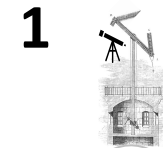
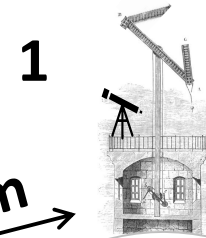
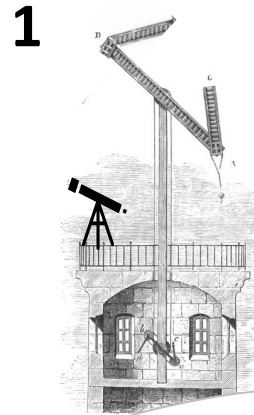
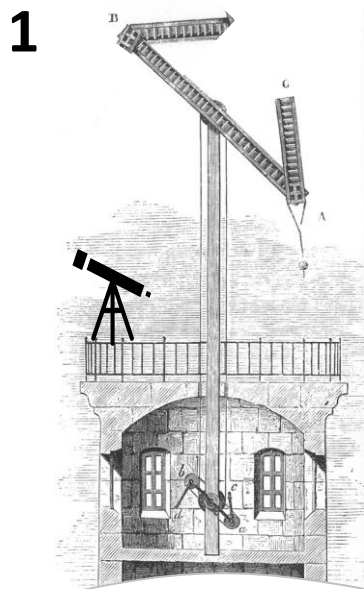


# 1- The Physical Layer

*“Wireless” well before radios...*

# Chappe's optical telegraph (late 18<sup>th</sup> century)



Some km

# A smart fraud (1834-1837)

## **Blanc brothers' goal**

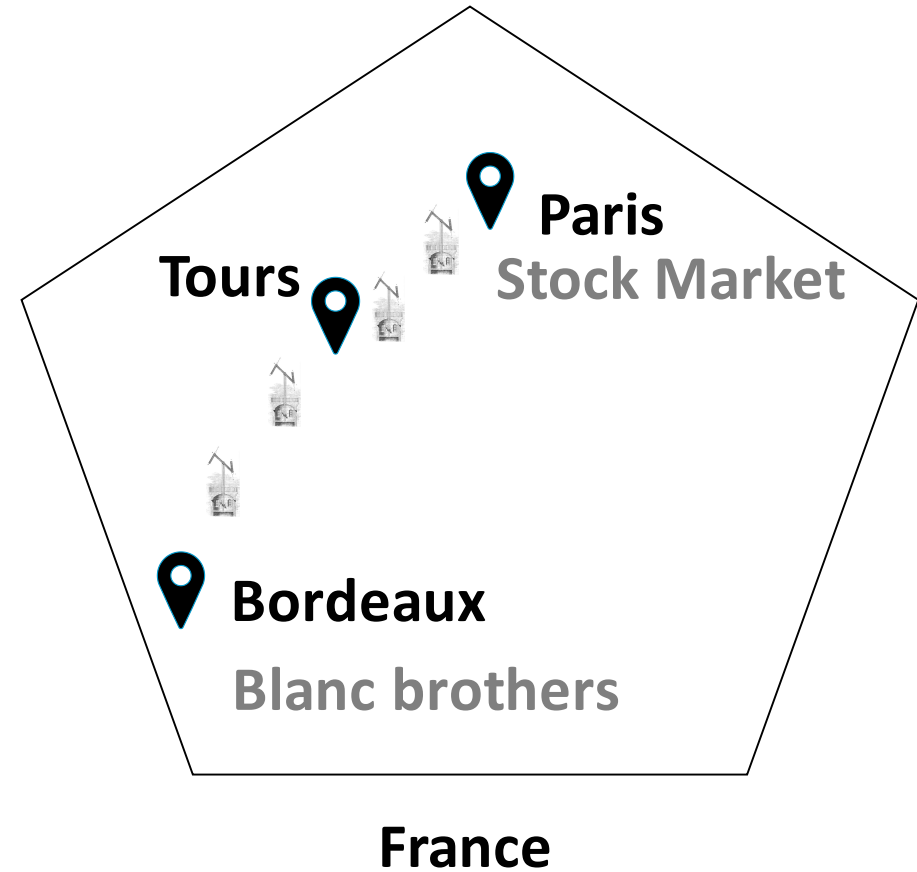
Get stock market news before competitors

## **The solution**

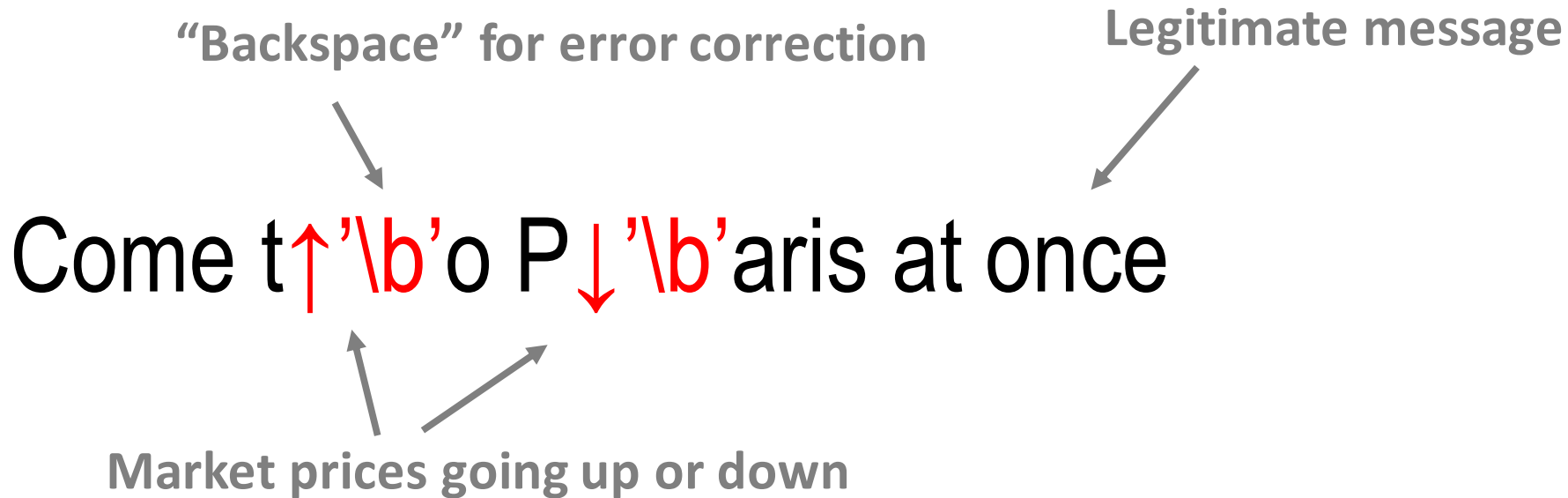
Hack the optical telegraph  
Covert channel faster than mail

## **How??**

Exploit error correction!



# Hiding stock market trends



1. Added by an accomplice operator in Tours
2. Observed by an accomplice in Bordeaux
2. Discarded by legitimate receiver thanks to '\b'

# References

“1834: The First Cyberattack - Schneier on Security,” accessed June 28, 2021, [https://www.schneier.com/blog/archives/2018/05/1834\\_the\\_first\\_.html](https://www.schneier.com/blog/archives/2018/05/1834_the_first_.html).

“Journal Des Débats Politiques et Littéraires,” issue, Gallica, January 29, 1837, <https://gallica.bnf.fr/ark:/12148/bpt6k4393846>.

“What the Count of Monte Cristo Can Teach Us About Cybersecurity - IEEE Spectrum,” IEEE Spectrum: Technology, Engineering, and Science News, accessed June 28, 2021, <https://spectrum.ieee.org/tech-talk/telecom/security/what-the-count-of-monte-cristo-can-teach-us-about-cybersecurity>.

Radio communications

# A brief history



1950



2020

## **End of the 19<sup>th</sup> Century**

Electromagnetism

Radio communications

## **20<sup>th</sup> Century**

Huge development

Many applications + Integration

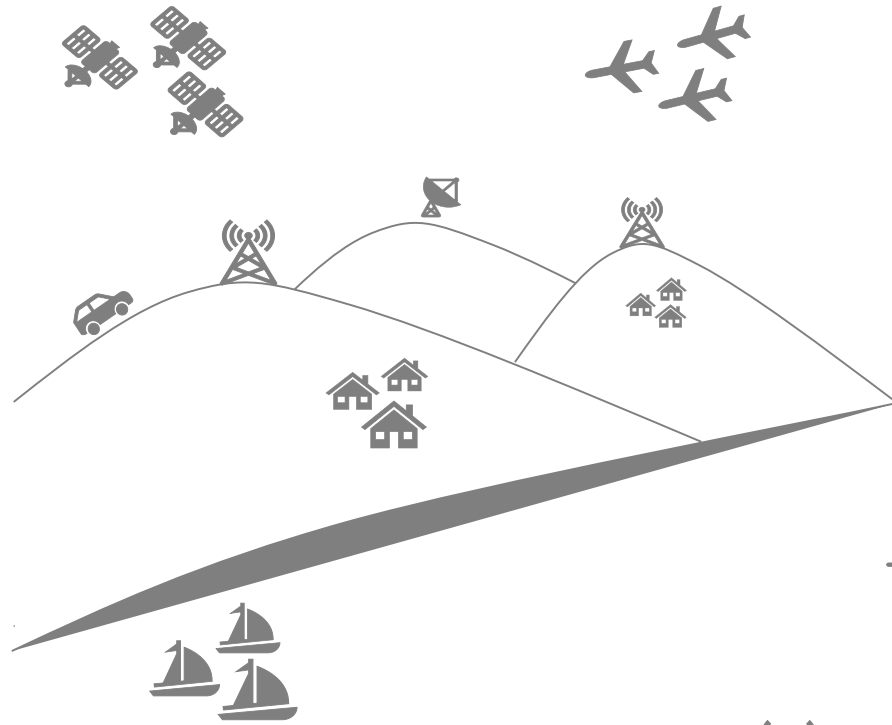
## **21<sup>st</sup> Century**

Integration + computation + embedded

Smartphones, Embedded, IoT, sensors

Software Defined Radios





# How many radios?

Broadcast Radar IoT

Positioning

Mobile

Embedded



# How many radios on a smartphone?

**GNSS (km)**

**Cellular (km)**

**FM (km)**

**WiFi (m)**

**BT/BLE (m)**

**NFC (mm)**

**UWB (m)**



# References

G. R. M. Garratt, T. B. A. Senior, and John L. Volakis, The Early History of Radio: From Faraday to Marconi (Institution of Engineering and Technology, 1994).

Massimo Guarnieri, “A Question of Coherence [Historical],” IEEE Industrial Electronics Magazine 10, no. 3 (September 2016): 54–58, <https://doi.org/10.1109/MIE.2016.2590718>.

“Hedy Lamarr,” in Wikipedia, June 25, 2021, [https://en.wikipedia.org/w/index.php?title=Hedy\\_Lamarr&oldid=1030354762](https://en.wikipedia.org/w/index.php?title=Hedy_Lamarr&oldid=1030354762).

How do radio communications work?  
(A minimalistic overview)

# The goal



## **Transmit information**

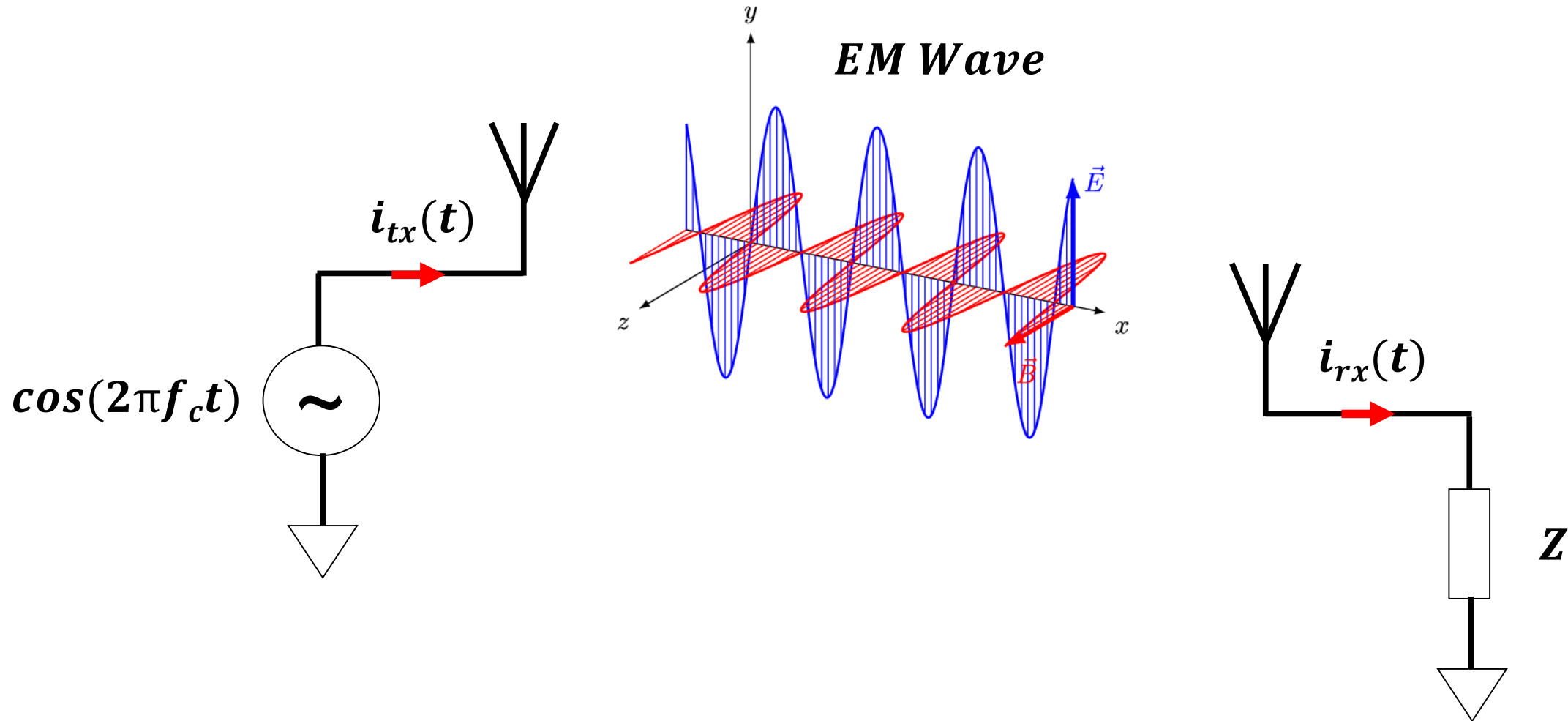
Which physical signal?

How to encode information?

What circuits?

How to deal with errors?

# Propagation



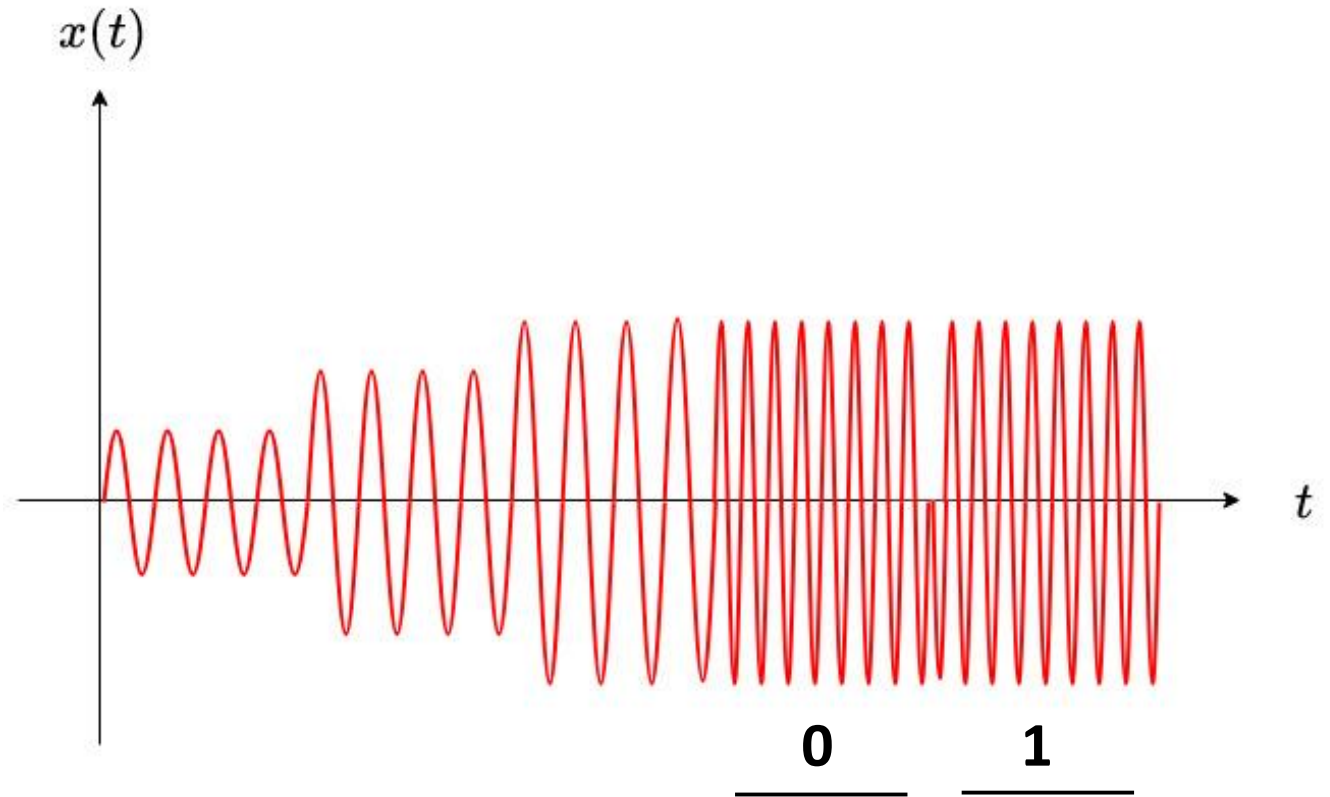
# Transmitting information: Modulation

## Intuition

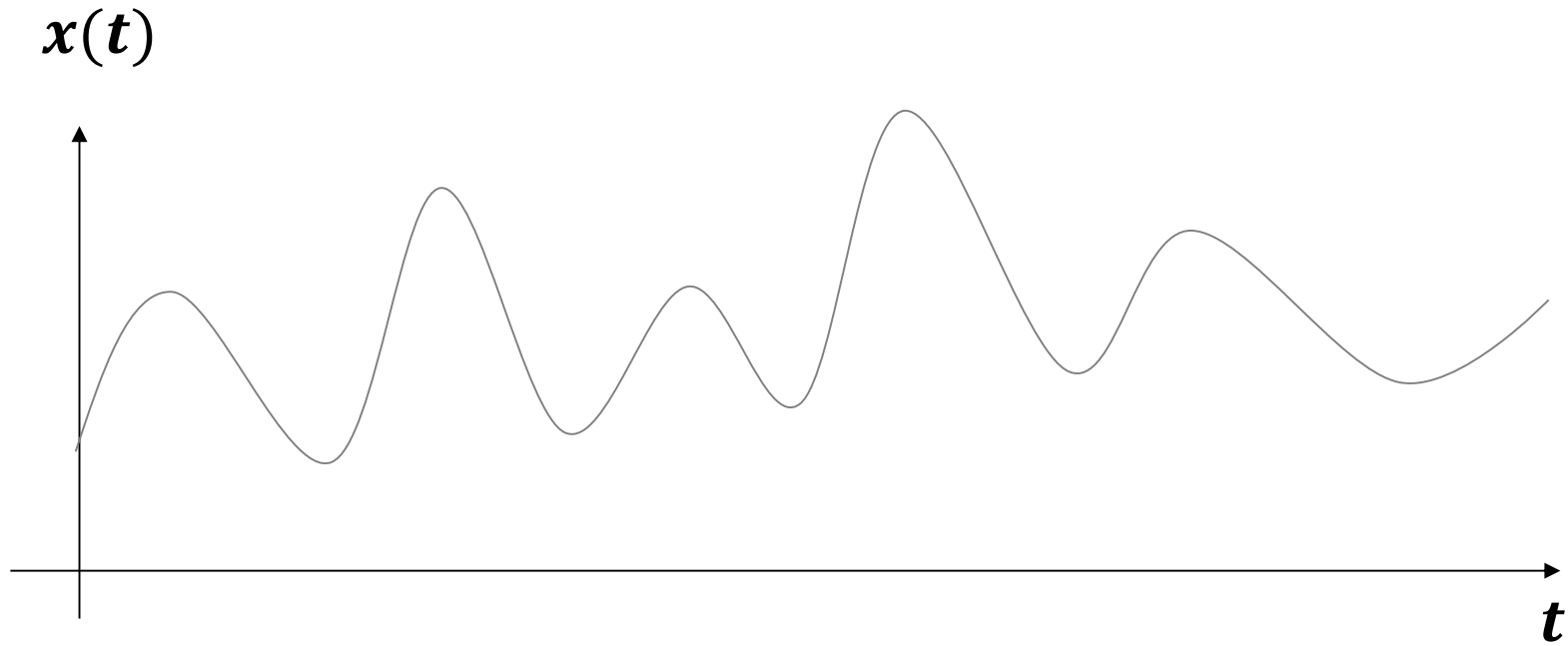
Sinusoidal radio signal (carrier)

Modulate (information)

- Amplitude
- Frequency
- Phase



# Some math...



**A signal**

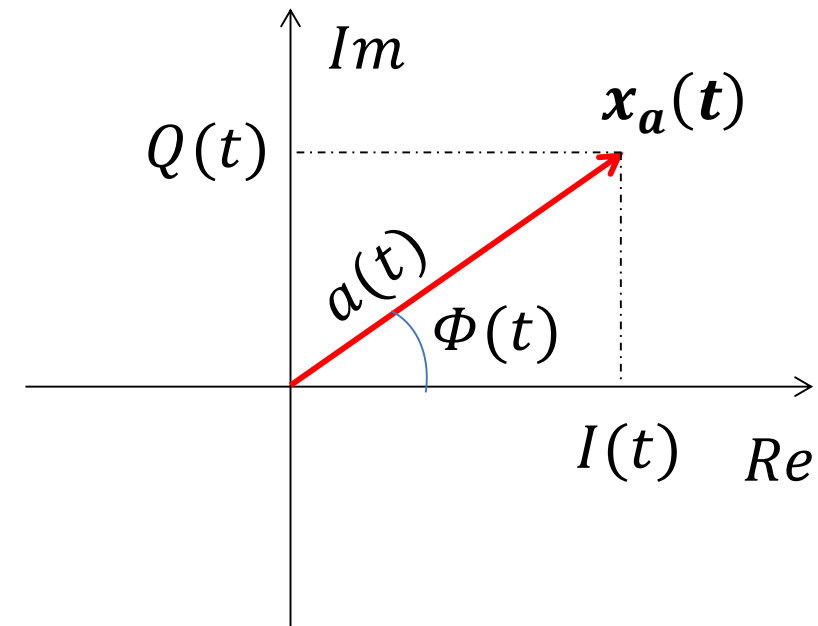
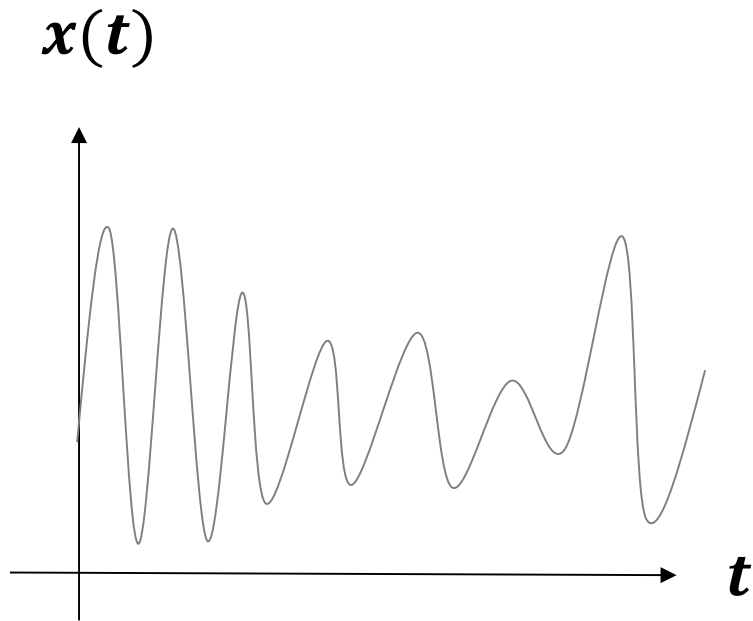
E.g., a quantity that varies over time



# Some math...

## Intuition

See the signal as the projection on the real axis of a rotating vector in the complex plane



## Analytic signal representation

$$x(t) = \text{Re}\{x_a(t)\} = \text{Re}\{a(t)e^{i\Phi(t)}\} = a(t)\cos(\Phi(t))$$

# Analytical signal

$$x(t) = \text{Re}\{x_a(t)\} = \text{Re}\{a(t)e^{j\Phi(t)}\} = a(t)\cos(\Phi(t))$$

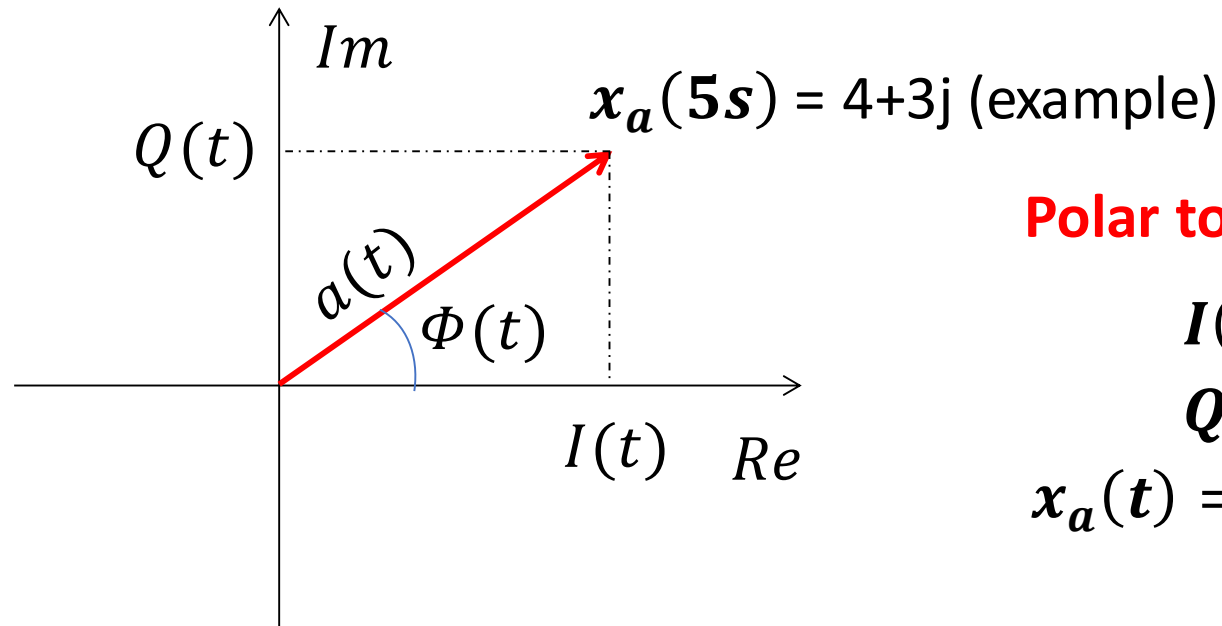
Analytic signal

Amplitude

Phase

$$f(t) = \frac{1}{2\pi} \frac{d\Phi(t)}{dt}$$

Frequency



Polar to quadrature

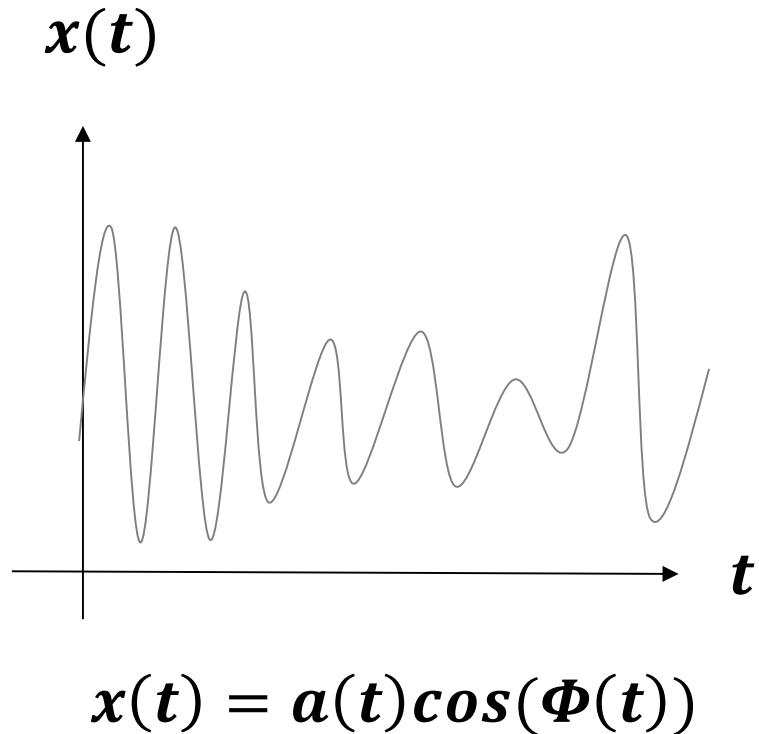
$$I(t) = a(t) \cos(\Phi(t))$$

$$Q(t) = a(t) \sin(\Phi(t))$$

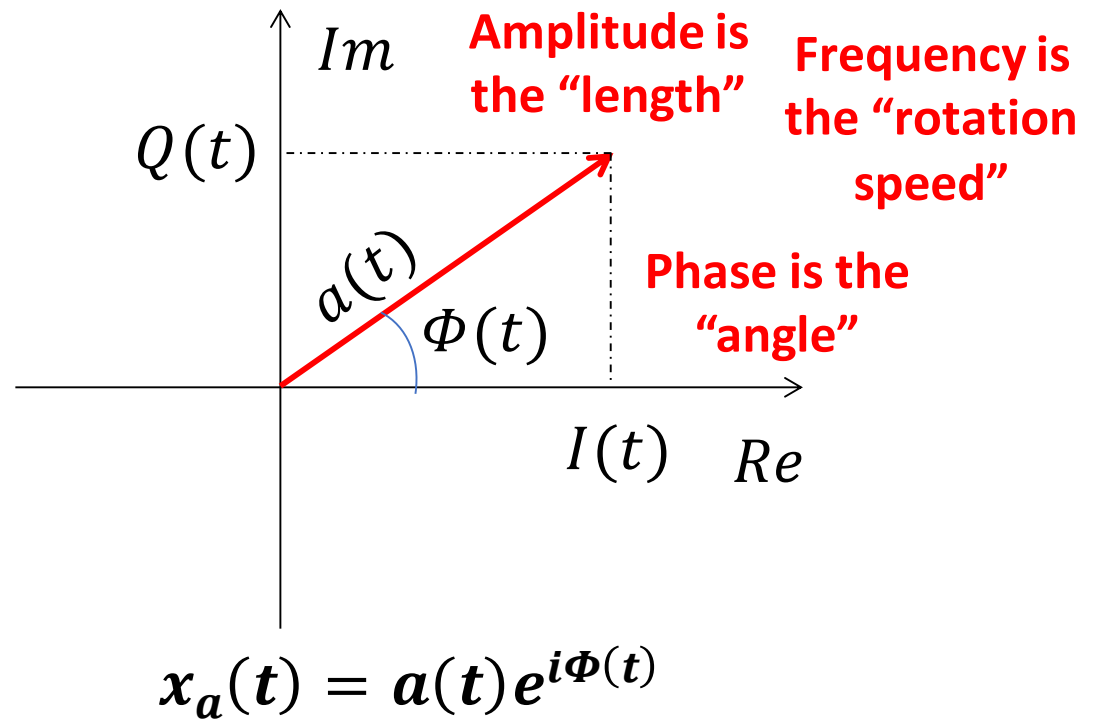
$$x_a(t) = I(t) + jQ(t) = a(t)e^{j\Phi(t)}$$

$$*\sin(x) = \cos(90-x)$$

# Don't be confused by math

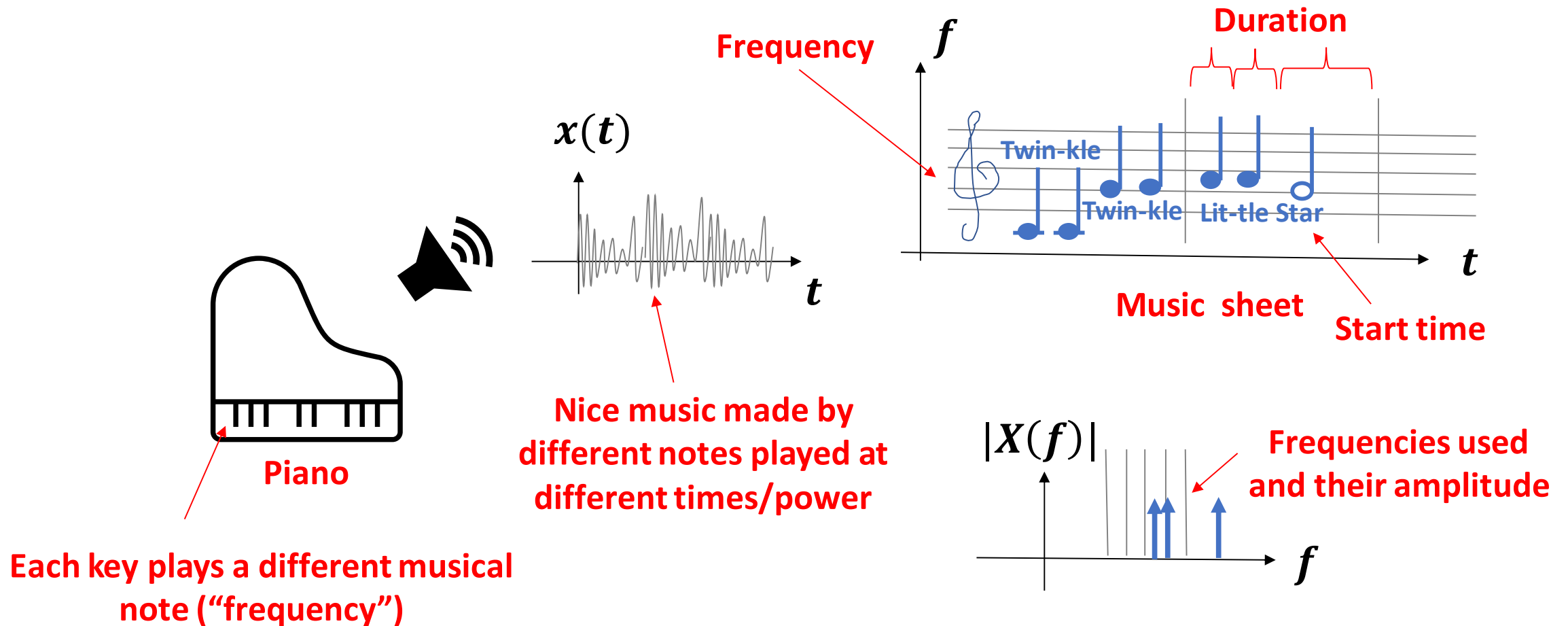


**The physical signal  
(The real part)**

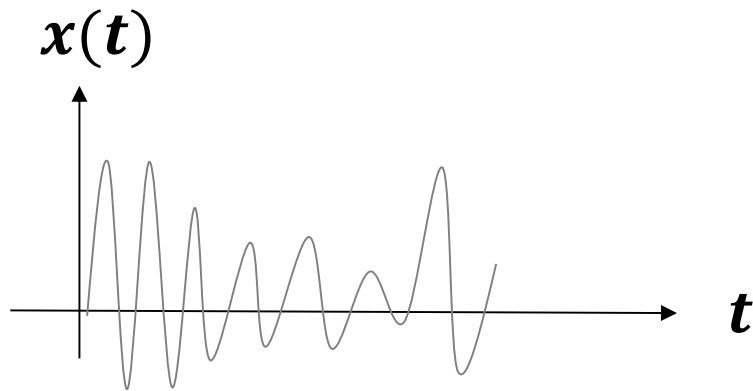


**The mathematical representation  
(The complex analytical signal)**

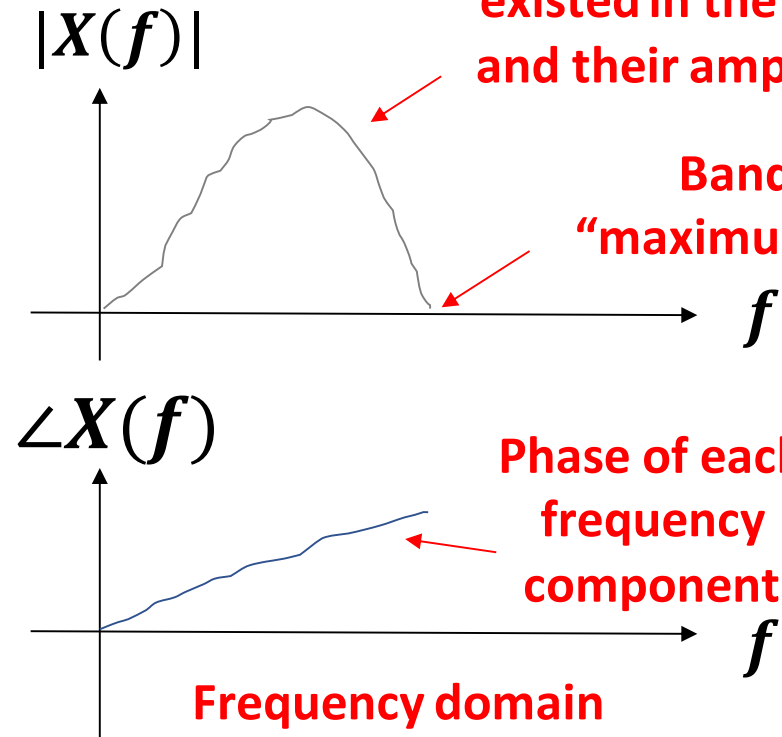
# On time, frequency, and frequency over time



# Frequency analysis



Time domain



For real signals the transform is symmetric so we sometimes draw only the right side

Frequencies that existed in the signal and their amplitude

Bandwidth or "maximum frequency"

Phase of each frequency component

Frequency domain

$$X(f) = F(x(t)) = \int_{-\infty}^{+\infty} x(t) e^{-i\pi 2ft} dt$$

Fourier Transform

Decompose  $x(t)$  into an infinite sum of complex sinewaves at different frequency

$$\cos x = \operatorname{Re}(e^{ix}) = \frac{e^{ix} + e^{-ix}}{2},$$

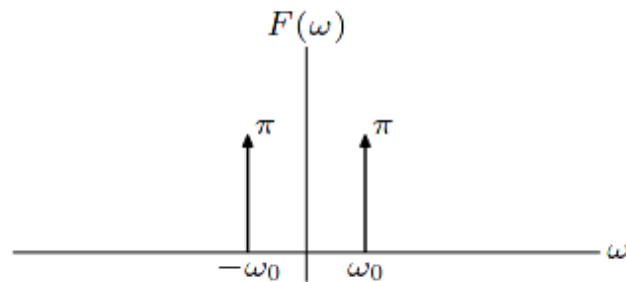
$$\sin x = \operatorname{Im}(e^{ix}) = \frac{e^{ix} - e^{-ix}}{2i}.$$

$$\omega = 2\pi f$$

# Some examples

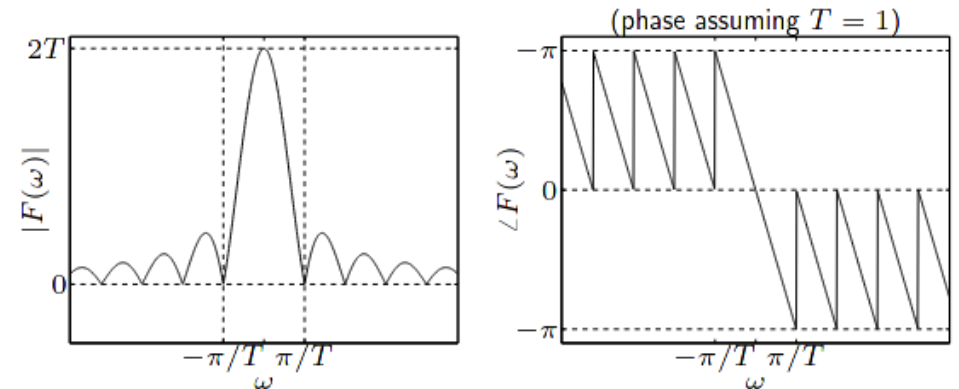
**sinusoidal signals:** Fourier transform of  $f(t) = \cos \omega_0 t$

$$\begin{aligned} F(\omega) &= \frac{1}{2} \int_{-\infty}^{\infty} (e^{j\omega_0 t} + e^{-j\omega_0 t}) e^{-j\omega t} dt \\ &= \frac{1}{2} \int_{-\infty}^{\infty} e^{-j(\omega - \omega_0)t} dt + \frac{1}{2} \int_{-\infty}^{\infty} e^{-j(\omega + \omega_0)t} dt \\ &= \pi \delta(\omega - \omega_0) + \pi \delta(\omega + \omega_0) \end{aligned}$$



**shifted rectangular pulse:**  $f(t) = \begin{cases} 1 & 1-T \leq t \leq 1+T \\ 0 & t < 1-T \text{ or } t > 1+T \end{cases}$

$$\begin{aligned} F(\omega) &= \int_{1-T}^{1+T} e^{-j\omega t} dt = \frac{-1}{j\omega} (e^{-j\omega(1+T)} - e^{-j\omega(1-T)}) \\ &= \frac{-e^{-j\omega}}{j\omega} (e^{-j\omega T} - e^{j\omega T}) \\ &= \frac{2 \sin \omega T}{\omega} e^{-j\omega} \end{aligned}$$



<https://web.stanford.edu/class/ee102/lectures/fourtran>

<https://ethz.ch/content/dam/ethz/special-interest/baug/ibk/structural-mechanics-dam/education/identmeth/fourier.pdf>

# Power Spectral Density (PSD)

Sometimes it is convenient to reason in terms of power

- **Signal:**

- $x(t)$

$$x_T(t) = x(t) \text{ if } -\frac{T}{2} < t < \frac{T}{2} \text{ else } 0$$

- **Power in the time domain**

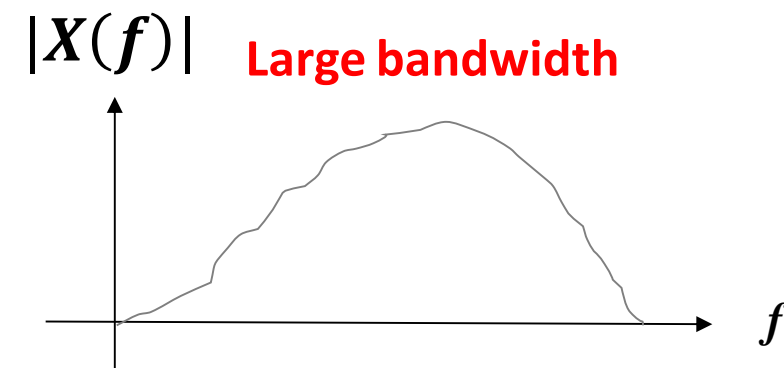
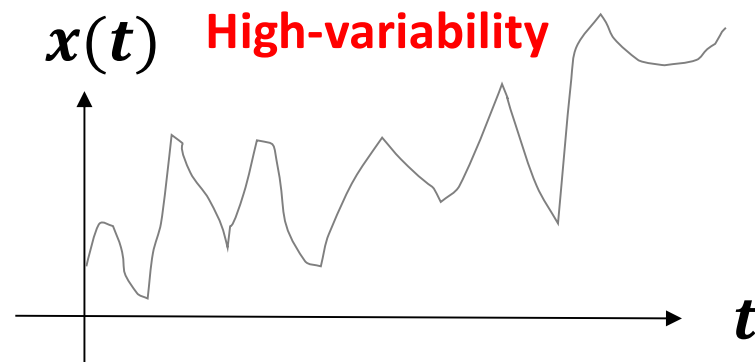
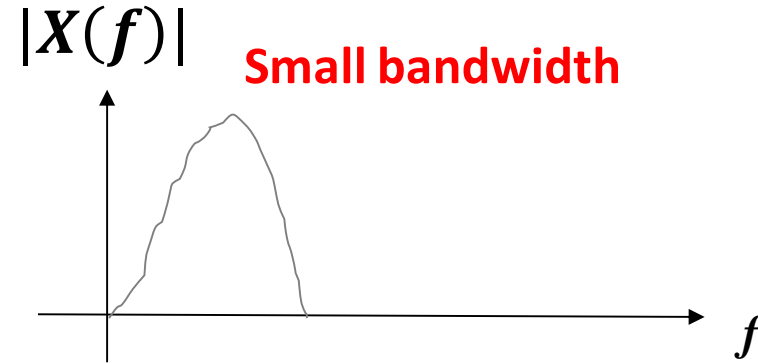
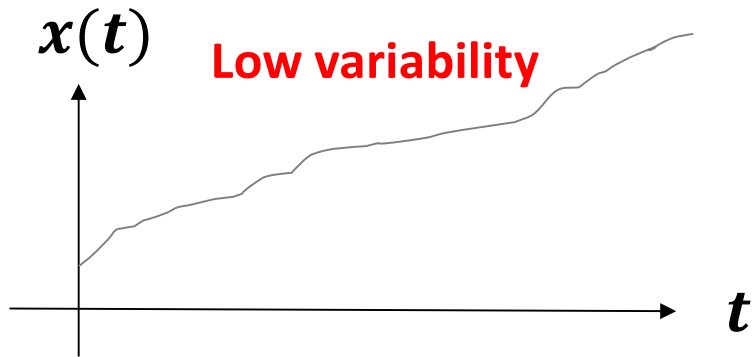
- **Power:**  $\lim_{T \rightarrow \infty} \frac{1}{T} \int |x_T(t)|^2 dt$

- **Power in the frequency domain**

- **Power Spectral Density (PSD):**  $PSD(f) = \lim_{T \rightarrow \infty} \frac{1}{T} \int |X_T(f)|^2 dt$

It tells us the distribution of power over the frequency components of  $x(t)$

# High data-rate => Large bandwidth

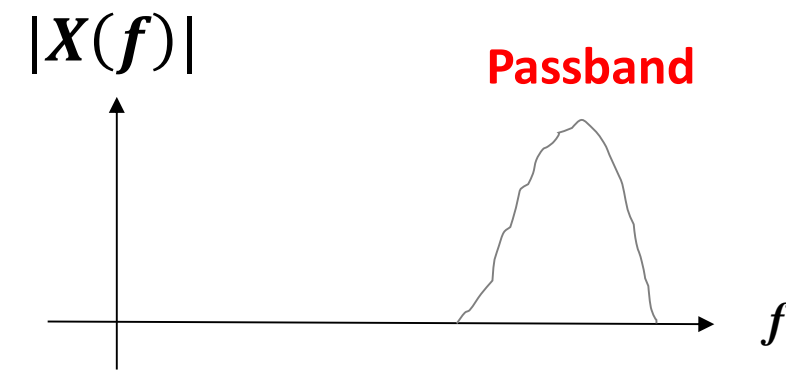
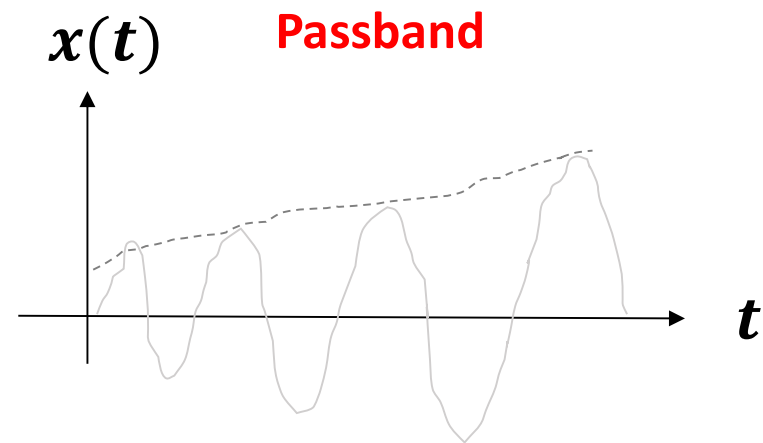
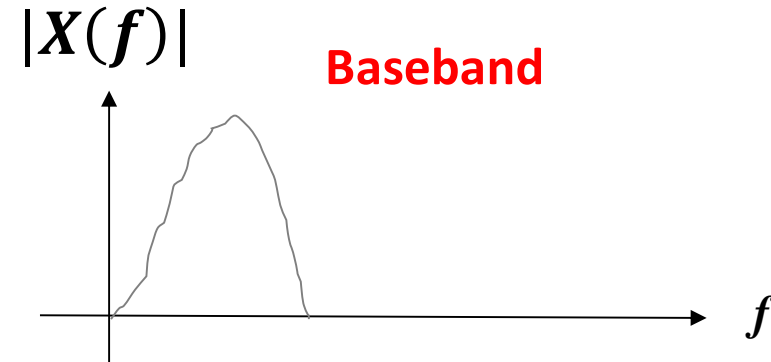
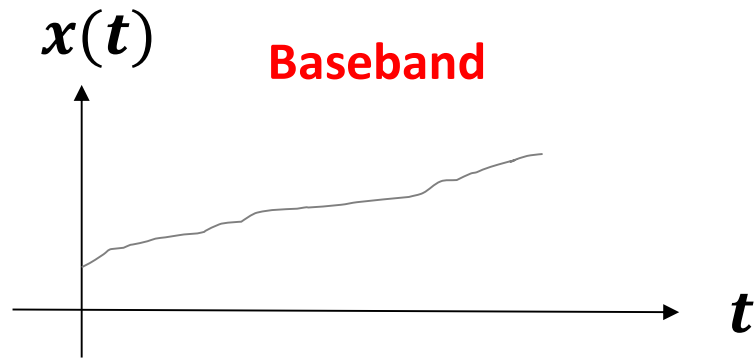


Time domain

Frequency domain



# Baseband to passband



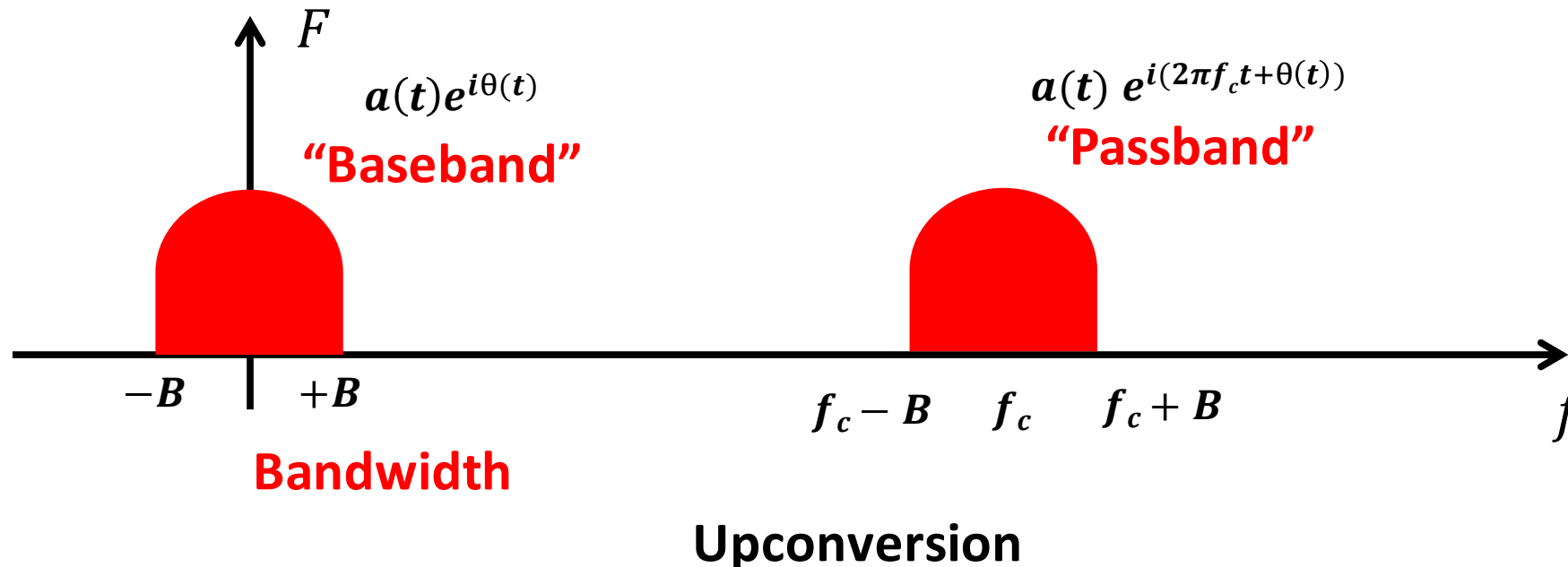
**Time domain**

**Frequency domain**

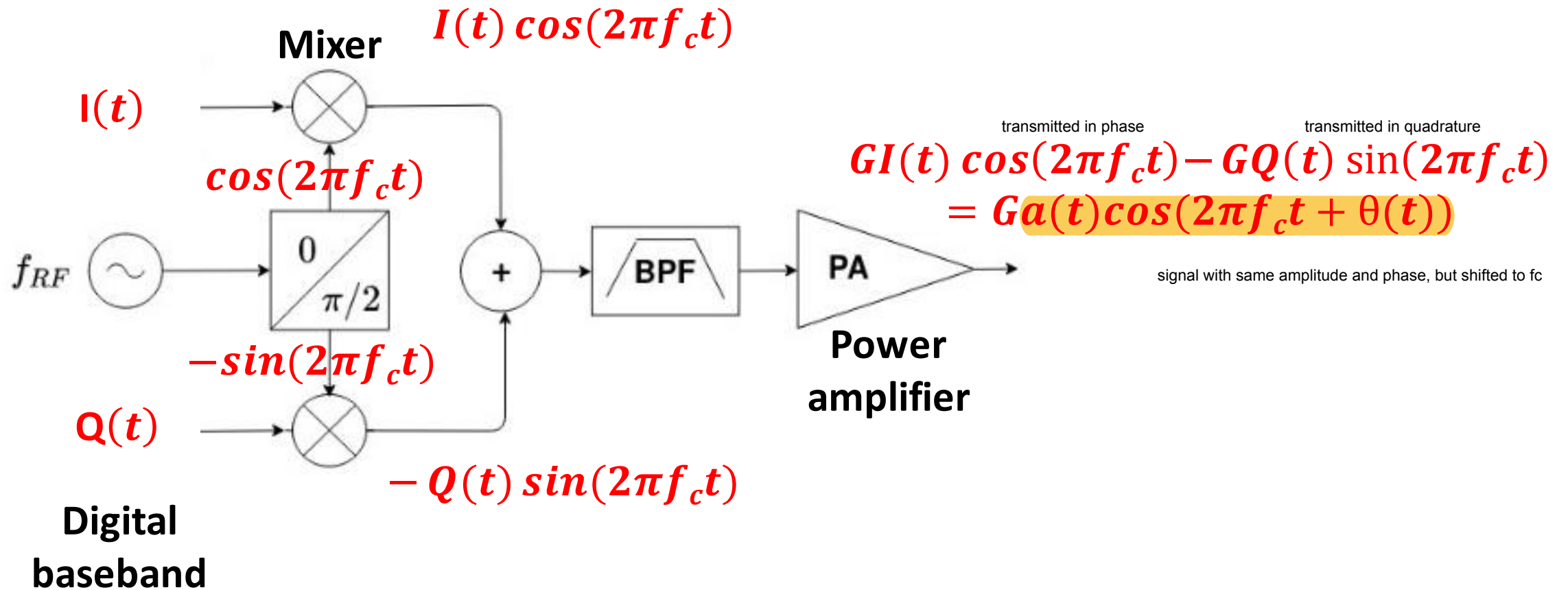
# Baseband and passband

$$x_{RF}(t) = RE\{\underbrace{a(t)e^{i\theta(t)}}_{\text{Complex envelope}} \underbrace{e^{i2\pi f_c t}}_{\text{Carrier}}\} = \underbrace{a(t)}_{\text{Amplitude}} \cos(2\pi \underbrace{f_c}_{\text{Carrier frequency}} t + \underbrace{\theta(t)}_{\text{Phase}})$$

$$f(t) = f_c + \frac{1}{2\pi} \frac{d\theta(t)}{dt}$$



# The Electronics

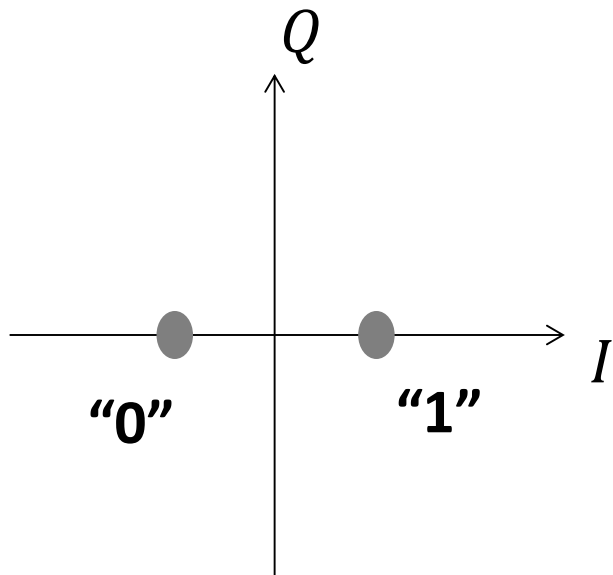


## Quadrature Modulator

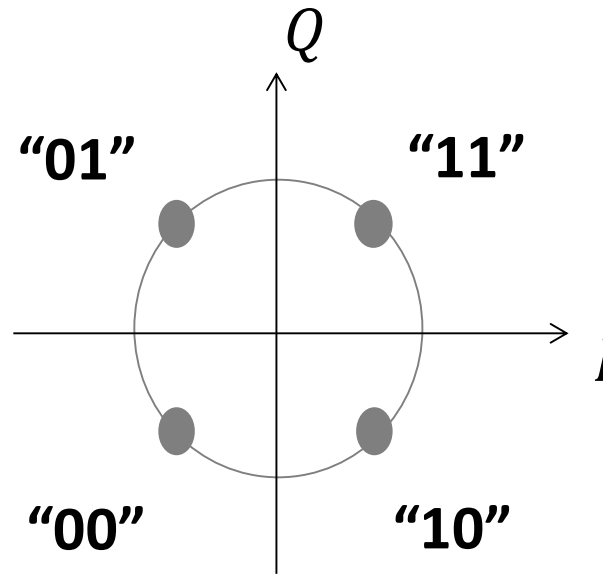
(This is just one possible architecture!)

It's time for some examples

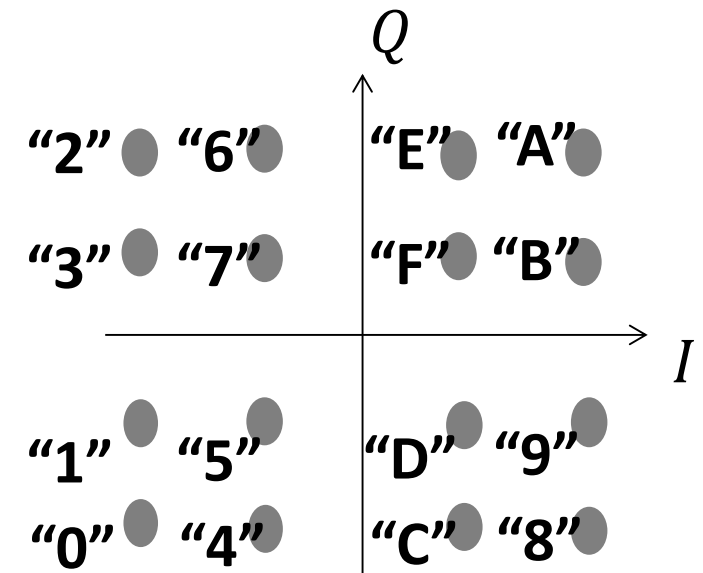
# Phase-shift Keying (PSK) and Quadrature Amplitude Modulation (QAM)



**Binary-PSK**



**Quadrature-PSK**



**QAM 16**

# BPSK with square pulses

```
bits = np.array([0,1,0,1,1,1,0,0,1,1,1,0,1,0,1,1])
```

Input bits one by one

```
symbols_psk = bits
```

```
bpsk = np.array((-1+0j, +1+0j))
```

Constellation

```
Mbpsk = np.repeat(bpsk[symbols_psk], Ns)
```

Baseband IQ  
samples

Find symbol in  
constellation

Repeat for the  
entire duration of  
the symbol

Q

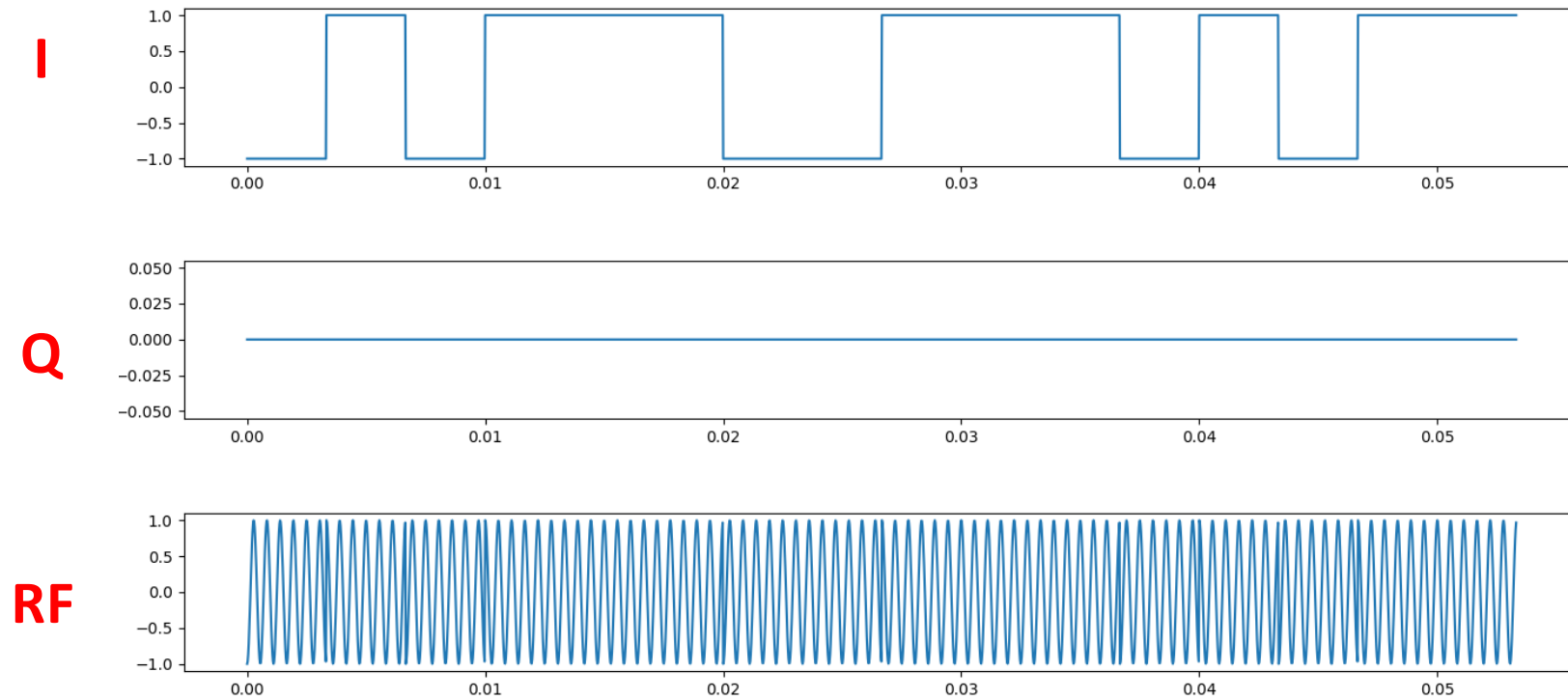
I

```
bpsk = Mbpsk.real*np.cos(2*np.pi*f0*t_bpsk) - Mbpsk.imag*np.sin(2*np.pi*f0*t_bpsk)
```

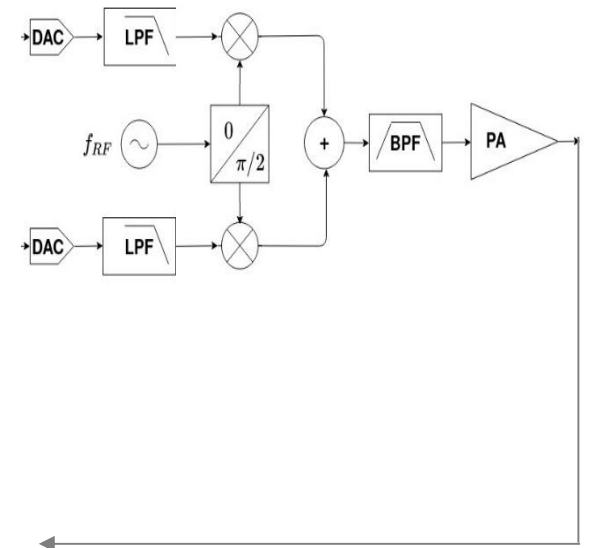
Simulate quadrature modulator

# BPSK with square pulses

```
bits = np.array([0,1,0,1,1,1,0,0,1,1,1,0,1,0,1,1])
```



*time (s)*



# QPSK with square pulses

```
bits = np.array([0,1,0,1,1,1,0,0,1,1,1,0,1,0,1,1])
```

Input bits two by two

```
symbols_qpsk = np.array([BitArray(i).uint for i in bits.reshape(-1,2)])
```

```
qpsk = np.sqrt(2)*np.array((-1-1j, -1+1j, +1-1j, +1+1j))/2
```

```
Mqpsk = np.repeat(qpsk[symbols_qpsk], Ns)
```

Baseband IQ  
samples

Find symbol in  
constellation

Repeat for the  
entire duration of  
the symbol

Constellation

Q

I

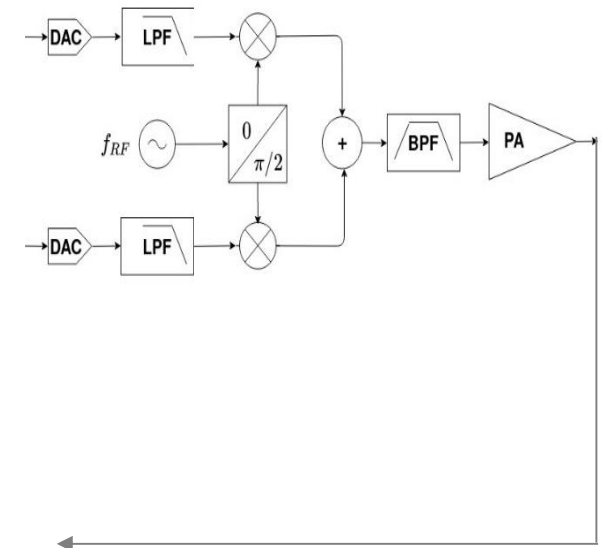
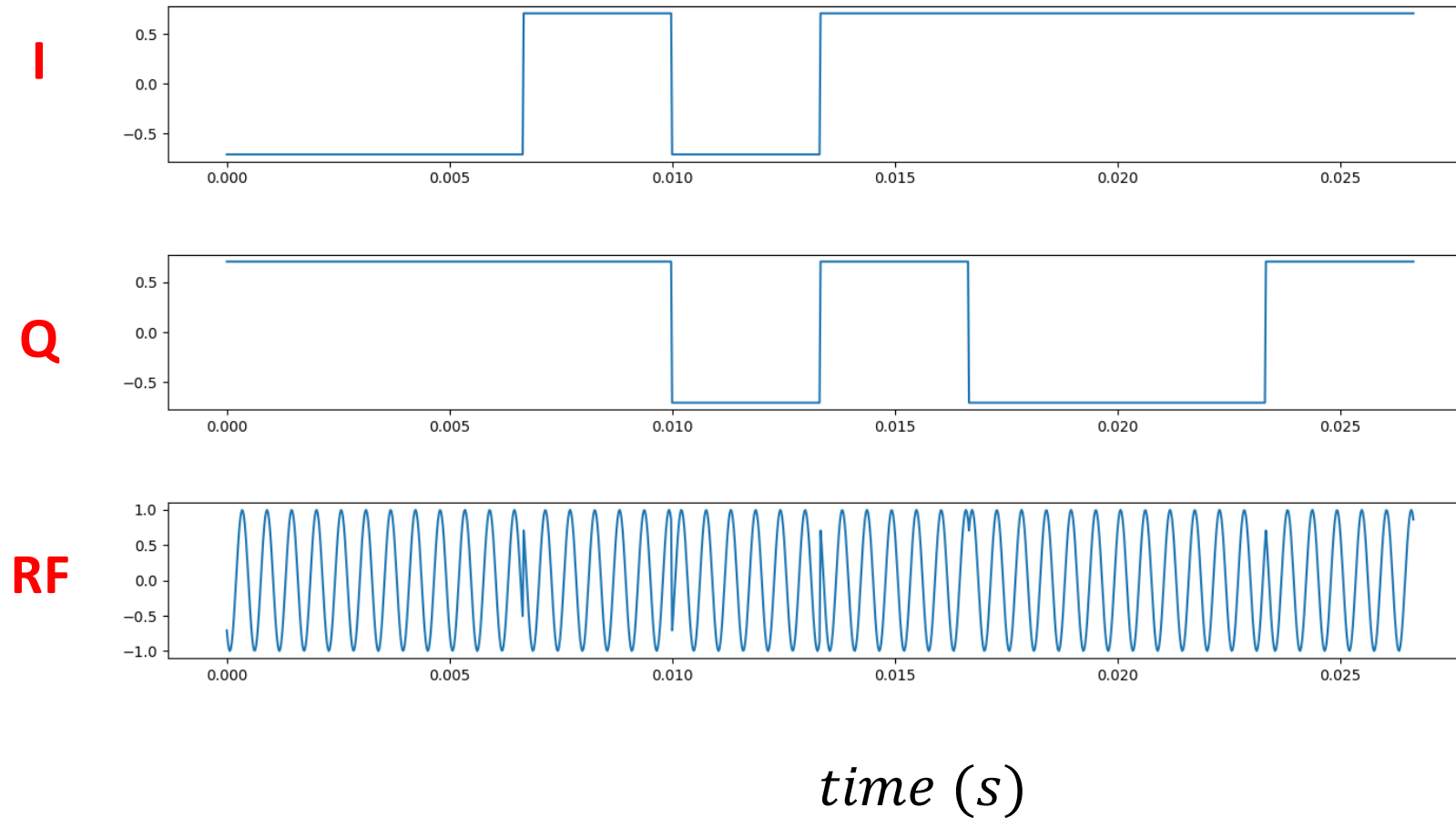
```
qpsk = Mqpsk.real*np.cos(2*np.pi*f0*t_qpsk) - Mqpsk.imag*np.sin(2*np.pi*f0*t_qpsk)
```

Simulate quadrature modulator



# QPSK with square pulses

```
bits = np.array([0,1,0,1,1,1,0,0,1,1,1,0,1,0,1,1])
```



# QAM16 with square pulses

```
bits = np.array([0,1,0,1,1,1,0,0,1,1,1,0,1,0,1,1])
symbols_qam16 = np.array([BitArray(i).uint for i in bits.reshape(-1,4)])
qam16 = np.sqrt(2)*np.array((-3-3j, -3-1j, -3+3j, -3+1j, -1-3j, -1-1j, -1+3j, -1+1j,
                             +3-3j, +3-1j, +3+3j, +3+1j, +1-3j, +1-1j, +1+3j, +1+1j))/4
Mqam16 = np.repeat(qam16[symbols_qam16], Ns)
```

Input bits four by four

Baseband IQ  
samples

Find symbol in  
constellation

Repeat for the  
entire duration of  
the symbol

Constellation

Q

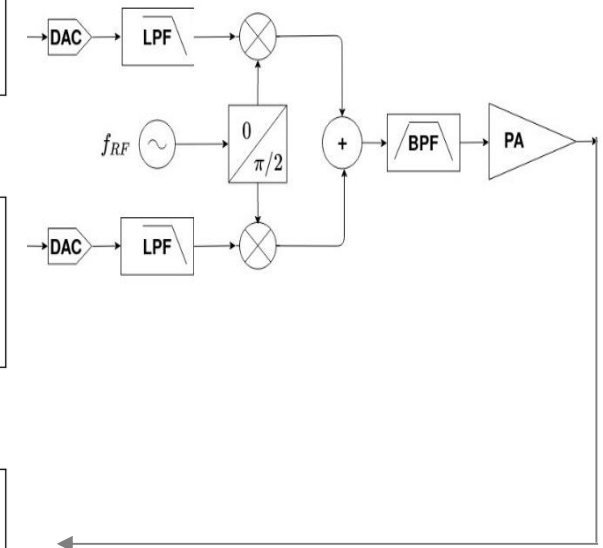
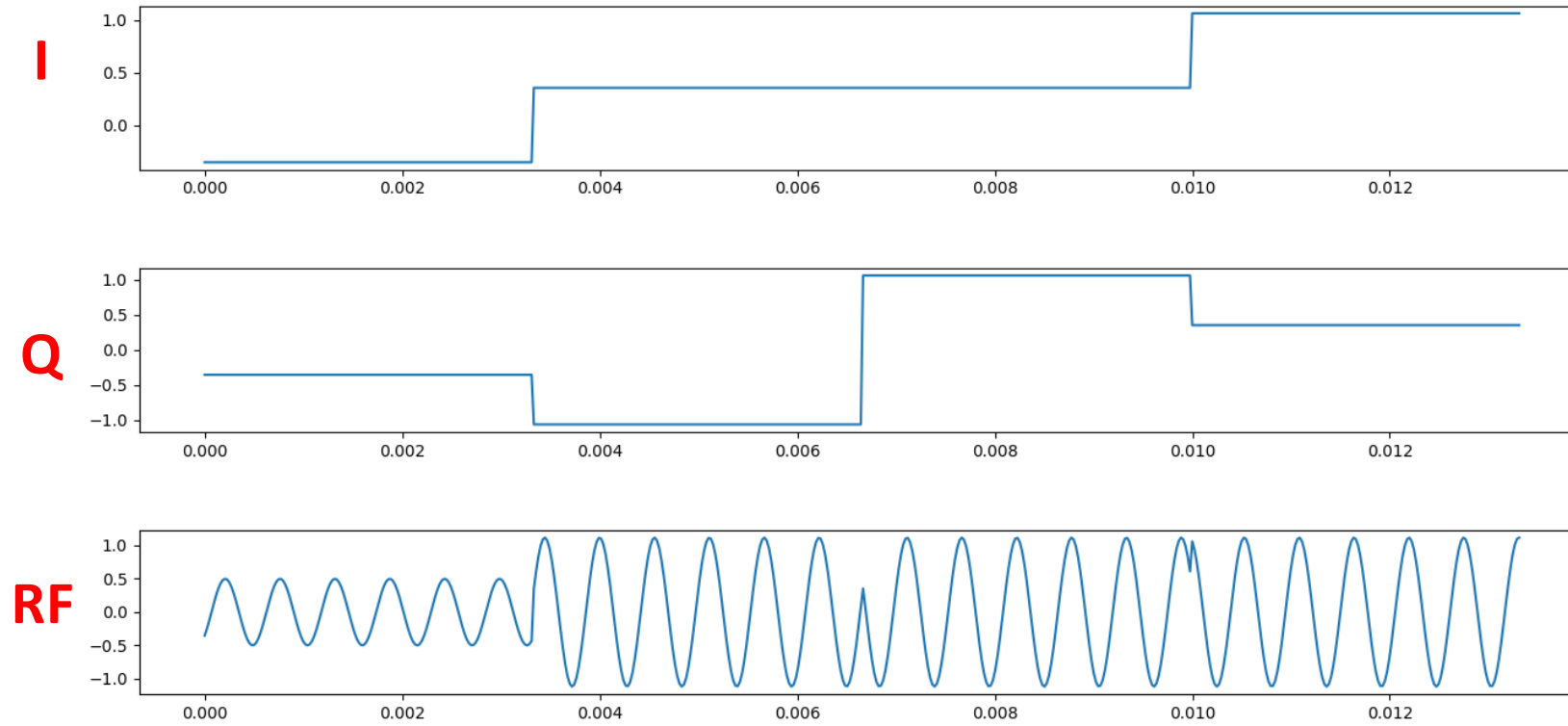
I

```
qam16 = Mqam16.real*np.cos(2*np.pi*f0*t_qam16) - Mqam16.imag*np.sin(2*np.pi*f0*t_qam16)
```

Simulate quadrature modulator

# QAM16 with square pulses

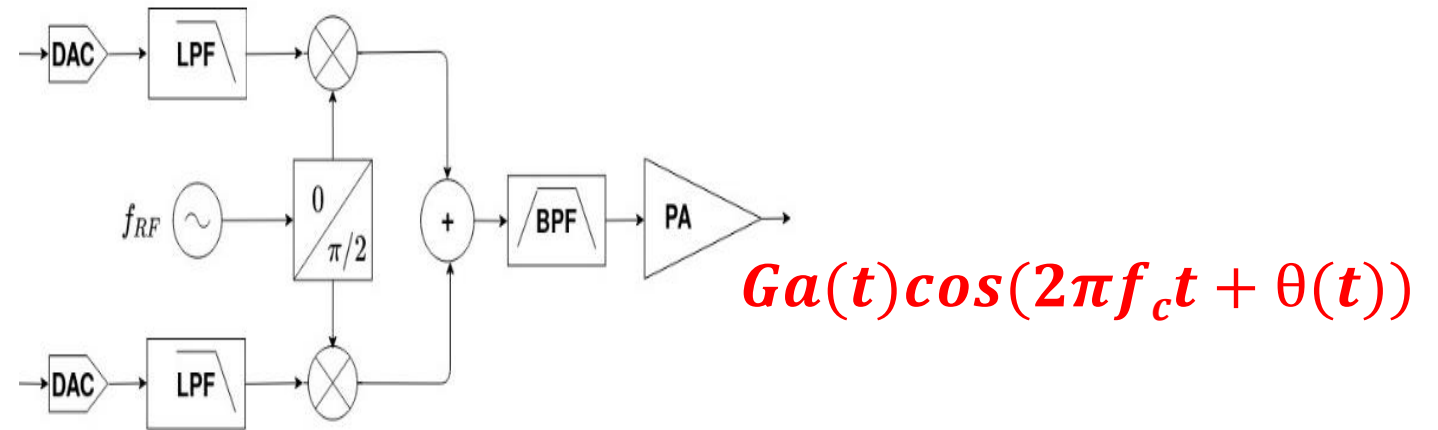
```
bits = np.array([0,1,0,1,1,1,0,0,1,1,1,0,1,0,1,1])
```



# More in general, a generic up-convter

$$I(nT_s) = a(nT_s) \cos(\Phi(nT_s))$$

$$Q(nT_s) = a(nT_s) \sin(\Phi(nT_s))$$



- By properly choosing I and Q we can apply any analog/digital amplitude/frequency/phase modulation to the carrier
- In any case, I and Q can be generated in the digital domain (hardware or software) and then converted into physical signals with a (multi-bit) DAC
- The PSK/QAM examples seen before are a specific case of phase or phase+amplitude modulation

# Some references

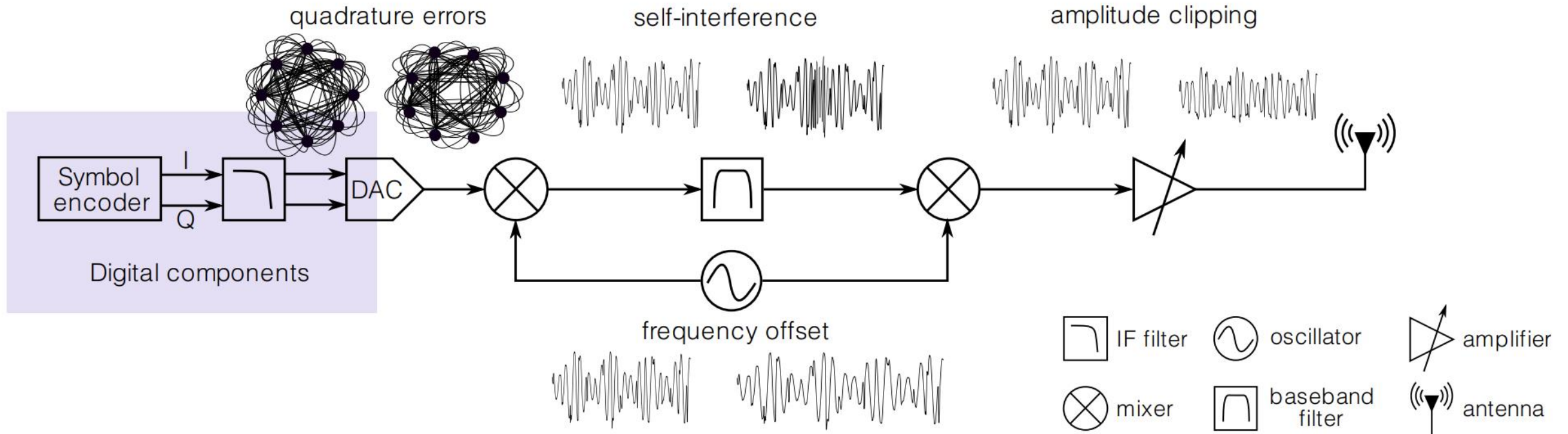
Check the full script plus look at the following links for more examples including other modulations

<https://inst.eecs.berkeley.edu/~ee123/sp15/lab/lab6/Pre-Lab6-Intro-to-Digital-Communications.html>

[https://pysdr.org/content/digital\\_modulation.html](https://pysdr.org/content/digital_modulation.html)

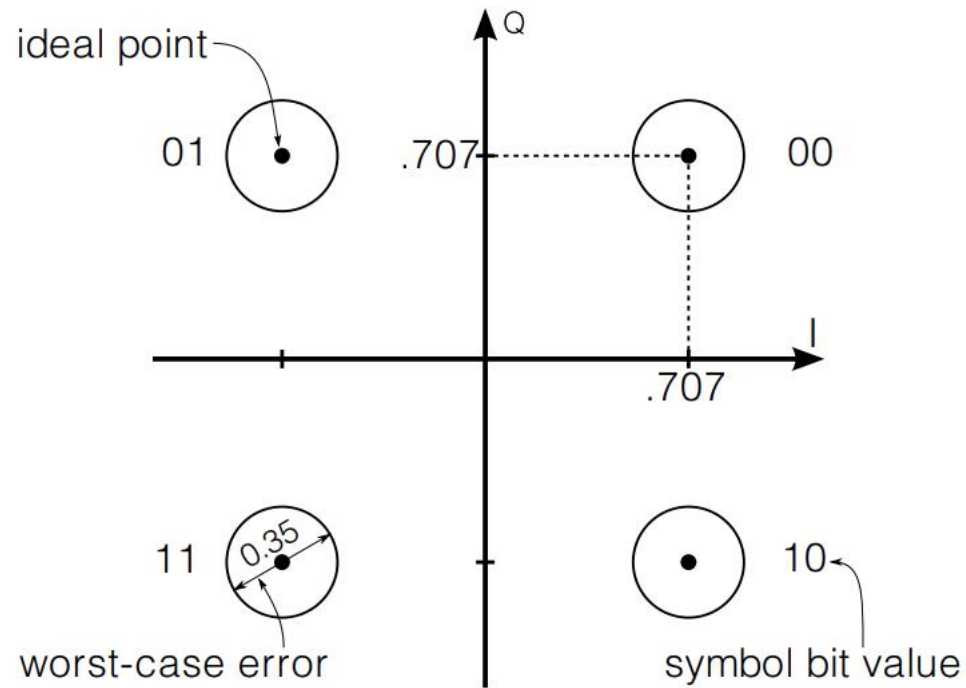
# Security Implications

# Fingerprinting based on Quadrature Errors



**Figure 1: Common transmitter impairments and their sources**

# Fingerprinting based on Quadrature Errors

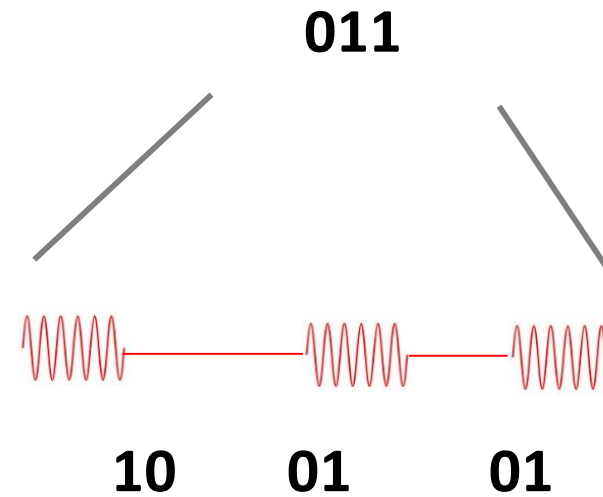


**Figure 4: The 4 symbols of QPSK on I/Q plane**



Some more considerations

# Sending data in practice

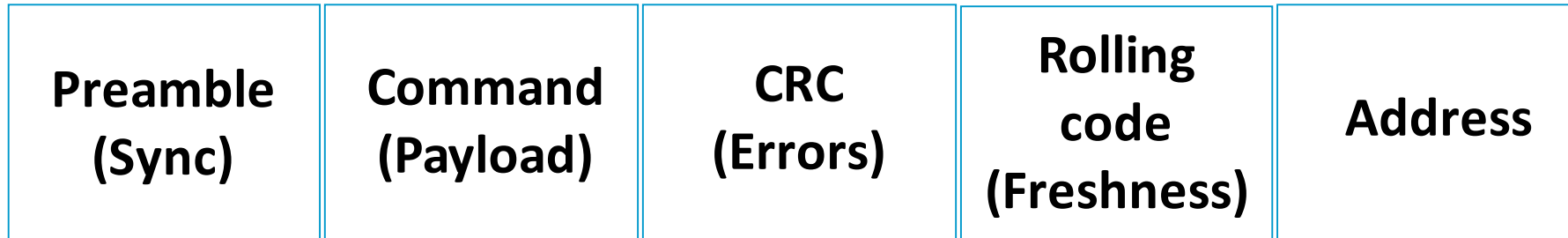


E.g., On-Off Keying (OOK)  
and Manchester Encoding

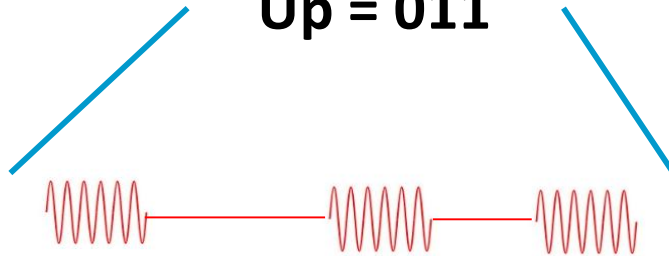
# Sending data in practice

Upper layers  
(link, network, app, ...)

Example of simple packet (a real remote, simplified)



Up = 011



10

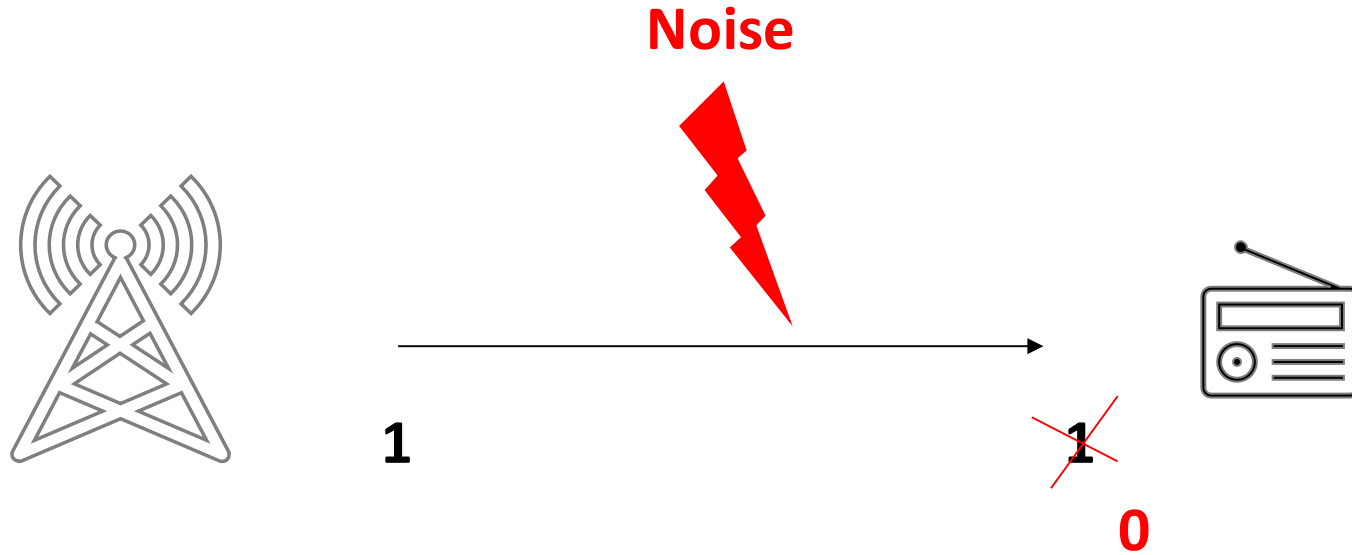
01

01

On-Off Keying (OOK)  
+ Manchester encoding

Physical  
layer

# Dealing with a noise (+ *channel* – *not shown*)

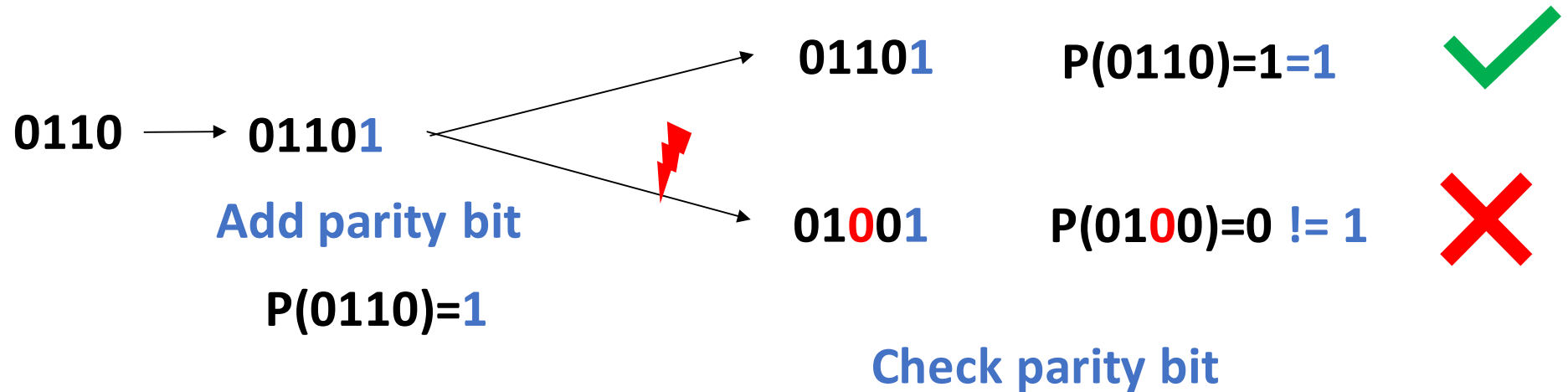


**We need to deal with noise**

Bit errors happen

How to correct errors?

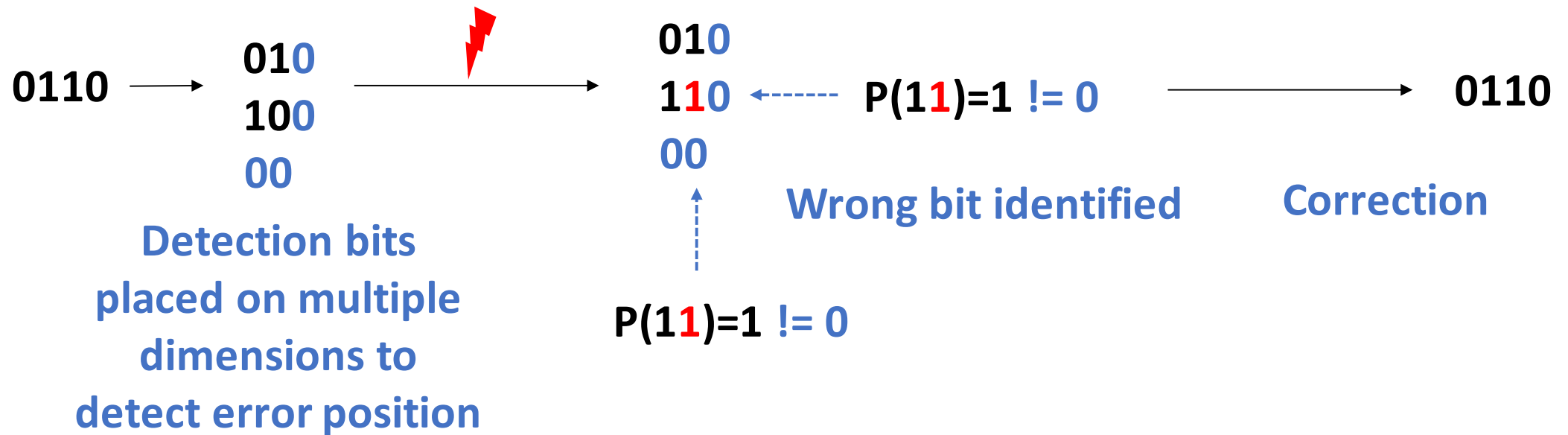
# Error detection and correction (intuition only)



## Error Detection

(Add redundant bits for checking errors)

# Error detection and correction (intuition only)



## Error Detection & Correction

(Add redundant bits to detect errors and their position)

# Interleaving (intuition only)

Adviser expects TEMPEST becomes quickly serious problem

Interleaving  "Shuffle in time"

AxMokum eEccoer Teilles burbstT qeoicSs srveEey pdpPmls

# References

“A Foundation in Digital Communication,” accessed May 11, 2021,  
[https://www.afidc.ethz.ch/A\\_Foundation\\_in\\_Digital\\_Communication/Home.html](https://www.afidc.ethz.ch/A_Foundation_in_Digital_Communication/Home.html).

Arya Behzad, Wireless LAN Radios: System Definition to Transistor Design (IEEE Press Series on Microelectronic Systems) (Hoboken, NJ, USA: John Wiley & Sons, Inc., 2008).



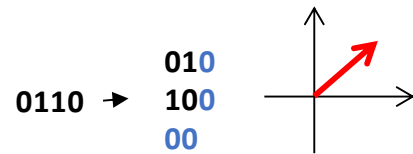
# Quick recap of this part

- Transmitting information with radio waves:
  - EM waves at radio frequency propagate from transmitter to receiver
    - Currents in antennas generate EM signals (TX)
    - EM signals propagate (Propagation)
    - EM signals generate currents in antennas (RX)
  - The waves are modulated to transmit information
    - Analytical signals are a convenient representation
    - AM/FM/PM modulation
    - Baseband vs. passband (Up/Down-conversion)
  - Transmission in practice
    - Electronic circuits in a typical transmitter (receiver is symmetrical)
    - Encoding, modulation, packets, upper protocol layers
    - Dealing with noise and bit errors:
      - Detection, detection and correction, interleaving

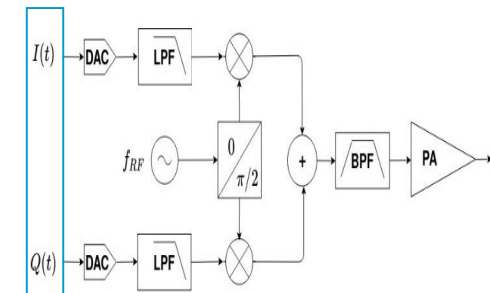
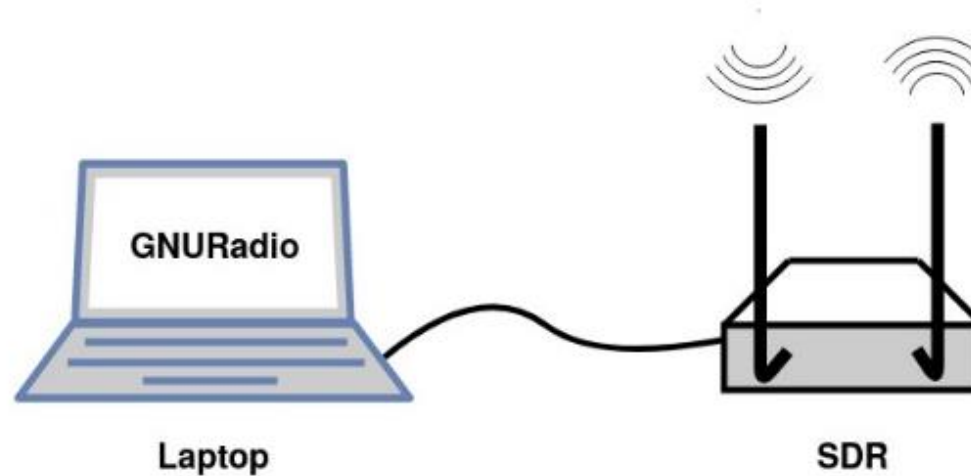
# Software Defined Radios (SDR)

## (A quick introduction)

# Software Defined Radio (SDR)



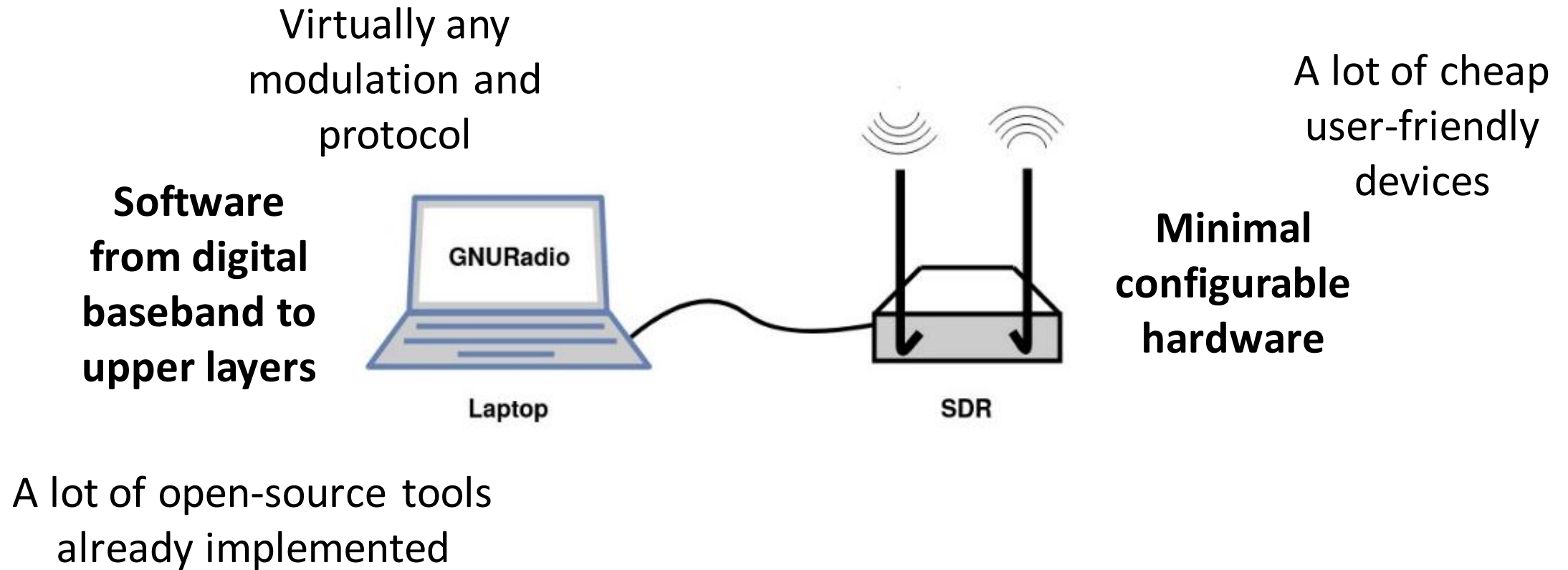
Adviser expects TEMPEST becomes quickly serious problem  
Interleaving  
AsMokum eEccoeT Teilles burbaT qeicSs arveEry pdpPnls  
Noisy channel  
Burst error (cannot be corrected with FEC)  
AsMokum eEccoeT Teilles burbaT qeicSs arveEry pdpPnls  
XXXXXXXX  
Deinterleaving  
Adviser expects TEMPEST becomes quickly serious problem  
Error spread over multiple words (can be corrected with FEC)



“Radio in which some or all of the **physical layer functions** are software-defined”

Software Defined Radio Forum, “SDRF Cognitive Radio Definitions Working Document SDRF-06-R-0011-V1.0.0”, 2007, [http://www.sdrforum.org/pages/documentLibrary/documents/SDRF-06-R-0011-V1\\_0\\_0.pdf](http://www.sdrforum.org/pages/documentLibrary/documents/SDRF-06-R-0011-V1_0_0.pdf).

# Software Defined Radio (SDR)



# SDR hardware examples

**Warning:**  
There is more! This is just an  
example, no advertisement!



## RTL-SDR

<https://www.rtl-sdr.com/>

Entry level, simple, only RX, cheap 20 euros



## HackRF

<https://greatscottgadgets.com/hackrf/>

RX/TX, higher bandwidth and range, more expensive



## USRP B210

<https://www.ettus.com/all-products/ub210-kit/>

RX/TX, dual channel, high quality, expensive

# SDR software examples

**Warning:**  
There are so many  
more! And you can  
write your own

<https://gqrx.dk/>  
<https://cubicsdr.com/>

Simple AM/FM/...

<https://www.gnuradio.org/>  
<https://github.com/bastibl/gr-ieee802-11>  
[https://github.com/tapparelj/gr-lora\\_sdr](https://github.com/tapparelj/gr-lora_sdr)  
gr-\* many more projects

Generic framework

A lot of projects

<https://github.com/osqzss/gps-sdr-sim>  
<https://gnss-sdr.org/>

GPS spoofing and GNSS Rx

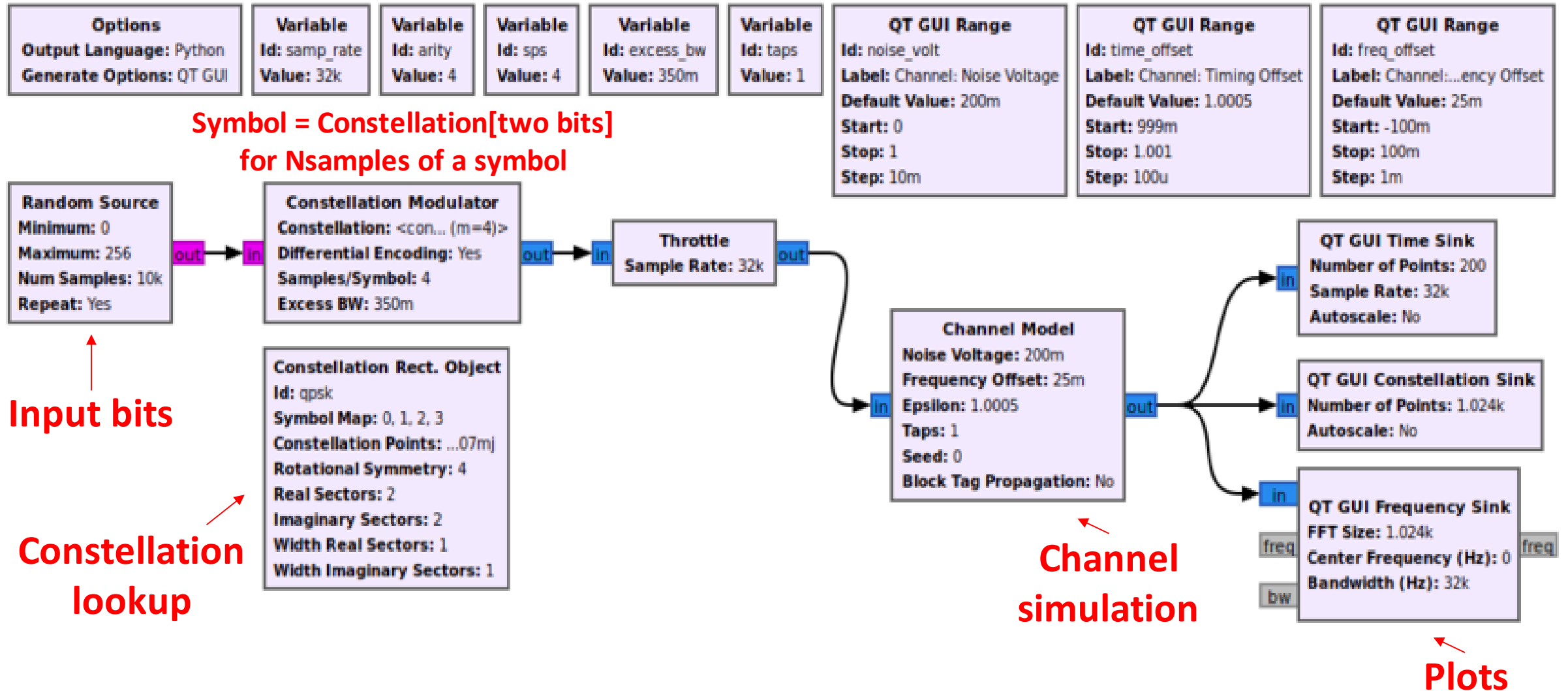
<https://fr.wikipedia.org/wiki/FIDigi>  
<https://physics.princeton.edu/pulsar/K1JT/wsjsx.html>

Ham radio (Amateur)

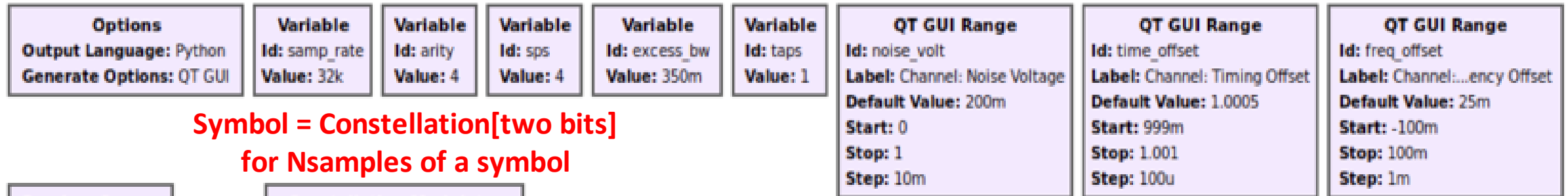
<https://github.com/jopohl/urh>  
<https://batchdrake.github.io/SigDigger/>

Reverse engineering  
radio protocols

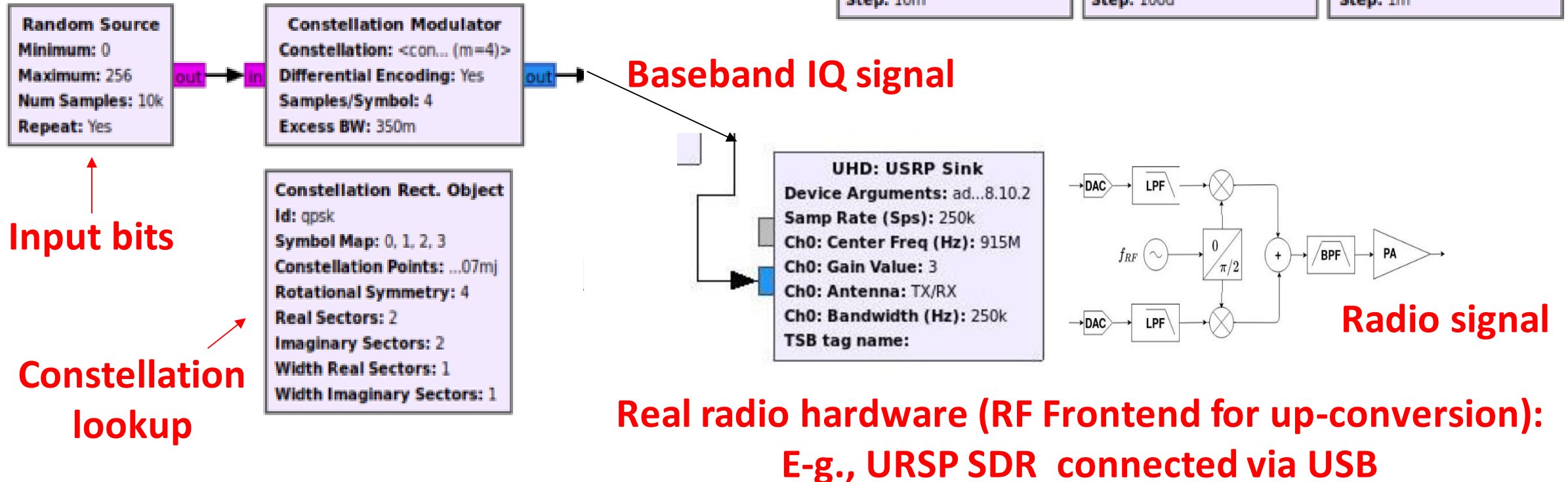
# An example: QPSK simulation



# An example: QPSK transmission

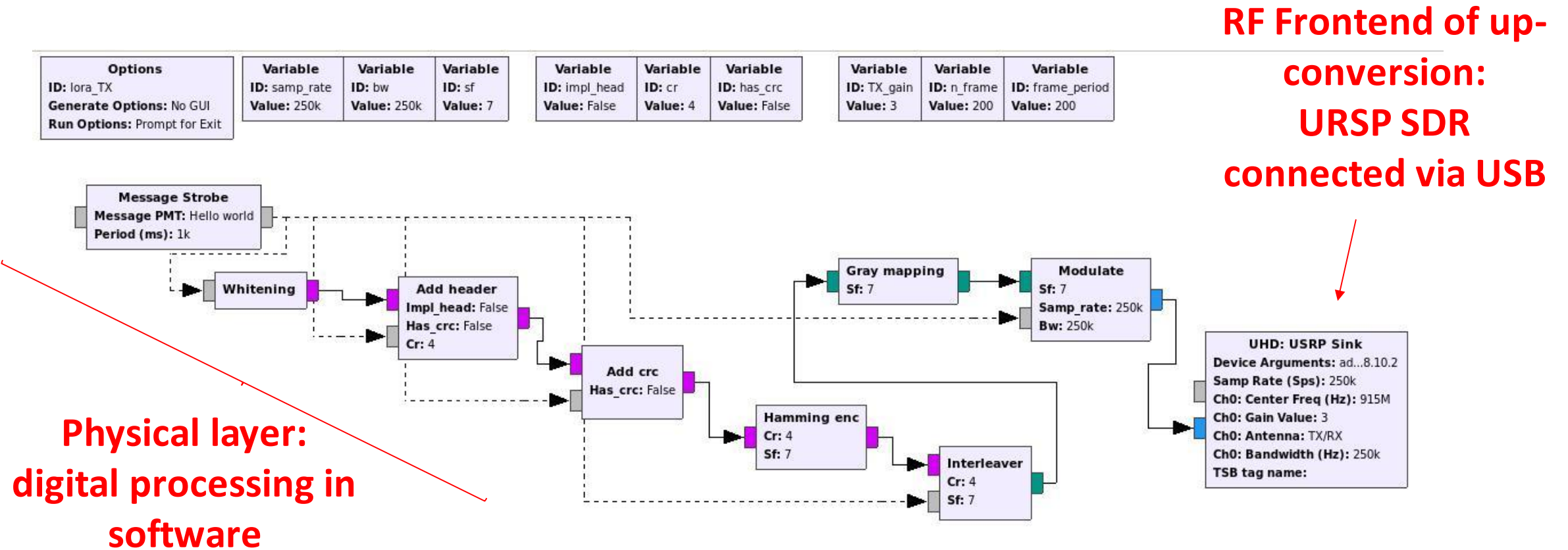


**Symbol = Constellation[two bits]  
for Nsamples of a symbol**





# An example: LoRa



J. Tapparel, O. Afisiadis, P. Mayoraz, A. Balatsoukas-Stimming, and A. Burg, "An Open-Source LoRa Physical Layer Prototype on GNU Radio"

# References

Software Defined Radio Forum, “SDRF Cognitive Radio Definitions Working Document SDRF-06-R-0011-V1.0.0”, 2007,  
[http://www.sdrforum.org/pages/documentLibrary/documents/SDRF-06-R-0011-V1\\_0\\_0.pdf](http://www.sdrforum.org/pages/documentLibrary/documents/SDRF-06-R-0011-V1_0_0.pdf).

<https://www.gnuradio.org/>

<https://wiki.gnuradio.org/index.php/Tutorials>

**“Homework”:**

- 1. Familiarize with GNURadio**
  - 2. Start studying the tutorials**
- It will be useful for the lab!**

# Important to Know

- Analytical Signal Representation vs Real Signal
- Frequency Representation: Baseband vs Passband
- Operation of the Quadrature Modulator
- What is an IQ diagram and How are Modulations Mapped onto it
- Basic Packet Structure and Error Correction

# Next Week:

- Basics of the Wireless Communication Channel
- Physical Layer Based Security

Questions?