

Michele Bugliesi

Stefano Calzavara

Enrico Steffinlongo

May 26, 2014

#### Abstract

In many software systems as modern web browsers the user and his sensitive data often interact with the untrusted outer world. This scenario can pose a serious threat to the user's private data and gives new relevance to an old story in computer science: providing controlled access to untrusted components, while preserving usability and ease of interaction. To address the threats of untrusted components, modern web browsers propose privilege-separated architectures, which isolate components that manage critical tasks and data from components which handle untrusted inputs. The former components are given strong permissions, possibly coinciding with the full set of permissions granted to the user, while the untrusted components are granted only limited privileges, to limit possible malicious behaviours: all the interactions between trusted and untrusted components is handled via message passing. In this thesis we introduce a formal semantics for privilege-separated architectures and we provide a general definition of privilege separation: we discuss how different privilege-separated architectures can be evaluated in our framework, identifying how different security threats can be avoided, mitigated or disregarded. Specifically, we evaluate in detail the existing Google Chrome Extension Architecture in our formal model and we discuss how its design can mitigate serious security risks, with only limited impact on the user experience.

## Contents

1	Mo	tivation	
	1.1	Privilege escalation attacks	
	1.2	Chrome extension architecture overview	
	1.3	Chrome extension architecture weaknesses	
	1.4	Proposal	
<b>2</b>	Background		
	2.1	Chrome extension architecture details	
	2.2	Flow logic	
3	Formalization		
	3.1	Calculus	
	3.2	Safety properties	
	3.3	Analysis specification	
		3.3.1 Abstract succinct	
		3.3.2 Compositional Verbose	
	3.4	Theorem	
	3.5	Requirements for correctness	
4	Abstract Domains 15		
	4.1	Abstract domains choice	
	4.2	Abstract operations	
	4.3	Requirements verification	
5	Imp	plementation 17	
	5.1	Constraint generation	
	5.2	Constraint solving	
	5.3	Implementation-specific details	
6	Experiments 2		
	6.1	Findings	
	6.2	Performance	
7	Conclusion 23		
	7.1	Conclusions	
	7.2	Future works (unbundling)	

### Motivation

- 1.1 Privilege escalation attacks
- 1.2 Chrome extension architecture overview

Web browser in the last decade experienced a massive increment of usage. Such increment influenced all features of the browsers, from the efficiency of the plain browsing to

- 1.3 Chrome extension architecture weaknesses
- 1.4 Proposal

## Background

- 2.1 Chrome extension architecture details
- 2.2 Flow logic

### Formalization

- 3.1 Calculus
- 3.2 Safety properties
- Analysis specification 3.3
- 3.3.1 Abstract succinct

Abstract cache  $\hat{C}: \mathcal{L} \to \hat{V}$ Abstract variable environment  $\hat{\Gamma}: \mathcal{V} \to \hat{V}$ 

Abstract memory  $\hat{\mu}: \mathcal{L} \times \mathcal{P} \to \hat{V}$ Abstract permission cache  $\hat{P}: \mathcal{L} \to \mathcal{P}$ 

```
(\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} c : \hat{v} \text{ iff } \{d_c\} \subseteq \hat{v}
[PE-Val]
                                                 (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} x : \hat{v} \text{ iff } \hat{\Gamma}(x) \subseteq \hat{v}
[PE-Var]
                                                 (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} \lambda x.e : \hat{v} \text{ iff } \{\lambda x.e\} \subseteq \hat{v}
[PE-Lambda]
                                                 (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} \{\overrightarrow{str_i : e_i}\} : \hat{v} \gg \rho \text{ iff}
[PE-Obj]
                                                       \forall i : (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} e_i : \hat{v}_i \gg \rho_i \land
                                                               \{\overrightarrow{str_i:\hat{v_i}}\}\subseteq \hat{v} \wedge
                                                               \rho_i \sqsubseteq \rho
                                                 (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} \mathbf{let} \ \overrightarrow{x_i = e_i} \ \mathbf{in} \ e' : \hat{v} \gg \rho \ \mathrm{iff}
[PE-Let]
                                                        (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} e' : \hat{v} \gg \rho' \wedge
                                                        \rho' \sqsubseteq \rho \land
                                                        \forall i:
                                                               (\Gamma, \hat{\mu}) \models_{\rho_s} e_i : \hat{v}_i \gg \rho_i \wedge
                                                               \hat{v}_i \subseteq \Gamma(x_i) \land
                                                               \rho_i \sqsubseteq \rho
[PE-App]
                                                 (\Gamma, \hat{\mu}) \models_{\rho_s} e_1 e_2 : \hat{v} \gg \rho \text{ iff}
                                                        (\Gamma, \hat{\mu}) \models_{\rho_s} e_1 : \hat{v}_1 \gg \rho_1 \wedge
                                                        (\Gamma, \hat{\mu}) \models_{\rho_s} e_2 : \hat{v}_2 \gg \rho_2 \wedge
                                                        \rho_1 \sqsubseteq \rho \land
                                                        \rho_2 \sqsubseteq \rho \land
                                                        \forall (\lambda x.e_0) \in \hat{v}_1:
                                                               \hat{v}_2 \subseteq \Gamma(x) \wedge
                                                               (\Gamma, \hat{\mu}) \models_{\rho_s} e_0 : \hat{v}_0 \gg \rho_0 \wedge
                                                               \rho_0 \sqsubseteq \rho \land
                                                               \hat{v}_0 \subseteq \hat{v}
[PE-Op]
                                                 (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} op(\overrightarrow{e_i}) : \hat{v} \gg \rho \text{ iff}
                                                               (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} e_i : \hat{v}_i \gg \rho_i \wedge

\begin{array}{c}
\rho_i \sqsubseteq \rho \land \\
\widehat{op}(\overrightarrow{\hat{v}_i}) \subseteq \widehat{v}
\end{array}

[PE-Cond]
                                                 (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} \mathbf{if} (e_0) \{ e_1 \} \mathbf{else} \{ e_2 \} : \hat{v} \gg \rho \mathbf{iff}
                                                        (\Gamma, \hat{\mu}) \models_{\rho_s} e_0 : \hat{v}_0 \gg \rho_0 \wedge
                                                        \rho_0 \sqsubseteq \rho \land
                                                        \mathbf{true} \in \hat{v}_0 \Rightarrow
                                                                (\dot{\Gamma}, \hat{\mu}) \models_{\rho_s} e_1 : \hat{v}_1 \gg \rho_1 \wedge \hat{v}_1 \subseteq \hat{v} \wedge \rho_1 \sqsubseteq \rho \wedge
                                                        false \in \hat{v}_0 \Rightarrow
                                                               (\Gamma, \hat{\mu}) \models_{\rho_s} e_2 : \hat{v}_2 \gg \rho_2 \wedge \hat{v}_2 \subseteq \hat{v} \wedge \rho_2 \sqsubseteq \rho
[PE-While]
                                                 (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} \mathbf{while} (e_1) \{ e_2 \} : \hat{v} \gg \rho \text{ iff}
                                                        (\Gamma, \hat{\mu}) \models_{\rho_s} e_1 : \hat{v}_1 \gg \rho_1 \wedge
                                                        \rho_1 \sqsubseteq \rho \land
                                                        true \in \hat{v}_1 \Rightarrow
                                                               (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} e_2 : \hat{v}_2 \gg \rho_2 \wedge \hat{v}_2 \subseteq \hat{v} \wedge \rho_2 \sqsubseteq \rho \wedge
                                                        false \in \hat{v}_1 \Rightarrow
                                                               undefined \subseteq \hat{v}
                                                (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} e_1[e_2] : \hat{v} \gg \rho \text{ iff}
[PE-GetField]
                                                        (\Gamma, \hat{\mu}) \models_{\rho_s} e_1 : \hat{v}_1 \gg \rho_1 \wedge_{\Omega}
                                                        \rho_1 \sqsubseteq \rho \land
                                                        (\Gamma, \hat{\mu}) \models_{\rho_s} e_2 : \hat{v}_2 \gg \rho_2 \wedge
                                                        \rho_2 \sqsubseteq \rho \land
                                                        get(\hat{v}_1, \hat{v}_2) \subseteq \hat{v}
```

```
(\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} e_0[e_1] = e2 : \hat{v} \gg \rho \text{ iff}
[PE-SetField]
                                                             (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} e_0 : \hat{v}_0 \gg \rho_0 \wedge
                                                             \rho_0 \sqsubseteq \rho \land
                                                             (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} e_1 : \hat{v}_1 \gg \rho_1 \wedge
                                                             \rho_1 \sqsubseteq \rho \land
                                                             (\Gamma, \hat{\mu}) \models_{\rho_s} e_2 : \hat{v}_2 \gg \rho_2 \wedge
                                                             \rho_2 \sqsubseteq \rho \land
                                                             set(\hat{v}_0, \hat{v}_1, \hat{v}_2) \subseteq \hat{v}
                                             (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} \mathbf{delete} \ e_1[e_2] : \hat{v} \gg \rho \ \mathrm{iff}
[PE-DelField]
                                                             (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} e_1 : \hat{v}_1 \gg \rho_1 \wedge
                                                             \rho_1 \sqsubseteq \rho \land
                                                             (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} e_2 : \hat{v}_2 \gg \rho_2 \wedge
                                                             \rho_2 \sqsubseteq \rho \land
                                                             del(\hat{v}_1, \hat{v}_2) \subseteq \hat{v}
[PE-Ref]
                                             (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} \mathbf{ref}_{r,\rho_r} \ e : \{r\} \gg \rho \text{ iff}
                                                             (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} e : \hat{v} \gg \rho \wedge
                                                             \rho_r \sqsubseteq \rho_s \Rightarrow \hat{v} \subseteq \hat{\mu}(r, \rho_r)
                                             (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} \mathbf{deref} \ e : \hat{v} \gg \rho \text{ iff}
[PE-DeRef]
                                                             (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} e : \hat{v}_1 \gg \rho_1 \wedge
                                                             \rho_1 \sqsubseteq \rho \land
                                                             \forall r \in \hat{v}_1 : \forall \rho_r \sqsubseteq \rho_s : \hat{\mu}(r, \rho_r) \subseteq \hat{v}
[PE\text{-}SetRef]
                                              (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} e_1 = e_2 : \hat{v} \gg \rho \text{ iff}
                                                             (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} e : \hat{v}_1 \gg \rho_1 \wedge
                                                             \rho_1 \sqsubseteq \rho \land
                                                             (\hat{\Gamma}, \hat{\mu}) \models_{\rho_s} e_2 : \hat{v}_2 \gg \rho_2 \wedge
                                                             \rho_2 \sqsubseteq \rho \land
                                                             \forall r \in \hat{v}_1 : \forall \rho_r \sqsubseteq \rho_s :
                                                                   \hat{v}_2 \subseteq \hat{\mu}(r, \rho_r) \land
                                                                   \hat{v}_2 \subseteq \hat{v}
[PE\text{-}Send]
                                              . . .
[PE-Err]
                                              . . .
[PE	ext{-}Exercise]
```

#### 3.3.2 Compositional Verbose

$$[CV-Val] \qquad (\hat{C}, \hat{\Gamma}, \hat{\mu}, \hat{P}) \vDash_{cp} (c)^{\ell} \text{ iff } \{d_{c}\} \subseteq \hat{C}(\ell)$$

$$[CV-Var] \qquad (\hat{C}, \hat{\Gamma}, \hat{\mu}, \hat{P}) \vDash_{cp} (x)^{\ell} \text{ iff } \hat{\Gamma}(x) \subseteq \hat{C}(\ell)$$

$$[CV-Lambda] \qquad (\hat{C}, \hat{\Gamma}, \hat{\mu}, \hat{P}) \vDash_{cp} (\lambda x.c_{0}^{t_{0}})^{\ell} \text{ iff }$$

$$\{\lambda x.c_{0}^{t_{0}}\} \subseteq \hat{C}(\ell) \wedge$$

$$(\hat{C}, \hat{\Gamma}, \hat{\mu}, \hat{P}) \vDash_{cp} (\delta C)^{\ell}$$

$$(\hat{C}, \hat{\Gamma},$$

```
[CV\text{-}GetField] \quad (\hat{C}, \hat{\Gamma}, \hat{\mu}, \hat{P}) \models_{c\rho_s} (e_1^{\ell_1}[e_2^{\ell_2}])^{\ell} \text{ iff}
                                                                   (\hat{C}, \hat{\Gamma}, \hat{\mu}, \hat{P}) \models_{c\rho_s} e_1^{\ell_1} \wedge
                                                                   \hat{P}(\ell_1) \sqsubseteq \hat{P}(\ell) \wedge
                                                                    (\hat{C}, \hat{\Gamma}, \hat{\mu}, \hat{P}) \models_{c\rho_s} e_2^{\ell_2} \wedge
                                                                    \hat{P}(\ell_2) \sqsubseteq \hat{P}(\ell) \wedge
                                                                   \widehat{get}(\hat{C}(\ell_1),\hat{C}(\ell_2)) \subseteq \hat{C}(\ell)
                                                  (\hat{C}, \hat{\Gamma}, \hat{\mu}, \hat{P}) \models_{c\rho_s} (e_0^{\ell_0}[e_1^{\ell_1}] = e_2^{\ell_2})^{\ell} iff
[CV	ext{-}SetField]
                                                                   (\hat{C}, \hat{\Gamma}, \hat{\mu}, \hat{P}) \models_{c\rho_s} e_0^{\ell_0} \wedge
                                                                   \hat{P}(\ell_0) \sqsubseteq \hat{P}(\ell) \wedge
                                                                   (\hat{C}, \hat{\Gamma}, \hat{\mu}, \hat{P}) \models_{c\rho_s} e_1^{\ell_1} \wedge
                                                                    \hat{P}(\ell_1) \sqsubseteq \hat{P}(\ell) \wedge
                                                                   (\hat{C}, \hat{\Gamma}, \hat{\mu}, \hat{P}) \models_{c\rho_s} e_2^{\ell_2} \wedge
                                                                    \hat{P}(\ell_2) \sqsubseteq \hat{P}(\ell) \wedge
                                                                   \widehat{set}(\hat{C}(\ell_0), \hat{C}(\ell_1), \hat{C}(\ell_2)) \subseteq \hat{C}(\ell)
                                                  (\hat{C}, \hat{\Gamma}, \hat{\mu}, \hat{P}) \models_{c\rho_s} (\mathbf{delete} \ e_1^{\ell_1}[e_2^{\ell_2}])^{\ell}  iff
[CV-DelField]
                                                                   (\hat{C}, \hat{\Gamma}, \hat{\mu}, \hat{P}) \models_{c\rho_s} e_1^{\ell_1} \wedge
                                                                   \hat{P}(\ell_1) \sqsubseteq \hat{P}(\ell) \wedge
                                                                   (\hat{C}, \hat{\Gamma}, \hat{\mu}, \hat{P}) \models_{c\rho_s} e_2^{\ell_2} \wedge
                                                                   \hat{P}(\ell_2) \sqsubseteq \hat{P}(\ell) \wedge
                                                                   \widehat{del}(\widehat{C}(\ell_1), \widehat{C}(\ell_2)) \subseteq \widehat{C}(\ell)
                                                  (\hat{C}, \hat{\Gamma}, \hat{\mu}, \hat{P}) \models_{c\rho_s} (\mathbf{ref}_{r,\rho_r} \ e_1^{\ell_1})^{\ell} \text{ iff}
[CV-Ref]
                                                                   (\hat{C}, \hat{\Gamma}, \hat{\mu}, \hat{P}) \models_{c\rho_s} e_1^{\ell_1} \wedge
                                                                    \{r\} \subseteq \hat{C}(\ell) \land
                                                                   \hat{P}(\ell_1) \sqsubseteq \hat{P}(\ell) \wedge

\rho_r \sqsubseteq \rho_s \Rightarrow \hat{C}(\ell_1) \subseteq \hat{\mu}(r, \rho_r)

                                                  (\hat{C}, \hat{\Gamma}, \hat{\mu}, \hat{P}) \models_{c\rho_s} (\mathbf{deref} \ e_1^{\ell_1})^{\ell}  iff
[CV-DeRef]
                                                                   (\hat{C}, \hat{\Gamma}, \hat{\mu}, \hat{P}) \models_{c\rho_s} e_1^{\ell_1} \wedge
                                                                   \hat{P}(\ell_1) \sqsubseteq \hat{P}(\ell) \wedge
                                                                   \forall r \in \hat{C}(\ell_1) : \forall \rho_r \sqsubseteq \rho_s :
                                                                          \hat{\mu}(r,\rho_r)\subseteq \hat{C}(\ell)
                                                  (\hat{C}, \hat{\Gamma}, \hat{\mu}, \hat{P}) \models_{c\rho_s} (e_1^{\ell_1} = e_2^{\ell_2})^{\ell} iff
[CV	ext{-}SetRef]
                                                                   (\hat{C}, \hat{\Gamma}, \hat{\mu}, \hat{P}) \models_{c\rho_s} e_1^{\ell_1} \wedge
                                                                   \hat{P}(\ell_1) \sqsubseteq \hat{P}(\ell) \wedge
                                                                   (\hat{C}, \hat{\Gamma}, \hat{\mu}, \hat{P}) \models_{c\rho_s} e_2^{\ell_2} \wedge
                                                                   \hat{P}(\ell_2) \sqsubseteq \hat{P}(\ell) \wedge
                                                                  \forall r \in \hat{C}(\ell_1) : \forall \rho_r \sqsubseteq \rho_s :
                                                                          C(\ell_2) \subseteq \hat{\mu}(r, \rho_r) \wedge
                                                                   \hat{C}(\ell_2) \subseteq \hat{C}(\ell)
[PE\text{-}Send]
[PE-Err]
[PE-Exercise]
```

- 3.4 Theorem
- 3.5 Requirements for correctness

### **Abstract Domains**

### 4.1 Abstract domains choice

$$R_1 = \{\overrightarrow{\widehat{str_i}} : \widehat{v_i}\} \sqsubseteq \{\overrightarrow{\widehat{str_j}} : \widehat{v_j}\} = R_2 \text{ sse:}$$

- 1.  $R_1$  ha meno campi di  $R_2$
- 2. ogni campo di  $R_1$  e' piu' preciso del **corrispondente** campo di  $R_2$

$$\forall i, \exists j : \widehat{str_i} \sqsubseteq \widehat{str_j}$$
 
$$\forall i, \exists j : \widehat{str_i} \sqsubseteq \widehat{str_j} \Rightarrow \widehat{v_i} \sqsubseteq \widehat{v_j}$$
 Set:

- Exact
  - $-\exists \rightarrow Union$
  - $\not \exists \rightarrow addinprefix$
- Prefix
  - aggiungo in \*

$$\hat{v} \sqsubseteq \hat{v}' \text{ iff } \forall \hat{u}_i \in \hat{v}, \exists \hat{u}_j \in \hat{v}' : \hat{u}_i \sqsubseteq \hat{u}_j.$$
  
If Galois connection then  $\hat{v} \sqsubseteq \hat{v}' \text{ iff } \gamma(\hat{v}) \subseteq \gamma(\hat{v}')$ 

where  $\gamma: \widehat{V} \to P(V)$  is the concretisation function.

$$\gamma_p: \widehat{PV} \to P(V)$$

$$\gamma(\widehat{v}) = \bigcup_{\widehat{u}_i \in \widehat{v}} \gamma_p(\widehat{u}_i)$$

```
\widehat{pre_{bool}} = \widehat{true} | \widehat{false} |
\widehat{u_{bool}} = \{ \overrightarrow{\widehat{pre_{bool}}} \}
\widehat{pre_{int}} = \oplus |0| \ominus
                                                                                                                                                                                             with \sqsubseteq = \subseteq
\widehat{u_{int}} = \{\overline{\widehat{pre_{int}}}\}
                                                                                                                                                                                             with \sqsubseteq = \subseteq
\widehat{pre_{string}} = s|s*
\widehat{u_{string}} = \{ \overrightarrow{pre_{string}} \}
                                                                                                                                                                                             with \sqsubseteq = \subseteq
                                                                                                                                                                                              — Giulia's spec. is more tricky than \subseteq
\widehat{pre_{ref}} = r
\widehat{u_{ref}} = \{\overrightarrow{\widehat{pre_{ref}}}\}
\widehat{pre_{\lambda}} = \underline{\lambda}
                                                                                                                                                                                             with \sqsubseteq = \subseteq
\widehat{u_{\lambda}} = \{\overrightarrow{\widehat{pre_{\lambda}}}\}
                                                                                                                                                                                             with \sqsubseteq = \subseteq
\widehat{pre_{rec}} = \{ \overrightarrow{\widehat{str_i}} : \widehat{v_i} \}
\widehat{u_{rec}} = \widehat{pre_{rec}}
                                                                                                                                                                                             with \sqsubseteq = \widehat{u_{rec}}_{\sqsubseteq}
\widehat{\boldsymbol{v}} = (\widehat{u_{bool}}, \widehat{u_{int}}, \widehat{u_{string}}, \widehat{u_{ref}}, \widehat{u_{\lambda}}, \widehat{u_{rec}}, \{\widehat{Null}\}, \{\widehat{Undef}\})
                                                                                                                                                                                             with \hat{v} \sqsubseteq \hat{v}' iff
                                                                                                                                                                                           \widehat{u_{bool}} \sqsubseteq \widehat{u_{bool}}' \wedge
                                                                                                                                                                                           \widehat{u_{int}} \sqsubseteq \widehat{u_{int}}' \wedge
                                                                                                                                                                                           \widehat{u_{string}} \sqsubseteq \widehat{u_{string}}' \wedge
                                                                                                                                                                                           \widehat{u_{ref}} \sqsubseteq \widehat{u_{ref}}' \wedge
                                                                                                                                                                                           \widehat{u_{\lambda}} \sqsubseteq \widehat{u_{\lambda}}' \wedge
                                                                                                                                                                                           \widehat{u_{rec}} \sqsubseteq \widehat{u_{rec}}' \wedge
                                                                                                                                                                                           \widehat{Null} \not\in \hat{v}' \lor \widehat{Null} \in \hat{v} \land \widehat{Null} \in \hat{v}' \land
                                                                                                                                                                                           \widehat{Undef} \notin \hat{v}' \vee \widehat{Undef} \in \hat{v} \wedge \widehat{Undef} \in \hat{v}'
```

#### 4.2 Abstract operations

#### 4.3 Requirements verification

### Implementation

#### 5.1 Constraint generation

Constraint elements: E.

 $\begin{array}{llll} \textit{Cache element} & \mathsf{C}(\ell) & : & \mathcal{L} \to \hat{V} \\ \textit{Var element} & \mathsf{\Gamma}(x) & : & \mathcal{V} \to \hat{V} \\ \textit{State element} & \mathsf{M}(\mathcal{P}, ref) & : & \mathcal{L} \times \mathcal{P} \to \hat{V} \\ \end{array}$ 

Permission Element:  $P(\ell): \mathcal{L} \to \mathcal{P}$ 

Constraint form.

Misc:

 $r_*$  is the set of all references of the program;  $lambda_*$  is the set of all lambdas of the program;

```
[CG-Val]
                                                                                                 \mathcal{C}_{*\rho_s}[\![(c)^\ell]\!] = \{d_c\} \subseteq \mathsf{C}(\ell)
 [CG-Var]
                                                                                                 \mathcal{C}_{*\rho_s} \llbracket (x)^\ell \rrbracket = \Gamma(x) \subseteq \mathsf{C}(\ell)
                                                                                                 \mathcal{C}_{*\rho_s} \llbracket (\lambda x.e_0^{\ell_0})^{\ell} \rrbracket =
 [CG-Lambda]
                                                                                                                 \{\{\lambda x.e_0^{\ell_0}\}\subseteq \mathsf{C}(\ell)\}\cup
                                                                                                               C_{*\rho_s}[(e_0^{\ell_0})]
                                                                                                 \mathcal{C}_{*\rho_s} \llbracket (\{\overline{str_i : e_i^{\ell_i}}\})^{\ell} \rrbracket =
[CG-Obj]
                                                                                                                 \bigcup_{i} (\mathcal{C}_{*\rho_{s}} \llbracket (e_{i}^{\ell_{i}}) \rrbracket \cup
                                                                                                                                \{\mathsf{P}(\ell_i) \sqsubseteq \mathsf{P}(\ell)\}) \cup
                                                                                                                 \{\{\overrightarrow{str_i}: C(\ell_i)\}\subseteq C(\ell)\}
                                                                                                \mathcal{C}_{*\rho_s}[\![(\mathbf{let}\ \overrightarrow{x_i = e_i^{\ell_i}}\ \mathbf{in}\ e'^{\ell'})^{\ell}]\!] =
[CG-Let]
                                                                                                                 \bigcup_{i} (\mathcal{C}_{*\rho_s} \llbracket (e_i^{\ell_i}) \rrbracket \cup
                                                                                                                                \{\mathsf{C}(\ell_i)\subseteq\mathsf{\Gamma}(x_i)\}\cup
                                                                                                                                \{P(\ell_i) \subseteq P(\ell)\}) \cup
                                                                                                               \mathcal{C}_{*\rho_s}\llbracket(e'^{\ell'})\rrbracket\cup
                                                                                                                 \{P(\ell') \sqsubseteq P(\ell)\} \cup
                                                                                                                 \{C(\ell')\subseteq C(\ell)\}
                                                                                                 C_{*\rho_s} \llbracket (e_1^{\ell_1} e_2^{\ell_2})^{\ell} \rrbracket =
[CG-App]
                                                                                                                \mathcal{C}_{*\rho_s}[\![(e_1^{\ell_1})]\!] \cup \mathcal{C}_{*\rho_s}[\![(e_2^{\ell_2})]\!] \cup
                                                                                                                 \{\mathsf{P}(\ell_1) \sqsubseteq \mathsf{P}(\ell)\} \cup \{\mathsf{P}(\ell_2) \sqsubseteq \mathsf{P}(\ell)\} \cup
                                                                                                                 \{\{t\}\subseteq \mathsf{C}(\ell_1)\Rightarrow \mathsf{C}(\ell_2)\subseteq \mathsf{\Gamma}(x)
                                                                                                                                |t = (\lambda x.e_0^{\ell_0}) \in lambda_*\} \cup
                                                                                                                  \{\{t\}\subseteq \mathsf{C}(\ell_1)\Rightarrow \mathsf{C}(\ell_0)\subseteq \mathsf{C}(\ell)\}
                                                                                                                                |t = (\lambda x. e_0^{\ell_0}) \in lambda_* \} \cup
                                                                                                                  \{\{t\}\subseteq \mathsf{C}(\ell_1)\Rightarrow \mathsf{P}(\ell_0)\sqsubseteq \mathsf{P}(\ell)\}
                                                                                                                               |t = (\lambda x.e_0^{\ell_0}) \in lambda_*\} \cup
                                                                                                \mathcal{C}_{*o_s} \llbracket (op(\overrightarrow{e_i^{\ell_i}}))^{\ell} \rrbracket =
[CG-Op]
                                                                                                                \bigcup_{i}(\mathcal{C}_{*\rho_{s}}\llbracket(e_{i}^{\ell_{i}})\rrbracket \cup \{\mathsf{P}(\ell_{i})\sqsubseteq\mathsf{P}(\ell)\}) \cup
                                                                                                                  \{\widehat{op}(\mathsf{C}(\ell_i))\subseteq\mathsf{C}(\ell)\}\
                                                                                                 C_{*\rho_s} [(\mathbf{if} (e_0^{\ell_0}) \{ e_1^{\ell_1} \} \mathbf{else} \{ e_2^{\ell_2} \})^{\ell}] =
[CG-Cond]
                                                                                                                C_{*\rho_s}[(e_0^{\ell_0})] \cup C_{*\rho_s}[(e_1^{\ell_1})] \cup C_{*\rho_s}[(e_2^{\ell_2})] \cup
                                                                                                                 \{\hat{P}(\ell_0) \sqsubseteq \hat{P}(\ell)\} \cup
                                                                                                                  \{\widehat{\mathbf{true}} \in \mathsf{C}(\ell_0) \Rightarrow \mathsf{C}(\ell_1) \subseteq \mathsf{C}(\ell)\} \cup
                                                                                                                  \{ \widehat{\mathbf{true}} \in \mathsf{C}(\ell_0) \Rightarrow \mathsf{P}(\ell_1) \sqsubseteq \mathsf{P}(\ell) \} \cup
                                                                                                                  \{ \mathbf{false} \in \mathsf{C}(\ell_0) \Rightarrow \mathsf{C}(\ell_2) \subseteq \mathsf{C}(\ell) \} \cup \{ \mathsf{C}(\ell_0) \} \cup \{ \mathsf{C}(\ell_0)
                                                                                                                  \{false \in C(\ell_0) \Rightarrow P(\ell_2) \sqsubseteq P(\ell) \}
                                                                                                C_{*\rho_s}[(\mathbf{while}\ (e_1^{\ell_1})\ \{\ e_2^{\ell_2}\ \})^{\ell}]] =
[CG-While]
                                                                                                                 C_{*\rho_s}[(e_1^{\ell_1})] \cup C_{*\rho_s}[(e_2^{\ell_2})] \cup
                                                                                                                 \{P(\ell_1) \sqsubseteq P(\ell)\} \cup
                                                                                                                  \{\widehat{\mathbf{true}} \in \mathsf{C}(\ell_1) \Rightarrow \mathsf{C}(\ell_2) \subseteq \mathsf{C}(\ell)\} \cup
                                                                                                                  \{\widehat{\mathbf{true}} \in \mathsf{C}(\ell_1) \Rightarrow \mathsf{P}(\ell_2) \subseteq \mathsf{P}(\ell)\} \cup
                                                                                                                  \{false \in C(\ell_1) \Rightarrow undefined \subseteq C(\ell)\}
```

```
[CG\text{-}GetField] \quad \mathcal{C}_{*\rho_s}[[(e_1^{\ell_1}[e_2^{\ell_2}])^{\ell}]] =
                                                      C_{*\rho_s}[(e_1^{\ell_1})] \cup C_{*\rho_s}[(e_2^{\ell_2})] \cup
                                                       \{P(\ell_1) \sqsubseteq P(\ell)\} \cup
                                                      \{P(\ell_2) \sqsubseteq P(\ell)\} \cup
                                                      \widehat{qet}(\mathsf{C}(\ell_1),\mathsf{C}(\ell_2))\subset\mathsf{C}(\ell)
                                        C_{*\rho_s} \llbracket (e_0^{\ell_0} [e_1^{\ell_1}] = e_2^{\ell_2}) \rrbracket =
[CG	ext{-}SetField]
                                                      C_{*\rho_s}[(e_0^{\ell_0})] \cup C_{*\rho_s}[(e_1^{\ell_1})^{\ell}] \cup C_{*\rho_s}[(e_2^{\ell_2})] \cup
                                                       \{P(\ell_1) \sqsubseteq P(\ell)\} \cup
                                                       \{P(\ell_2) \sqsubseteq P(\ell)\} \cup
                                                       \{P(\ell_3) \sqsubseteq P(\ell)\} \cup
                                                      \widehat{set}(\mathsf{C}(\ell_1),\mathsf{C}(\ell_2),\mathsf{C}(\ell_2))\subseteq\mathsf{C}(\ell)
[CG-DelField]
                                         \mathcal{C}_{*\rho_s}[\![(\mathbf{delete}\ e_1^{\ell_1}[e_2^{\ell_2}])^{\ell}]\!] =
                                                      C_{*\rho_s}[[(e_1^{\ell_1})]] \cup C_{*\rho_s}[[(e_2^{\ell_2})]] \cup
                                                       \{P(\ell_1) \sqsubseteq P(\ell)\} \cup
                                                       \{P(\ell_2) \sqsubseteq P(\ell)\} \cup
                                                      del(C(\ell_1), C(\ell_2)) \subseteq C(\ell)
[CG-Ref]
                                         C_{*\rho_s}[\![(\mathbf{ref}_{r,\rho_r} e_1^{\ell_1})^{\ell}]\!] =
                                                      C_{*\rho_s}[\![(e_1^{\ell_1})]\!] \cup
                                                       \{\{r\}\subseteq \mathsf{C}(\ell)\}\cup
                                                       \{P(\ell_1) \sqsubseteq P(\ell)\} \cup
                                                      \{\rho_r \sqsubseteq \rho_s \Rightarrow \mathsf{C}(\ell_1) \subseteq \mathsf{M}(r,\rho_r)\}
                                        \mathcal{C}_{*\rho_s}[\![(\mathbf{deref}\ e_1^{\ell_1})^\ell]\!] =
[CG-DeRef]
                                                      C_{*\rho_s}[(e_1^{\ell_1})] \cup
                                                      \{P(\ell_1) \sqsubseteq P(\ell)\} \cup
                                                       \{r \in \mathsf{C}(\ell_1) \Rightarrow \mathsf{M}(r, \rho_r) \subseteq \mathsf{C}(\ell)\}
                                                           \mid r \in r_*, \rho_r \sqsubseteq \rho_s \}
                                        C_{*o_s}[(e_1^{\ell_1} = e_2^{\ell_2})^{\ell}] =
[CG	ext{-}SetRef]
                                                      C_{*\rho_s}[(e_1^{\ell_1})] \cup C_{*\rho_s}[(e_2^{\ell_2})] \cup
                                                       \{P(\ell_1) \sqsubseteq P(\ell)\} \cup
                                                       \{P(\ell_2) \sqsubseteq P(\ell)\} \cup
                                                       \{r \in \mathsf{C}(\ell_1) \Rightarrow \mathsf{C}(\ell_2) \subseteq \mathsf{M}(r, \rho_r)\}
                                                           | r \in r_*, \rho_r \sqsubseteq \rho_s \} \cup
                                                       \{C(\ell_2) \subseteq C(\ell)\}
[PE\text{-}Send]
[PE-Err]
[PE-Exercise]
```

#### 5.2 Constraint solving

#### 5.3 Implementation-specific details

## Experiments

- 6.1 Findings
- 6.2 Performance

SLOW... Very SLOW!!!

## Conclusion

- 7.1 Conclusions
- 7.2 Future works (unbundling)

[1]

## Bibliography

[1] HanneRiis Nielson and Flemming Nielson. Flow logic: A multi-paradigmatic approach to static analysis. In TorbenÆ. Mogensen, DavidA. Schmidt, and I.Hal Sudborough, editors, *The Essence of Computation*, volume 2566 of *Lecture Notes in Computer Science*, pages 223–244. Springer Berlin Heidelberg, 2002.