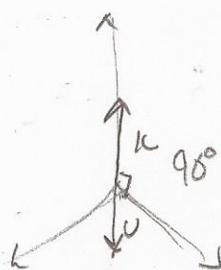


Exercise 1. Determine the dot product of $\mathbf{u} = 2\mathbf{i} - 6\mathbf{j}$ and $\mathbf{v} = 12\mathbf{k}$.

$$\vec{u} = \langle 2, -6, 0 \rangle \quad \vec{v} = \langle 0, 0, 12 \rangle \quad \left(\text{or } \sqrt{2^2 + 6^2} \times \sqrt{12^2} \times \cos 90^\circ \right)$$

$$\mathbf{u} \cdot \mathbf{v} = (2 \times 0) + (-6 \times 0) + (0 \times 12) = 0 \quad \sqrt{40} \times 12 \times 0 = 0$$



Exercise 2. Determine the angle between $\mathbf{u} = \langle 1, -1, 0 \rangle$ and $\mathbf{v} = \langle 1, 0, 1 \rangle$. (Hint: use the Law of Cosines!)

$$\vec{u} = \langle 1, -1, 0 \rangle \quad \vec{v} = \langle 1, 0, 1 \rangle$$

$$\vec{u} \cdot \vec{v} = (1 \times 1) + (-1 \times 0) + (0 \times 1) = 1$$

$$1 = |\mathbf{u}| \cdot |\mathbf{v}| \cdot \cos \theta$$

$$\sqrt{2} \cdot \sqrt{2} \cdot \cos \theta$$

$$\frac{1}{2} = \cos \theta \Rightarrow \theta = \frac{\pi}{3}$$

