

# Neurális hálók

Nyelvi adatok feldolgozása – 2019/20 tavasz

12. óra

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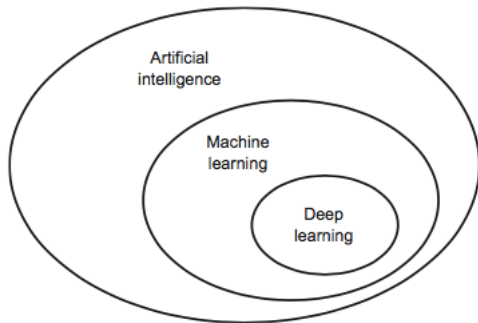
2020. május 11.

MTA Nyelvtudományi Intézet

1. Bevezetés
2. Történeti áttekintés
3. Units
4. The XOR problem
5. Feedforward Neural Networks
6. Training Neural Nets
7. Neural Language Models
8. Irodalom

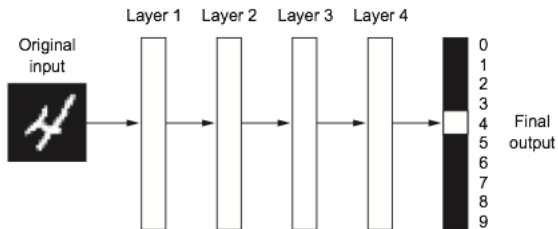
# Bevezetés

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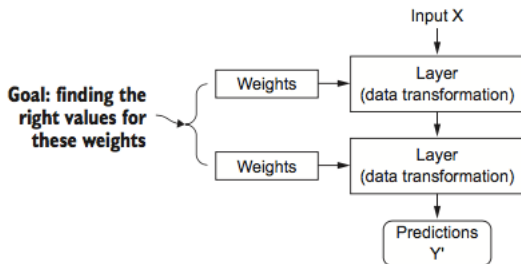
**Figure 1.1** Artificial intelligence, machine learning, and deep learning

# The 'deep' in deep learning



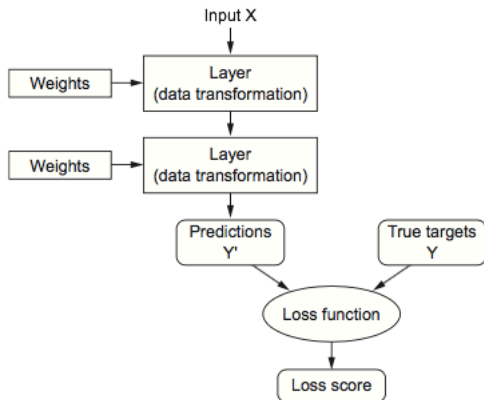
**Figure 1.5** A deep neural network for digit classification

# Understanding how deep learning works 1.



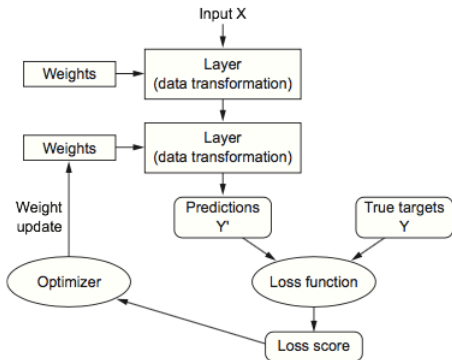
**Figure 1.7** A neural network is parameterized by its weights.

## Understanding how deep learning works 2.



**Figure 1.8** A loss function measures the quality of the network's output.

## Understanding how deep learning works 3.



**Figure 1.9** The loss score is used as a feedback signal to adjust the weights.

the fundamental trick is to use the loss score as a feedback signal to adjust the value of the weights a little, in a direction that will lower the loss score



# Training loop

- kezdetben a súlyok random értékek → az output távol van az ideálistól, a loss score nagyon magas
- a súlyok minden egyes tanulási kör során egy kicsit módosulnak → a loss score kisebb lesz
- ha ezt a tanulási kört elégszer iteráljuk, akkor elérjük a loss score minimumát
- a minimális loss score-ral rendelkező rendszer kimenete lesz a legközelebb a gold standardhez

# Történeti áttekintés

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## mottó:

*“Don’t believe in the short-term hype, but do believe in the long-term vision.”*

a deep learning sok mindenre jó, de nem mindenre a legjobb eszköz:

- kevés az adat
- más algoritmus jobban használható az adott feladatra

# AI winters

AI winter: high expectations for the short term → technology fails to deliver → research investment dries up, slowing progress for a long time

1. 1960s: symbolic AI

Marvin Minsky 1967: “Within a generation ... the problem of creating artificial intelligence will substantially be solved.”

1969-70: first AI winter

2. 1980s: expert systems

a few initial success stories → expensive to maintain, difficult to scale, and limited in scope

early 1990s: second AI winter

- 1940s: McCulloch–Pitts neuron: a simplified model of the human neuron as a kind of computing element
- 1950/60s: perceptron (Rosenblatt, 1958), bias (Widrow and Hoff, 1960), XOR (Minsky and Papert, 1969)
- 1980s: backpropagation (Rumelhart et al., 1986), handwriting recognition with backpropagation and convolutional neural networks (LeCun et al., 1989)
- 1990s: recurrent networks (Elman, 1990), Long Short-Term Memory (1997)
- 2010s: Geoffrey Hinton et al., Yoshua Bengio et al.

# Why now?

## Hardware

- Graphical Processing Unit (GPU): developed for gaming
- 2007: NVIDIA launched CUDA, a programming interface for its line of GPUs
- a small number of GPUs can replace massive clusters of CPUs
- parallelizable matrix multiplications
- 2016: Tensor Processing Unit (TPU) by Google

## Data

*“if deep learning is the steam engine of this revolution, then data is its coal”*

## Why now? – cont.

### Algorithms

The feedback signal used to train neural networks would fade away as the number of layers increased.

- better activation functions
- better weight-initialization schemes
- better optimization schemes

Only when these improvements began to allow for training models with 10 or more layers did deep learning start to shine.

### A new wave of investment

total investment in AI: 2011: \$19 million → 2014: \$394 million

### The democratization of deep learning

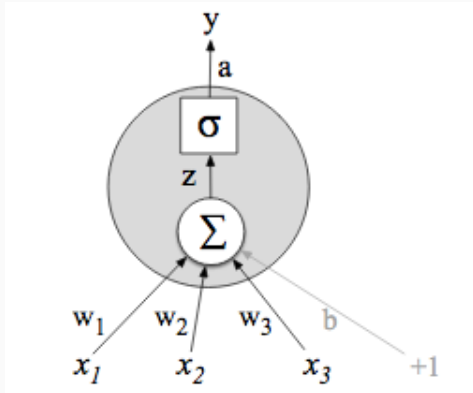
early days: doing deep learning required significant programming expertise → now: basic Python scripting skills are sufficient (PyTorch, TensorFlow, Keras) → no feature engineering



# Units

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# A neural unit



The building block of a neural network is a single computational unit. A unit takes a set of real valued numbers as input, performs some computation on them, and produces an output.

a neural unit is taking a weighted sum of its inputs, with one additional term in the sum called a bias term

$$z = b + \sum_i w_i x_i$$

expressing this weighted sum using vector notation: replacing the sum with dot product ( $z \in \mathbb{R}$ ):

$$z = w \cdot x + b$$

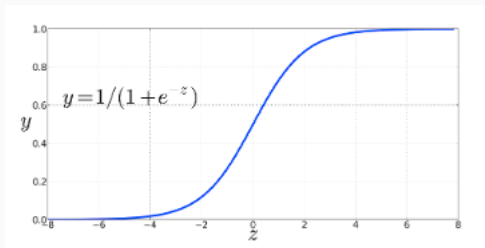
instead of using  $z$ , neural units apply a non-linear function  $f$  to  $z \rightarrow$  the output of this function is the activation value for the unit  $a$

$$y = a = f(z)$$

the final output of the network is  $y$ , and since here we have a single unit,  $y$  and  $a$  are the same

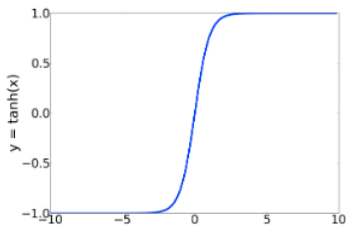
## Non-linear functions – sigmoid

$$y = \sigma(z) = \frac{1}{1 + e^{-z}}$$



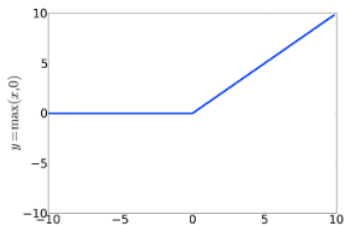
# Non-linear functions – tanh and ReLU

$$y = \frac{e^z - e^{-z}}{e^z + e^{-z}}$$



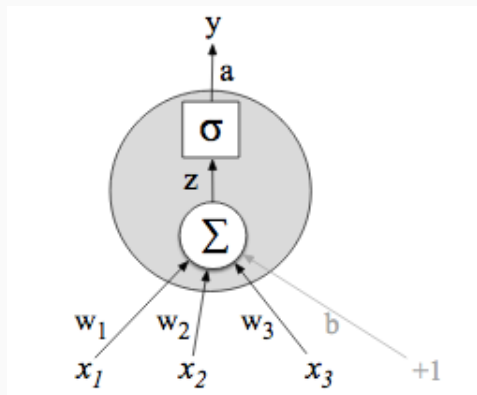
(a)

$$y = \max(x, 0)$$



(b)

## Summary – a unit



## The XOR problem

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# The XOR problem

- the power of neural networks comes from combining these units into larger networks
- one of its most clever demonstration was the proof by Minsky and Papert (1969): a single unit cannot compute XOR

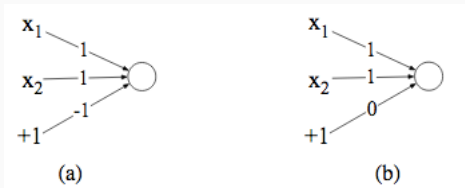
AND			OR			XOR		
x1	x2	y	x1	x2	y	x1	x2	y
0	0	0	0	0	0	0	0	0
0	1	0	0	1	1	0	1	1
1	0	0	1	0	1	1	0	1
1	1	1	1	1	1	1	1	0

# A perceptron

## a perceptron

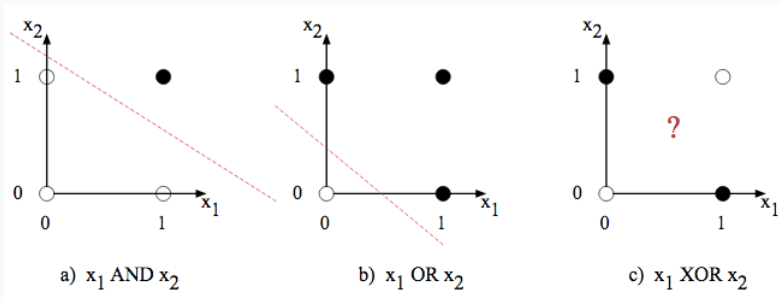
is a simple neural unit that has a binary output and does not have a non-linear activation function

$$y = \begin{cases} 0, & \text{if } w \cdot x + b \leq 0 \\ 1, & \text{if } w \cdot x + b > 0 \end{cases}$$

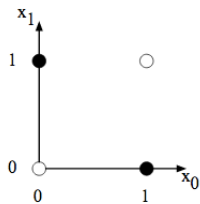
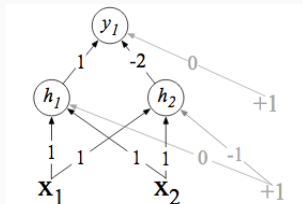


# Decision boundary

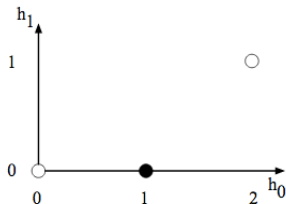
a perceptron is a linear classifier



# XOR solution



a) The original  $x$  space



b) The new  $h$  space

# Feedforward Neural Networks

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# A feedforward network

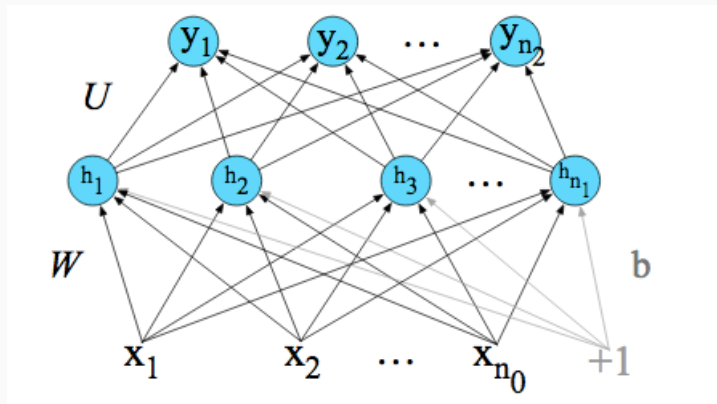
## a feedforward network

is a multilayer network

- in which the units are connected with no cycles;
- the outputs from units in each layer are passed to units in the next higher layer, and
- no outputs are passed back to lower layers

(networks with cycles are called recurrent neural networks (RNNs))

## Three kinds of nodes



input units, hidden units, and output units

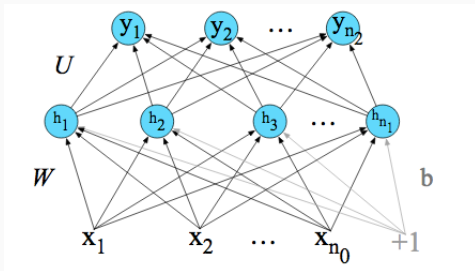
# The hidden layer

- the hidden layer is formed of hidden units, each of which is a neural unit, taking a weighted sum of its inputs and then applying a non-linearity
- fully-connected: each hidden unit sums over all the input units



# Weight matrix

We represent the parameters for the entire hidden layer by combining the weight vector  $w_i$  and bias  $b_i$  for each unit  $i$  into a single weight matrix  $W$  and a single bias vector  $b$  for the whole layer. Each element  $W_{ij}$  of the weight matrix  $W$  represents the weight of the connection from the  $i$ th input unit  $x_i$  to the  $j$ th hidden unit  $h_j$ .



# Matrix operations

## 3 steps:

1. multiplying the weight matrix by the input vector  $x$
2. adding the bias vector  $b$
3. applying the activation function  $g$

$$h = \sigma(Wx + b)$$

- the number of inputs:  $n_0$
- $x$  is a vector of real numbers of dimension  $n_0$ :  $x \in \mathbb{R}^{n_0}$
- the hidden layer has dimensionality  $n_1$ , so  $h \in \mathbb{R}^{n_1}$
- $W \in \mathbb{R}^{n_1 \times n_0}$

# The role of the output layer

- the resulting value  $h$  forms a representation of the input
- the role of the output layer: to take this representation and compute the final output
- the output can be a real-valued number, but it is rather a probability distribution across the output nodes

## Intermediate output

- the output layer also has a weight matrix ( $U$ )
- some models don't include a bias vector  $b$ , so here we eliminate it
- the weight matrix  $U$  is multiplied by the vector  $h$  to produce the intermediate output  $z$ :

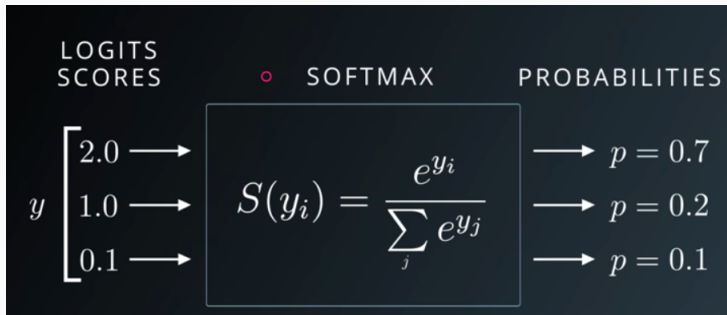
$$z = Uh$$

- $U \in \mathbb{R}^{n_2 \times n_1}$
- element  $U_{ij}$  is the weight from unit  $j$  in the hidden layer to unit  $i$  in the output layer

# The softmax function

converting a vector of real-valued numbers to a vector encoding a probability distribution:

$$\text{softmax}(z_i) = \frac{e^{z_i}}{\sum_{j=1}^d e^{z_j}} \quad 1 \leq i \leq d$$



## Summary – feedforward network

the final equations for a feedforward network with a single hidden layer, which takes an input vector  $x$ , outputs a probability distribution  $y$ , and is parameterized by weight matrices  $W$  and  $U$  and a bias vector  $b$ :

$$h = \sigma(Wx + b)$$

$$z = Uh$$

$$y = \text{softmax}(z)$$

### activation functions:

- at the internal layers: ReLU or tanh
- at the final layer:
  - for binary classification: sigmoid
  - for multinomial classification: softmax

# Training Neural Nets

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- the correct output:  $y$
- the system's estimate of the true  $y$ :  $\hat{y}$
- the goal of the training procedure: to learn parameters  $W^{[i]}$  and  $b^{[i]}$  for each layer  $i$  that make  $\hat{y}$  as close as possible to the true  $y$



# How to do that?

1. we need a loss function that models the distance between  $\hat{y}$  and  $y \rightarrow$  cross-entropy loss
2. we have to minimize the loss function  $\rightarrow$  an optimization algorithm for iteratively updating the weights: gradient descent
3. we have to know the gradient of the loss function  $\rightarrow$  error backpropagation

## Cross-entropy loss

if the neural network is used as a binary classifier:

$$L_{CE}(\hat{y}, y) = -\log p(y|x) = -[y \log \hat{y} + (1 - y) \log(1 - \hat{y})]$$

if the neural network is used as a multinomial classifier:

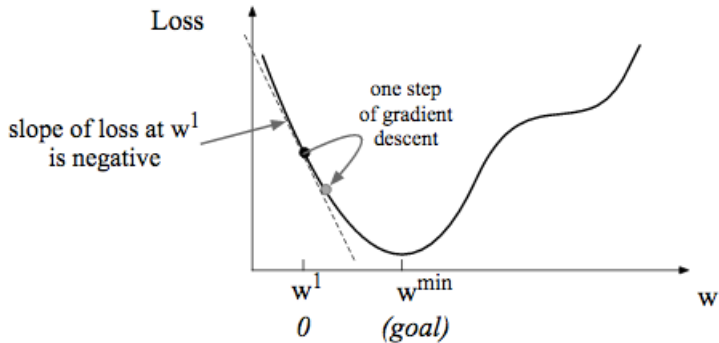
$$L_{CE}(\hat{y}, y) = -\sum_{i=1}^C y_i \log \hat{y}_i$$

hard classification task:

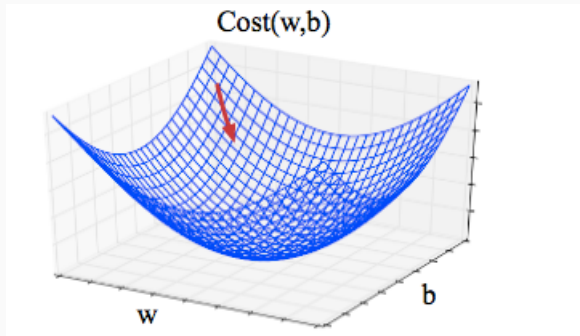
$$L_{CE}(\hat{y}, y) = -\log \hat{y}_i$$

we want this loss lower, if  $\hat{y}$  is closer to  $y$ , and higher, if farer

## Computing the Gradient – one parameter



## Computing the Gradient – two parameters



for more parameters → **error backpropagation** or backward differentiation → all parameters can be calibrated together  
non-convex optimization problem with possible local minima

- to prevent overfitting → dropout: randomly dropping some units and their connections from the network during training
- tuning hyperparameters:
  - the number of layers
  - the number of hidden nodes per layer
  - the choice of activation functions
  - ...

# Neural Language Models

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## language modeling:

predicting upcoming words from prior word context

neural language modeling (NLM) has advantages over n-gram language modeling:

- NLM does not need smoothing
- NLM can handle much longer histories
- NLM can generalize over contexts of similar words
- NLM has much higher predictive accuracy

## a feedforward NLM is

a standard feedforward network that takes as input at time  $t$  a representation of some number of previous words

$w_{t-1}, w_{t-2}, \dots$ , and outputs a probability distribution over possible next words

$$P(w_t | w_1^{t-1}) \approx P(w_t | w_{t-N+1}^{t-1})$$

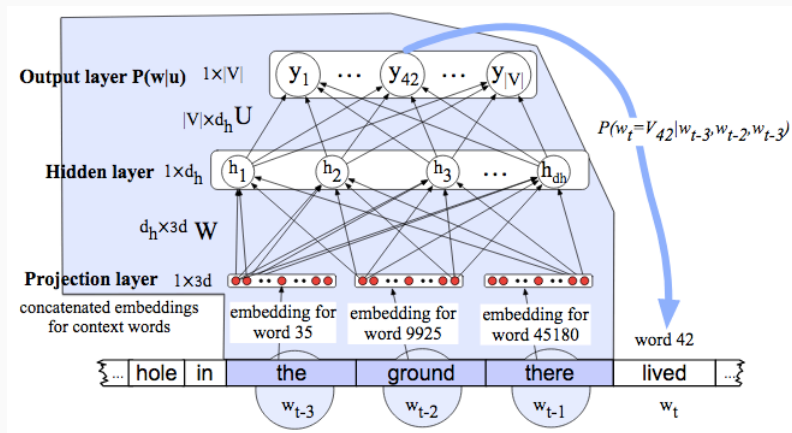


the prior context is represented by embeddings of the previous words → allows NLM to generalize to unseen data much better than n-gram models

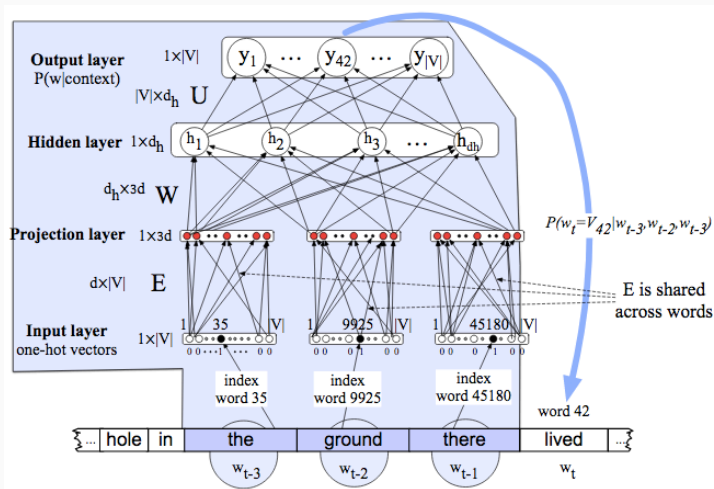
## 2 ways of using embeddings:

1. pretrained embeddings: we get the embeddings from an embedding dictionary  $E$  for each word in our vocabulary  $V$
2. learning embeddings simultaneously with training the network

# Using pretrained embeddings



# Learning embeddings



the final equations for NLM:

$$e = (E_{x_1}, E_{x_2}, \dots, E_x)$$

$$h = \sigma(We + b)$$

$$z = Uh$$

$$y = \text{softmax}(z)$$

training such a network will result both in an algorithm for language modeling and a new set of embeddings

Irodalom

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- Jurafsky 3rd edition 5. & 7. chapter
- Francois Chollet: Deep Learning with Python. Manning, Shelter Island, 2018.: <https://www.manning.com/books/deep-learning-with-python>