

Introduction to Computation Theory

Quiz 4 – In-class (20 pts)

Answer all questions

⑥ $\sqcup \rightarrow \text{accept}$

1. Examine the formal definition of a Turing machine to answer the following questions and explain your reasoning.

- Can a Turing machine ever write the blank symbol \sqcup on its tape?
- Can the tape alphabet Γ be the same as the input alphabet Σ ?
- Can a Turing machine's head ever be in the same location in two successive steps?
- Can a Turing machine contain just a single state?

a) Yes! a Turing machine can write any letters in its Alphabet

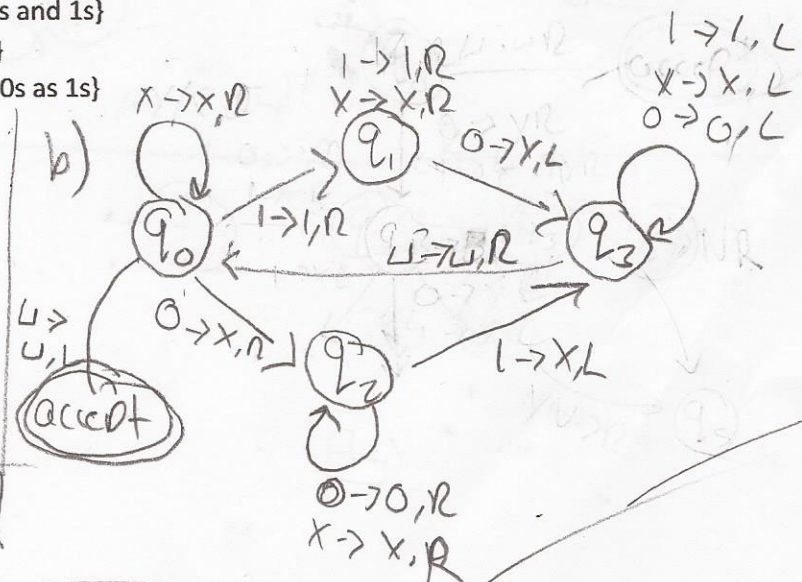
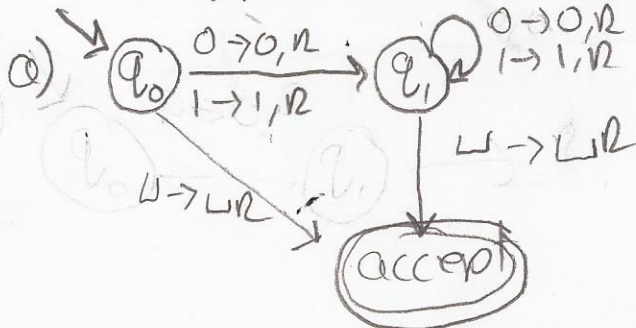
b) No! the ' \sqcup ' is in Γ but never in Σ

c) yes! At the left end of the tape a move to the left stays in place

d) No! at a minimum a Turing machine has an accept and reject state.

2. Give implementation-level descriptions of Turing machines that decide the following

- languages over the alphabet $\{0,1\}$.
- Aa. $\{w \mid w \text{ contains an equal number of 0s and 1s}\}$
- b. $\{w \mid w \text{ contains twice as many 0s as 1s}\}$
- c. $\{w \mid w \text{ does not contain twice as many 0s as 1s}\}$



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c) TM where $\{u\}$ contains 2x as many 0's as 1's

