

$$\begin{pmatrix} \cos \theta_1 & \cos \theta_2 \\ \sin \theta_2 & \sin \theta_2 \end{pmatrix} \begin{pmatrix} v_1 \\ v_2 \end{pmatrix} = \begin{pmatrix} \cos \theta'_1 & \cos \theta'_2 \\ \sin \theta'_2 & \sin \theta'_2 \end{pmatrix} \begin{pmatrix} v'_1 \\ v'_2 \end{pmatrix} \quad (1)$$

$$\begin{pmatrix} v'_1 \\ v'_2 \end{pmatrix} = \begin{pmatrix} \cos \theta'_1 & \cos \theta'_2 \\ \sin \theta'_2 & \sin \theta'_2 \end{pmatrix}^{-1} \begin{pmatrix} \cos \theta_1 & \cos \theta_2 \\ \sin \theta_2 & \sin \theta_2 \end{pmatrix} \begin{pmatrix} v_1 \\ v_2 \end{pmatrix} \quad (2)$$

$$\begin{pmatrix} v'_1 \\ v'_2 \end{pmatrix} = \frac{1}{\sin(\theta'_1 - \theta'_2)} \begin{pmatrix} \sin(\theta_1 - \theta'_2) & \sin(\theta_2 - \theta'_2) \\ -\sin(\theta_1 - \theta'_1) & \sin(\theta_2 - \theta'_1) \end{pmatrix} \begin{pmatrix} v_1 \\ v_2 \end{pmatrix} \quad (3)$$

$$\begin{pmatrix} v'_1 \\ v'_2 \end{pmatrix} = \begin{pmatrix} \cos \theta_\delta & -\sin \theta_\delta \\ \sin \theta_\delta & \cos \theta_\delta \end{pmatrix} \begin{pmatrix} v_2 \\ v_1 \end{pmatrix} \quad (4)$$

=

$$\begin{pmatrix} v'_1 \\ v'_2 \end{pmatrix} = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} v_1 \\ v_2 \end{pmatrix} = \begin{pmatrix} v_2 \\ v_1 \end{pmatrix} \quad (5)$$