

# 1 Parsing-as-deduction rules for noisy channel

## 1.1 Item format

Each item has the following entries. In general, numerical indices are denoted by lowercase letters and other entries are denoted by uppercase letters.

1. frame index ( $i, j, \dots$ )
2. PLU-internal HMM state ( $s \in \{start, mid, end\}$ )
3. PLU bottom type ( $A, B, \dots$ )
4. PLU bottom index ( $a, b, \dots$ )
5. edit operation type ( $E \in \{IB, IT, SUB\}$ )
6. PLU top index ( $m, n, \dots$ )
7. the probability of the item ( $P$  or  $P'$ )

We also assume the existence of the following functions:

- $TOP(m)$  returns the type of the PLU at position  $M$  in the top-level PLU sequence.
- $p_{hmm}(s_1 \rightarrow s_2)$  returns the probability of transitioning from PLU-internal HMM state  $s_1$  to  $s_2$ . This is always 0.5 under the current implementation.
- $p_{op}(E)$  returns the probability of the given operation type ( $\{IB, IT, SUB\}$ ).
- $p_{ib}(A)$  returns the probability of the insert bottom operation for PLU  $A$ , given that  $E = IB$ .
- $p_{it}(M)$  returns the probability of the insert top operation for PLU  $M$ , given that  $E = IT$ .
- $p_{sub}(M, A)$  returns the probability of the substitute operation that substitutes PLU  $A$  for PLU  $M$ , given that  $E = SUB$ .
- $lh(A, s, i)$  returns the likelihood of state  $s$  of PLU  $A$  at frame  $i$  (based on the audio input).

## 1.2 Moves in Levenshtein matrix (PLU transitions)

### 1.2.1 Insert Bottom

$$\frac{[i, end, A, a, E, m, P]}{[i + 1, start, B, a + 1, IB, m, P' = P \cdot p_{hmm}(end \rightarrow start) \cdot p_{op}(IB) \cdot p_{ib}(B) \cdot lh(B, start, i + 1)]}$$

### 1.2.2 Insert Top

$$\frac{[i, end, A, a, E, m, P]}{[i, end, A, a, IT, m + 1, P' = P \cdot p_{op}(IT) \cdot p_{it}(TOP(m + 1))]}$$

### 1.2.3 Substitute

$$\frac{[i, end, A, a, E, m, P]}{[i + 1, start, B, a + 1, SUB, m + 1, P' = P \cdot p_{hmm}(end \rightarrow start) \cdot p_{op}(SUB) \cdot p_{sub}(TOP(m + 1), B) \cdot lh(B, start, i + 1)]}$$

## 1.3 PLU-internal transitions

### 1.3.1 HMM-state-internal transition

$$\frac{[i, s, A, a, E \in \{IB, SUB\}, m, P]}{[i + 1, s, A, a, E, m, P' = P \cdot p_{hmm}(s \rightarrow s) \cdot lh(A, s, i + 1)]}$$

### 1.3.2 PLU-internal HMM state transition

$$\frac{[i, s \in \{start, mid\}, A, a, E \in \{IB, SUB\}, m, P]}{[i + 1, s + 1, A, a, E, m, P' = P \cdot p_{hmm}(s \rightarrow s + 1) \cdot lh(A, s + 1, i + 1)]}$$

## 1.4 Start items

The start items look like this, for all  $A \in PLU$ s:

$$[i = 0, start, A, a = 0, E, m = 0, P = lh(A, start, 0)]$$

## 1.5 Completion rules

The parse is complete when an item of the following format is reached, where  $x$  is the number of frames in the audio input and  $y$  is the number of PLUs in the top-level sequence.

$$[\mathbf{i} = \mathbf{n}, end, A, a, E, \mathbf{m} = \mathbf{y}, P]$$

## 2 Implementation details

### 2.1 Iteration order

Iterating through the items in a correct order, such that all items from which item  $x$  is reachable are completed before item  $x$  is entered, is nontrivial.

As a starting point for thinking about ordering, below is a list of all items from which item  $x = [i, s, A, a, E, m, P]$  is reachable, and thus must be completed before  $x$  is entered, given certain conditions on the parameters.

| Item                                    | Conditions                                 | Transition type                  |
|-----------------------------------------|--------------------------------------------|----------------------------------|
| $[i - 1, end, B, a - 1, E', m, P']$     | if $E = IB, s = start$                     | Insert-bottom operation          |
| $[i, end, A, a, E', m - 1, P']$         | if $E = IT, s = end$                       | Insert-top operation             |
| $[i - 1, end, B, a - 1, E', m - 1, P']$ | if $E = SUB, s = start$                    | Substitute operation             |
| $[i - 1, s, A, a, E, m, P']$            | if $E \in \{IB, SUB\}$                     | PLU-internal HMM self-transition |
| $[i - 1, s - 1, A, a, E, m, P']$        | if $E \in \{IB, SUB\}, s \in \{mid, end\}$ | PLU-internal HMM transition      |