```
library(dplyr)
 1
 2
    library(MASS)
    library(glmnet)
    library(randomForest)
    library(e1071)
 5
    library(ggplot2)
 6
 7
    library(reshape)
    library(gridExtra)
 8
 9
    options(expressions = 5e5)
10
11
12
    a = read.csv("pdata.csv")
    dim(a)
13
14
    colnames(a)[dim(a)[2]] = c("Class")
    colMeans(a)
15
    t.data = a
16
17
    # standardize the dataset
18
    t.data[,-dim(t.data)[2]] = scale(t.data[,-dim(t.data)[2]])
19
20
    colMeans(t.data)
21
    apply(t.data, 2, sd)
22
    mean(t.data$Class)
23
    attach(t.data)
24
25
    # data structure and rates
    n1 = dim(t.data %>% filter(Class == 1))[1]
26
    n0 = dim(t.data %>% filter(Class == 0))[1]
27
28
    n = n1 + n0
    p = dim(t.data)[2]-1
29
30
31
    # Modelling factors
32
    iterations = 100
    Dlearn_rate = 0.5
33
34
    sampling.rate = 1
    weight = c("0" = 1/n0, "1" = 1/n1)
35
36
37
    # train and test error rate matrix
38
    train_error = matrix(0, nrow = iterations, ncol = 7)
39
    colnames(train_error) = c("RF", "R-SVM", "Log", "Log-LASSO", "Log-Ridge", "00B", "00Bsd")
40
41
    cv_error = matrix(0, nrow = iterations, ncol = 3)
42
    colnames(cv_error) = c("R-SVM", "Log-LASSO","Log-Ridge")
43
```

```
44
     test error = matrix(0, nrow = iterations, ncol = 5)
     colnames(test_error) = c("RF", "R-SVM", "Log", "Log-LASSO", "Log-Ridge")
45
46
47
    lasso.coef = matrix(0, ncol = iterations, nrow = p+1)
48
    ridge.coef = matrix(0, ncol = iterations, nrow = p+1)
49
50
    # convert to data frame
51
    train_error = data.frame(train_error)
52
    test error = data.frame(test error)
53
54
    # time of cv and fit
55
    time.cv = matrix(0, nrow = iterations, ncol = 3)
56
    colnames(time.cv) = c("SVM", "LASSO", "Ridge")
57
58
    time.fit = matrix(0, nrow = iterations, ncol = 4)
    colnames(time.fit) = c("SVM", "LASSO", "Ridge", "RF")
59
60
    # rf importance
61
    rf.importace = matrix(0, nrow = iterations, ncol = 400)
62
63
64
    # sampling from t.data
65
    sampling = sample(n,n*sampling.rate)
66
    sampling.data = data.frame(t.data[sampling,])
67
    sampling.n = dim(sampling.data)[1]
68
69
    # preparation for lasso and ridge
    X = model.matrix(Class ~., sampling.data)[,-1]
70
71
    y = sampling.data$Class
72
73
74
    # 100 iteration for error rates, time, and coefficients
    for(m in 1:iterations){
75
76
77
78
       # create a training data vector for dividing the data set.
       train = sample(sampling.n, sampling.n*Dlearn_rate)
79
80
81
            = data.frame(sampling.data[train,])
82
       datt = data.frame(sampling.data[-train,])
83
84
       # svm
85
       # record svm cv time
86
       ptm = proc.time()
       tune.svm = tune(svm, as.factor(Class)~., data=dat,
87
                          ranges = list(cost = 10^seq(-2, 2, length.out = 5),
88
89
                                        gamma = 10^seq(-2,2,length.out = 5)), scale = F)
```

```
ptm = proc.time() - ptm
 90
        time.cv[m,1] = ptm["elapsed"]
91
92
93
        # record cv error
 94
        cv error[m,1] = tune.svm$best.performance
        # tune.svm$performances
95
96
        # tune.svm$best.parameters[1]
97
        # record svm fit time
98
        ptm = proc.time()
        # svm.fit = svm(as.factor(Class)~., data = dat,
99
                       cost = tune.svm$best.parameters[1], gamma = tune.svm$best.parameters[2])
100
101
        svm.fit = tune.svm$best.model
        ptm = proc.time() - ptm
102
103
        time.fit[m,1] = ptm["elapsed"]
104
105
        svm.pred = predict(svm.fit, dat, type = "class")
106
        train_error[m,2] = mean(dat[,dim(sampling.data)[2]] != svm.pred)
        # table(dat[,dim(sampling.data)[2]],svm.pred)
107
        svm.pred = predict(svm.fit, datt, type = "class")
108
109
        test error[m,2] = mean(datt[,dim(sampling.data)[2]] != svm.pred)
        # table(datt[,dim(sampling.data)[2]], svm.pred)
110
111
112
        # logistic regression
113
        log.mod = glm(Class ~., data = dat, family = "binomial",
114
                      weights = ifelse(dat$Class == 0, 1/n0, 1/n1))
115
        log.pred = predict(log.mod, newdata = sampling.data[train,], type = "response")
        log.pred = ifelse(log.pred > 0.5, 1, 0)
116
        train error[m,3] = mean( sampling.data[train,dim(sampling.data)[2]]!= log.pred)
117
        log.pred = predict(log.mod, newdata = sampling.data[-train,], type = "response")
118
119
        log.pred = ifelse(log.pred > 0.5, 1, 0)
        test error[m,3] = mean( sampling.data[-train,dim(sampling.data)[2]]!= log.pred)
120
121
122
        # lasso cross validation and tune lambda
123
        # record lasso cv time
124
        ptm = proc.time()
        cv.lasso = cv.glmnet(X[train,], y[train], alpha = 1, family = "binomial",
125
                             intercept = T, type.measure="class",
126
                             weights = ifelse(y[train] == 0, 1/n0, 1/n1))
127
128
        ptm = proc.time() - ptm
129
        time.cv[m,2] = ptm["elapsed"]
130
131
        cv error[m,2] = min(cv.lasso$cvm)
132
        bestlam = cv.lasso$lambda.min
133
        # record lasso fit time
134
135
        ptm = proc.time()
```

```
lasso.mod = glmnet(X[train,], y[train], alpha = 1, family = "binomial",
136
                           intercept = T, lambda = bestlam,
137
                           standardize = F)
138
139
        ptm = proc.time() - ptm
140
        time.fit[m,2] = ptm["elapsed"]
141
142
        lasso.coef[,m] = coef(lasso.mod)[,1]
143
        lasso.pred = predict(lasso.mod, s = bestlam, newx = X[train,], type ="class")
144
        train_error[m,4] = mean(y[train] != lasso.pred)
        lasso.pred = predict(lasso.mod, s = bestlam, newx = X[-train,], type="class",)
145
        test error[m,4] = mean(y[-train] != lasso.pred)
146
147
        # ridge cross validation and tune lambda
148
        # record ridge cv time
149
        ptm = proc.time()
150
        cv.ridge = cv.glmnet(X[train,], y[train], alpha = 0, family = "binomial",
151
                             intercept = T, type.measure="class",
152
                             weights = ifelse(y[train] == 0, 1/n0, 1/n1))
153
154
        ptm = proc.time() - ptm
        time.cv[m,3] = ptm["elapsed"]
155
156
157
        cv_error[m,3] = min(cv.ridge$cvm)
        bestlam = cv.ridge$lambda.min
158
159
160
        # record ridge fit time
161
        ptm = proc.time()
        ridge.mod = glmnet(X[train,], y[train], alpha = 0, family = "binomial",
162
                           intercept = T, lambda = bestlam,
163
                           standardize = F)
164
        ptm = proc.time() - ptm
165
        time.fit[m,3] = ptm["elapsed"]
166
167
        ridge.coef[,m] = as.matrix(coef(ridge.mod))
168
        ridge.pred = predict(ridge.mod, s = bestlam, newx = X[train,], type = "class")
169
        train error[m,5] = mean(y[train] != ridge.pred)
170
        ridge.pred = predict(ridge.mod, s = bestlam, newx = X[-train,], type = "class")
171
        test_error[m,5] = mean(y[-train] != ridge.pred)
172
173
174
        #random forest with 500 bootstrapped trees
175
        ptm = proc.time()
176
        rf = randomForest(x = sampling.data[train,-dim(sampling.data)[2]],
177
                          y = as.factor(sampling.data[train,dim(sampling.data)[2]]), data =
      sampling.data[train,],
178
                          mtry = sqrt(p), classwt = weight)
        ptm = proc.time() - ptm
179
        time.fit[m,4] = ptm["elapsed"]
180
```

```
181
       rf.pred = predict(rf, sampling.data[train,-dim(sampling.data)[2]], type = "class")
182
       train_error[m,1] = mean(sampling.data[train,dim(sampling.data)[2]] != rf.pred)
183
       train_error[m,6] = mean(rf$err.rate[,1])
184
185
       train error[m,7] = sd(rf$err.rate[,1])
       rf.pred = predict(rf, sampling.data[-train,], type = "class")
186
187
       test error[m,1] = mean(sampling.data[-train,dim(sampling.data)[2]] != rf.pred)
188
189
190
191
192
     193
     194
     # store error rate and coef
195
196
     write.csv(ridge.coef, file = "D50_rdige_coef.csv")
197
     write.csv(lasso.coef, file = "D50 lasso coef.csv")
198
     write.csv(cv error, file = "D50 cv error.csv")
199
200
     write.csv(test error, file = "D50 test error.csv")
201
     write.csv(train_error, file = "D50_train_error.csv")
202
203
     write.csv(time.cv, file = "D50 time cv.csv")
204
     write.csv(time.fit, file = "D50 time fit.csv")
205
206
     # read csv files of project results
     D5.r.coef = read.csv("D50 rdige coef.csv")
207
208
     D5.1.coef = read.csv("D50 lasso coef.csv")
209
210
     D5.cv.error = read.csv("D50 cv error.csv")
     D5.test.error = read.csv("D50 test error.csv")
211
212
     D5.train.error = read.csv("D50 train error.csv")
213
     colnames(D5.train.error)[7:8] = c("RF.OOB", "RF.OOBsd")
214
215
     D5.time.cv = read.csv("D50 time cv.csv")
     D5.time.fit = read.csv("D50 time fit.csv")
216
217
218
     D9.r.coef = read.csv("D90 rdige coef.csv")
     D9.1.coef = read.csv("D90 lasso coef.csv")
219
220
     D9.cv.error = read.csv("D90 cv error.csv")
221
     D9.test.error = read.csv("D90 test error.csv")
222
223
     D9.train.error = read.csv("D90 train error.csv")
224
     colnames(D9.train.error)[7:8] = c("RF.00B", "RF.00Bsd")
225
226
     D9.time.cv = read.csv("D90 time cv.csv")
```

```
227
     D9.time.fit = read.csv("D90 time fit.csv")
228
229
     # boxplot of error rates for each nlearn
230
     f1_1 = ggplot(melt(D5.train.error[,2:7]), aes(x = variable, y = value, color = variable)) +
231
       geom_boxplot() + ylim(0,0.25) + theme(legend.position="none") +
     scale color brewer(palette="Dark2") +
232
       labs(x = element blank(), y = "Train Error Rate", title =
     expression(n[learn]~"="~n/2~~Train~Error~Rate))
     f1_2 = ggplot(melt(D5.test.error[,2:6]), aes(x = variable, y = value, color = variable)) +
233
       geom_boxplot() + ylim(0,0.25) + theme(legend.position="none") +
234
     scale color brewer(palette="Dark2") +
235
       labs(x = element_blank(), y = "Test Error Rate", title =
     expression(n[learn]~"="~n/2~~Test~Error~Rate))
     f1_3 = ggplot(melt(D5.cv.error[,2:4]), aes(x = variable, y = value, color = variable)) +
236
       geom boxplot() + ylim(0,0.25) + theme(legend.position="none") +
237
     scale_color_brewer(palette="Dark2") +
       labs(x = element_blank(), y = "CV Error Rate", title =
238
     expression(n[learn]~"="~n/2~~CV~Error~Rate))
239
     f1 4 = ggplot(melt(D9.train.error[,2:7]), aes(x = variable, y = value, color = variable)) +
240
       geom_boxplot() + ylim(0,0.25) + theme(legend.position="none") +
241
     scale_color_brewer(palette="Dark2") +
242
       labs(x = element blank(), y = "Train Error Rate", title =
     expression(n[learn]~"="~0.9~n~~Train~Error~Rate))
243
     f1_5 = ggplot(melt(D9.test.error[,2:6]), aes(x = variable, y = value, color = variable)) +
244
       geom boxplot() + ylim(0,0.25) + theme(legend.position="none") +
     scale color brewer(palette="Dark2") +
       labs(x = element blank(), y = "Test Error Rate", title =
245
     expression(n[learn]~"="~0.9~n~~Test~Error~Rate))
     f1_6 = ggplot(melt(D9.cv.error[,2:4]), aes(x = variable, y = value, color = variable)) +
246
       geom boxplot() + ylim(0,0.25) + theme(legend.position="none") +
247
     scale color brewer(palette="Dark2") +
       labs(x = element_blank(), y = "CV Error Rate", title =
248
     expression(n[learn]~"="~0.9~n~~CV~Error~Rate))
     print(f1 3)
249
250
     f1.1 = grid.arrange(f1_1, f1_2, f1_3, nrow = 1, widths = c(1.5, 1.5, 1))
251
     f1.2 = grid.arrange(f1_4, f1_5, f1_6, nrow = 1, widths = c(1.5, 1.5, 1))
252
253
     # cv ridge error
254
     cv.ridge$lambda
255
     length(cv.ridge$lambda)
256
     which.min(cv.ridge$cvm)
257
258
     cv.ridge.coef = matrix(0, nrow = length(cv.ridge$lambda), ncol = 1)
     for (i in 1:length(cv.ridge$lambda)) {
259
       cv.ridge.coef[i,] = sqrt(sum(coef(cv.ridge, s = cv.ridge$lambda[i])[-1,]^2))
260
```

```
261
262
      cv.ridge.rate.coef = round(cv.ridge.coef/cv.ridge.coef[length(cv.ridge$lambda),1],3)
     cv.ridge.error.and.rate.coef = data.frame(cbind(cv.ridge.rate.coef,cv.ridge$cvm))
263
264
265
     # cv lasso error
266
     length(cv.lasso$lambda)
267
     which.min(cv.lasso$cvm)
268
     cv.lasso.coef = matrix(0, nrow = length(cv.lasso$lambda), ncol = 1)
269
     for (j in 1:length(cv.lasso$lambda)) {
       cv.lasso.coef[j,] = sqrt(sum(coef(cv.lasso, s = cv.lasso$lambda[j])[-1,]^2))
270
     }
271
272
      cv.lasso.rate.coef = round(cv.lasso.coef/cv.lasso.coef[length(cv.lasso$lambda),1],3)
      cv.lasso.error.and.rate.coef = data.frame(cbind(cv.lasso.rate.coef,cv.lasso$cvm))
273
274
275
     D9.cv.lasso.error.and.rate.coef = read.csv("D90 cv.lasso.error.and.rate.coef.csv")
276
     D9.cv.ridge.error.and.rate.coef = read.csv("D90_cv.ridge.error.and.rate.coef.csv")
277
278
     # svm cv error rate
279
      cv.svm.error = data.frame(tune.svm$performances)
280
     D9.cv.svm.error = read.csv("D9 cv.svm.error.csv")
281
282
      # plot cv error rate for lasso, ridge, and svm
     f2 1 = ggplot() +
283
284
        geom line(data = cv.lasso.error.and.rate.coef, aes(x = X1, y = X2, color = "LASSO")) +
285
        geom_point(data = cv.lasso.error.and.rate.coef, aes(x = X1[which.min(X2)],
286
                                                             y = min(X2), color = "LASSO")) +
        geom line(data = cv.ridge.error.and.rate.coef, aes(x = X1, y = X2, color = "Ridge")) +
287
        geom_point(data = cv.ridge.error.and.rate.coef, aes(x = X1[which.min(X2)],
288
                                                             y = min(X2), color = "Ridge")) +
289
290
       labs(x = "L2 Norm Beta Hat Ratio", y = "CV Error Rate",
             title = expression(n[learn]~"="~n/2~~CV~LASSO~and~Ridge~Error~Rate)) +
291
        scale color manual(name = element blank(), values = c("LASSO" = "red", "Ridge" = "blue")) +
292
293
       ylim(0,.6)
      print(f2_1)
294
     f2 2 = ggplot(data = cv.svm.error, aes(as.factor(cost), as.factor(gamma), fill = error)) +
295
296
        geom tile()+
        labs(x = "cost", y = "gamma",
297
             title = expression(n[learn]~"="~n/2~~CV~SVM~Error~Rate),fill = "CV Error Rate")
298
299
300
        geom_line(data = D9.cv.lasso.error.and.rate.coef, aes(x = X1, y = X2, color = "LASSO")) +
301
        geom point(data = cv.lasso.error.and.rate.coef, aes(x = X1[which.min(X2)],
302
                                                             y = min(X2), color = "LASSO")) +
303
        geom_line(data = D9.cv.ridge.error.and.rate.coef, aes(x = X1, y = X2, color = "Ridge")) +
        geom_point(data = D9.cv.ridge.error.and.rate.coef, aes(x = X1[which.min(X2)],
304
                                                             y = min(X2), color = "Ridge")) +
305
        labs(x = "L2 Norm Beta Hat Ratio", y = "CV Error Rate",
306
```

```
307
             title = expression(n[learn]~"="~0.9~n~~CV~LASSO~and~Ridge~Error~Rate)) +
        scale color manual(name = element blank(), values = c("LASSO" = "red", "Ridge" = "blue")) +
308
309
        ylim(0,.6)
310
     f2_4 = ggplot(data = D9.cv.svm.error, aes(as.factor(cost), as.factor(gamma), fill = error)) +
311
       geom tile()+
        labs(x = "cost", y = "gamma",
312
313
             title = expression(n[learn]~"="~0.9~n~~CV~SVM~Error~Rate),fill = "CV Error Rate")
314
     f2 = grid.arrange(f2_1, f2_2, f2_3, f2_4, nrow = 2, widths = c(1,1))
315
316
     # time analysis
317
     colMeans(D5.time.cv)
318
     apply(D5.time.cv, 2, sd)
319
     colMeans(D9.time.cv)
     apply(D9.time.cv, 2, sd)
320
321
322
     colMeans(D5.time.fit)
323
     apply(D5.time.fit, 2, sd)
      colMeans(D9.time.fit)
324
325
      apply(D9.time.fit, 2, sd)
326
327
     colMeans(D5.test.error)
328
     apply(D5.test.error, 2, sd)
329
      colMeans(D9.test.error)
330
     apply(D9.test.error, 2, sd)
331
332
      # variable importance
333
     D5.1.coef = D5.1.coef[-1,-1]
     D5.1.variable.importance = data.frame(t(abs(rowMeans(D5.1.coef))))
334
     sort(D5.1.variable.importance, decreasing = T)[1:10]
335
336
337
     D5.r.coef = D5.r.coef[-1,-1]
338
     D5.r.variable.importance = data.frame(t(abs(rowMeans(D5.r.coef))))
339
     sort(D5.r.variable.importance, decreasing = T)[1:10]
340
341
     D5.rf.variable.importance = data.frame(t(read.csv("D5 rf.variable.importance.csv")[-1]))
     sort(D5.rf.variable.importance, decreasing = T)[1:10]
342
343
344
     D9.1.coef = D9.1.coef[-1,-1]
345
     D9.1.variable.importance = data.frame(t(abs(rowMeans(D9.1.coef))))
346
     sort(D9.1.variable.importance, decreasing = T)[1:10]
347
348
     D9.r.coef = D9.r.coef[-1,-1]
349
     D9.r.variable.importance = data.frame(t(abs(rowMeans(D9.r.coef))))
350
     sort(D9.r.variable.importance, decreasing = T)[1:10]
351
352
     D9.rf.variable.importance = data.frame(t(read.csv("D9_rf.variable.importance.csv")[-1]))
```

```
353
      sort(D9.rf.variable.importance, decreasing = T)[1:10]
354
355
      # names of important variables
356
      important.variables = rbind(names(sort(D5.1.variable.importance, decreasing = T)[1:10]),
357
     names(sort(D5.r.variable.importance, decreasing = T)[1:10]),
      names(sort(D5.rf.variable.importance, decreasing = T)[1:10]),
358
359
     names(sort(D9.1.variable.importance, decreasing = T)[1:10]),
360
     names(sort(D9.r.variable.importance, decreasing = T)[1:10]),
361
     names(sort(D9.rf.variable.importance, decreasing = T)[1:10]))
      write.csv(important.variables, file = "important.variables.csv")
362
363
364
     f3_1 = ggplot(melt(D5.1.variable.importance), aes(x = variable, y = value, color = variable))
365
        geom bar(stat="identity") + ylim(0,1) + theme(legend.position="none")+
366
367
        labs(x = element_blank(), y = "Absolute Value of Coefficients",
             title = expression(n[learn]~"="~n/2~~LASSO~Varible~Importance)) +
368
        theme(axis.text.x=element_blank(), axis.ticks.x=element_blank())
369
      f3 2 = ggplot(melt(D5.r.variable.importance), aes(x = variable, y = value, color = variable))
370
        geom_bar(stat="identity") + ylim(0,1) + theme(legend.position="none")+
371
372
        labs(x = element blank(), y = "Absolute Value of Coefficients",
373
             title = expression(n[learn]~"="~n/2~~Ridge~Varible~Importance)) +
374
        theme(axis.text.x=element blank(), axis.ticks.x=element blank())
375
     f3_3 = ggplot(melt(D5.rf.variable.importance), aes(x = variable, y = value, color = variable))
        geom bar(stat="identity") + ylim(0,20) + theme(legend.position="none")+
376
        labs(x = element blank(), y = "Variable Importance",
377
             title = expression(n[learn]~"="~n/2~~RF~Varible~Importance)) +
378
379
        theme(axis.text.x=element blank(), axis.ticks.x=element blank())
      f3 4 = ggplot(melt(D9.1.variable.importance), aes(x = variable, y = value, color = variable))
380
        geom_bar(stat="identity") + ylim(0,1) + theme(legend.position="none")+
381
382
        labs(x = element blank(), y = "Absolute Value of Coefficients",
             title = expression(n[learn]~"="~0.9~n~~LASSO~Varible~Importance)) +
383
384
        theme(axis.text.x=element_blank(), axis.ticks.x=element_blank())
     f3_5 = ggplot(melt(D9.r.variable.importance), aes(x = variable, y = value, color = variable))
385
386
        geom bar(stat="identity") + ylim(0,1) + theme(legend.position="none")+
        labs(x = element_blank(), y = "Absolute Value of Coefficients",
387
388
             title = expression(n[learn]~"="~0.9~n~~Ridge~Varible~Importance)) +
389
        theme(axis.text.x=element_blank(), axis.ticks.x=element_blank())
390
      f3_6 = ggplot(melt(D9.rf.variable.importance), aes(x = variable, y = value, color = variable))
        geom bar(stat="identity") + ylim(0,20) + theme(legend.position="none")+
391
        labs(x = element_blank(), y = "Variable Importance",
392
```

```
393
             title = expression(n[learn]~"="~0.9~n~~RF~Varible~Importance)) +
394
        theme(axis.text.x=element blank(), axis.ticks.x=element blank())
      f3 = grid.arrange(f3_1, f3_2, f3_3, f3_4, f3_5, f3_6, nrow = 2)
395
396
397
      D5.importance = matrix(0,nrow = 400,ncol = 6)
      D5.importance[,1:6] = cbind(t(D5.1.variable.importance)[,1], t(D5.r.variable.importance)[,1],
398
399
                            t(D5.rf.variable.importance)[,1],t(D9.1.variable.importance)[,1],
400
                            t(D9.r.variable.importance)[,1],
401
                            t(D9.rf.variable.importance)[,1])
402
      colMeans(D5.importance)
     D9.1.variable.importance = data.frame(t(abs(rowMeans(D9.1.coef))))
403
404
      sort(D9.1.variable.importance, decreasing = T)[1:10]
405
     D9.r.coef = D9.r.coef[-1,-1]
406
     D9.r.variable.importance = data.frame(t(abs(rowMeans(D9.r.coef))))
407
408
     sort(D9.r.variable.importance, decreasing = T)[1:10]
409
     D9.rf.variable.importance = data.frame(t(read.csv("D9_rf.variable.importance.csv")[-1]))
410
     sort(D9.rf.variable.importance, decreasing = T)[1:10]
411
412
413
414
     x = rep(1:20,20)
415
     y = c(rep(1,20), rep(2,20), rep(3,20), rep(4,20), rep(5,20),
416
            rep(6,20),rep(7,20),rep(8,20),rep(9,20),rep(10,20),
417
            rep(11,20),rep(12,20),rep(13,20),rep(14,20),rep(15,20),
418
            rep(16,20),rep(17,20),rep(18,20),rep(19,20),rep(20,20))
419
      w = data.frame(cbind(x,y,D5.importance[,1:6]))
420
     f5_1 = ggplot(w, aes(x = x, y = y, fill = w[,3])) +
421
422
       geom tile() + labs(x = "X pixel", y = "Y pixel",
423
                        title = "n/2, Estimated Position of Nucleus by LASSO", fill = "V.Imp")
     f5 2 = ggplot(w, aes(x = x, y = y, fill = w[,4])) +
424
425
        geom_tile() + labs(x = "X pixel", y = "Y pixel",
426
                           title = "n/2, Estimated Position of Nucleus by Ridge", fill = "V.Imp")
427
     f5 \ 3 = ggplot(w, aes(x = x, y = y, fill = w[,5])) +
        geom tile() + labs(x = "X pixel", y = "Y pixel",
428
                           title = "n/2, Estimated Position of Nucleus by RF",fill = "V.Imp")
429
430
     f5_4 = ggplot(w, aes(x = x, y = y, fill = w[,6])) +
431
       geom tile() + labs(x = "X pixel", y = "Y pixel",
432
                           title = "0.9n, Estimated Position of Nucleus by LASSO", fill = "V.Imp")
433
     f5 5 = ggplot(w, aes(x = x, y = y, fill = w[,7])) +
434
        geom_tile() + labs(x = "X pixel", y = "Y pixel",
435
                           title = "0.9n, Estimated Position of Nucleus by Ridge", fill = "V.Imp")
     f5_6 = ggplot(w, aes(x = x, y = y, fill = w[,8])) +
436
        geom tile() + labs(x = "X pixel", y = "Y pixel",
437
                           title = "0.9n, Estimated Position of Nucleus by RF", fill = "V.Imp")
438
```

```
f5 = grid.arrange(f5_1, f5_2, f5_3, f5_4, f5_5, f5_6, nrow = 2)
439
440
441
442
     # two test error rate difference t.test
443
     test.error = cbind(D5.test.error, D9.test.error[,-1])
444
     test.error.difference = matrix(0, nrow = 100, ncol = 5)
445
     test.error.difference = test.error[,2:6] - test.error[,7:11]
446
     t.test(test.error.difference$RF, mu = 0)
     t.test(test.error.difference$R.SVM, mu = 0)
447
     t.test(test.error.difference$Log, mu = 0)
448
     t.test(test.error.difference$Log.LASSO, mu = 0)
449
450
     t.test(test.error.difference$Log.Ridge, mu = 0)
451
```