### Statistics for the Sciences

**Correspondence Analysis** 

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# **Outline**

- Idea of CA
- Example
- Lab

- Correspondence analysis (CA) is a statistical visualization method for picturing the associations between the levels of a two-way contingency table.
  - CA is for the relationship between two categorical variables.
  - ► The term correspondance denotes a system of associations between the levels of the two sets.
- CA is used to check in a two-way contingency table whether certain levels of one categorical variable are associated with some levels of another.
- CA is a geometric technique for displaying the rows and columns of a two-way contingency table as points in a low-dimensional space, such that the positions of the row and column points are consistent with their associations in the table.

• The form of a contingency table for two categorical variables

Two-Way Contingency Table

	Column				Marginals
Row	1	2		С	
1	O <sub>11</sub>	$O_{12}$		$O_{1c}$	$R_1$ .
2	$O_{21}$	$O_{22}$		$O_{2c}$	$R_2$ .
		•		•	
r	$O_{r1}$	$O_{r2}$		$O_{rc}$	$R_r$ .
Marginals	C.1	C. <sub>2</sub>		C. <sub>c</sub>	n

- Divide each cell count by the total number of observations n, we get the matrix of joint cell probabilities.
  - ▶ In the following table,  $p_{ij} = Oij/n, i = 1, ..., r, j = 1, ..., n$ .
  - ▶ They are actually estimates the cell probabilities.

Two-Way Table of Proportions

	Column				Marginals
row	1	2		С	
1	$p_{11}$	$p_{12}$		$p_{1c}$	$p_1$ .
2	$p_{21}$	$p_{22}$		$p_{2c}$	$p_{2}$ .
•					-
•					
r	$p_{r1}$	$p_{r2}$		$p_{rc}$	$p_r$ .
Marginals	$p_{\cdot 1}$	p. <sub>2</sub>		<i>p</i> . <i>c</i>	1

• Consider a  $3 \times 3$  contingency table

```
## Col1 Col2 Col3
## Row1 3 2 4
## Row2 3 6 6
## Row3 10 5 9
```

• The matrix **P** of joint cell probabilities

```
## [1] "matrix of joint cell probabilities P="

## Col1 Col2 Col3

## Row1 0.0625000 0.04166667 0.08333333

## Row2 0.0625000 0.12500000 0.12500000

## Row3 0.2083333 0.10416667 0.18750000
```

- Calculate the row margin r
  - called row masses

```
## [,1]
## Row1 0.1875
## Row2 0.3125
## Row3 0.5000
```

- Calculate the column margin c
  - called column masses

```
## [,1]
## Col1 0.3333333
## Col2 0.2708333
## Col3 0.3958333
```

```
## Col1 Col2 Col3 Rtotal
## Row1 0.0625000 0.04166667 0.08333333 0.1875
## Row2 0.0625000 0.12500000 0.12500000 0.3125
## Row3 0.2083333 0.10416667 0.18750000 0.5000
## Ctotal 0.3333333 0.27083333 0.39583333 1.0000
```

• Put the row masses in a diagonal matrix  $\mathbf{D_r}$ ,  $p_i$ , i = 1, 2, 3

```
## [,1] [,2] [,3]
## [1,] 0.1875 0.0000 0.0
## [2,] 0.0000 0.3125 0.0
## [3,] 0.0000 0.0000 0.5
```

ullet Put the column masses in a diagonal matrix  $oldsymbol{D_c}$ ,  $p_{\cdot j}, j=1,2,3$ 

```
## [,1] [,2] [,3]
## [1,] 0.3333333 0.0000000 0.00000000
## [2,] 0.0000000 0.2708333 0.0000000
## [3,] 0.0000000 0.0000000 0.3958333
```

- The matrix of row conditional probabilities
  - Each row of P divided by row masses

```
## Col1 Col2 Col3
## [1,] 0.3333333 0.2222222 0.4444444
## [2,] 0.2000000 0.4000000 0.4000000
## [3,] 0.4166667 0.2083333 0.3750000
```

- The matrix of column conditional probabilities
  - Each column of P divided by column masses

```
## [,1] [,2] [,3]
## Row1 0.1875 0.1538462 0.2105263
## Row2 0.1875 0.4615385 0.3157895
## Row3 0.6250 0.3846154 0.4736842
```

- The expected proportions  $\mathbf{E} = \mathbf{rc}^{\mathsf{T}}$ 
  - the proportions we expect in the case there is no relationship between the two categorical variables
  - ▶ that is,  $p_{ij} = p_{i.} \times p_{.j}$

```
## Col1 Col2 Col3
## Row1 0.0625000 0.05078125 0.07421875
## Row2 0.1041667 0.08463542 0.12369792
## Row3 0.1666667 0.13541667 0.19791667
```

• The residuals  $\mathbf{R} = \mathbf{P} - \mathbf{E}$  quantify the difference between the observed data and the data we would expect under the assumption that there is no relationship between the row and column categories of the table

```
## Col1 Col2 Col3
## Row1 0.00000000 -0.009114583 0.009114583
## Row2 -0.04166667 0.040364583 0.001302083
## Row3 0.04166667 -0.031250000 -0.010416667
```

- ullet Dividing the residuals by the expected values, we obtain the matrix  $oldsymbol{I_r}$  of indexed residuals
  - the further the value from the table, the larger the observed proportion relative to the expected proportion

```
## Col1 Col2 Col3
## Row1 0.00 -0.1794872 0.12280702
## Row2 -0.40 0.4769231 0.01052632
## Row3 0.25 -0.2307692 -0.05263158
```

• Finally, calculate the matrix of standardized residuals  $\mathbf{Z}$ , obtained by multiplying each element of  $\mathbf{I_r}$  by each element of  $\sqrt{\mathbf{E}}$ 

```
## [,1] [,2] [,3]
## [1,] 0.0000000 -0.04044689 0.03345646
## [2,] -0.1290994 0.13874726 0.00370218
## [3,] 0.1020621 -0.08492078 -0.02341465
```

- The standardized residuals matrix Z is used in correspondence analysis to visualize and interpret the relationships between row and column categories in a contingency table.
- Then a mathematical tool Singular Value Decomposition (SVD) will be used to Decompose Z
  - ► The squared singular values correspond to the eigenvalues of **Z**
  - In the reduced dimensional space, the left singular vectors represent the row coordinates, and
  - the right singular vectors represent the column coordinates.
  - thenn alculate the row and column scores
- The eigenvalues represent the amount of variance explained by each dimension in the reduced space.
  - Larger eigenvalues indicate dimensions that explain more variance.
- The row and column scores provide the coordinates for plotting the rows and columns in a biplot. These scores show the relationship between row and column categories.

# One Application of CA

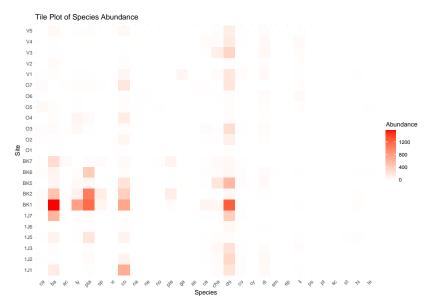
- The application of CA in ecology is radically different.
- For example, Abundance data
  - Abundance data are gathered from various physical samples (e.g., areas or volumes) where different species are identified and counted.
  - This results in a matrix is not a statistical contingency table, as the counts are not derived from random sampling.
- Since ecological samples (e.g., fixed-size quadrats in botany or fixed volumes in marine research) are often uniform in size, an important question arises:
  - Should abundances be profiled relative to the total abundance within each sample?
- CA can help us visualize relationships between species and environmental factors.

- (lemminvert2.csv): Lemmens et al. (2015) did a detailed study of various biotic communities in artificial ponds in Belgium. They sampled 28 ponds that represented different types of management, a combination of fish farming strategies (no fish, farming young fish, low intensity management, no management), and drainage frequencies (> 10 years ago, occasional, annual). They also quantified taxon abundances for fish, zooplankton, and macro-invertebrates (different families and species within some groups) and covers of submerged, floating, and emergent vegetation.
  - ► The macroinvertebrate dataset only included 23 ponds and we will use these data to illustrate CA by examining the ordination of the macroinvertebrate community (abundances of families).

• Remove the first 2nd and 3rd columns, and check some statistics

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• Get a tile plot to check relative abundance of each species within each site



Regard variables site as row names/labels

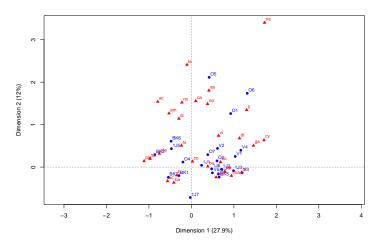
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## Value
              0.364603 0.156342 0.147145 0.135003 0.124771 0.098519 0.080732
## Percentage 27.91%
                      11.97%
                               11.26%
                                        10.33%
                                                 9.55%
                                                           7.54%
                                                                    6.18%
##
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                                10
                                         11
                                                           13
                                                                   14
## Value
              0.046041 0.040712 0.031388 0.026204 0.018642 0.01379 0.006885
## Percentage 3.52%
                      3.12%
                                2.4%
                                         2.01%
                                                 1.43%
                                                           1.06%
                                                                  0.53%
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## Value
              0.005144 0.004454 0.003261 0.001128 0.000886 0.000536 0.000155
                                        0.09%
## Percentage 0.39%
                      0.34%
                               0.25%
                                                 0.07%
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                                                                    0.01%
##
## Value
              9.8e - 05
## Percentage 0.01%
##
##
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   Rows:
##
               1J1
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                                              1J5
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                                                                            BK1
## Mass
           0.061626 0.032120
                              0.022676 0.028172
                                                  0.006723
                                                            0.056984 0.309519
## ChiDist 1.201693 0.933132
                              1.171392 1.148363
                                                  1.722272
                                                           1.105904 0.468482
## Inertia 0.088992 0.027968
                              0.031116 0.037152
                                                  0.019942 0.069693 0.067932
## Dim. 1 0.396955 1.179828 1.641302 -0.779788 0.789258 -0.044049 -0.485453
## Dim. 2 0.106377 -0.129481 -0.215181 1.095410 -0.109035 -1.811533 -0.508792
##
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## Mass
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                     0.068563 0.041351 0.035268 0.001334 0.014193 0.025878
## ChiDist 1.001979 0.895062 1.218067 1.798732 5.509043 0.966582 1.024400
## Inertia 0.130490 0.054928 0.061352 0.114109 0.040483 0.013260 0.027156
## Dim. 1 -1.426088 1.082130 -0.791462 -0.897415 1.532024 0.998728 1.050517
## Dim 2
           0 743469 -0 592846
                               1.540257 -0.609251 3.187125 0.369797 -0.398976
##
                  04
                          05
                                    06
                                             07
                                                     V1
                                                              V2
                                                                         V3
## Mass
           0.017661 0.009124 0.007683 0.028972 0.026891 0.006776
## ChiDist 1.149777 3.381547 3.207381 1.112261 2.268350 1.423040 1.483498
## Inertia 0.023347 0.104330 0.079040 0.035842 0.138368 0.013722 0.069280
## Dim. 1 -0.329851 0.691269 2.177059 0.638978 1.709381 1.016049 1.978599
## Dim 2
           0.299910 5.343375 4.392634 0.739371 0.633688 1.111008 -0.339015
##
                 ٧4
                          V5
## Mass
           0.018781 0.018248
## ChiDist 1.645441 0.623136
## Inertia 0.050850 0.007086
## Dim 1 1 927954 0 817559
```

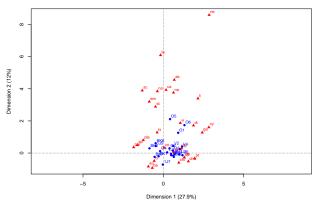
Proportion of variation explained

```
##
## Principal inertias (eigenvalues):
##
                        %
##
    dim
            value
                            cum%
                                    scree plot
##
    1
            0.364603
                       27.9
                             27.9
                                    *****
##
            0.156342
                       12.0
                             39.9
                                    ***
##
            0.147145
                       11.3
                             51.1
                                    ***
##
            0.135003
                       10.3
                             61.5
                                    ***
                       9.6
##
            0.124771
                             71.0
                                    **
##
    6
            0.098519
                       7.5
                             78.6
                                    **
##
    7
            0.080732
                       6.2
                             84.7
##
    8
            0.046041
                        3.5
                             88.3
##
    9
            0.040712
                        3.1
                             91.4
##
    10
            0.031388
                        2.4
                             93.8 *
                             95.8 *
##
    11
            0.026204
                        2.0
##
    12
            0.018642
                        1.4
                             97.2
##
    13
            0.013790
                        1.1
                             98.3
                        0.5
##
    14
            0.006885
                             98.8
##
    15
            0.005144
                        0.4
                             99.2
##
    16
            0.004454
                        0.3
                             99.5
##
    17
            0.003261
                        0.2
                             99.8
##
    18
            0.001128
                        0.1
                             99.9
##
    19
            0.000886
                        0.1
                             99.9
    20
            0.000536
                       0.0 100.0
##
##
    21
            0.000155
                       0.0 100.0
##
    22
            9.8e-050
                        0.0 100.0
##
```

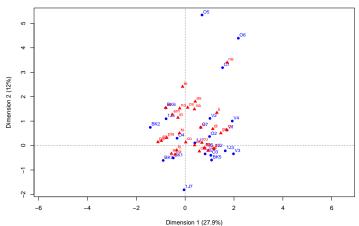
- Visualization of relationships among categories
- row/col points near each other are positively associated
- The red points are for columns



- In standard CA, the distances between row and column coordinates are exaggerated, and there isn't a straightforward interpretation of relationships between row and column categories.
- To interpret the relationships between row coordinates, we use row principal normalization
  - Points that are closer together in the plot indicate rows (sites) that have similar species compositions.



- To interpret the relationships between column coordinates, we use column principal normalization
  - Points that are closer together in the plot indicate columns (species) that have similar distributions across the rows (sites).



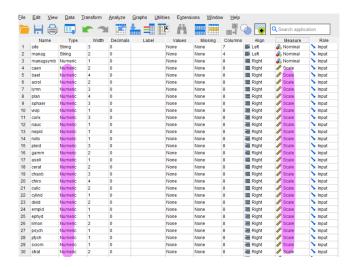
• CA is for a contingency table. In SPSS so we need to reshape the data from

	var <sub>1</sub>	var <sub>2</sub>		var <sub>29</sub>
row1	<i>x</i> <sub>11</sub>	<i>X</i> <sub>12</sub>		X <sub>1,29</sub>
row2	<i>x</i> <sub>21</sub>	<i>X</i> <sub>22</sub>	• • •	$x_{2,29}$
:	:		:	:
row23	<i>X</i> <sub>23,1</sub>	X <sub>23,2</sub>	• • •	X <sub>23,29</sub>

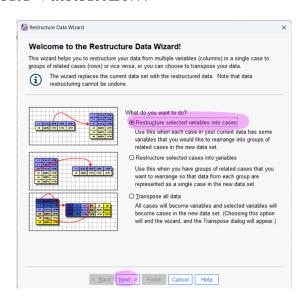
to

Row	Column	Count
row1	var <sub>1</sub>	X <sub>11</sub>
:	:	:
row1	var <sub>29</sub>	<i>X</i> <sub>1,29</sub>
row2	var <sub>1</sub>	<i>X</i> <sub>21</sub>
<u>:</u>	:	:
row2	var <sub>29</sub>	$X_{2,29}$
<u>:</u>	:	:
row23	var <sub>1</sub>	$x_{23,1}$
:	:	:
row23	var <sub>29</sub>	X <sub>23,29</sub>

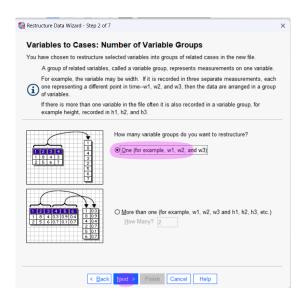
We import the data with measures of all numerical variables as Scale

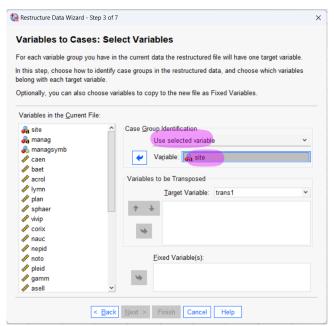


ullet Click on Data o Restructure...

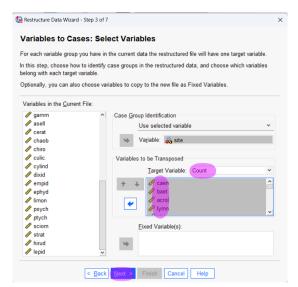


#### I ah

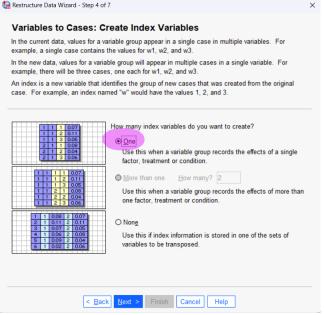




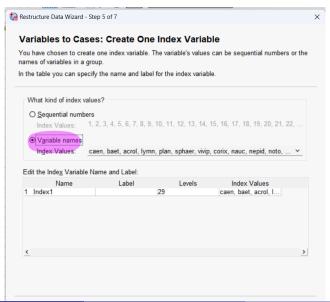
 Add all numerical variables to the Variables to be Transposed box, and name the Target Variable as Count



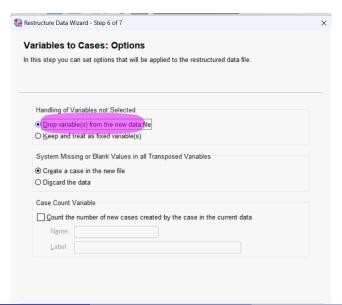
#### I ah



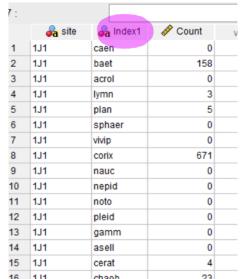
#### Use variable names as index



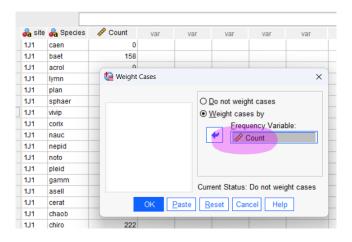
• Drop the other two variables.



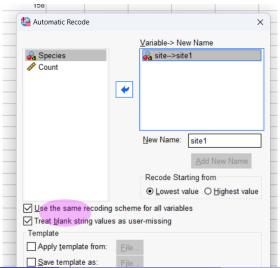
- The long data will be like this
  - ▶ Let's change the name of Index1 to Species



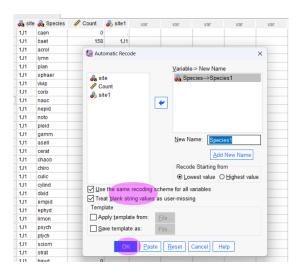
- We regard the values of Count as frequencies, so
  - lacktriangle Click on Data ightarrow Weight Cases...



- To conduct CA in SPSS, we need the two categorical variables Site and Species numerical
  - lacktriangle Click on Transform ightarrow Automatic Recode ...



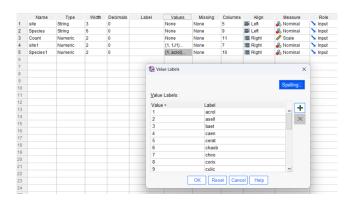
Do the same thing to Species



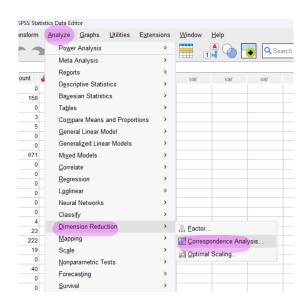
#### • The data now is like this

	🚜 site	🚜 Species		🚜 site1	🚜 Species1	var
1	1J1	caen	0			
2	1J1	baet	158	1J1	baet	
3	1J1	acrol	0			
4	1J1	lymn	3	1J1	lymn	
5	1J1	plan	5	1J1	plan	
6	1J1	sphaer	0			
7	1J1	vivip	0			
8	1J1	corix	671	1J1	corix	
9	1J1	nauc	0			
10	1J1	nepid	0			
11	1J1	noto	0			
12	1J1	pleid	0			
13	1J1	gamm	0			
14	1J1	asell	0			
15	1J1	cerat	4	1J1	cerat	
16	1J1	chaob	23	1J1	chaob	
17	1J1	chiro	222	1J1	chiro	
18	1J1	culic	19	1J1	culic	
19	1J1	cylind	0			
20	1J1	dixid	40	1J1	dixid	
21	1J1	empid	0			
22	1J1	ephyd	0			

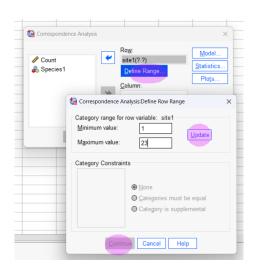
#### • The data now is like this



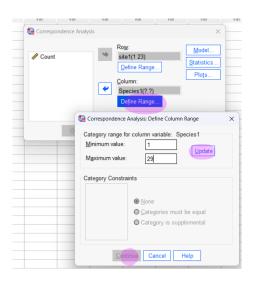
#### Finally,

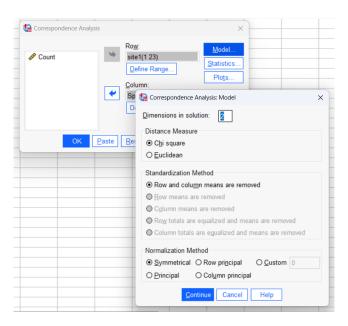


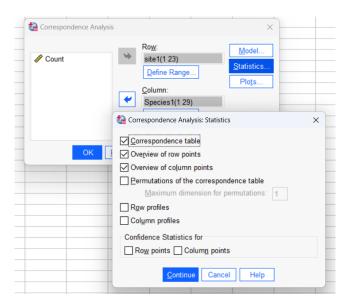
#### Row variable

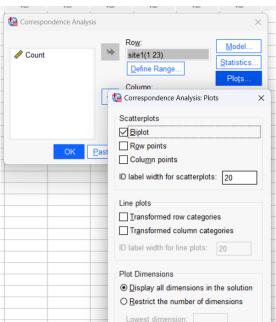


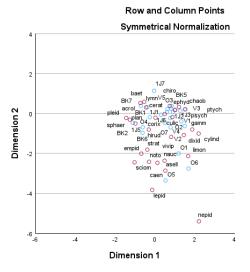
#### Column variable











osite1 Species1

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