property and the values are the properties calcu-

lated in those implicit solvent media. For properties that are method-dependent, the values are instead key-value pairs, with the keys being various methods and the values being the properties calculated using specific combinations of solvent and method.

## Provenance

As we have noted, data provenance is vital to allow users to verify the accuracy of a calculation and to trace processed data back to the raw data that they are based on. Throughout the construction of MPcules, we include provenance information, allowing users to trace back to individual DFT calculations/tasks.

Already, we have mentioned how provenance information is stored during the construction of associated and collected `MoleculeDocs` (see “Molecules”). In addition, each property document stores the IDs of the other documents used to calculate the relevant properties. For data obtained from a single task - for instance, atomic partial charges - the task ID for that property is stored. For data obtained from other property documents, the property ID is stored. When data for a particular document comes from other documents with different MPculeIDs, then the MPculeIDs of those other documents are also stored. Finally, `MoleculeSummaryDocs` store the property IDs of all of the documents used to construct them, linked to the relevant solvent and/or method through key-value pairs.

## Accessing Molecular Data

The data in MPcules can be accessed in three ways: 1) directly via the Materials Project API; 2) using the high-level Python interface to the Materials Project API, `mp-api`; or 3) via a web app on the Materials Project web site. Here, we briefly describe these means of accessing MPcules data. Further documentation can be found online (see <https://api.materialsproject.org/docs> and <https://docs.materialsproject.org>).

## The Materials Project API

A Materials Project API request begins with a uniform prefix (<https://api.materialsproject.org/>).

All data in MPcules can be accessed via an API endpoint under the /molecules/ root endpoint; for instance, molecules summary documents can be obtained from the endpoint /molecules/summary. Following these endpoints, query parameters can be provided to limit the results of the search.

Because the Materials Project API provides an OpenAPI-compliant specification, it is facile to incorporate this API into software using a variety of web frameworks and programming languages. However, to avoid having to interface with this specification directly, users can also use the `MPRester` class implemented in the `mp-api` Python package. `MPRester` includes straightforward Python interfaces to each of the MPcules API endpoints. For example, to search for a molecule summary document with charge +1 and formula C<sub>2</sub>H<sub>4</sub>, one can write the following Python code:

```
1 from mp_api.client import MPRester
2
3 with MPRester(api_key='<enter your api key>') as mpr:
4     mol_doc = mpr.molecules_summary.search(
5         charge=1,
6         formula="C2 H4"
7     )
```

We note that, in addition to obtaining complete task, molecule, property, and summary documents, we have also provided API endpoints that extract more targeted information. For instance, using the /molecules/tasks/trajectory endpoint, it is possible to extract information from a task related to a geometry optimization trajectory, including the structures, energies, and forces along that trajectory.

## The Molecules Explorer

The new Molecules Explorer web app is built using the `Crystal Toolkit` Python framework for data visualization,<sup>61</sup> as well as suites of custom React JavaScript components (`mp-react-components`) and Plotly Dash components (`dash-mp-components`). The root of the Molecules Explorer presents a search interface for discovering new molecules.

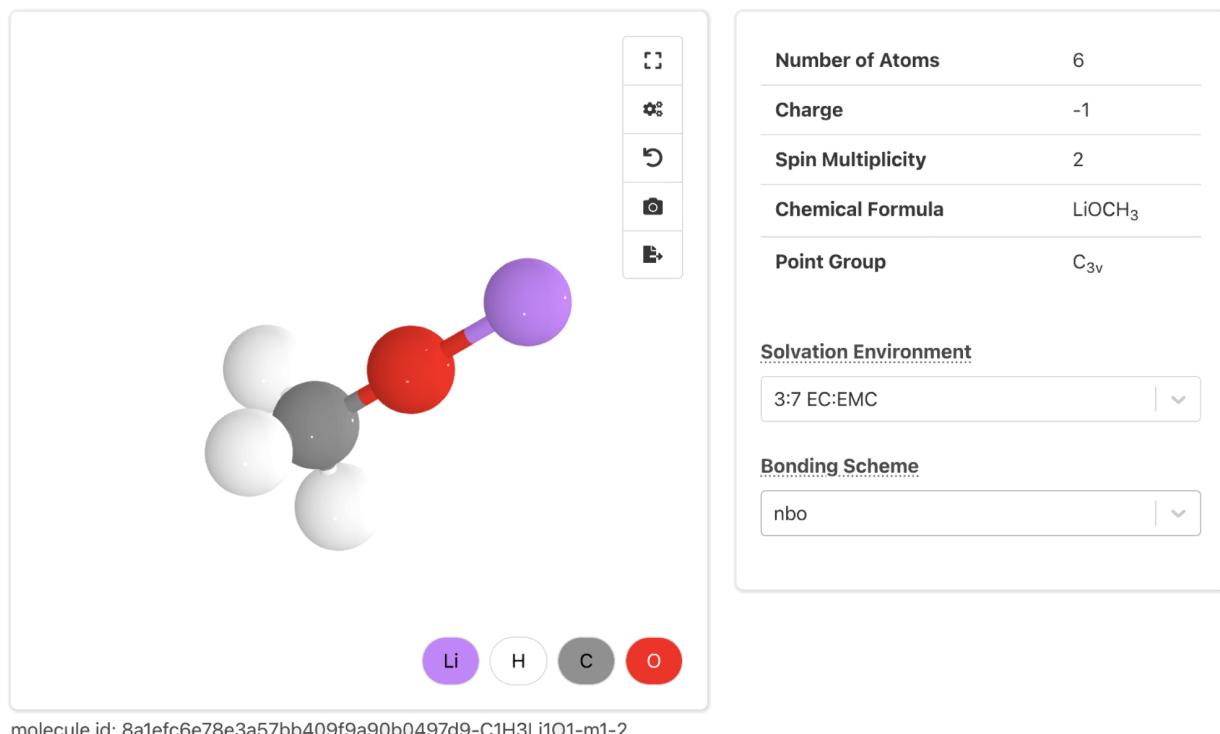


Figure 5: The summary section of the Molecule Details Page.

The Molecule Details Page (Figure 5) visualizes data from the summary document of each molecule. It allows users to explore key computed properties under different solvent media and bonding schemes. At the top, solvent-invariant properties (e.g. number of atoms, charge, and spin multiplicity) are shown alongside a 3D molecular visualization rendered with `Crystal Toolkit`. The solvent medium and bonding scheme can be selected from two drop-down boxes that determine the computed properties displayed on the rest of the page. Below this, a set of property sections are shown that closely map onto the MPcules database schema. Namely, we have created sections for Bonding, Thermodynamic Stability (contain-

ing molecular thermodynamics data), Partial Charges and Spins (containing data on atomic partial charges and atomic partial spins), Vibrations (containing information on vibrational properties), and Redox Stability (containing redox and electrochemical properties). We plan to add sections describing orbital information from NBO and metal binding properties.

Each property section consists of a data tab including the processed data from the summary document, a methods tab describing how the data was obtained from DFT and post-processing, and an API tab describing how users can programmatically access the data. For example, the data tab for the Partial Charges and Spins section (Figure 6) consists of two drop-down menus to select the method for calculating charges and spins, a table of atomic charge and spin values, and a 2D molecular visualization of the molecule. Selecting rows in the table highlights the corresponding atoms in the molecular visualization and shows the total charge and spin of the selected atoms. This provides a map between atoms in the table and their position in the molecular topology. The other property sections each contain unique user interface elements. The Bonding section contains an interactive 2D visualization of bond distances, angles, and dihedrals; the Thermodynamic Stability and Redox Stability sections present tables of properties; and the Vibrations sections contains an interactive simulated IR spectra. At the bottom of the page, after the property sections, the parameters for the selected solvent method are shown.

## The Current State of MPcules

MPcules currently contains data on 172,874 (collected) molecules (248,302 associated molecules) based on 568,004 tasks (Figure 7). Most properties are present for all relevant molecules. Because atomic partial charges and electronic energy are calculated by default for all DFT calculations in Q-Chem, there is at least one partial charge document and one molecular thermodynamics document per molecule. Likewise, there is at least one bonding document per molecule (because bonding can be assessed from an optimized geometry

## Partial Charges and Spins

Data   Methods   API

**Partial Charges Method**

**Partial Spins Method**

Selected atoms: 3, 2, 4.  
Total charge: -1.128  
Total spin: -0.011

| <input type="checkbox"/>            | Element | Partial Charges | Partial Spins |
|-------------------------------------|---------|-----------------|---------------|
| <input type="checkbox"/>            | Li      | -1.15           | 1.023         |
| <input type="checkbox"/>            | O       | 0.9699          | -0.008765     |
| <input checked="" type="checkbox"/> | C       | -1.743          | -0.0052       |
| <input checked="" type="checkbox"/> | H       | 0.3075          | -0.002881     |
| <input checked="" type="checkbox"/> | H       | 0.3075          | -0.00288      |
| <input type="checkbox"/>            | H       | 0.3075          | -0.002873     |

Select atoms to view partial charges and spins.

Figure 6: The Partial Charges and Spins section of a Molecule Detail Page on the Materials Project. An interactive molecule visualization allows users to select atoms and see their atomic partial charges and spins; these are also represented in tabular form.

without any further electronic structure calculations) and at least one atomic partial spins document for each open-shell molecule. While we do not strictly require that optimized structures be validated by performing a vibrational frequency analysis, all molecules currently in MPcules that are not single atoms have been subjected to such analyses. As such, almost all molecules in MPcules have vibrational properties calculated. Other properties - namely natural atomic and molecular orbital properties, redox properties, and metal binding properties - are available only for a subset of molecules, either because these properties require specialized calculations (e.g. NBO analysis must be performed for orbital properties, and single-point calculations at different charges must be performed to calculate vertical redox properties) or because the calculation of certain properties for a given molecule require other molecules with specific structures and charges to be present (e.g. calculating a metal binding energy requires three molecules - the metal ion, the molecule-metal complex, and the same molecule not bound to the metal).

We note that some of the data in MPcules has been previously released in different collections. Specifically, we previously reported the Lithium-Ion Battery Electrolyte (LIBE) dataset,<sup>56</sup> a collection of the properties of 17,190 molecules relevant to electrolyte decomposition and interphase formation in Li-ion batteries with carbonate electrolytes. LIBE was calculated at the  $\omega$ B97X-V/def2-TZVPPD/SMD level of theory. More recently, we released the MAgnesium Dataset of Electrolyte and Interphase ReAgents (MADEIRA),<sup>7</sup> containing properties of 11,502 species relevant to electrolyte degradation and gas evolution in Mg-ion electrolytes consisting of magnesium bis triflimide dissolved in diglyme. In addition to the molecules in LIBE and MADEIRA, MPcules contains molecules relevant to Mg-ion battery electrolytes with tetrahydrofuran electrolytes, as well as large numbers of small organic molecules, the properties of which have been calculated in vacuum and in many cases in water.

Figure 8 details the current composition of the MPcules database. In contrast to many existing molecular datasets, MPcules contains molecules with diverse charges and spin mul-

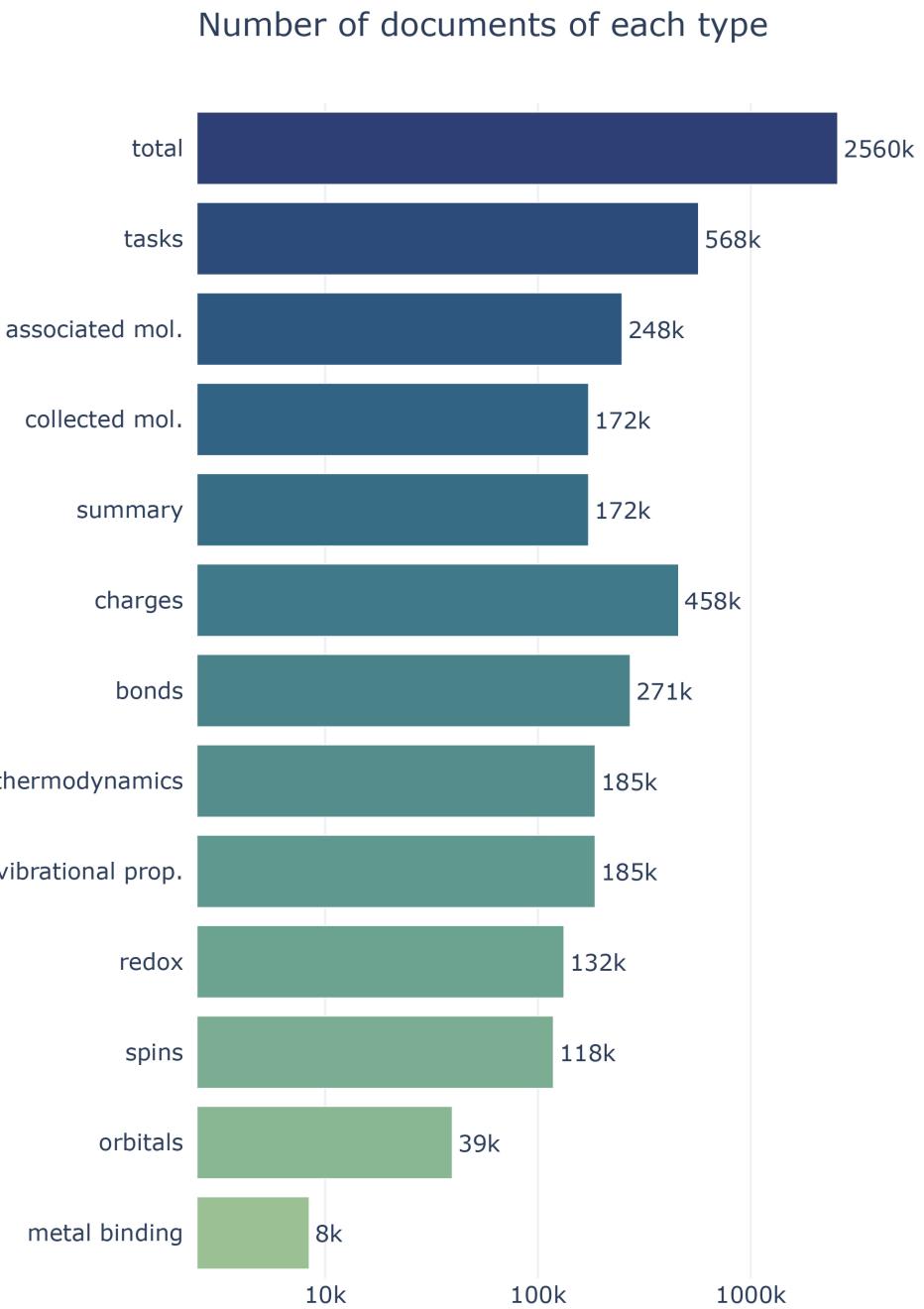


Figure 7: Scale of the current MPcules database in terms of number of documents, broken down by type.

tiplicities (Figure 8a–b). Currently, there are more ions in MPcules (98,480) than neutral molecules (74,394) and more radicals (89,715) than closed-shell molecules (83,159). Most ions have charge  $\pm 1$ , with nontrivial numbers of molecules with charge  $\pm 2$ . A very small number of ions with charge -3 (7) and +3 (6) are also included. These are all single atoms, the properties of which were studied in order to calculate redox properties. Currently, MPcules contains a relatively small number of triplets (2,942); this presents a natural area for dataset expansion.

In terms of elements (Figure 8c), MPcules is skewed towards organic molecules containing C, H, N, and O. In large part because of the previous LIBE and MADEIRA datasets, there are many ( $>10,000$ ) molecules containing F, Li, Mg, and S. While we do believe that MPcules is relatively diverse in terms of elements and chemical formulas, there are obviously many opportunities to expand its coverage through the addition of molecules containing B, P, halogens (e.g. Cl and Br), Si, or transition metals.

## Future Work

Just as the Materials Project has evolved from its initial release in 2011 to today, increasing in scale, scope, and structure, MPcules will continue to develop over time. We have already mentioned types of molecules that we intend to add to MPcules (e.g. transition-metal complexes and triplets). Here, we outline further plans to expand MPcules. We note that while we aim to internally develop the MPcules code(s) and dataset, we welcome user-submitted contributions of data as well as features (in the form of code contributions to `emmet-core`, `emmet-builders`, `emmet-api`, and the other Materials Project packages).

## Calculation Methods and Sources

Currently, MPcules accepts only DFT calculations from Q-Chem. This means that we are presently excluding calculations using high-quality wavefunction methods based on e.g.

## Number of documents with given charge, spin, and element

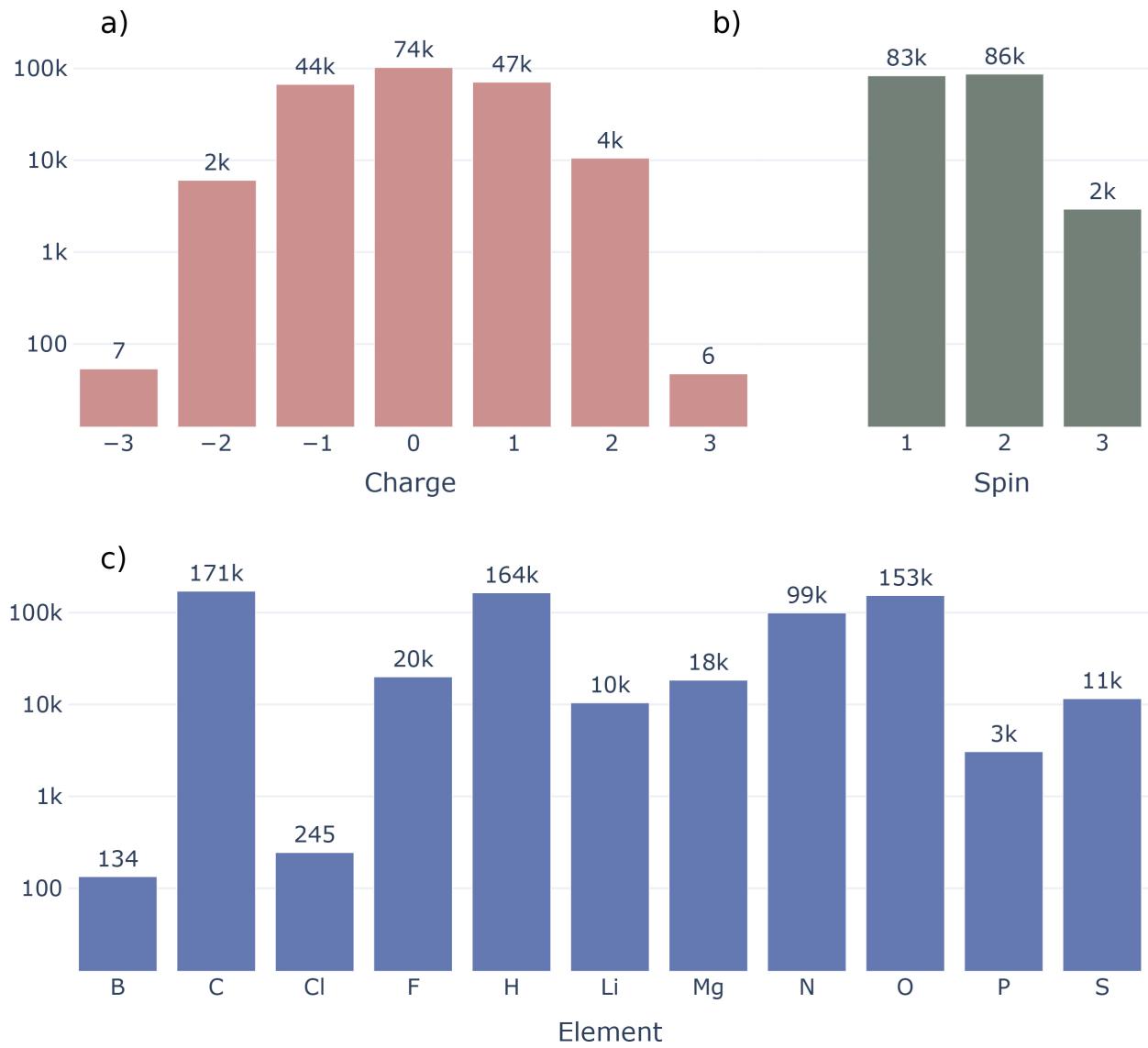


Figure 8: Composition of the MPcules database. a) Number of molecules with different charges; c) number of molecules with different spin multiplicities; c) number of molecules including different elements.

coupled-cluster theory and multireference methods, which might be useful for benchmarking electronic structure methods or for  $\Delta$ -machine learning of electronic energy and other molecular properties. At the same time, we exclude calculations based on semiempirical quantum chemistry methods such as self-consistent extended tight-binding (e.g. GFN2-xTB),<sup>62</sup> which have become increasingly popular for generating large datasets of molecules at low computational cost. Even within the narrower realm of DFT, the restriction to using a single electronic structure code could limit the ease with which users can contribute data to MPcules.

In the future, we intend to create a more flexible interface which can parse and construct molecule and molecule property documents from calculations using a variety of DFT and non-DFT methods with multiple quantum chemistry codes (e.g. xTB,<sup>62</sup> ORCA,<sup>63,64</sup> or NWChem).<sup>65</sup>

## Molecular Properties

MPcules already contains diverse atomic, molecular, and reaction properties. In the future, we aim to expand the properties available, both to aid in chemical analysis and to enable the development of ML methods. In particular, we are interested in expanding properties in two directions: spectroscopy and electronic densities. At present, the only spectra included in MPcules are IR spectra obtained via vibrational analysis. With modest modifications to our existing workflows, we should be able to additionally obtain molecular Raman spectra, including Raman activities and intensities. We also intend to incorporate nuclear magnetic resonance (NMR), including chemical shifts and J-couplings. In terms of charge densities, NBO provides detailed information regarding atomic and hybrid orbitals but does not describe the spatial extent of such orbitals or the total charge density around atoms in a molecule. Inspired by the recently developed charge density dataset included in the Materials Project,<sup>66</sup> we intend to present total molecular charge densities to MPcules users via the Materials Project API and web site, as well as information regarding the electron densities of individual molecular orbitals.

## Conclusions

As chemical research grows increasingly reliant on big data and ML approaches, high-quality and open datasets of molecular properties will become vital cornerstone resources, accelerating the understanding of existing chemical systems and the design of novel functional molecules with optimized properties. MPcules, expanding on the existing Materials Project database, is a database of molecular calculations adhering to FAIR principles. The MPcules database currently contains over 170,000 molecules which can be accessed through an API and featureful web app. MPcules is unique both because it grants users facile access to data and because that data is particularly diverse, containing many charged, open-shell, and metal-coordinated species as well as properties related to molecular bonding, electronic structure, thermodynamics, electrochemistry, vibrations, and reactions. Since MPcules relies on a suite of open source software, it is possible for users to add calculations to MPcules or to develop standalone datasets based on the same underlying schema. We believe that MPcules could serve as a community center for chemical datasets, with collaborative contributions of both code and data from users.

## Conflicts of interest

There are no conflicts to declare.

## Software Availability

The Materials Project software stack used to develop MPcules is publicly available on GitHub:

- `pymatgen`: <https://github.com/materialsproject/pymatgen>
- `custodian`: <https://github.com/materialsproject/custodian>

- `atomate`: <https://github.com/hackingmaterials/atomate>
- `emmet`: <https://github.com/materialsproject/emmet>
- `mp-api`: <https://github.com/materialsproject/api>
- `Crystal Toolkit`: <https://github.com/materialsproject/crystaltoolkit>
- `mp-react-components`: <https://github.com/materialsproject/mp-react-components>
- `dash-mp-components`: <https://github.com/materialsproject/dash-mp-components>

## Data Availability

All data discussed in this work is publicly available through the Materials Project API, which can be accessed directly or via `mp-api`. Most data can also be accessed through the Materials Project web site (<https://materialsproject.org/molecules>).

## Acknowledgements

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## Author Contributions

- E.W.C.S.-S.: Conceptualization, data curation, formal analysis, funding acquisition, investigation, methodology, project administration, software, visualization, writing - original draft, writing - review & editing
- O.A.C.: Funding acquisition, methodology, software, visualization, writing - original draft, writing - review & editing
- S.M.B.: Conceptualization, data curation, formal analysis, funding acquisition, investigation, methodology, writing - review & editing
- J.M.M.: Data curation, methodology, software, supervision, writing - review & editing
- R.Y.: Methodology, software, writing - review & editing
- R.D.G.: Investigation, writing - review & editing
- H.D.P.: Investigation, writing - review & editing
- S.V.: Investigation, writing - review & editing
- P.H.: Data curation, writing - review & editing
- R.K.: Methodology, writing - review & editing
- M.K.H.: Methodology, supervision, writing - review & editing
- K.A.P.: Conceptualization, funding acquisition, project administration, resources, supervision, writing - review & editing

## Supplementary Information

Further details on ranking of levels of theory; composition of MPcules in terms of level of theory; comparison of Mulliken and NBO atomic partial charges and atomic partial spins; description of the MPculeID unique ID format. References:<sup>29,38–43,67–73</sup>

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