Grading Multiple Choice exams at the DPECS

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Method

Risbo's method

Grades are calculated from score using a single linear interpolation between the point of the passing grade, P_1 , and the highest possible grade, P_2 . The smallest score of passing the exam has to fulfil the criterion of at least 55% knowledge, that is, 55% correct questions after guessing correction. The calculated passing score will to be rounded up.

For example, if we have n = 40 questions with 4 choices, the guessing correction is set to $c_g = 40/4 = 10$. With a passing criterion $k_p = .55$ and a passing grade $g_p = 5.5$, the passing score s_p is:

$$s_p = k_p(n - c_q) + c_q = .55(40 - 10) + 10 = 26.5 \rightarrow 27$$

Thus, if the highest possible grade is $g_h = 10$, the interpolation used the following points:

$$P_1 = (s_p, g_p) = (27, 5.5)$$

$$P_2 = (n, q_h) = (40, 10)$$

Remindo's method

Remindo's method¹ is somewhat different from the method used by Risbo:

- 1. If answer option of some questions post hoc exluded for the test, the guessing correction will be accordingly adapted.
- 2. For the passing score will be be rounded up. With the example above, interpolation uses the point $P_1 = (26.5, 5.5)$
- 3. The method uses a bi-liniear interpolation:

¹Please note that I have only access to the grades of a few exams and I don't know whether that applies to all Remindo exam.

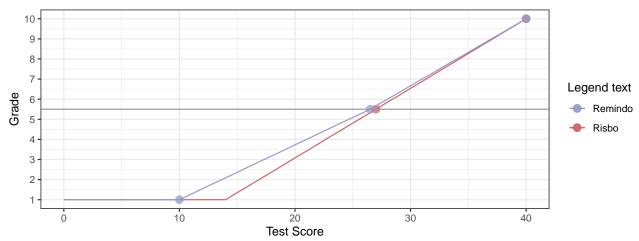
Grading tables

MC exam with 40 questions and 4 choises

Risbo's method:

$$grade = \begin{cases} -3.846 + 0.346 \cdot score & \text{if } score > 14\\ 1 & \text{if } score \leq 14 \end{cases}$$

$$grade = \begin{cases} -3.333 + 0.333 \cdot score & \text{if } score \geq 26.5 \\ -1.727 + 0.273 \cdot score & \text{if } 10 < score < 26.5 \\ 1 & \text{if } score \leq 10 \end{cases}$$



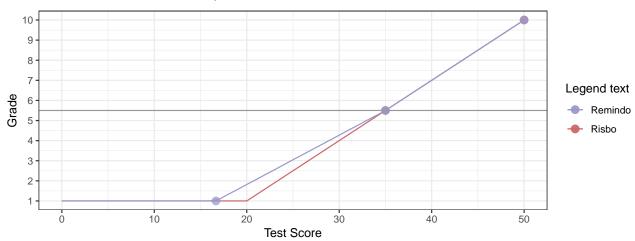
score.1	risbo.1	remindo.1	score.2	risbo.2	remindo.2
1	1.00	1.00	21	3.42	4.00
2	1.00	1.00	22	3.77	4.27
3	1.00	1.00	23	4.12	4.55
4	1.00	1.00	24	4.46	4.82
5	1.00	1.00	25	4.81	5.09
6	1.00	1.00	26	5.15	5.36
7	1.00	1.00	27	5.50	5.67
8	1.00	1.00	28	5.85	6.00
9	1.00	1.00	29	6.19	6.33
10	1.00	1.00	30	6.54	6.67
11	1.00	1.27	31	6.88	7.00
12	1.00	1.55	32	7.23	7.33
13	1.00	1.82	33	7.58	7.67
14	1.00	2.09	34	7.92	8.00
15	1.35	2.36	35	8.27	8.33
16	1.69	2.64	36	8.62	8.67
17	2.04	2.91	37	8.96	9.00
18	2.38	3.18	38	9.31	9.33
19	2.73	3.45	39	9.65	9.67
20	3.08	3.73	40	10.00	10.00

${ m MC}$ exam with 50 questions and 3 choises

Risbo's method:

$$grade = \begin{cases} -5 + 0.3 \cdot score & \text{if } score > 20 \\ 1 & \text{if } score \leq 20 \end{cases}$$

$$grade = \begin{cases} -5 + 0.3 \cdot score & \text{if } score \geq 35 \\ -3.091 + 0.245 \cdot score & \text{if } 16.67 < score < 35 \\ 1 & \text{if } score \leq 16.67 \end{cases}$$



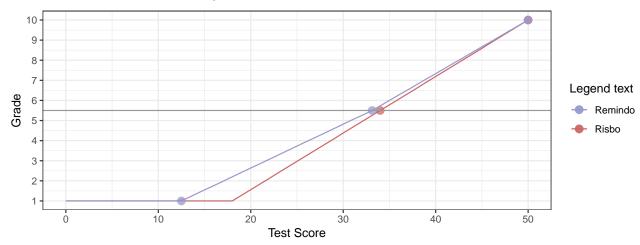
score.1	risbo.1	remindo.1	score.2	risbo.2	remindo.2	score.3	risbo.3	remindo.3
1	1	1.00	21	1.3	2.06	41	7.3	7.3
2	1	1.00	22	1.6	2.31	42	7.6	7.6
3	1	1.00	23	1.9	2.55	43	7.9	7.9
4	1	1.00	24	2.2	2.80	44	8.2	8.2
5	1	1.00	25	2.5	3.05	45	8.5	8.5
6	1	1.00	26	2.8	3.29	46	8.8	8.8
7	1	1.00	27	3.1	3.54	47	9.1	9.1
8	1	1.00	28	3.4	3.78	48	9.4	9.4
9	1	1.00	29	3.7	4.03	49	9.7	9.7
10	1	1.00	30	4.0	4.27	50	10.0	10.0
11	1	1.00	31	4.3	4.52	NA	NA	NA
12	1	1.00	32	4.6	4.76	NA	NA	NA
13	1	1.00	33	4.9	5.01	NA	NA	NA
14	1	1.00	34	5.2	5.25	NA	NA	NA
15	1	1.00	35	5.5	5.50	NA	NA	NA
16	1	1.00	36	5.8	5.80	NA	NA	NA
17	1	1.08	37	6.1	6.10	NA	NA	NA
18	1	1.33	38	6.4	6.40	NA	NA	NA
19	1	1.57	39	6.7	6.70	NA	NA	NA
20	1	1.82	40	7.0	7.00	NA	NA	NA

MC exam with 50 questions and 4 choises

Risbo's method:

$$grade = \begin{cases} -4.062 + 0.281 \cdot score & \text{if } score > 18 \\ 1 & \text{if } score \leq 18 \end{cases}$$

$$grade = \begin{cases} -3.333 + 0.267 \cdot score & \text{if } score \ge 33.12 \\ -1.727 + 0.218 \cdot score & \text{if } 12.5 < score < 33.12 \\ 1 & \text{if } score \le 12.5 \end{cases}$$



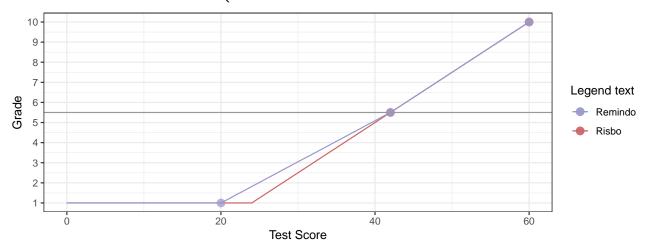
score.1	risbo.1	remindo.1	score.2	risbo.2	remindo.2	score.3	risbo.3	remindo.3
1	1.00	1.00	21	1.84	2.85	41	7.47	7.60
2	1.00	1.00	22	2.12	3.07	42	7.75	7.87
3	1.00	1.00	23	2.41	3.29	43	8.03	8.13
4	1.00	1.00	24	2.69	3.51	44	8.31	8.40
5	1.00	1.00	25	2.97	3.73	45	8.59	8.67
6	1.00	1.00	26	3.25	3.95	46	8.88	8.93
7	1.00	1.00	27	3.53	4.16	47	9.16	9.20
8	1.00	1.00	28	3.81	4.38	48	9.44	9.47
9	1.00	1.00	29	4.09	4.60	49	9.72	9.73
10	1.00	1.00	30	4.38	4.82	50	10.00	10.00
11	1.00	1.00	31	4.66	5.04	NA	NA	NA
12	1.00	1.00	32	4.94	5.25	NA	NA	NA
13	1.00	1.11	33	5.22	5.47	NA	NA	NA
14	1.00	1.33	34	5.50	5.73	NA	NA	NA
15	1.00	1.55	35	5.78	6.00	NA	NA	NA
16	1.00	1.76	36	6.06	6.27	NA	NA	NA
17	1.00	1.98	37	6.34	6.53	NA	NA	NA
18	1.00	2.20	38	6.62	6.80	NA	NA	NA
19	1.28	2.42	39	6.91	7.07	NA	NA	NA
20	1.56	2.64	40	7.19	7.33	NA	NA	NA

MC exam with 60 questions and 3 choises

Risbo's method:

$$grade = \begin{cases} -5 + 0.25 \cdot score & \text{if } score > 24 \\ 1 & \text{if } score \leq 24 \end{cases}$$

$$grade = \begin{cases} -5 + 0.25 \cdot score & \text{if } score \ge 42 \\ -3.091 + 0.205 \cdot score & \text{if } 20 < score < 42 \\ 1 & \text{if } score \le 20 \end{cases}$$



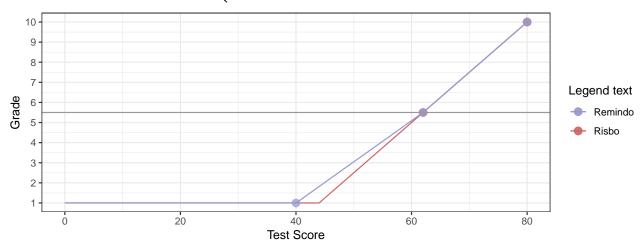
score.1	risbo.1	remindo.1	score.2	risbo.2	remindo.2	score.3	risbo.3	remindo.3
1	1	1	21	1.00	1.20	41	5.25	5.30
2	1	1	22	1.00	1.41	42	5.50	5.50
3	1	1	23	1.00	1.61	43	5.75	5.75
4	1	1	24	1.00	1.82	44	6.00	6.00
5	1	1	25	1.25	2.02	45	6.25	6.25
6	1	1	26	1.50	2.23	46	6.50	6.50
7	1	1	27	1.75	2.43	47	6.75	6.75
8	1	1	28	2.00	2.64	48	7.00	7.00
9	1	1	29	2.25	2.84	49	7.25	7.25
10	1	1	30	2.50	3.05	50	7.50	7.50
11	1	1	31	2.75	3.25	51	7.75	7.75
12	1	1	32	3.00	3.45	52	8.00	8.00
13	1	1	33	3.25	3.66	53	8.25	8.25
14	1	1	34	3.50	3.86	54	8.50	8.50
15	1	1	35	3.75	4.07	55	8.75	8.75
16	1	1	36	4.00	4.27	56	9.00	9.00
17	1	1	37	4.25	4.48	57	9.25	9.25
18	1	1	38	4.50	4.68	58	9.50	9.50
19	1	1	39	4.75	4.89	59	9.75	9.75
20	1	1	40	5.00	5.09	60	10.00	10.00

MC exam with 80 questions and 2 choises

Risbo's method:

$$grade = \begin{cases} -10 + 0.25 \cdot score & \text{if } score > 44 \\ 1 & \text{if } score \leq 44 \end{cases}$$

$$grade = \begin{cases} -10 + 0.25 \cdot score & \text{if } score \ge 62 \\ -7.182 + 0.205 \cdot score & \text{if } 40 < score < 62 \\ 1 & \text{if } score \le 40 \end{cases}$$



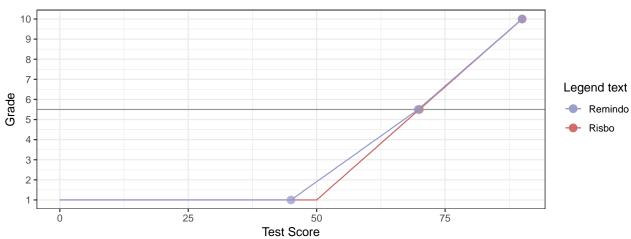
score.1	risbo.1	remindo.1 sco	re.2	risbo.2	remindo.2 so	ore.3	risbo.3	remindo.3 sco	ore.4	risbo.4	remindo.4
1	1	1	21	1	1	41	1.00	1.20	61	5.25	5.30
2	1	1	22	1	1	42	1.00	1.41	62	5.50	5.50
3	1	1	23	1	1	43	1.00	1.61	63	5.75	5.75
4	1	1	24	1	1	44	1.00	1.82	64	6.00	6.00
5	1	1	25	1	1	45	1.25	2.02	65	6.25	6.25
6	1	1	26	1	1	46	1.50	2.23	66	6.50	6.50
7	1	1	27	1	1	47	1.75	2.43	67	6.75	6.75
8	1	1	28	1	1	48	2.00	2.64	68	7.00	7.00
9	1	1	29	1	1	49	2.25	2.84	69	7.25	7.25
10	1	1	30	1	1	50	2.50	3.05	70	7.50	7.50
11	1	1	31	1	1	51	2.75	3.25	71	7.75	7.75
12	1	1	32	1	1	52	3.00	3.45	72	8.00	8.00
13	1	1	33	1	1	53	3.25	3.66	73	8.25	8.25
14	1	1	34	1	1	54	3.50	3.86	74	8.50	8.50
15	1	1	35	1	1	55	3.75	4.07	75	8.75	8.75
16	1	1	36	1	1	56	4.00	4.27	76	9.00	9.00
17	1	1	37	1	1	57	4.25	4.48	77	9.25	9.25
18	1	1	38	1	1	58	4.50	4.68	78	9.50	9.50
19	1	1	39	1	1	59	4.75	4.89	79	9.75	9.75
20	1	1	40	1	1	60	5.00	5.09	80	10.00	10.00

MC exam with 90 questions and 2 choises

Risbo's method:

$$grade = \begin{cases} -10.25 + 0.225 \cdot score & \text{if } score > 50 \\ 1 & \text{if } score \leq 50 \end{cases}$$

$$grade = \begin{cases} -10 + 0.222 \cdot score & \text{if } score \geq 69.75 \\ -7.182 + 0.182 \cdot score & \text{if } 45 < score < 69.75 \\ 1 & \text{if } score \leq 45 \end{cases}$$



score.	1 ris	bo.1 remi	ndostore.2	2 ris	sbo.2 remino	los 2 ore.	3 risbo.	3 remin	.do st ore.	4 risbo.	4 remin	dostore.5	risbo.	5 remindo.5
1	1	1	21	1	1	41	1.00	1.00	61	3.47	3.91	81	7.98	8.00
2	1	1	22	1	1	42	1.00	1.00	62	3.70	4.09	82	8.20	8.22
3	1	1	23	1	1	43	1.00	1.00	63	3.93	4.27	83	8.43	8.44
4	1	1	24	1	1	44	1.00	1.00	64	4.15	4.45	84	8.65	8.67
5	1	1	25	1	1	45	1.00	1.00	65	4.38	4.64	85	8.88	8.89
6	1	1	26	1	1	46	1.00	1.18	66	4.60	4.82	86	9.10	9.11
7	1	1	27	1	1	47	1.00	1.36	67	4.83	5.00	87	9.32	9.33
8	1	1	28	1	1	48	1.00	1.55	68	5.05	5.18	88	9.55	9.56
9	1	1	29	1	1	49	1.00	1.73	69	5.28	5.36	89	9.78	9.78
10	1	1	30	1	1	50	1.00	1.91	70	5.50	5.56	90	10.00	10.00
11	1	1	31	1	1	51	1.22	2.09	71	5.72	5.78	NA	NA	NA
12	1	1	32	1	1	52	1.45	2.27	72	5.95	6.00	NA	NA	NA
13	1	1	33	1	1	53	1.68	2.45	73	6.18	6.22	NA	NA	NA
14	1	1	34	1	1	54	1.90	2.64	74	6.40	6.44	NA	NA	NA
15	1	1	35	1	1	55	2.12	2.82	75	6.62	6.67	NA	NA	NA
16	1	1	36	1	1	56	2.35	3.00	76	6.85	6.89	NA	NA	NA
17	1	1	37	1	1	57	2.58	3.18	77	7.07	7.11	NA	NA	NA
18	1	1	38	1	1	58	2.80	3.36	78	7.30	7.33	NA	NA	NA
19	1	1	39	1	1	59	3.03	3.55	79	7.53	7.56	NA	NA	NA
20	1	1	40	1	1	60	3.25	3.73	80	7.75	7.78	NA	NA	NA