

# SNAG: Correlations

Shuying Yu

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## Variables

Because correlations require observations with the same vector length, this was done for participants who have all tasks completed.

### Dependent variables:

Names of variables and brief description

- SBSOD (Santa Barbara Sense of Direction scale)
- SOT (estimated angle [SOT\_Angle] and angular error [SOT\_Error]; if anything, just SOT\_Angle is the measure we care about)
- MRM (Money Road Map)
- DSP\_Wayfinding (proportion correct)
- DSP\_SI (solution index strict coding)
- MAZE\_Wayfinding (proportion correct)
- MAZE\_Moves (number of moves during exploration)
- LOOP\_MeanPositionErr (average meters across 3 radii)
- LOOP\_PositionPSTD (average PSTD for position error across 3 radii)
- LOOP\_MeanDegrees (average degrees across 3 radii)
- LOOP\_DegreesPSTD (average PSTD for degrees traveled across 3 radii)

## Data

```
#Load data
corr_dat <- read.csv("Correlations_ALL.csv")

#Remove SubjectID column
corr_dat <- corr_dat[,c(2:13)]

#Show first 10 rows/subjects
head(corr_dat, 10)
```

##	SBSOD	SOT_Angle	SOT_Error	MRM	DSP_Wayfinding	DSP_SI
## 1	3.333333	176.4167	33.583333	100.00000	0.65	0.15384615
## 2	4.200000	170.0833	30.250000	100.00000	0.60	0.25000000
## 3	5.400000	198.4167	74.750000	80.00000	0.75	0.00000000
## 4	4.066667	182.7500	24.750000	100.00000	0.65	0.23076923

```
## 5 6.000000 180.4167 31.083333 75.00000 0.60 0.08333333
## 6 6.400000 209.5000 35.500000 94.11765 1.00 0.20000000
## 7 6.533333 194.7500 10.250000 100.00000 0.75 0.20000000
## 8 4.333333 194.3333 9.166667 100.00000 0.65 0.15384615
## 9 5.600000 182.5833 17.750000 100.00000 0.75 0.40000000
## 10 4.400000 179.6667 24.666667 92.85714 0.45 0.33333333
## MAZE_Wayfinding MAZE_Moves LOOP_MeanPositionErr LOOP_PositionPSTD
## 1 0.000000 269 1.370606 0.8371334
## 2 8.333333 266 1.171936 0.7405337
## 3 20.833333 288 1.438188 0.9525353
## 4 12.500000 299 1.989072 0.9758353
## 5 4.166667 266 1.555377 1.0987158
## 6 62.500000 273 2.062230 1.1552127
## 7 12.500000 315 1.230118 0.7726145
## 8 8.333333 269 2.328188 0.8999634
## 9 29.166667 274 1.243972 0.6625947
## 10 4.166667 288 2.879014 0.8607178
## LOOP_MeanDegrees LOOP_DegreePSTD
## 1 396.5134 35.59109
## 2 332.6236 33.17871
## 3 350.5439 37.01638
## 4 416.8381 68.13490
## 5 347.5976 69.32251
## 6 420.3662 58.15037
## 7 344.9175 44.90391
## 8 332.4740 83.55519
## 9 341.1140 41.96415
## 10 258.1615 70.45680
```

## Correlation matrix with p-values

```
#Save correlation matrix into variable
res <- rcorr(as.matrix(corr_dat), type = "pearson")
res
```

```
## SBSOD SOT_Angle SOT_Error MRM DSP_Wayfinding DSP_SI
## SBSOD 1.00 0.26 -0.17 0.34 0.03 0.06
## SOT_Angle 0.26 1.00 -0.49 0.09 0.10 -0.11
## SOT_Error -0.17 -0.49 1.00 -0.40 -0.15 0.09
## MRM 0.34 0.09 -0.40 1.00 -0.10 0.05
## DSP_Wayfinding 0.03 0.10 -0.15 -0.10 1.00 -0.24
## DSP_SI 0.06 -0.11 0.09 0.05 -0.24 1.00
## MAZE_Wayfinding 0.04 0.05 0.03 0.01 0.49 0.22
## MAZE_Moves -0.17 -0.07 0.00 -0.02 0.07 -0.08
## LOOP_MeanPositionErr -0.26 -0.29 0.21 -0.41 -0.03 0.04
## LOOP_PositionPSTD 0.00 -0.02 0.31 -0.30 -0.02 -0.08
## LOOP_MeanDegrees 0.01 -0.20 0.22 0.02 -0.03 -0.05
## LOOP_DegreePSTD -0.02 0.04 0.06 -0.20 -0.02 -0.17
## MAZE_Wayfinding MAZE_Moves LOOP_MeanPositionErr
## SBSOD 0.04 -0.17 -0.26
## SOT_Angle 0.05 -0.07 -0.29
## SOT_Error 0.03 0.00 0.21
## MRM 0.01 -0.02 -0.41
```

```

## DSP_Wayfinding          0.49      0.07      -0.03
## DSP_SI                  0.22     -0.08       0.04
## MAZE_Wayfinding        1.00      0.34       0.05
## MAZE_Moves             0.34      1.00     -0.01
## LOOP_MeanPositionErr    0.05     -0.01       1.00
## LOOP_PositionPSTD       0.03      0.15       0.36
## LOOP_MeanDegrees       -0.10     -0.07       0.11
## LOOP_DegreePSTD        -0.11      0.08       0.39
##
##          LOOP_PositionPSTD LOOP_MeanDegrees LOOP_DegreePSTD
## SBSOD          0.00          0.01       -0.02
## SOT_Angle      -0.02         -0.20       0.04
## SOT_Error       0.31          0.22       0.06
## MRM            -0.30          0.02     -0.20
## DSP_Wayfinding -0.02         -0.03     -0.02
## DSP_SI         -0.08         -0.05     -0.17
## MAZE_Wayfinding 0.03         -0.10     -0.11
## MAZE_Moves      0.15         -0.07       0.08
## LOOP_MeanPositionErr 0.36          0.11       0.39
## LOOP_PositionPSTD   1.00          0.09       0.65
## LOOP_MeanDegrees   0.09          1.00       0.29
## LOOP_DegreePSTD    0.65          0.29       1.00
##
## n= 41
##
##
## P
##
##          SBSOD  SOT_Angle SOT_Error MRM      DSP_Wayfinding
## SBSOD          0.0956   0.2918   0.0281 0.8379
## SOT_Angle      0.0956         0.0010   0.5923 0.5142
## SOT_Error      0.2918 0.0010         0.0092 0.3537
## MRM            0.0281 0.5923   0.0092     0.5405
## DSP_Wayfinding 0.8379 0.5142   0.3537   0.5405
## DSP_SI         0.7162 0.4943   0.5733   0.7371 0.1342
## MAZE_Wayfinding 0.8063 0.7727   0.8722   0.9409 0.0010
## MAZE_Moves     0.3006 0.6786   0.9812   0.9087 0.6836
## LOOP_MeanPositionErr 0.0960 0.0670   0.1794   0.0085 0.8410
## LOOP_PositionPSTD 0.9822 0.8834   0.0514   0.0574 0.8863
## LOOP_MeanDegrees 0.9490 0.2160   0.1632   0.8950 0.8350
## LOOP_DegreePSTD 0.9119 0.8078   0.7185   0.2078 0.8886
##
##          DSP_SI MAZE_Wayfinding MAZE_Moves
## SBSOD      0.7162 0.8063         0.3006
## SOT_Angle   0.4943 0.7727         0.6786
## SOT_Error   0.5733 0.8722         0.9812
## MRM         0.7371 0.9409         0.9087
## DSP_Wayfinding 0.1342 0.0010         0.6836
## DSP_SI      0.1713         0.6389
## MAZE_Wayfinding 0.1713         0.0290
## MAZE_Moves  0.6389 0.0290
## LOOP_MeanPositionErr 0.7831 0.7498         0.9660
## LOOP_PositionPSTD 0.6142 0.8523         0.3622
## LOOP_MeanDegrees 0.7433 0.5459         0.6415
## LOOP_DegreePSTD 0.2894 0.4889         0.6368
##
##          LOOP_MeanPositionErr LOOP_PositionPSTD
## SBSOD      0.0960         0.9822

```

## SOT_Angle	0.0670	0.8834
## SOT_Error	0.1794	0.0514
## MRM	0.0085	0.0574
## DSP_Wayfinding	0.8410	0.8863
## DSP_SI	0.7831	0.6142
## MAZE_Wayfinding	0.7498	0.8523
## MAZE_Moves	0.9660	0.3622
## LOOP_MeanPositionErr		0.0194
## LOOP_PositionPSTD	0.0194	
## LOOP_MeanDegrees	0.5112	0.5839
## LOOP_DegreePSTD	0.0109	0.0000
##	LOOP_MeanDegrees	LOOP_DegreePSTD
## SBSOD	0.9490	0.9119
## SOT_Angle	0.2160	0.8078
## SOT_Error	0.1632	0.7185
## MRM	0.8950	0.2078
## DSP_Wayfinding	0.8350	0.8886
## DSP_SI	0.7433	0.2894
## MAZE_Wayfinding	0.5459	0.4889
## MAZE_Moves	0.6415	0.6368
## LOOP_MeanPositionErr	0.5112	0.0109
## LOOP_PositionPSTD	0.5839	0.0000
## LOOP_MeanDegrees		0.0627
## LOOP_DegreePSTD	0.0627	

## Table

Formatting a correlation matrix into a table with 4 columns containing :

- Column 1 : row names (variable 1 for the correlation test)
- Column 2 : column names (variable 2 for the correlation test)
- Column 3 : the correlation coefficients
- Column 4 : the  $p$ -values of the correlations

```
#Create function to combine coefficients and p-values
```

```
#coeff_mat: matrix of the correlation coefficients
```

```
#p_mat : matrix of the correlation p-values
```

```
CorMat <- function(coeff_mat, p_mat) {
```

```
  #Save upper half triangle of coefficients
```

```
  #This is because the other half is redundant
```

```
  up_half <- upper.tri(coeff_mat)
```

```
  #Save into dataframe
```

```
  data.frame(
```

```
    #Variable 1
```

```
    Var1 = rownames(coeff_mat)[row(coeff_mat)[up_half]],
```

```
    #Variable 2
```

```
    Var2 = rownames(coeff_mat)[col(coeff_mat)[up_half]],
```

```
    #Correlation coefficient
```

```

    Corr =(coeff_mat)[up_half],
    #p-value
    p_value = p_mat[up_half]
  )
}

#Pearson correlation
res2 <- rcorr(as.matrix(corr_dat), type="pearson")

#Use function to place into table

#res2$r = correlation coefficient
#res2$P = associated p-value
CorMat(res2$r, res2$P)

```

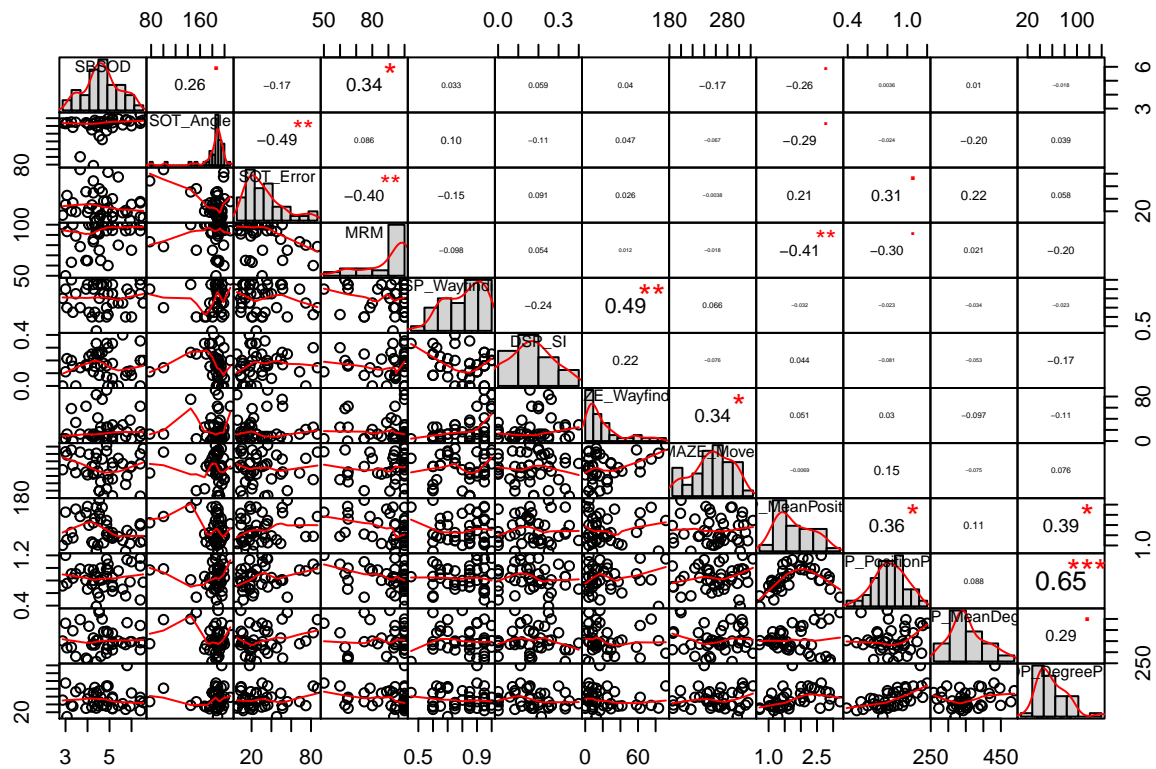
##	Var1	Var2	Corr	p_value
## 1	SBSOD	SOT_Angle	0.263770767	9.563712e-02
## 2	SBSOD	SOT_Error	-0.168658749	2.918280e-01
## 3	SOT_Angle	SOT_Error	-0.494369157	1.018526e-03
## 4	SBSOD	MRM	0.343019202	2.812320e-02
## 5	SOT_Angle	MRM	0.086136315	5.923167e-01
## 6	SOT_Error	MRM	-0.401691924	9.235629e-03
## 7	SBSOD	DSP_Wayfinding	0.032965705	8.378759e-01
## 8	SOT_Angle	DSP_Wayfinding	0.104837981	5.141870e-01
## 9	SOT_Error	DSP_Wayfinding	-0.148636267	3.536827e-01
## 10	MRM	DSP_Wayfinding	-0.098401485	5.404848e-01
## 11	SBSOD	DSP_SI	0.058529368	7.162368e-01
## 12	SOT_Angle	DSP_SI	-0.109824807	4.942615e-01
## 13	SOT_Error	DSP_SI	0.090578142	5.732941e-01
## 14	MRM	DSP_SI	0.054059111	7.371061e-01
## 15	DSP_Wayfinding	DSP_SI	-0.237874042	1.342309e-01
## 16	SBSOD	MAZE_Wayfinding	0.039505760	8.062760e-01
## 17	SOT_Angle	MAZE_Wayfinding	0.046530094	7.726727e-01
## 18	SOT_Error	MAZE_Wayfinding	0.025922672	8.721881e-01
## 19	MRM	MAZE_Wayfinding	0.011938209	9.409464e-01
## 20	DSP_Wayfinding	MAZE_Wayfinding	0.494226307	1.022495e-03
## 21	DSP_SI	MAZE_Wayfinding	0.217821637	1.712813e-01
## 22	SBSOD	MAZE_Moves	-0.165656040	3.006286e-01
## 23	SOT_Angle	MAZE_Moves	-0.066697417	6.786351e-01
## 24	SOT_Error	MAZE_Moves	-0.003798538	9.811953e-01
## 25	MRM	MAZE_Moves	-0.018489419	9.086524e-01
## 26	DSP_Wayfinding	MAZE_Moves	0.065619856	6.835542e-01
## 27	DSP_SI	MAZE_Moves	-0.075507548	6.389245e-01
## 28	MAZE_Wayfinding	MAZE_Moves	0.341227693	2.900984e-02
## 29	SBSOD	LOOP_MeanPositionErr	-0.263513495	9.597306e-02
## 30	SOT_Angle	LOOP_MeanPositionErr	-0.288827174	6.703277e-02
## 31	SOT_Error	LOOP_MeanPositionErr	0.213857946	1.794002e-01
## 32	MRM	LOOP_MeanPositionErr	-0.405941657	8.454177e-03
## 33	DSP_Wayfinding	LOOP_MeanPositionErr	-0.032312093	8.410487e-01
## 34	DSP_SI	LOOP_MeanPositionErr	0.044341955	7.830997e-01
## 35	MAZE_Wayfinding	LOOP_MeanPositionErr	0.051367419	7.497637e-01
## 36	MAZE_Moves	LOOP_MeanPositionErr	-0.006878604	9.659543e-01
## 37	SBSOD	LOOP_PositionPSTD	0.003588921	9.822328e-01
## 38	SOT_Angle	LOOP_PositionPSTD	-0.023630030	8.834105e-01

## 39	SOT_Error	LOOP_PositionPSTD	0.306297958	5.144967e-02
## 40	MRM	LOOP_PositionPSTD	-0.299217710	5.737083e-02
## 41	DSP_Wayfinding	LOOP_PositionPSTD	-0.023047564	8.862654e-01
## 42	DSP_SI	LOOP_PositionPSTD	-0.081105266	6.141921e-01
## 43	MAZE_Wayfinding	LOOP_PositionPSTD	0.029999024	8.522966e-01
## 44	MAZE_Moves	LOOP_PositionPSTD	0.146064389	3.621661e-01
## 45	LOOP_MeanPositionErr	LOOP_PositionPSTD	0.363815291	1.937290e-02
## 46	SBSOD	LOOP_MeanDegrees	0.010309374	9.489922e-01
## 47	SOT_Angle	LOOP_MeanDegrees	-0.197436384	2.159621e-01
## 48	SOT_Error	LOOP_MeanDegrees	0.221908150	1.631911e-01
## 49	MRM	LOOP_MeanDegrees	0.021257347	8.950485e-01
## 50	DSP_Wayfinding	LOOP_MeanDegrees	-0.033551509	8.350344e-01
## 51	DSP_SI	LOOP_MeanDegrees	-0.052743899	7.432825e-01
## 52	MAZE_Wayfinding	LOOP_MeanDegrees	-0.097104093	5.458628e-01
## 53	MAZE_Moves	LOOP_MeanDegrees	-0.074924274	6.415245e-01
## 54	LOOP_MeanPositionErr	LOOP_MeanDegrees	0.105585664	5.111741e-01
## 55	LOOP_PositionPSTD	LOOP_MeanDegrees	0.088090442	5.839137e-01
## 56	SBSOD	LOOP_DegreePSTD	-0.017820876	9.119422e-01
## 57	SOT_Angle	LOOP_DegreePSTD	0.039178855	8.078487e-01
## 58	SOT_Error	LOOP_DegreePSTD	0.058038704	7.185179e-01
## 59	MRM	LOOP_DegreePSTD	-0.200935995	2.077690e-01
## 60	DSP_Wayfinding	LOOP_DegreePSTD	-0.022564442	8.886344e-01
## 61	DSP_SI	LOOP_DegreePSTD	-0.169491196	2.894180e-01
## 62	MAZE_Wayfinding	LOOP_DegreePSTD	-0.111177900	4.889244e-01
## 63	MAZE_Moves	LOOP_DegreePSTD	0.075989905	6.367775e-01
## 64	LOOP_MeanPositionErr	LOOP_DegreePSTD	0.393534924	1.091006e-02
## 65	LOOP_PositionPSTD	LOOP_DegreePSTD	0.649551570	4.328181e-06
## 66	LOOP_MeanDegrees	LOOP_DegreePSTD	0.293282301	6.274341e-02

## Visualize correlation matrix

### Scatter and chart

```
#Scatter plot, histogram, and correlation value
chart.Correlation(corr_dat, histogram=TRUE, pch=19)
```



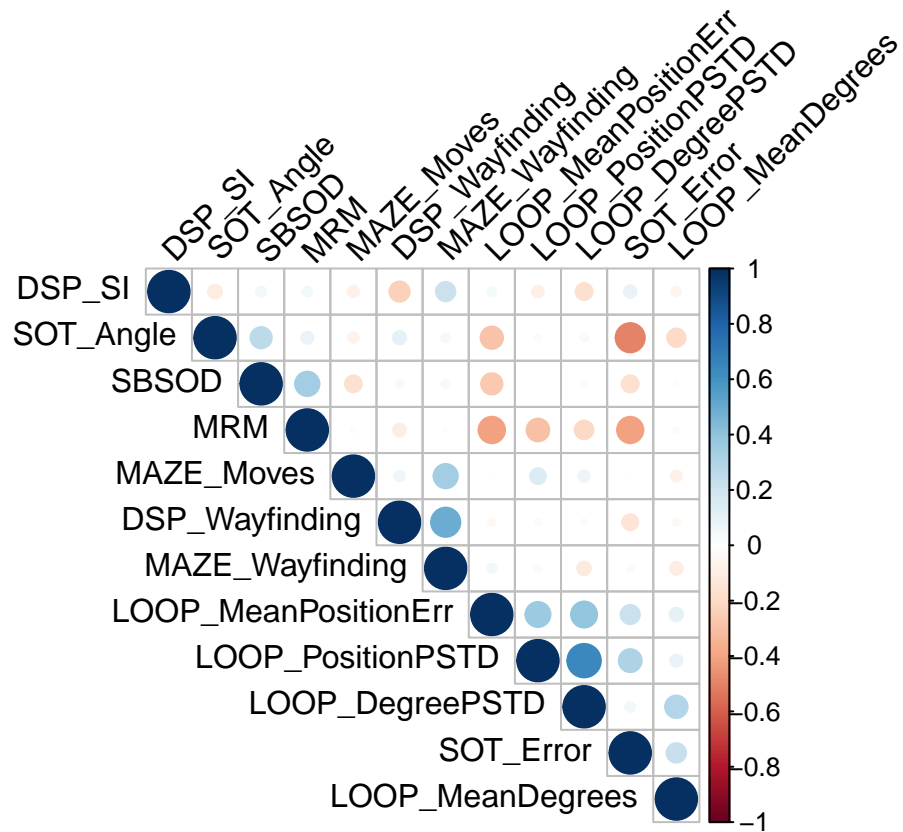
In the above plot:

- The distribution of each variable is shown on the diagonal.
- On the bottom of the diagonal : the bivariate scatter plots with a fitted line are displayed
- On the top of the diagonal : the value of the correlation plus the significance level as stars
- Each significance level is associated to a symbol :  $p$ -values(0, 0.001, 0.01, 0.05, 0.1, 1)  $\Leftrightarrow$  symbols(\*\*\*, \*\*, \*, ., ' ')

## Correlation

*#Display only "upper" triangular portion to cut redundancy*

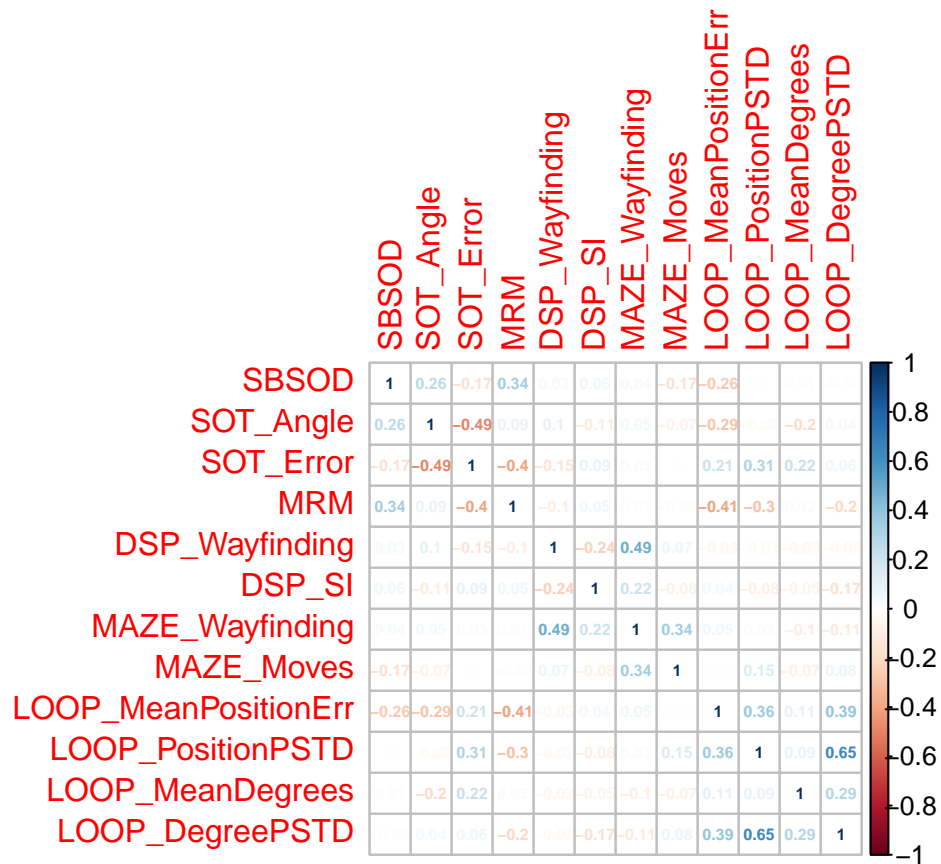
```
corrplot(res2$r, type = "upper", order = "hclust",
         tl.col = "black", tl.srt = 45)
```



*#Show correlation coefficient numbers*

```
corrplot(res2$r, method="number", number.cex=0.5)
```

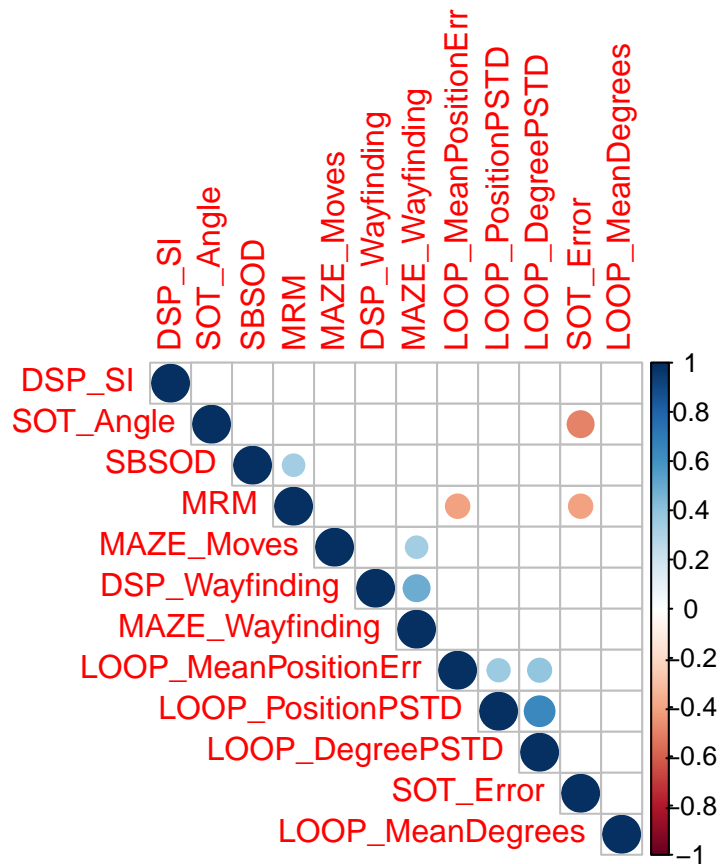




*#Significance at  $p = 0.05$*

*#Insignificant correlations are left blank*

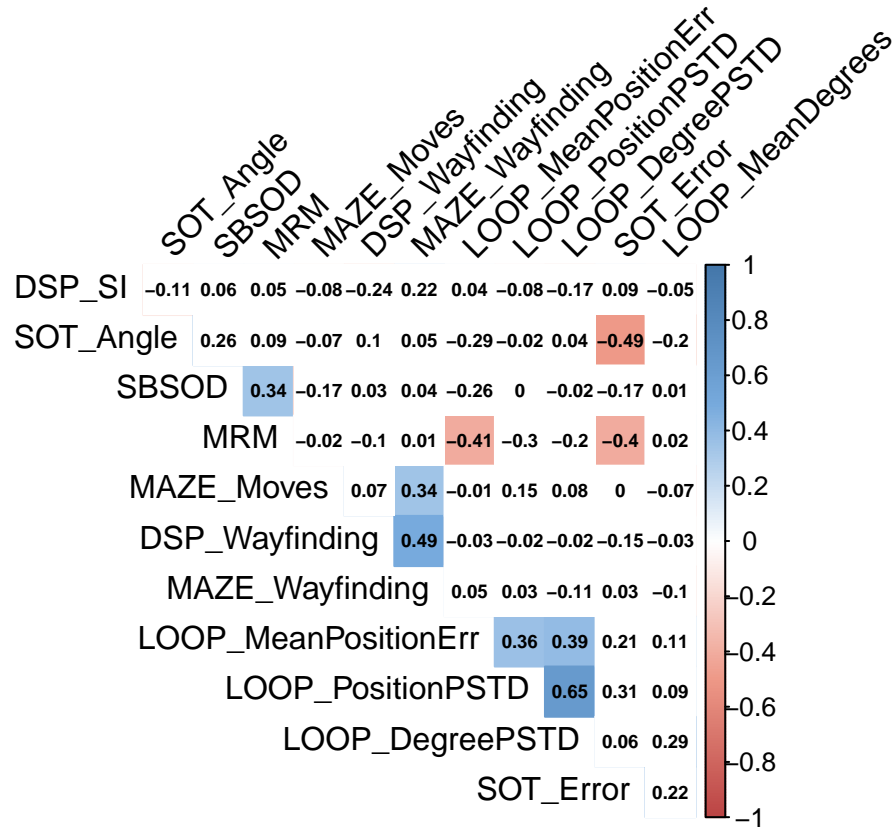
```
corrplot(res2$r, type="upper", order="hclust",
  p.mat = res2$P, sig.level = 0.05, insig = "blank")
```



```
#Numbers are correlation coefficients
#Colored squares are those that meet significance (alpha = 0.05)

#Color palette taken from Reference [1] and [2]
col <- colorRampPalette(c("#BB4444", "#EE9988", "#FFFFFF", "#77AADD", "#4477AA"))

corrplot(res2$r, method="color", col=col(200),
  type="upper", order="hclust",
  #Add coefficient of correlation
  addCoef.col = "black",
  #Text label color and rotation
  tl.col="black", tl.srt=45,
  # Combine with significance
  p.mat = res2$P, sig.level = 0.05, insig = "blank", number.cex=0.6,
  #Hide correlation coefficient on the principal diagonal
  diag=FALSE
)
```



Positive correlations are displayed in blue and negative correlations in red color. Color intensity and the size of the circle are proportional to the correlation coefficients. On the right side of the correlogram, the legend color shows the correlation coefficients and the corresponding colors.

## References

1. Correlation matrix : A quick start guide to analyze, format and visualize a correlation matrix using R softwards. <http://www.sthda.com/english/wiki/correlation-matrix-a-quick-start-guide-to-analyze-format-and-visualize-a-correlation-matrix-using-r-software>
2. Visualize correlation matrix using correlogram. <http://www.sthda.com/english/wiki/visualize-correlation-matrix-using-correlogram>