

# STAT 331 Final Project

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## Requirement of the project

Your 7–10 page report must contain the following components:

- 1. Summary: A maximum of 200 words describing the objective of the report, an overview of the statistical analysis, and summary of the main results.
- 2. Objective: Describe your goals for the analysis.
- 3. Exploratory Data Analysis: Conduct exploratory data analyses: report summary statistics, visualize data (histograms, scatter plots, etc.). Report on any interesting findings and comment on how these inform the rest of your analysis.
- 4. Methods: Describe your statistical analysis: What is your model? Did you use any transformations or extensions of the basic multiple linear regression model? How did you select a model? Does the model fit the data well? Are the necessary assumptions met? Be sure to explain and justify your decisions.
- 5. Results: Report on the findings of your analysis
- 6. Discussion: Comment on your findings/conclusions; describe any limitations of your analysis.

## 1. Summary

A maximum of 200 words describing the objective of the report, an overview of the statistical analysis, and summary of the main results.

## 2. Objective

The goal of this project is to analyze the pollutants.csv data and write a report on your analysis. The specific goals of your analysis are up to you to decide.

## 3. Exploratory Data Analysis

Conduct exploratory data analyses: report summary statistics, visualize data (histograms, scatter plots, etc.). Report on any interesting findings and comment on how these inform the rest of your analysis.

can use this as a tutorial <https://r4ds.had.co.nz/exploratory-data-analysis.html>

Take a peak at the first 5 entries

```
# CHANGE ABSOLUTE PATH
# setwd("~/Desktop/stat341/R331project/data")
# setwd("~/School/4A/STAT 331/R331project/data")
setwd("~/Desktop/R331project/data")

pollutants <- read.csv("pollutants.csv", header = TRUE)
head(pollutants)
```

```
##      X      length POP_PCB1 POP_PCB2 POP_PCB3 POP_PCB4 POP_PCB5 POP_PCB6 POP_PCB7
## 1 1 1.1587651    20000     7600     3700     14700     18900     5300     5500
## 2 2 0.9011283    43900    14900     9700     32300     55500    13400    18700
## 3 3 1.2753948     3300     3300     3300     3300     3300     3300     3300
## 4 4 0.9369063     8500     4100     6000     11500     13500     6900    13500
## 5 5 0.7027998    159000    60200    29800    170000    215000    79200    47400
## 6 6 1.1516147     14400     7100    16900     28200     37200    22000    10200
##      POP_PCB8 POP_PCB9 POP_PCB10 POP_PCB11 POP_dioxin1 POP_dioxin2 POP_dioxin3
## 1         5700     2000     15.6     23.1         70.9         50.0         173
## 2        12000    16200     35.4     31.1        116.0        129.0         709
## 3         3300     3300      1.8      9.3         29.9          5.4         148
## 4         4100     4100      4.5     21.1         50.4         29.4         668
## 5        41400    53900     59.2     80.3         98.1         80.1         875
## 6         3800     6400     19.2     70.0        106.0         47.4         533
##      POP_furan1 POP_furan2 POP_furan3 POP_furan4 whitecell_count lymphocyte_pct
## 1          6.9         5.6          0.8         15.6             5.4             33.8
## 2         18.5        15.4         20.3          2.3             5.6             16.8
## 3          1.3         1.4          1.2          2.9             6.3             35.3
## 4          2.2         2.4          2.3         43.2             8.4             23.0
## 5         13.7         1.2          0.8         11.0             6.7             24.5
## 6          8.3         7.0          3.4         19.4             4.7             39.5
##      monocyte_pct eosinophils_pct basophils_pct neutrophils_pct BMI edu_cat
## 1          8.1             51.2          6.2          0.6 27.50         2
## 2         10.2             69.4          3.2          0.5 27.46         3
## 3          7.3             54.9          1.6          0.9 36.13         1
## 4          6.4             68.8          1.7          0.2 21.79         4
## 5          7.5             64.3          3.0          0.8 31.46         2
## 6          4.4             54.2          1.3          0.8 40.68         1
##      race_cat male ageyrs yrssmoke smokenow ln_lbxcot
## 1          4      1      41          0          0 -2.312635
## 2          4      0      77          0          0 -4.509860
## 3          2      0      22          0          0 -4.017384
## 4          4      0      27          0          0 -3.863233
## 5          4      1      78          0          0 -1.826351
## 6          3      0      35          0          0 -2.207275
```

## Covariates

```
names(pollutants)
```

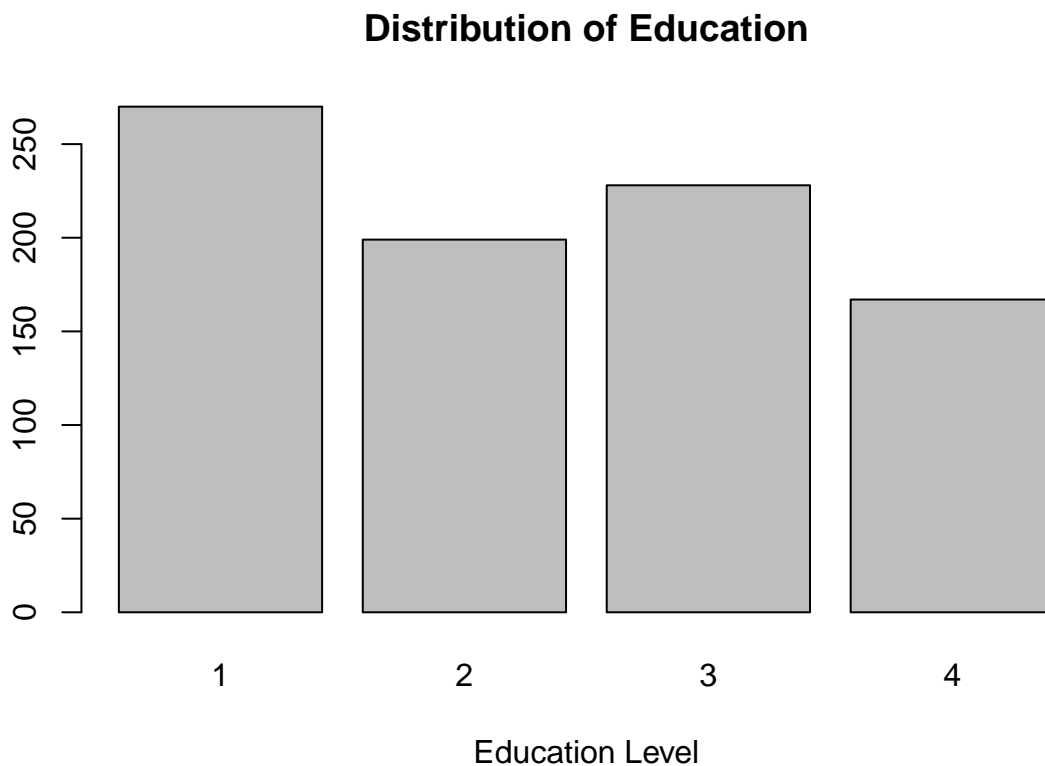
```
## [1] "X"                "length"           "POP_PCB1"         "POP_PCB2"
## [5] "POP_PCB3"         "POP_PCB4"         "POP_PCB5"         "POP_PCB6"
## [9] "POP_PCB7"         "POP_PCB8"         "POP_PCB9"         "POP_PCB10"
## [13] "POP_PCB11"        "POP_dioxin1"      "POP_dioxin2"      "POP_dioxin3"
## [17] "POP_furan1"      "POP_furan2"      "POP_furan3"      "POP_furan4"
```

```
## [21] "whitecell_count" "lymphocyte_pct" "monocyte_pct" "eosinophils_pct"
## [25] "basophils_pct" "neutrophils_pct" "BMI" "edu_cat"
## [29] "race_cat" "male" "ageyrs" "yrssmoke"
## [33] "smokenow" "ln_lbxcot"
```

Note that “edu\_cat”, “race\_cat”, “male”, “smokenow” are categorical data.

```
# 1 = Less Than 9th Grade or 9-11th Grade (Includes 12th grade with no diploma)
# 2 = High School Grad/GED or Equivalent
# 3 = Some College or AA degree
# 4 = College Graduate
```

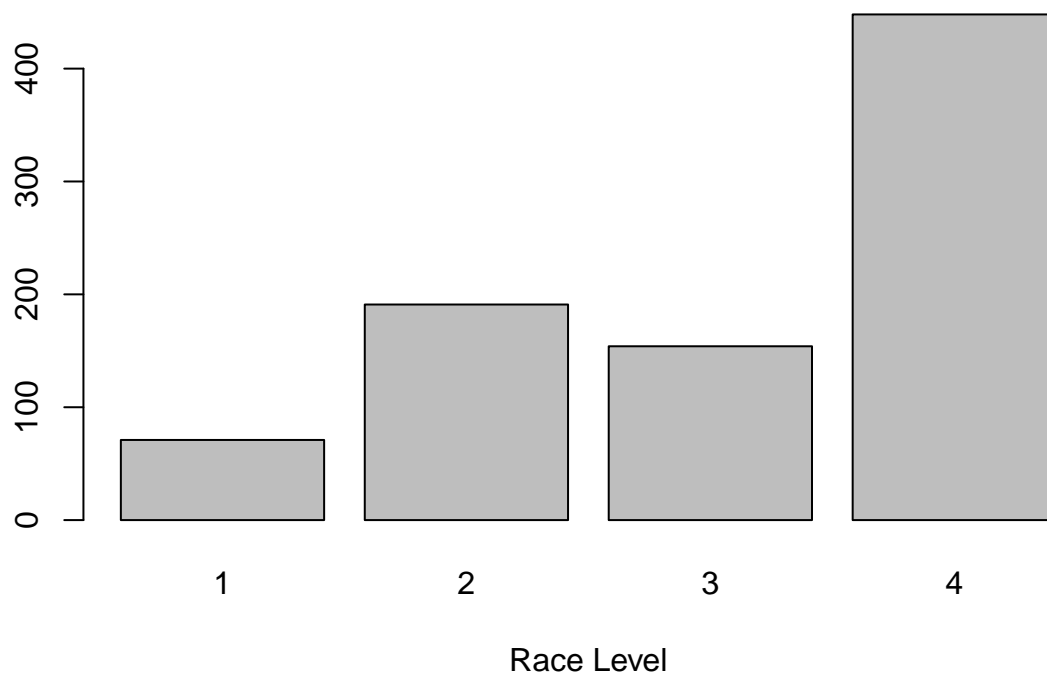
```
edu_factor=as.factor(pollutants$edu_cat)
plot(edu_factor,
     main="Distribution of Education",
     xlab="Education Level")
```



```
# 1 = Other Race (Including Multi-Racial);
# 2 = Mexican American;
# 3 = Non-Hispanic Black;
# 4 = Non-Hispanic White
```

```
race_factor=as.factor(pollutants$race_cat)
plot(race_factor,
     main="Distribution of Race",
     xlab="Race Level")
```

## Distribution of Race



```
# Estella's work 1
library(corrplot)
```

```
## corrplot 0.84 loaded
```

```
library(ggplot2)
```

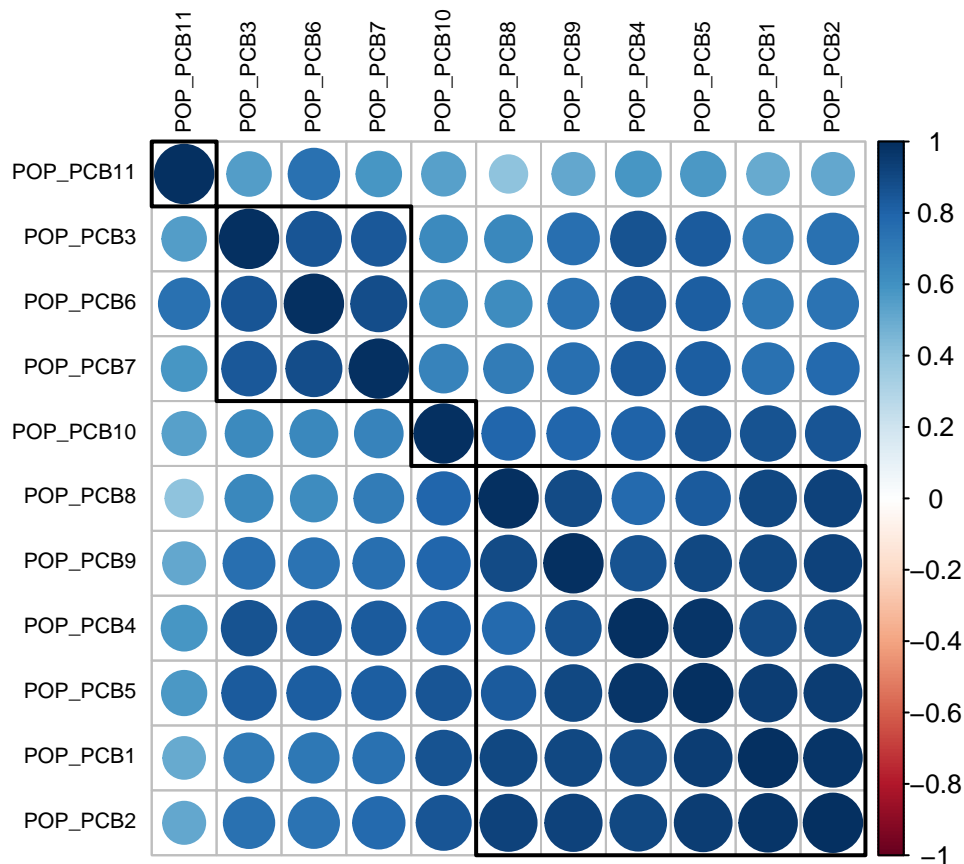
```
summary(pollutants)
```

```
##           X           length      POP_PCB1      POP_PCB2
## Min.      : 1.0      Min.      :0.5266      Min.      : 2000      Min.      : 2000
## 1st Qu.:216.8      1st Qu.:0.8754      1st Qu.: 9975      1st Qu.: 4800
## Median :432.5      Median :1.0286      Median : 27600     Median : 11500
## Mean      :432.5      Mean      :1.0543      Mean      : 38082     Mean      : 15637
## 3rd Qu.:648.2      3rd Qu.:1.2095      3rd Qu.: 53325     3rd Qu.: 21825
## Max.      :864.0      Max.      :2.3512      Max.      :572000     Max.      :165000
## POP_PCB3      POP_PCB4      POP_PCB5      POP_PCB6
## Min.      : 2000      Min.      : 2100      Min.      : 2100      Min.      : 2000
## 1st Qu.: 3700      1st Qu.: 11475      1st Qu.: 15600      1st Qu.: 4400
## Median : 6200      Median : 25550      Median : 36300      Median : 9400
## Mean      : 10158      Mean      : 38456      Mean      : 52650      Mean      : 16820
## 3rd Qu.: 12000      3rd Qu.: 50650      3rd Qu.: 68625      3rd Qu.: 19500
## Max.      :123000      Max.      :487000      Max.      :708000      Max.      :319000
## POP_PCB7      POP_PCB8      POP_PCB9      POP_PCB10
## Min.      : 1100      Min.      : 1100      Min.      : 1100      Min.      : 1.70
## 1st Qu.: 4000      1st Qu.: 3800      1st Qu.: 3900      1st Qu.: 9.10
## Median : 7450      Median : 6950      Median : 8050      Median : 18.35
## Mean      : 12682      Mean      : 10530      Mean      : 12220      Mean      : 24.49
## 3rd Qu.: 15625      3rd Qu.: 14425      3rd Qu.: 16025      3rd Qu.: 34.90
## Max.      :144000      Max.      :187000      Max.      :144000      Max.      :172.00
```

```
## POP_PCB11 POP_dioxin1 POP_dioxin2 POP_dioxin3
## Min. : 1.30 Min. : 1.90 Min. : 1.40 Min. : 36.8
## 1st Qu.: 14.80 1st Qu.: 23.90 1st Qu.: 21.27 1st Qu.: 197.0
## Median : 24.50 Median : 41.35 Median : 37.80 Median : 342.5
## Mean : 38.15 Mean : 57.65 Mean : 47.81 Mean : 494.4
## 3rd Qu.: 42.95 3rd Qu.: 71.62 3rd Qu.: 62.42 3rd Qu.: 603.0
## Max. :845.00 Max. :760.00 Max. :281.00 Max. :8190.0
## POP_furan1 POP_furan2 POP_furan3 POP_furan4
## Min. : 1.000 Min. : 0.800 Min. : 0.700 Min. : 0.90
## 1st Qu.: 3.200 1st Qu.: 2.600 1st Qu.: 2.200 1st Qu.: 6.40
## Median : 5.200 Median : 4.200 Median : 5.050 Median : 9.65
## Mean : 6.371 Mean : 5.390 Mean : 6.669 Mean : 11.54
## 3rd Qu.: 7.700 3rd Qu.: 6.825 3rd Qu.: 9.300 3rd Qu.: 14.00
## Max. :44.400 Max. :33.500 Max. :38.300 Max. :234.00
## whitecell_count lymphocyte_pct monocyte_pct eosinophils_pct
## Min. : 2.300 Min. : 5.80 Min. : 1.600 Min. :21.60
## 1st Qu.: 5.600 1st Qu.:24.00 1st Qu.: 6.600 1st Qu.:52.35
## Median : 6.900 Median :28.95 Median : 7.700 Median :59.30
## Mean : 7.191 Mean :29.92 Mean : 7.936 Mean :58.62
## 3rd Qu.: 8.300 3rd Qu.:35.42 3rd Qu.: 9.100 3rd Qu.:65.22
## Max. :20.100 Max. :73.40 Max. :23.800 Max. :88.10
## basophils_pct neutrophils_pct BMI edu_cat
## Min. : 0.000 Min. :0.0000 Min. :16.16 Min. :1.000
## 1st Qu.: 1.500 1st Qu.:0.4000 1st Qu.:23.88 1st Qu.:1.000
## Median : 2.300 Median :0.6000 Median :27.38 Median :2.000
## Mean : 2.903 Mean :0.6669 Mean :28.09 Mean :2.338
## 3rd Qu.: 3.700 3rd Qu.:0.8000 3rd Qu.:31.17 3rd Qu.:3.000
## Max. :28.200 Max. :5.5000 Max. :62.99 Max. :4.000
## race_cat male ageyrs yrssmoke
## Min. :1.000 Min. :0.0000 Min. :20.00 Min. : 0.0
## 1st Qu.:2.000 1st Qu.:0.0000 1st Qu.:34.00 1st Qu.: 0.0
## Median :4.000 Median :0.0000 Median :46.00 Median : 0.0
## Mean :3.133 Mean :0.4329 Mean :48.36 Mean :10.6
## 3rd Qu.:4.000 3rd Qu.:1.0000 3rd Qu.:63.00 3rd Qu.:20.0
## Max. :4.000 Max. :1.0000 Max. :85.00 Max. :69.0
## smokenow ln_lbxcot
## Min. :0.0000 Min. : -4.5099
## 1st Qu.:0.0000 1st Qu.: -4.0745
## Median :0.0000 Median : -2.7334
## Mean :0.2315 Mean : -0.9804
## 3rd Qu.:0.0000 3rd Qu.: 2.8000
## Max. :1.0000 Max. : 6.5848
```

```
POP_PCB = c("POP_PCB1", "POP_PCB2", "POP_PCB3", "POP_PCB4", "POP_PCB5", "POP_PCB6", "POP_PCB7", "POP_PCB8")
POP_PCB_data <- pollutants[, POP_PCB]
cc = cor(POP_PCB_data, method = "spearman")
```

```
# cluster my POP_PCB so that those with similar patterns of correlation coefficients are closer together
corrplot(cc, tl.col = "black", order = "hclust", hclust.method = "average", addrect = 4, tl.cex = 0.7)
```



<https://jkgzorz.github.io/2019/06/11/Correlation-heatmaps.html>

# Estella's work 3

```
f <- as.formula((paste("length", paste("(", paste(POP_PCB, collapse = " + "), ")^2"), sep = " ~"))
m <- lm(f, data = pollutants)
summary(m)
```

```
##
## Call:
## lm(formula = f, data = pollutants)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.53819 -0.16080 -0.01896  0.12149  1.20671
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    1.153e+00  2.892e-02  39.876 < 2e-16 ***
## POP_PCB1      -6.741e-06  3.521e-06  -1.915  0.05591 .
## POP_PCB2       3.801e-06  9.328e-06   0.407  0.68378
## POP_PCB3       6.747e-06  6.701e-06   1.007  0.31431
## POP_PCB4       1.373e-06  3.278e-06   0.419  0.67539
## POP_PCB5       1.920e-06  3.267e-06   0.588  0.55680
## POP_PCB6      -3.673e-06  4.336e-06  -0.847  0.39729
## POP_PCB7      -5.281e-06  4.697e-06  -1.124  0.26126
## POP_PCB8      -1.073e-05  8.331e-06  -1.288  0.19796
## POP_PCB9      -1.833e-06  5.806e-06  -0.316  0.75232
```

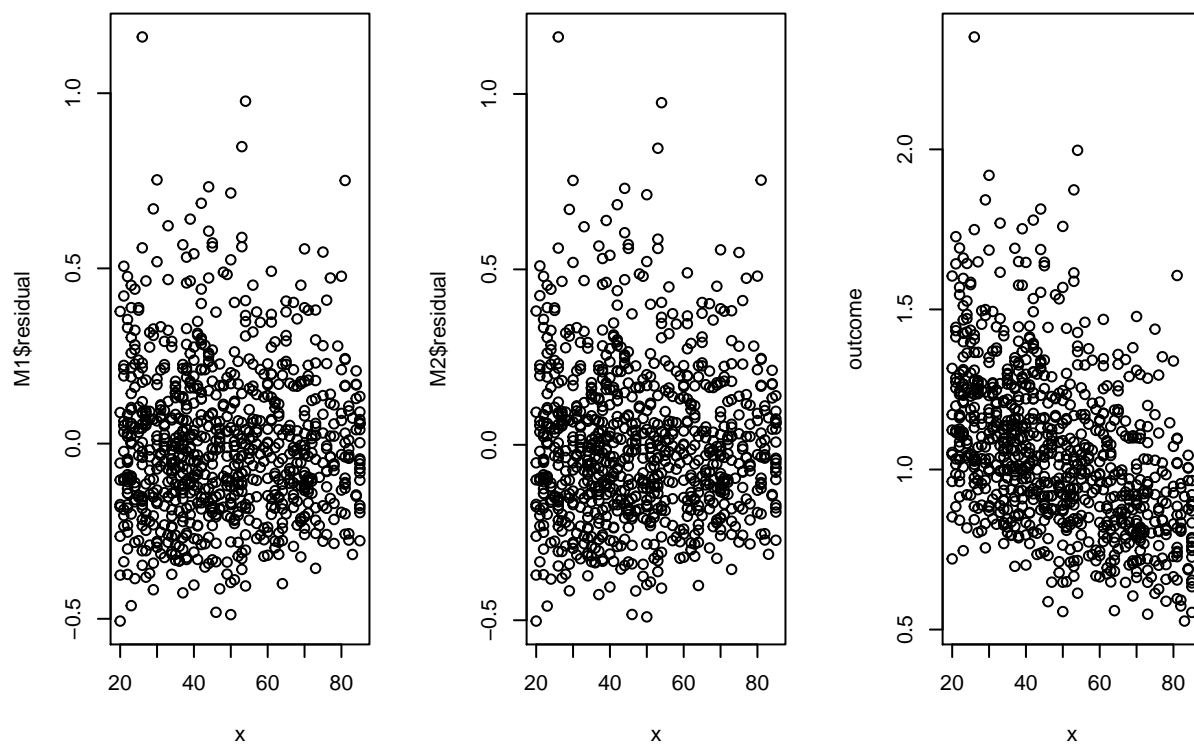
## POP_PCB10	2.720e-03	2.088e-03	1.303	0.19311
## POP_PCB11	4.644e-04	9.916e-04	0.468	0.63969
## POP_PCB1:POP_PCB2	9.529e-11	2.113e-10	0.451	0.65216
## POP_PCB1:POP_PCB3	-6.580e-10	4.156e-10	-1.583	0.11377
## POP_PCB1:POP_PCB4	1.116e-10	1.917e-10	0.582	0.56080
## POP_PCB1:POP_PCB5	-1.621e-11	1.318e-10	-0.123	0.90218
## POP_PCB1:POP_PCB6	6.244e-11	2.176e-10	0.287	0.77423
## POP_PCB1:POP_PCB7	2.221e-11	2.742e-10	0.081	0.93548
## POP_PCB1:POP_PCB8	-5.209e-10	2.693e-10	-1.935	0.05340 .
## POP_PCB1:POP_PCB9	4.146e-10	2.287e-10	1.813	0.07020 .
## POP_PCB1:POP_PCB10	1.675e-07	1.311e-07	1.277	0.20183
## POP_PCB1:POP_PCB11	-6.663e-08	7.321e-08	-0.910	0.36303
## POP_PCB2:POP_PCB3	1.673e-09	8.717e-10	1.919	0.05537 .
## POP_PCB2:POP_PCB4	-6.761e-10	4.688e-10	-1.442	0.14963
## POP_PCB2:POP_PCB5	3.840e-10	3.632e-10	1.057	0.29069
## POP_PCB2:POP_PCB6	-1.426e-09	5.834e-10	-2.444	0.01474 *
## POP_PCB2:POP_PCB7	1.532e-09	6.770e-10	2.264	0.02387 *
## POP_PCB2:POP_PCB8	2.135e-09	8.207e-10	2.602	0.00945 **
## POP_PCB2:POP_PCB9	-1.356e-09	7.249e-10	-1.870	0.06183 .
## POP_PCB2:POP_PCB10	-1.232e-06	4.242e-07	-2.904	0.00378 **
## POP_PCB2:POP_PCB11	3.388e-07	2.013e-07	1.683	0.09270 .
## POP_PCB3:POP_PCB4	-3.996e-11	1.199e-10	-0.333	0.73900
## POP_PCB3:POP_PCB5	4.665e-11	2.413e-10	0.193	0.84674
## POP_PCB3:POP_PCB6	-3.741e-10	2.662e-10	-1.405	0.16029
## POP_PCB3:POP_PCB7	6.438e-10	2.896e-10	2.223	0.02649 *
## POP_PCB3:POP_PCB8	7.340e-10	8.821e-10	0.832	0.40563
## POP_PCB3:POP_PCB9	-4.221e-10	5.470e-10	-0.772	0.44059
## POP_PCB3:POP_PCB10	-4.835e-07	2.555e-07	-1.892	0.05885 .
## POP_PCB3:POP_PCB11	7.155e-08	7.874e-08	0.909	0.36382
## POP_PCB4:POP_PCB5	3.002e-12	6.669e-11	0.045	0.96410
## POP_PCB4:POP_PCB6	1.788e-10	1.543e-10	1.159	0.24694
## POP_PCB4:POP_PCB7	-2.117e-10	1.579e-10	-1.341	0.18019
## POP_PCB4:POP_PCB8	-4.525e-11	3.961e-10	-0.114	0.90908
## POP_PCB4:POP_PCB9	1.217e-10	2.625e-10	0.464	0.64294
## POP_PCB4:POP_PCB10	1.345e-07	8.933e-08	1.505	0.13265
## POP_PCB4:POP_PCB11	1.685e-08	5.047e-08	0.334	0.73861
## POP_PCB5:POP_PCB6	4.714e-11	1.390e-10	0.339	0.73458
## POP_PCB5:POP_PCB7	-1.555e-10	1.446e-10	-1.076	0.28244
## POP_PCB5:POP_PCB8	-4.639e-10	3.185e-10	-1.457	0.14562
## POP_PCB5:POP_PCB9	-1.626e-11	1.822e-10	-0.089	0.92890
## POP_PCB5:POP_PCB10	9.703e-08	9.241e-08	1.050	0.29406
## POP_PCB5:POP_PCB11	-5.549e-08	4.079e-08	-1.360	0.17407
## POP_PCB6:POP_PCB7	-2.248e-11	1.147e-10	-0.196	0.84474
## POP_PCB6:POP_PCB8	7.086e-10	3.808e-10	1.861	0.06310 .
## POP_PCB6:POP_PCB9	4.295e-10	3.267e-10	1.315	0.18895
## POP_PCB6:POP_PCB10	2.152e-07	1.182e-07	1.820	0.06909 .
## POP_PCB6:POP_PCB11	-4.299e-08	2.038e-08	-2.109	0.03523 *
## POP_PCB7:POP_PCB8	-1.029e-09	4.279e-10	-2.404	0.01645 *
## POP_PCB7:POP_PCB9	-2.467e-10	3.622e-10	-0.681	0.49603
## POP_PCB7:POP_PCB10	-3.893e-08	1.308e-07	-0.298	0.76608
## POP_PCB7:POP_PCB11	4.226e-08	3.690e-08	1.145	0.25246
## POP_PCB8:POP_PCB9	1.317e-10	5.297e-10	0.249	0.80373
## POP_PCB8:POP_PCB10	5.264e-07	3.029e-07	1.738	0.08265 .
## POP_PCB8:POP_PCB11	-5.764e-08	1.285e-07	-0.449	0.65382

```
## POP_PCB9:POP_PCB10 -2.240e-08 1.448e-07 -0.155 0.87712
## POP_PCB9:POP_PCB11 7.916e-08 6.811e-08 1.162 0.24548
## POP_PCB10:POP_PCB11 -5.384e-05 2.694e-05 -1.999 0.04599 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2377 on 797 degrees of freedom
## Multiple R-squared:  0.1666, Adjusted R-squared:  0.09763
## F-statistic: 2.415 on 66 and 797 DF,  p-value: 1.316e-08

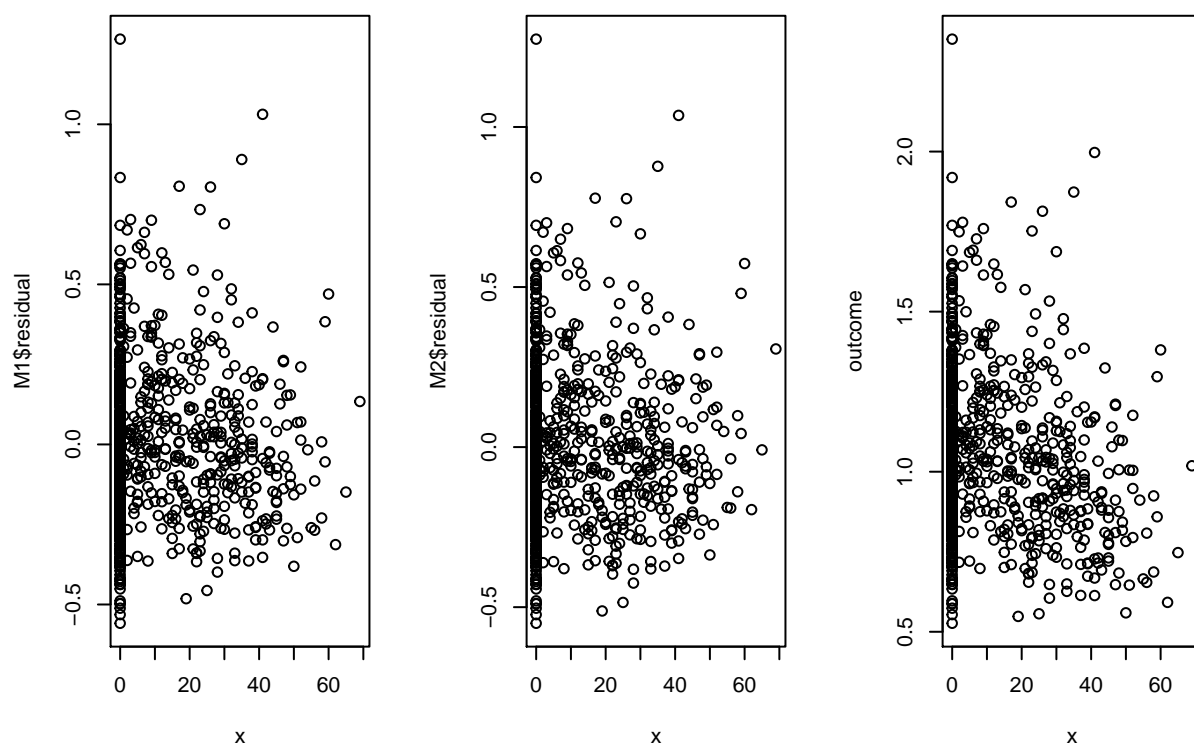
# Judy's work Part 1
# testing non-linearity in SLR
# if for any covariate, residual vs x for M1 has a pattern and
# residual vs x for M2 seems random, then y has a nonlinear
# relationship with x.
# M1: fitting y to x
# M2: fitting y to x^2
par(mfrow=c(1, 3))
outcome <- pollutants$length
check <- function(x) {
  M1 <- lm(outcome ~ x)
  print(paste("residual for M1: ", sigma(M1)))
  M2 <- lm(outcome ~ x + I(x^2))
  print(paste("residual for M2: ", sigma(M2)))
  plot(x, M1$residual)
  plot(x, M2$residual)
  plot(x, outcome)
}
list <- list(pollutants$ageyrs, pollutants$yrssmoke,
             pollutants$BMI, pollutants$ln_lbxcot,
             pollutants$whitecell_count, pollutants$lymphocyte_pct,
             pollutants$monocyte_pct, pollutants$eosinophils_pct,
             pollutants$basophils_pct, pollutants$neutrophils_pct)
for (column in list) {
  check(column)
}

## [1] "residual for M1: 0.224172364185412"
## [1] "residual for M2: 0.22429269961392"
```

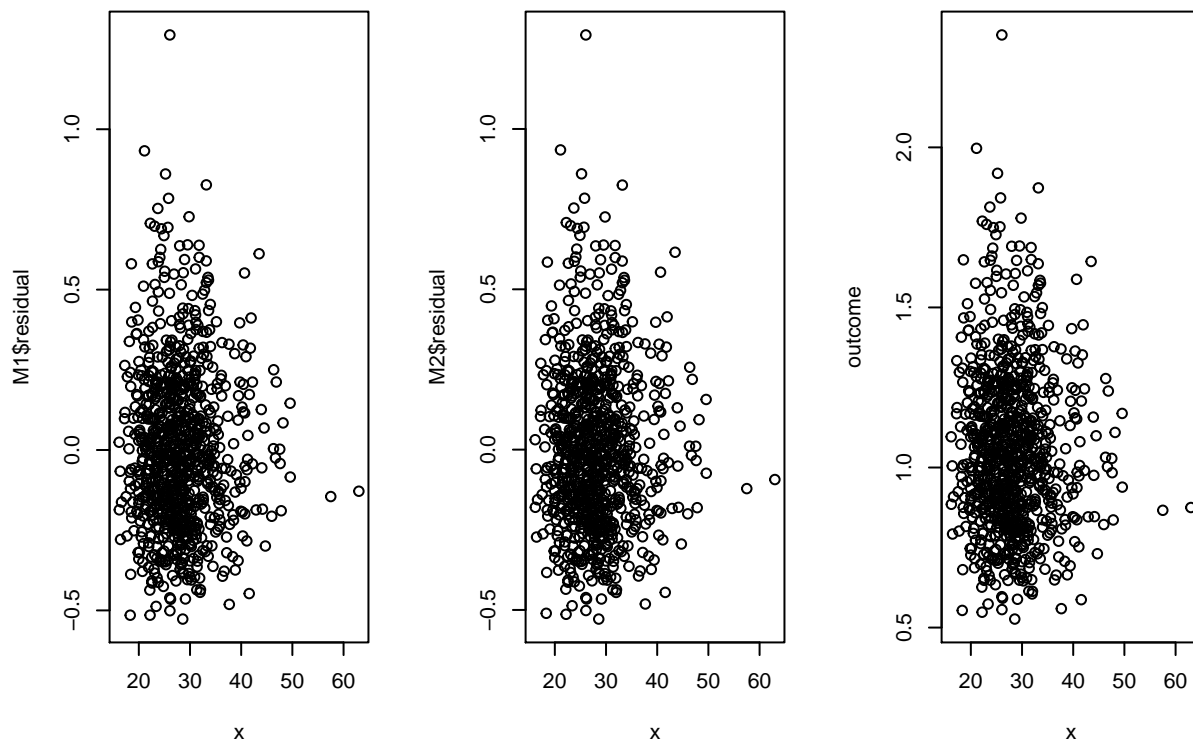




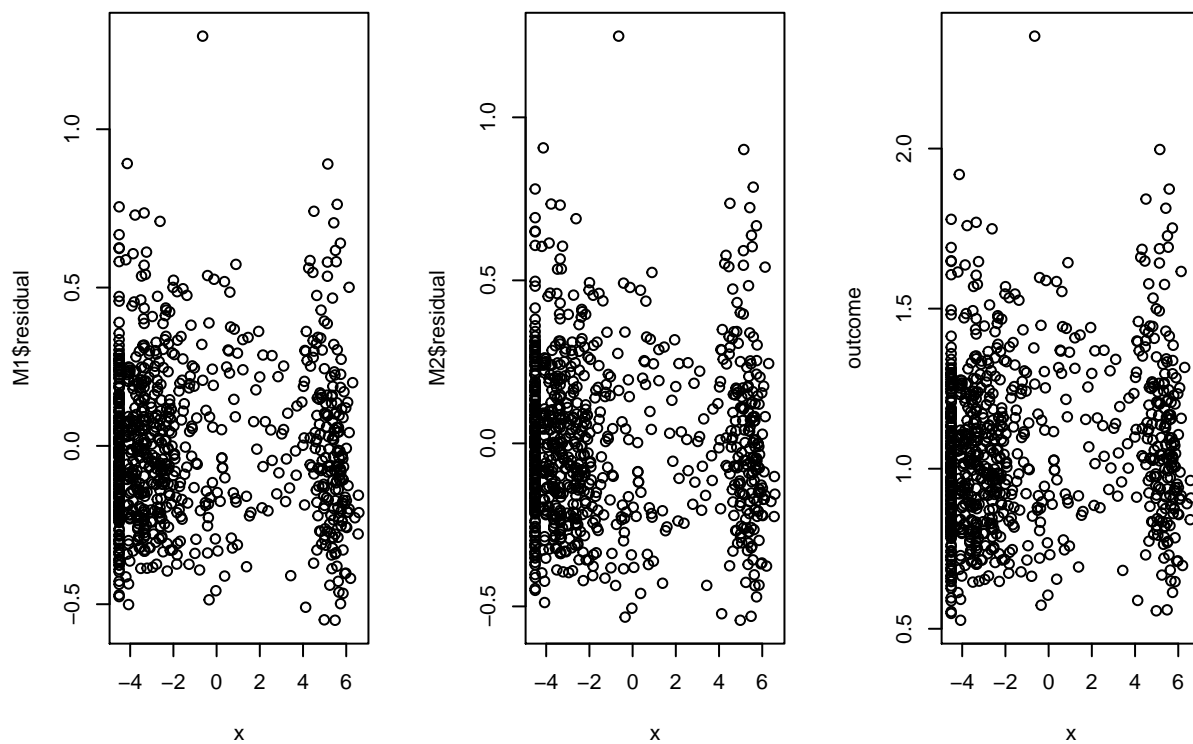
```
## [1] "residual for M1: 0.246320733146214"
## [1] "residual for M2: 0.245622720856213"
```



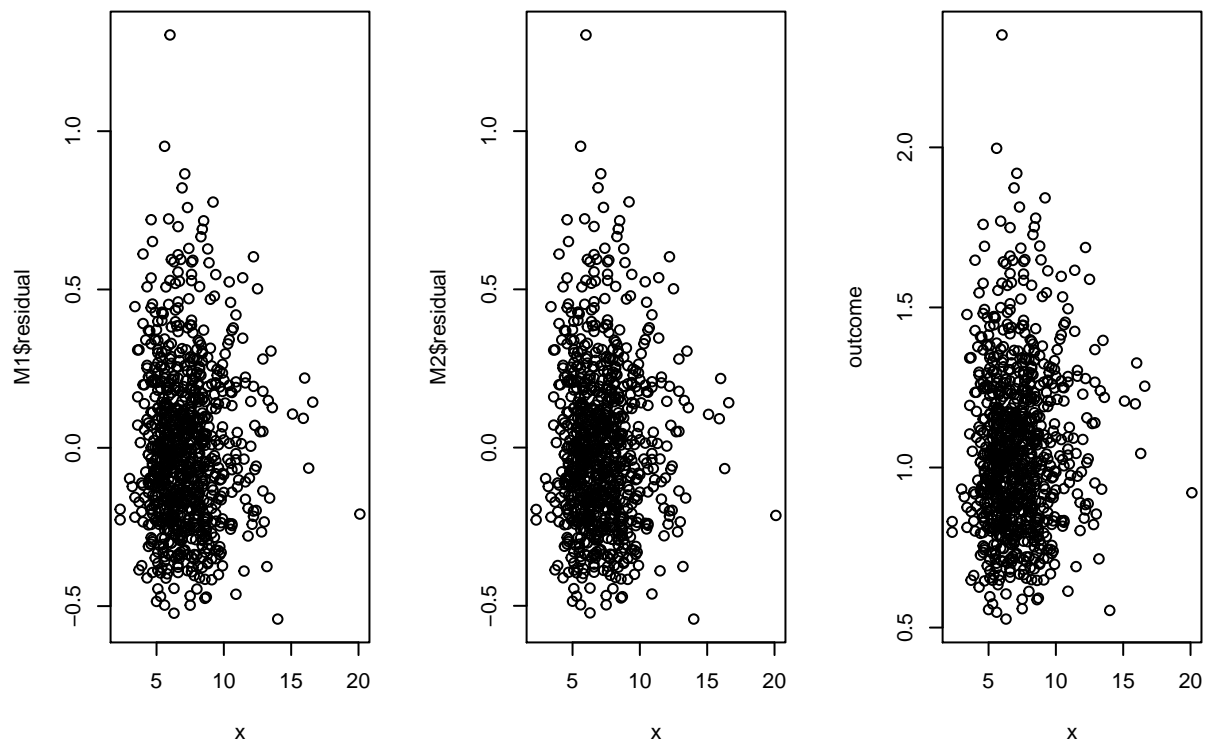
```
## [1] "residual for M1: 0.250228706427173"
## [1] "residual for M2: 0.25036248052387"
```



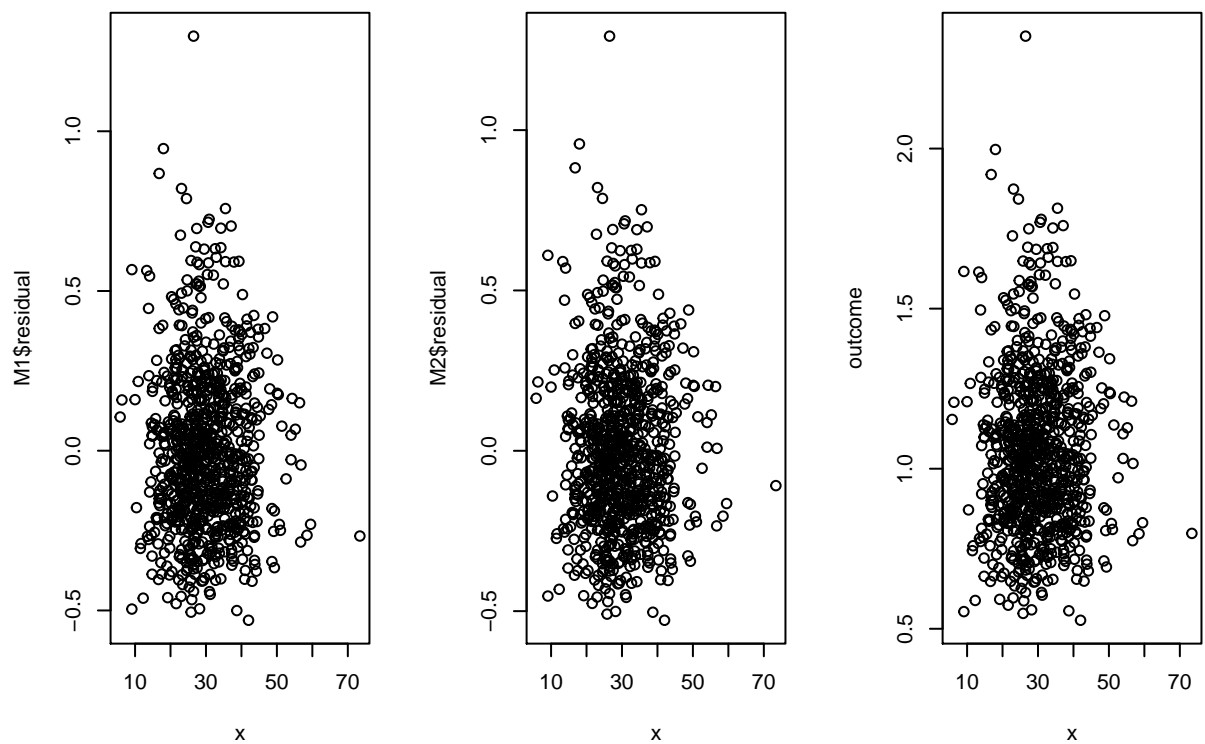
```
## [1] "residual for M1: 0.248212063673837"
## [1] "residual for M2: 0.24710732733351"
```



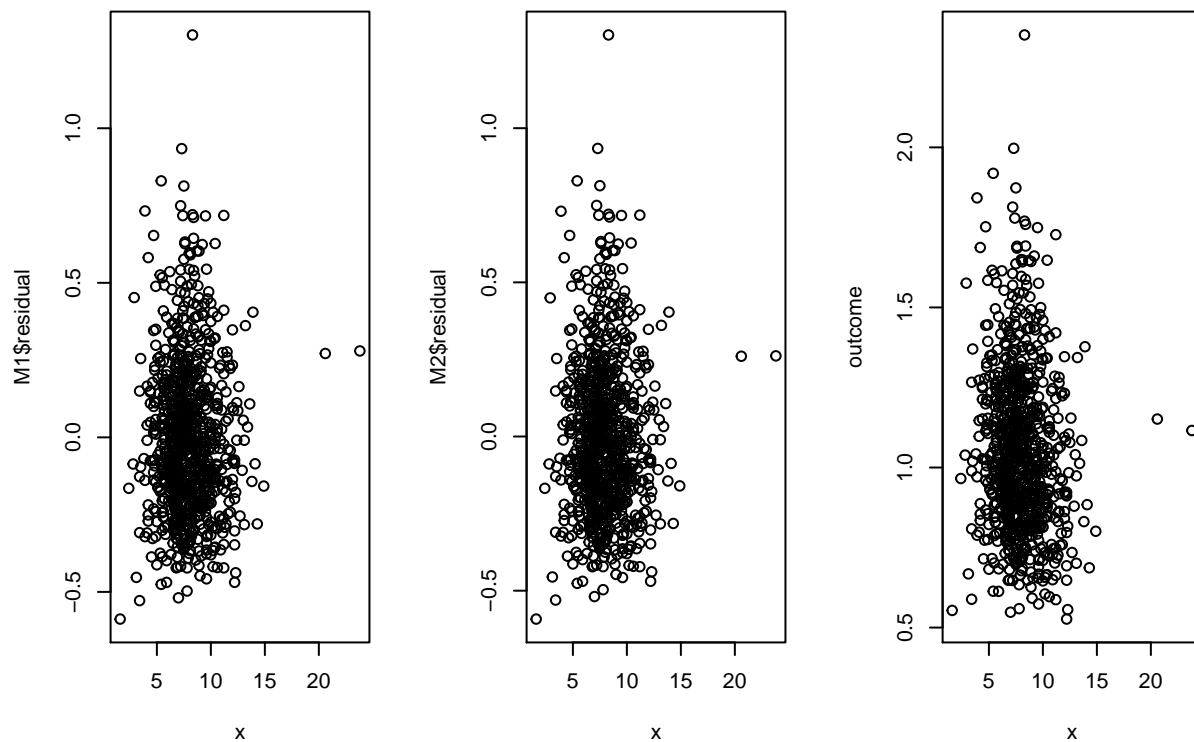
```
## [1] "residual for M1: 0.250065445847753"
## [1] "residual for M2: 0.250210403543218"
```



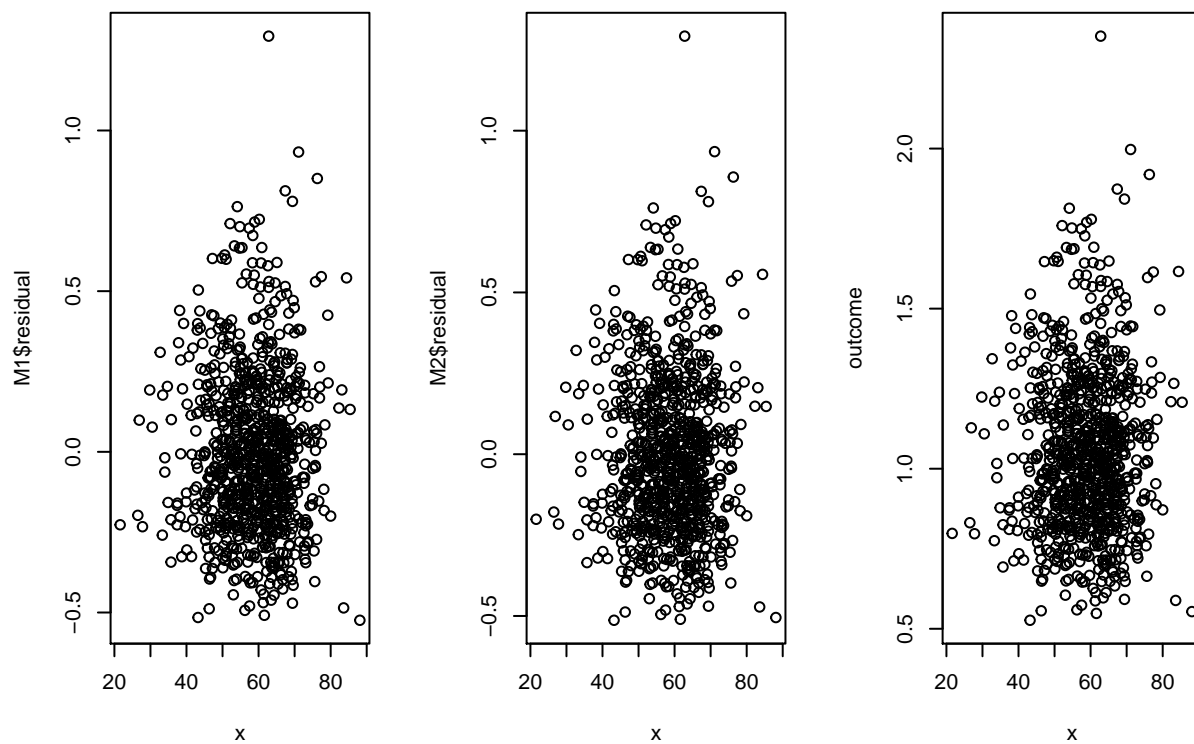
```
## [1] "residual for M1: 0.250373616826691"
## [1] "residual for M2: 0.250255208638358"
```



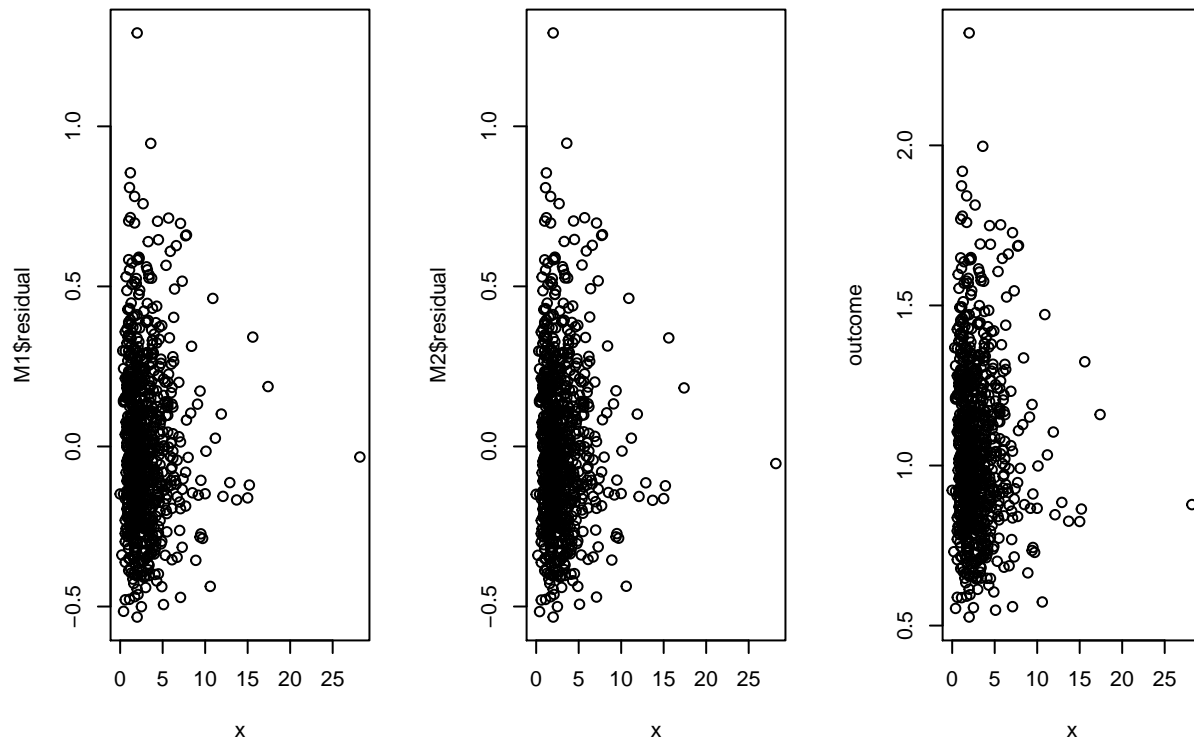
```
## [1] "residual for M1: 0.248704466454944"
## [1] "residual for M2: 0.248847192837983"
```



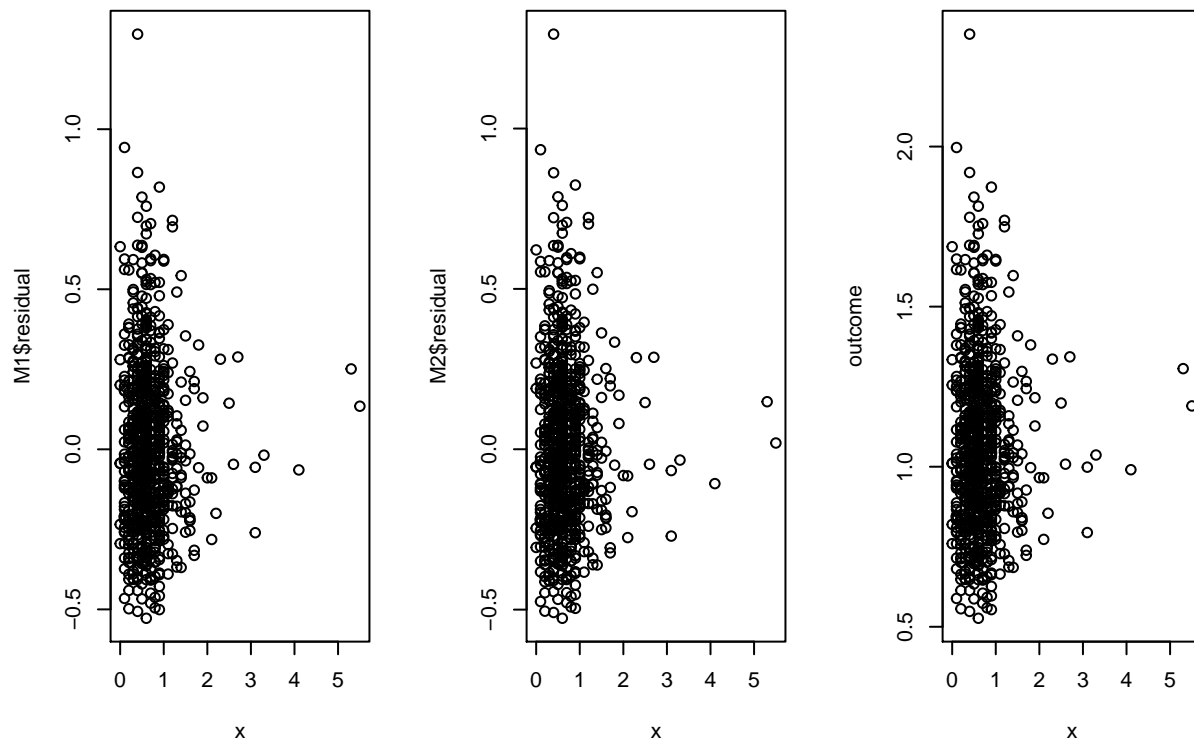
```
## [1] "residual for M1: 0.25026710930793"
## [1] "residual for M2: 0.250393729526099"
```



```
## [1] "residual for M1: 0.250043388210667"
## [1] "residual for M2: 0.25018695270193"
```



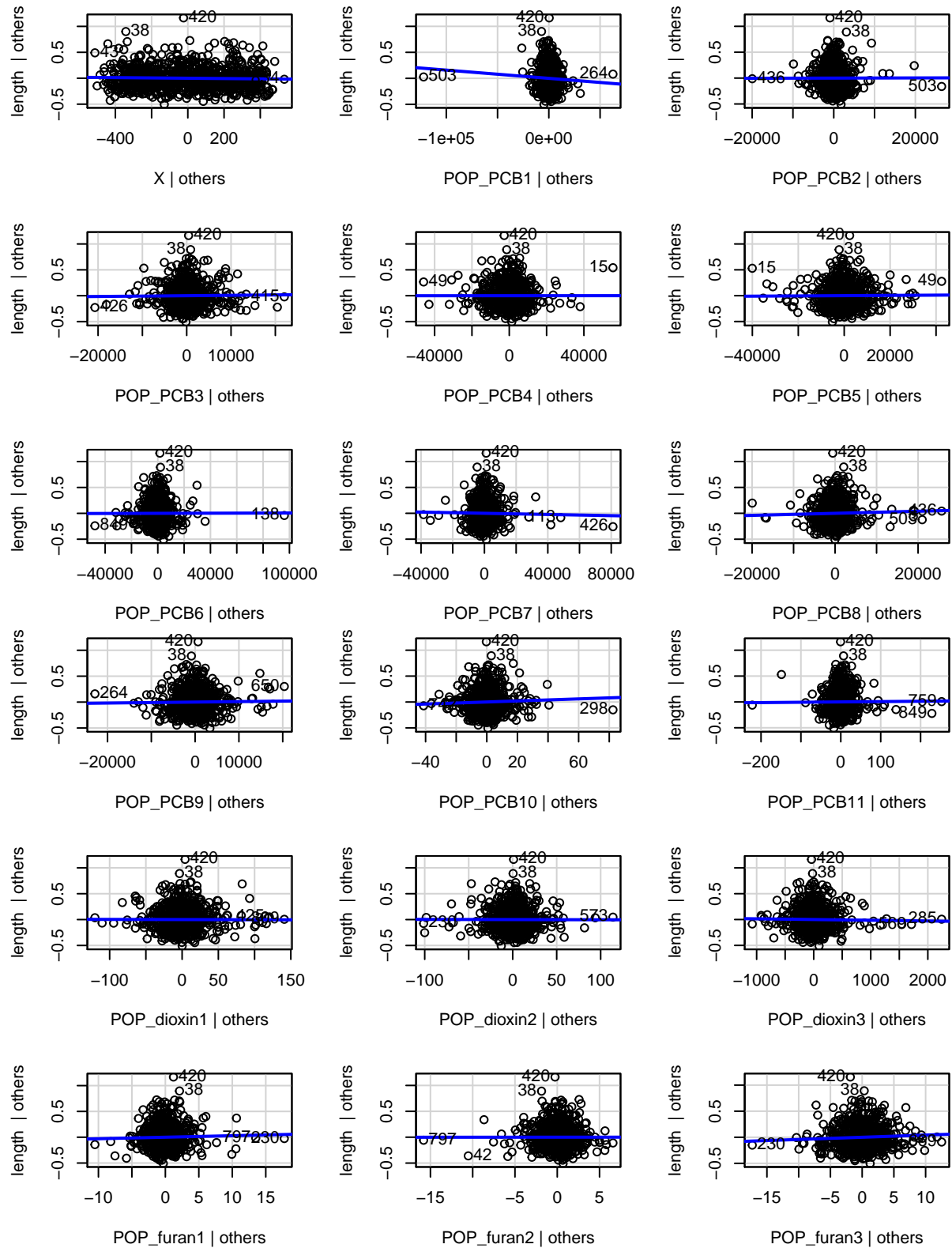
```
## [1] "residual for M1: 0.250382476371691"
## [1] "residual for M2: 0.25042580861039"
```

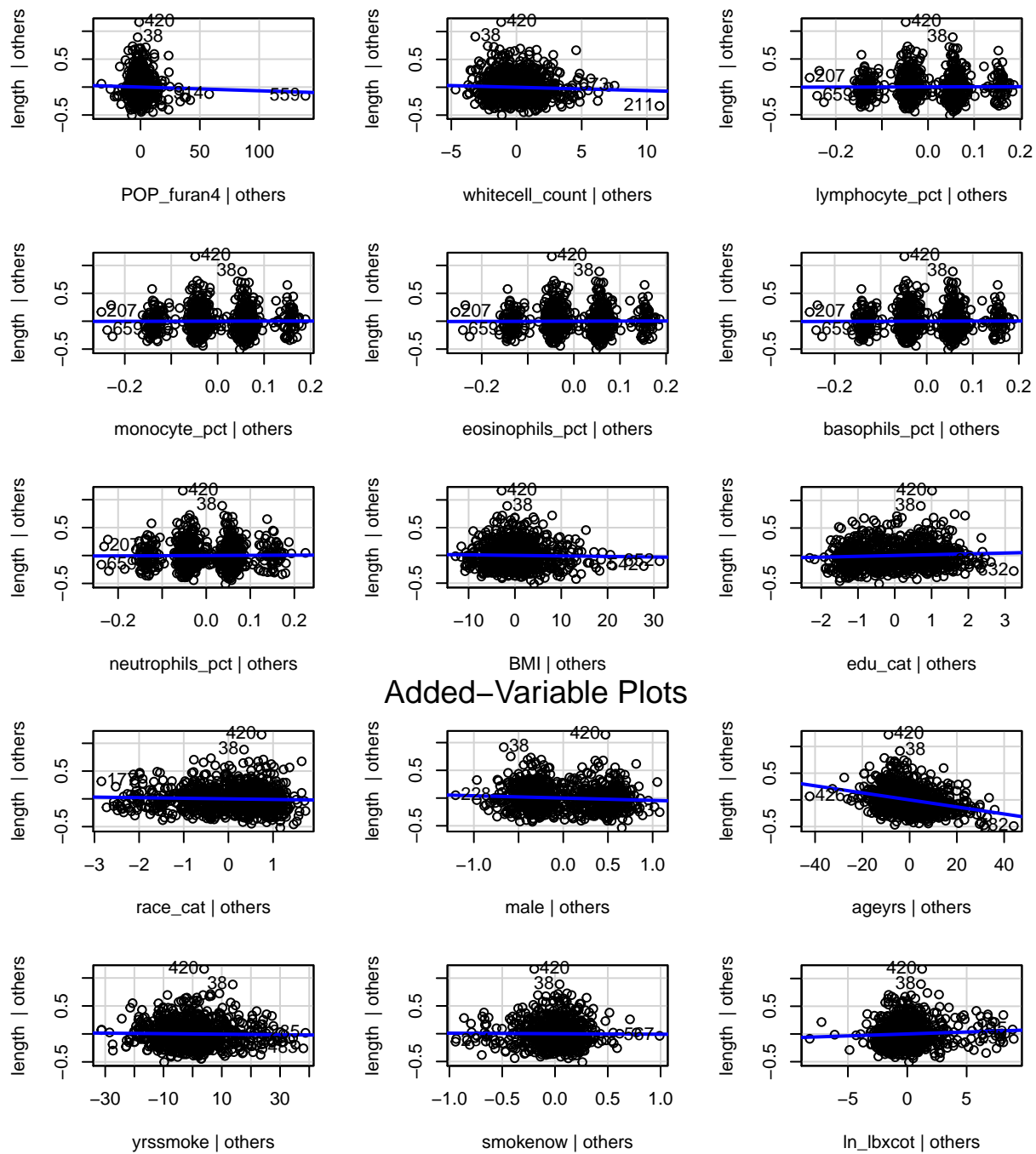


```
# Judy's work Part 2
# testing non-linearity in MLR
library(car)
```

```
## Loading required package: carData
```

```
M <- lm (length ~ ., data=pollutants)
avPlots(M)
```





### Added-Variable Plots