

Statistical Inference Project

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```
knitr::opts_chunk$set(echo = TRUE)
library(ggplot2)
```

Overview

Setup

The first step is to set our initial variables and set the seed so this is fully reproducible.

```
ECHO=TRUE
set.seed(1775)
lambda = 0.2
exp = 40
```

Next we run our simulation with the parameters set above.

```
sim_means = NULL
for (i in 1 : 1000) {
  sim_means = c(sim_means, mean(rexp(exp, lambda)))
}
```

Compare Sample and Theoretical Means

```
mean_sim_means <- mean(sim_means)
mean_sim_means
```

Sample Mean

```
## [1] 5.013338
```

Theoretical mean The theoretical mean of the distribution is λ^{-1}

```
theo_mean <- lambda^-1
theo_mean
```

```
## [1] 5
```

Comparison The difference is fairly small.

```
abs(mean_sim_means - theo_mean)
```

```
## [1] 0.013338
```

Sample Variance and Theoretical Variance

Sample Variance Again, this is very simple

```
var_sim <- var(sim_means)
```

Theoretical Variance The theoretical variance follows

```
theo_var <- (lambda * sqrt(exp))^-2
```

Compared variances Again, a very slight difference between the two

```
abs(var_sim - theo_var)
```

```
## [1] 0.02075072
```

Distribution

Next, I'll directly compare a density histogram of the one thousand simulations with the normal distribution, which has a mean of λ^{-1} and std deviation of $(\lambda \sqrt{n})^{-1}$, which is the theoretical distribution for the simulations. They are fairly similar, with the exception of the peak of the simulation occurring just after the peak of the theoretical mean.

```
df <- data.frame(sim_means)

ggplot(df, aes(x = (unlist(df)))) +
  geom_histogram(aes(y= ..density..), binwidth = 0.2) +
  stat_function(fun = dnorm,
               args = list(mean = lambda^-1,
                           sd=(lambda*sqrt(exp))^-1),
               size = 2) +
  labs(title = "Histogram of Simulations", x = "Mean of the Simulation")
```

Histogram of Simulations

