# Introduction to deep learning 1/?

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#### Introduction

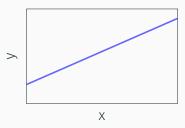
- 1. Building an artificial neural network (ANN)
- 2. Training the ANN
- 3. Transformation to a Convolutional Neural Network (CNN)

# Building a neural network: Linear regression

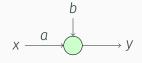
$$y = ax + b$$

### Building a neural network: Linear regression

$$y = ax + b$$



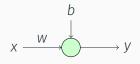
## Building a neural network: Linear regression



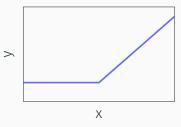
$$y = ax + b$$



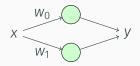
## Building a neural network: Artificial neuron



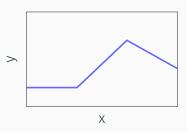
$$y = max(0, wx + b)$$



### Building a neural network: Artificial neural network (ANN)



$$y = max(0, w_0x + b_0) + max(0, w_1x + b_1)$$



#### Building a neural network: Universal approximation theorem

"Any relationship that can be described with a polynomial function can be approximated by a neural network with a single hidden layer."

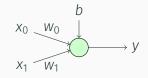
- Some guy in the 80s, probably

### Building a neural network: Universal approximation theorem

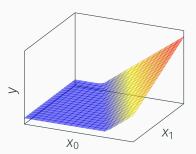
"Any relationship that can be described with a polynomial function can be approximated by a neural network with a single hidden layer."

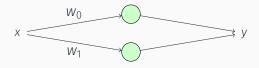
- Some guy in the 80s, probably

### Building a neural network: Increasing dimensionality

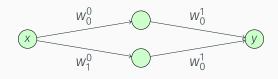


$$y = max(0, w_0x_0 + w_1x_1 + b)$$

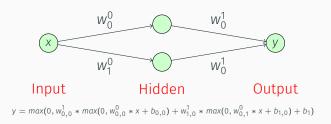


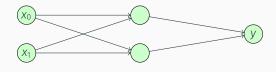


$$y = \max(0, w_0 x + b_0) + \max(0, w_1 x + b_1)$$

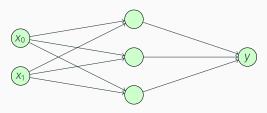


$$y = \max(0, w_{0,0}^1 * \max(0, w_{0,0}^0 * x + b_{0,0}) + w_{1,0}^1 * \max(0, w_{0,1}^0 * x + b_{1,0}) + b_1)$$

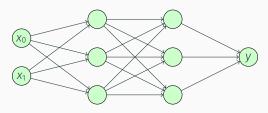




$$y = max(0, w_{0,0}^{1} * max(0, w_{0,0}^{0} * x_{0} + w_{1,0}^{0} * x_{1} + b_{0,0}) + w_{1,0}^{1} * max(0, w_{0,1}^{0} * x_{0} + w_{1,1}^{0} * x_{1} + b_{0,1}) + b_{1})$$



$$y = max(0, w_{0,0}^{1} * max(0, w_{0,0}^{0} * x_{0} + w_{1,0}^{0} * x_{1} + b_{0,0}) + w_{1,0}^{1} * max(0, w_{0,1}^{0} * x_{0} + w_{1,1}^{0} * x_{1} + b_{0,1}) + w_{2,0}^{1} * max(0, w_{0,2}^{0} * x_{0} + w_{1,2}^{0} * x_{1} + b_{0,2}) + b_{1})$$

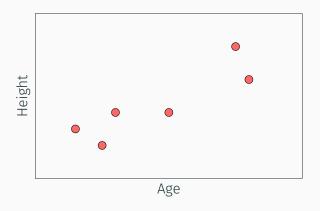


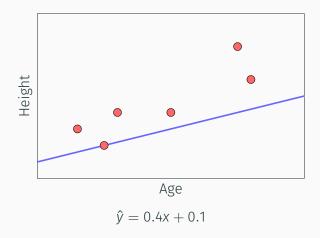
$$y = max(0, w_{0,0}^2 * max(0, w_{0,0}^1 * max(0, w_{0,0}^0 * x_0 + w_{1,0}^0 * x_1 + b_{0,0}) + w_{1,0}^1 * max(0, w_{0,1}^0 * x_0 + w_{1,1}^1 * w_1 + b_{0,1}) + w_{2,0}^2 * max(0, w_{0,2}^0 * x_0 + w_{1,2}^1 * w_1 + b_{0,2}) + b_{1,0}) + w_{1,0}^2 * max(0, w_{0,1}^0 * x_0 + w_{1,0}^0 * x_1 + b_{0,0}) + w_{1,1}^1 * max(0, w_{0,1}^0 * x_0 + w_{1,1}^0 * x_1 + b_{0,1}) + w_{1,1}^2 * max(0, w_{0,2}^0 * x_0 + w_{1,2}^1 * w_1 + b_{0,1}) + b_{1,1}) + w_{2,1}^2 * max(0, w_{0,2}^0 * x_0 + w_{1,2}^1 * w_1 + b_{0,2}) + b_{1,1}) + w_{2,0}^2 * max(0, w_{0,2}^0 * max(0, w_{0,2}^0 * x_0 + w_{1,1}^1 * w_1 + b_{0,1}) + w_{1,2}^1 * max(0, w_{0,1}^0 * x_0 + w_{1,1}^1 * w_1 + b_{0,1}) + w_{2,2}^1 * max(0, w_{0,1}^0 * x_0 + w_{1,1}^1 * w_1 + b_{0,1}) + b_{1,2}) + b_{1,2}) + b_{2})$$

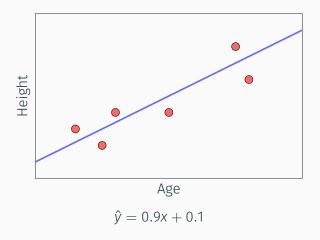
16

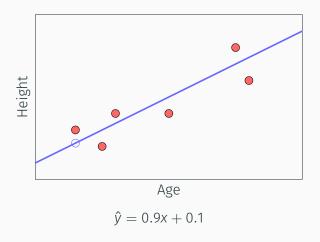
### Building a neural network: Summary

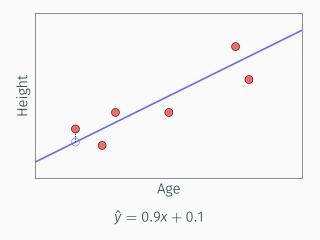
- Artificial neurons are (linear) weighted sums wrapped in non-linear activation functions
- Multiple artificial neurons stacked together in a layerwise fashion comprise an artificial neural network
- Artificial neural networks allow us to model arbitrarily complex relationships between inputs and outputs

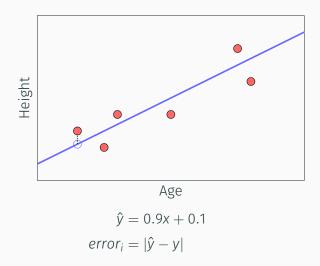


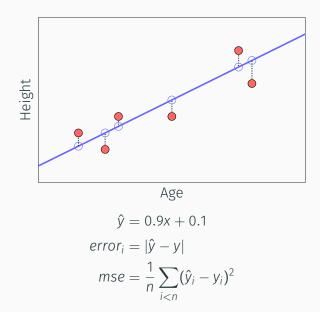


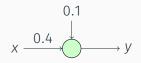








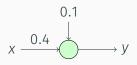




$$\hat{y} = 0.4x + 0.1$$
 loss =  $(y - \hat{y})^2$ 

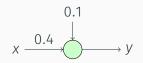


$$0.16 = 0.4 * 0.15 + 0.1$$
  $0.019 = (0.3 - 0.16)^2$ 

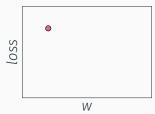


$$(0.3 - (0.4 * 0.15 + 0.1))^2 = 0.019$$

$$(0.3 - (0.4 * 0.15 + 0.1))^{2} = 0.019$$

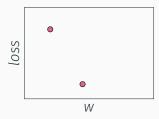


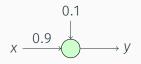
$$(0.3 - (0.4 * 0.15 + 0.1))^2 = 0.019$$



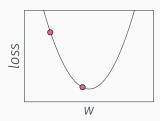


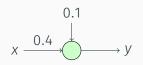
$$(0.3 - (0.9 * 0.15 + 0.1))^2 = 0.004$$



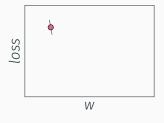


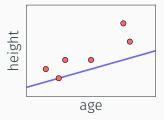
$$(0.3 - (0.9 * 0.15 + 0.1))^2 = 0.004$$





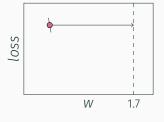
$$(0.3 - (0.4 * 0.15 + 0.1))^2 = 0.019$$

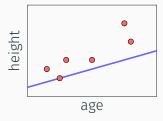


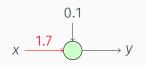




$$(0.3 - (0.4 * 0.15 + 0.1))^2 = 0.019$$

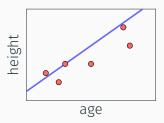


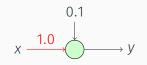




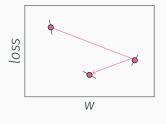
$$(0.3 - (1.7*0.15 + 0.1))^2 = 0.003$$

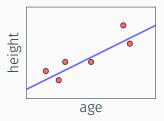






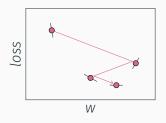
$$(0.3 - (1.0*0.15 + 0.1))^2 = 0.002$$

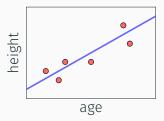






$$(0.3 - (1.2*0.15 + 0.1))^2 = 0.000$$

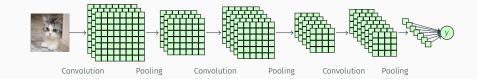




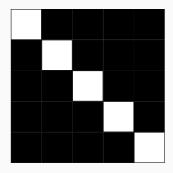
### Training a neural network: Summary

- The loss function is a precise formalization of what we want the model to learn
- Calculating the gradient allows us to see how we can update the parameters of the model to decrease the loss
- Using gradient descent we can update the parameters sequentially until we have the perfect model with zero loss

#### Convolutional neural networks: Architecture

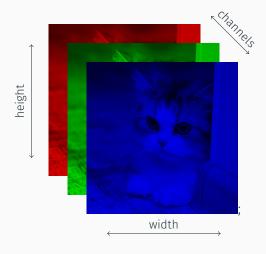


# Convolutional neural networks: Images

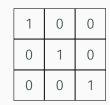


1	0	0	0	0
0	1	0	0	0
0	0	1	0	0
0	0	0	1	0
0	0	0	0	1

## Convolutional neural networks: Images



0	0	1
0	1	0
1	0	0



0	0	1
0	1	0
1	0	0



1	0	0
0	1	0
0	0	1

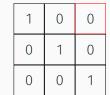
0\*1

0	0	1
0	1	0
1	0	0



1	0	0
0	1	0
0	0	1

0	0	1
0	1	0
1	0	0



0	0	1
0	1	0
1	0	0



0	0	1
0	1	0
1	0	0



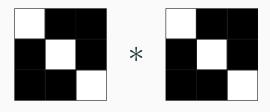
1	0	0
0	1	0
0	0	1

$$0*1+0*0+1*0+0*0+1*1+0*0+1*0+0*0+0*1=1$$

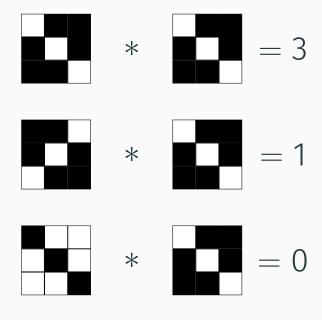
1	0	0
0	1	0
0	0	1



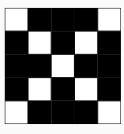
$$1*1+0*0+0*0+0*0+1*1+0*0+1*0+0*0+1*1=3$$



1\*1+0\*0+0\*0+0\*0+1\*1+0\*0+1\*0+0\*0+1\*1=3

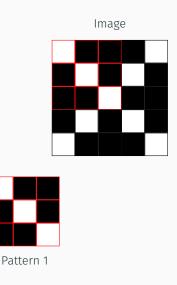




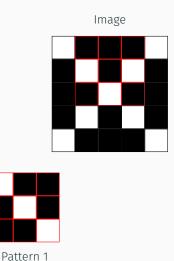




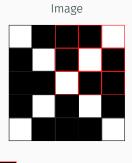
Pattern 1







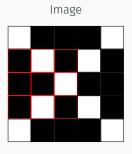








Pattern 1

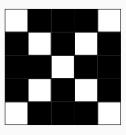






Pattern 1

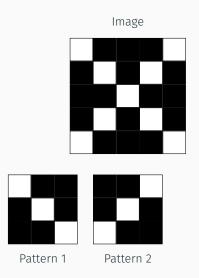
Image



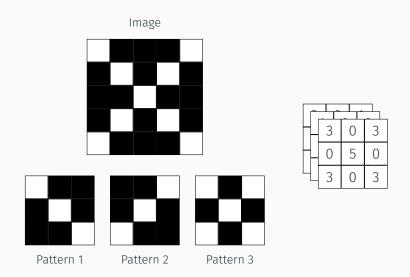
3	0	1
0	3	0
1	0	3

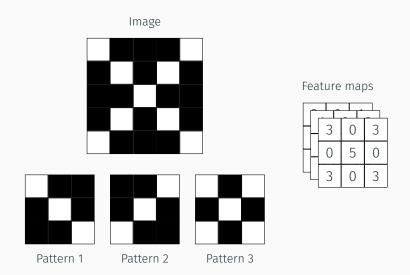


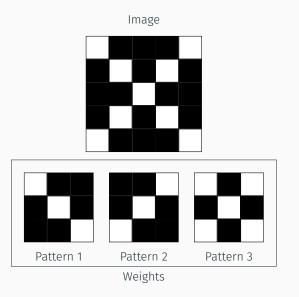
Pattern 1





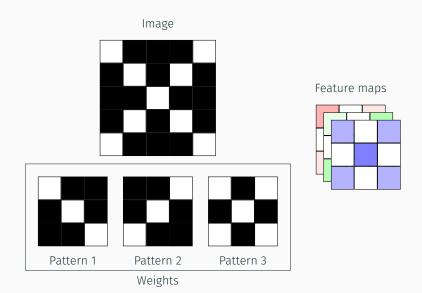






Feature maps





#### Feature map

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

#### Feature map

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

5

#### Feature map

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

5 7

#### Feature map

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15



#### Feature map

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

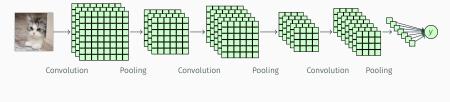
5	7
13	15

Feature map

1	2	3
5	6	7
9	10	11
13	14	15
	9	5 6 9 10

5	7
13	15

#### Convolutional neural networks: Architecture

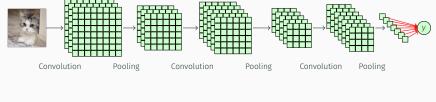








#### Convolutional neural networks: Architecture









### Convolutional neural networks: Summary

- Images in computers are stored as matrices of numbers
- · The convolution operation is a pattern matcher
- A convolutional layer is a battery of pattern matchers where the patterns are learned during training
- The pooling operation reduces spatial dimensions and distills information
- A convolutional neural network consists of alternating convolution and pooling, which means looking for more and more abstract patterns spanning larger and larger region of the images
- The final layer of the network makes a prediction based on the patterns it has found