

Name: Erik Sundblad

Worksheet 7

Exercise 1. Determine the equation of the plane through points $P(2, -1, 3)$, $Q(1, 4, 0)$, and $R(0, -1, 5)$. Then determine where it intersects the coordinate axes and find the intersection with the xy -plane.

Exercise 2. Sketch the cylinder $x^2 + 4y^2 = 16$.

xy plane intersection

$$5y + 4z + 0 = 21$$

$$\boxed{y = -\frac{4}{5}x + \frac{21}{5}} \text{ equation describing the line}$$

$$\vec{QR} = \langle -1, 5, 5 \rangle$$

$$\vec{PQ} = \langle -1, 5, -3 \rangle$$

$$\vec{PR} = \langle -2, 0, 2 \rangle$$

$$P_0P = \langle (x-2), (y+1), (z-3) \rangle$$

$$\vec{PQ} \times \vec{PR} = \begin{vmatrix} -1 & 5 & -3 \\ -2 & 0 & 2 \end{vmatrix} = \langle 10 - 0, 0 - 10, 0 - 10 \rangle$$

$$\langle 10, 8, 10 \rangle = \vec{n} \text{ at } P$$

Eq

$$\boxed{10(x-2) + 8(y+1) + 10(z-3) = 0}$$

y intercept

$$10(0-2) + 8(y+1) + 10(0-3) = 0$$

$$-20 + 8y + 8 - 30 = 0$$

$$8y = 42 \quad (0, 5.25, 0)$$

$$\boxed{y = 5.25}$$

x int

$$10(x-2) + 8(0+1) + 10(0-3) = 0$$

$$10x - 20 + 8 - 30 = 0$$

$$10x = 42 \quad (4.2, 0, 0)$$

where does

$$x=0$$

$$y=0$$

$$z=0$$

Cross y $\hat{=}$ $x, z=0$

$$x \text{ intercept} = z, y=0$$

$$z \text{ int} = x, y=0$$

$$10(0-2) + 8(0+1) + 10(z-3) = 0$$

$$-20 + 8 + 10z - 30 = 0$$

$$\boxed{z = 4.2}$$

$$(0, 0, 4.2)$$