

```
1  ###
2  # Setup
3  import numpy as np
4
5  F = (0, 0, 0)
6  G = (-2, -1, 1)
7  H = (1, -3, -2)
8
9  ###
10 # Find normal vector to find equation of plane
11 FG = [g - f for f, g in zip(F, G)]
12 GH = [h - g for g, h in zip(G, H)]
13 n = np.cross(FG, GH)
14 print(f"normal vec: {n}")
15 # u = n / np.linalg.norm(n)
16 # print(f"unit normal vec: {u}")
17
18 # %%
19 # Determine if point Q is inside triangle FGH
20 P = (7.0 / 3, 11.0 / 3, 14.0 / 3)
21 FP = [p - f for f, p in zip(F, P)]
22 A_FPG = 0.5 * np.linalg.norm(np.cross(FG, FP))
23
24 GP = [p - g for g, p in zip(G, P)]
25 A_GPH = 0.5 * np.linalg.norm(np.cross(GH, GP))
26
27 HF = [f - h for h, f in zip(H, F)]
28 HP = [p - h for h, p in zip(H, P)]
29 A_HPF = 0.5 * np.linalg.norm(np.cross(HF, HP))
30
31 FH = [h - f for f, h in zip(F, H)]
32 A_FGH = 0.5 * np.linalg.norm(np.cross(FG, FH))
33
34 print(
35     f"Area of triangle FGH: {A_FGH}\nSum of area of triangles FPG, GPH, HPF: {A_FPG+A_GPH+A_HPF}"
36 )
37
38 # %%
39
```