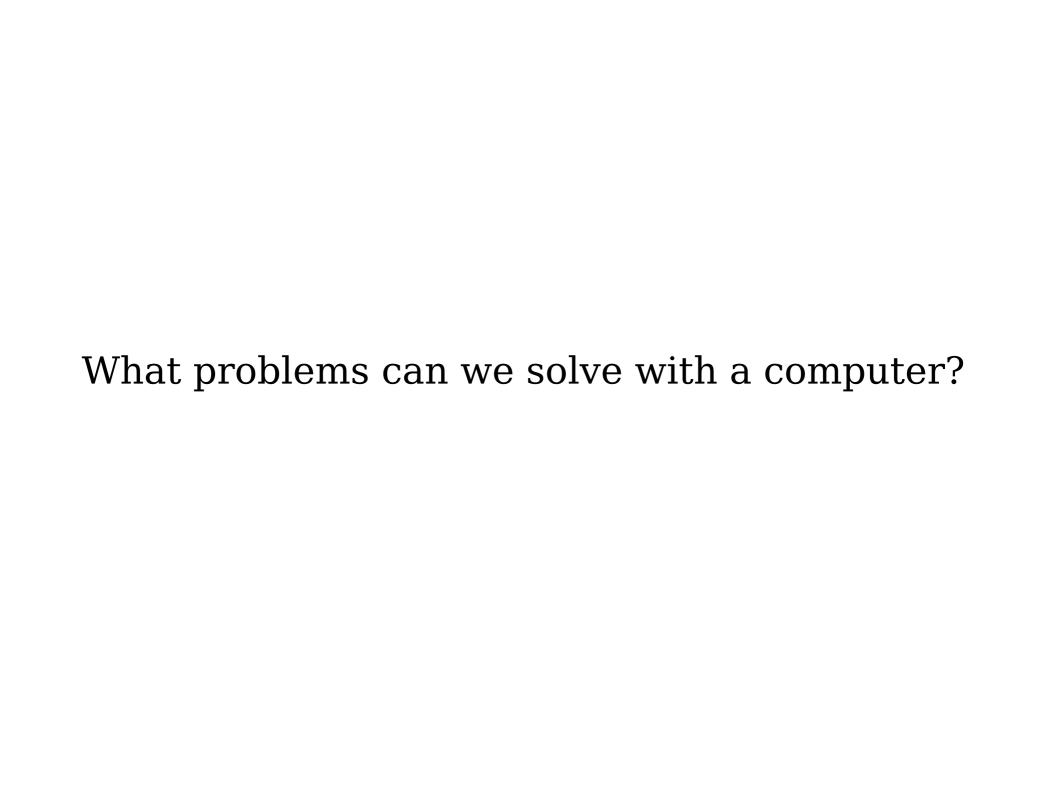
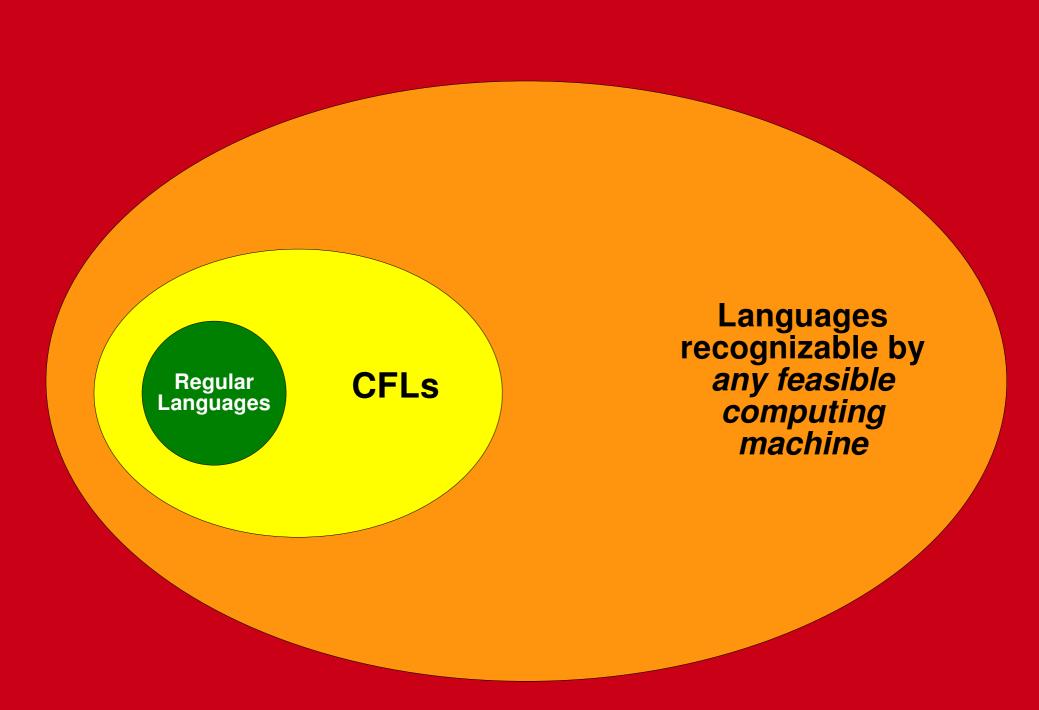
Turing Machines Part One





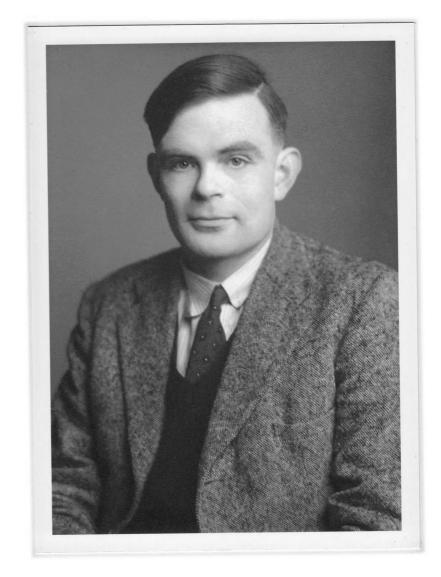
That same drawing, to scale.

The Problem

- Finite automata accept precisely the regular languages.
- We may need unbounded memory to recognize context-free languages.
 - e.g. { $\mathbf{a}^n \mathbf{b}^n \mid n \in \mathbb{N}$ } requires unbounded counting.
- How do we model a computing device that has unbounded memory?

A Brief History Lesson

- In March 1936, Alan Turing (aged 23!) published a paper detailing the *a-machine* (for *automatic machine*), an automaton for computing on real numbers.
- They're now more popularly referred to as *Turing machines* in his honor.
- He also later made contributions to computational biology, artificial intelligence, cryptography, etc. Seriously, Google this guy.



	1	1	1	1 1	1	
2 7 1	8 2	8 1	8 2	8 4	5 9	0
+ 3 1 4	1 5	9 2	6 5	3 5	8 9	7
5	9 8	7 4	4 8	2 0	4 8	7

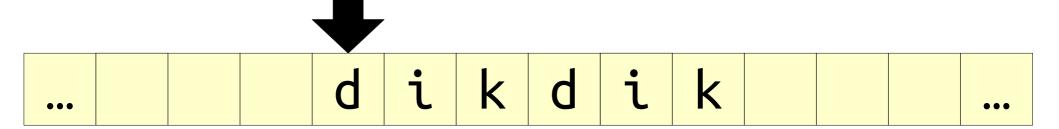
			1		1		1	1	1	1		
2 7	1	8	2	8	1	8	2	8	4	5	9	0
+ 3 1	4	1	5	9	2	6	5	3	5	8	9	7
8	5	9	8	7	4	4	8	2	0	4	8	7

					1		1		1	1	1	1		
	2	7	1	8	2	8	1	8	2	8	4	5	9	0
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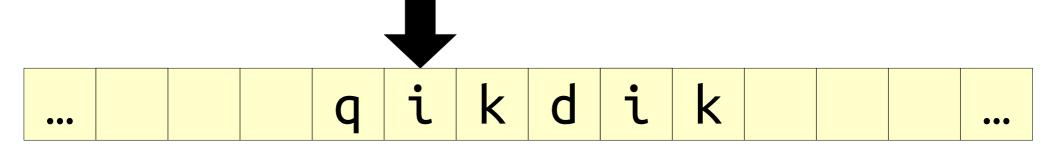
					1		1		1	1	1	1		
	2	7	1	8	2	8	1	8	2	8	4	5	9	0
<u>+</u>	3	1	4	1	5	9	2	6	5	3	5	8	9	7
	5	8	5	9	8	7	4	4	8	2	0	4	8	7

Key Idea: Even if you need huge amounts of scratch space to perform a calculation, at each point in the calculation you only need access to a small amount of that scratch space.

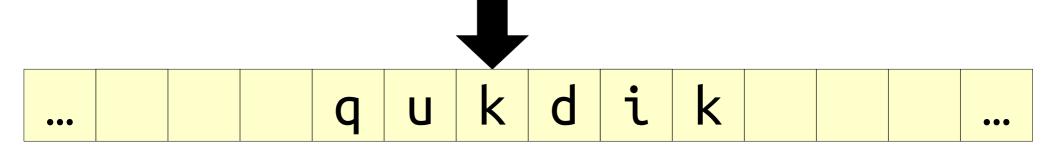
- To provide his machines extra memory, Turing gave his machines access to an *infinite tape* subdivided into a number of *tape cells*.
- A Turing machine can only see one tape cell at a time, the one pointed at by the tape head.
- The Turing machine can
 - read the cell under the tape head,
 - (possibly) change which symbol was written under the tape head, and
 - move its tape head to the left or to the right.



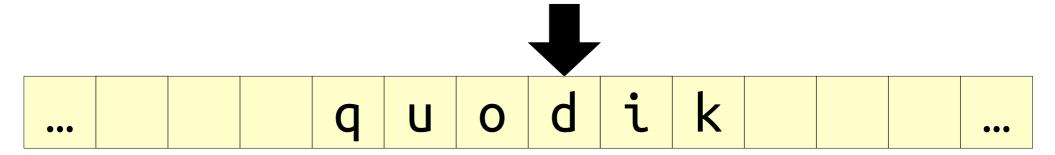
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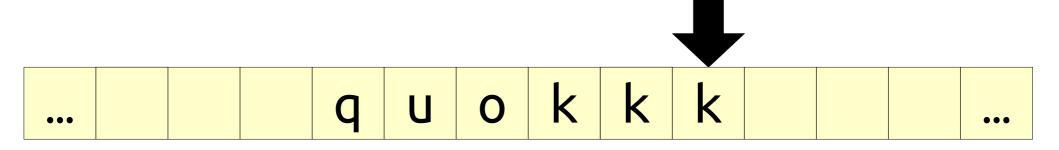
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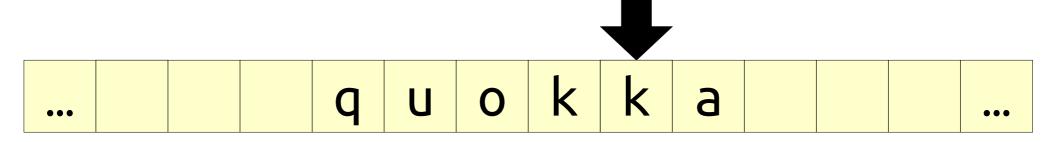
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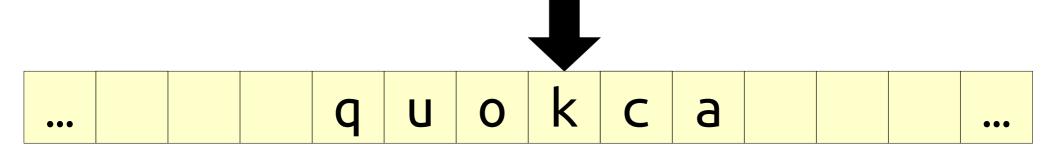
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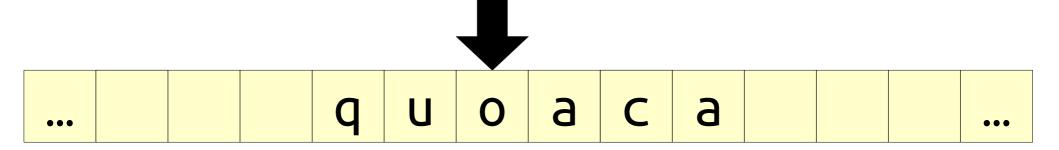
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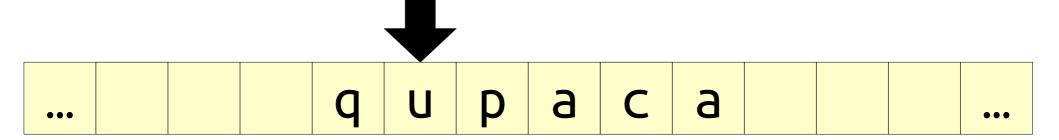
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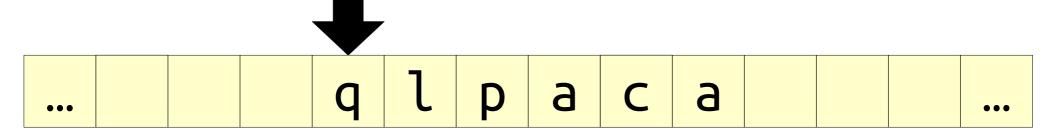
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- Over the years, there have been many simplifications and edits to Turing's original automata.
 - In practice, electronic computers are written in terms of individual instructions rather than states and transitions.
 - Turing's original paper deals with computing individual real numbers; we typically want to compute functions of inputs.
- What we're going to present as "Turing machines" in this class differ significantly from Turing's original description, while retaining the core essential ideas.
 - (Our model is closer to Emil Post's *Formulation 1* and Hao Wang's *Basic Machine B*, for those of you who are curious.)
- If you'd like to learn more about Turing's original version of the Turing machine, come chat with me after class!

- A TM is a series of instructions that control a tape head as it moves across an infinite tape.
- The tape begins with the input string written somewhere, surrounded by infinitely many blank cells.
 - Rule: The input string cannot contain blank cells.
- The tape head begins above the first character of the input. (If the input is ε , the tape head points somewhere on a blank tape.)

```
Start:
  If Blank Return True
  If 'b' Return False
  Write 'x'
  Move Right
  If Not 'b' Return False
  Write 'x'
  Move Right
  Goto Start
```



a b a b a b

- We begin at the Start label.
- Labels indicate different sections of code. The name Start is special and means "begin here."
- Labels have no effect when executed. We just move to the next line.

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 If symbol command

 checks if the character
 under the tape head is
 symbol.
- If so, it executes *command*.
- If not, nothing happens.

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The statement

Write symbol

writes *symbol* to the cell under the tape head.

• The *symbol* can either be Blank or a character in quotes.

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moves the tape head one step in the indicated direction (either Left or Right).

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x x a b a b		•••
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 This program just has a Start label, but most interesting programs have other labels beyond this.

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 A TM stops when executing the

Return result

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- Here, result can be either True or False.
- (If we "fall off" the bottom of the program, the TM acts as though it executes the Return False command.)

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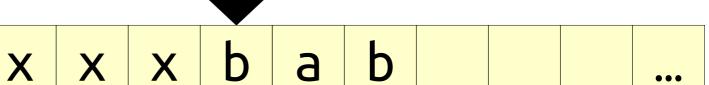
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- Here, result can be either True or False.
- (If we "fall off" the bottom of the program, the TM acts as though it executes the Return False command.)

Start:

If Blank Return True
If 'b' Return False
Write 'x'
Move Right
If Not 'b' Return False
Write 'x'
Move Right
Goto Start



... x x x a b ...

 A TM stops when executing the

Return result

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  Move Right
  Goto Start
```



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- (If we "fall off" the bottom of the program, the TM acts as though it executes the Return False command.)

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  Move Right
  If Not 'b' Return False
  Write 'x'
  Move Right
  Goto Start
```



x x x a b	•••
-----------	-----

 A TM stops when executing the

Return result

- Here, *result* can be either True or False.
- (If we "fall off" the bottom of the program, the TM acts as though it executes the Return False command.)

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Start:
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  Move Right
  If Not 'b' Return False
  Write 'x'
  Move Right
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```



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- (If we "fall off" the bottom of the program, the TM acts as though it executes the Return False command.)

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  If Not 'b' Return False
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  Move Right
  If Not 'b' Return False
  Write 'x'
  Move Right
  Goto Start
```

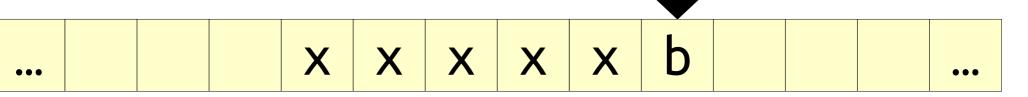


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Start:
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  If 'b' Return False
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  Move Right
  If Not 'b' Return False
  Write 'x'
  Move Right
  Goto Start
```



 A TM stops when executing the

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  If Not 'b' Return False
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  Move Right
  Goto Start
```



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  If Not 'b' Return False
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  Move Right
  Goto Start
```



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  If Not 'b' Return False
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```



 A TM stops when executing the

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 A TM stops when executing the

Return result

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```
Start:
  If Blank Return True
  If 'b' Return False
  Write 'x'
  Move Right
  If Not 'b' Return False
  Write 'x'
  Move Right
  Goto Start
```





 A TM stops when executing the

Return result

- Here, result can be either True or False.
- (If we "fall off" the bottom of the program, the TM acts as though it executes the Return False command.)

```
Start:
  If Blank Return True
  If 'b' Return False
  Write 'x'
  Move Right
  If Not 'b' Return False
  Write 'x'
  Move Right
  Goto Start
```





- This TM initially started up with the string ababab on its tape, so this means that TM returns true on the input ababab, not xxxxxx.
- An intuition for this: we gave this program an input. It therefore returned true with respect to that input, not whatever internal data it generated in making its decision.

```
Start:
  If Blank Return True
  If 'b' Return False
  Write 'x'
  Move Right
  If Not 'b' Return False
  Write 'x'
  Move Right
  Goto Start
```

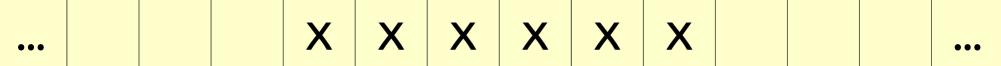




- To summarize, we only have six commands:
 - Move *direction*
 - Write symbol
 - Goto label
 - Return *result*
 - If symbol command
 - If Not symbol command
- Despite their simplicitly,
 TMs are surprisingly
 powerful. The rest of this
 lecture explores why.

Start: If Blank Return True If 'b' Return False Write 'x' Move Right If Not 'b' Return False Write 'x' Move Right Goto Start





Programming Turing Machines

Our First Challenge

The language

```
\{ \mathbf{a}^n \mathbf{b}^n \mid n \in \mathbb{N} \}
```

is a canonical example of a nonregular language. It's not possible to check if a string is in this language given only finite memory.

• Turing machines, however, are powerful enough to do this. Let's see how.

$$L = \{\mathbf{a}^n \mathbf{b}^n \mid n \in \mathbb{N} \}$$
... a a a b b b ...

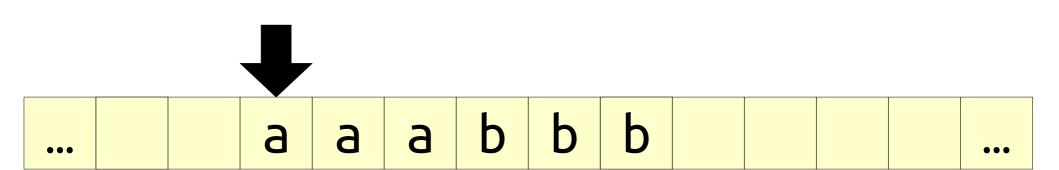
...

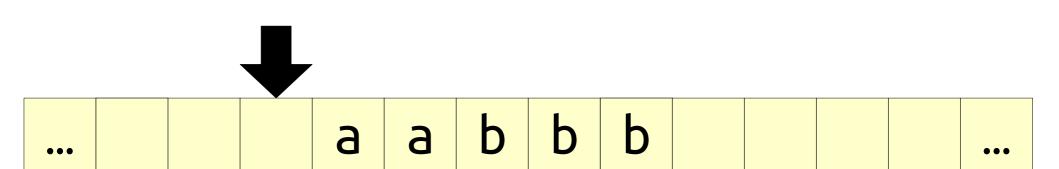
a b a

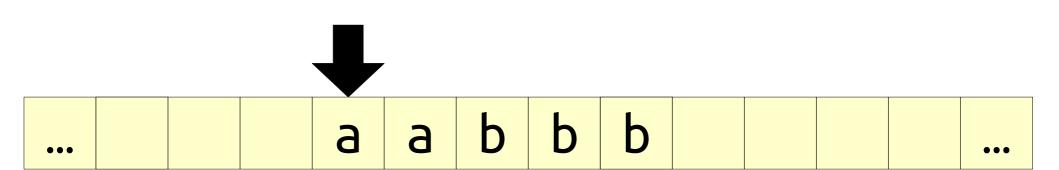
b b a a ...

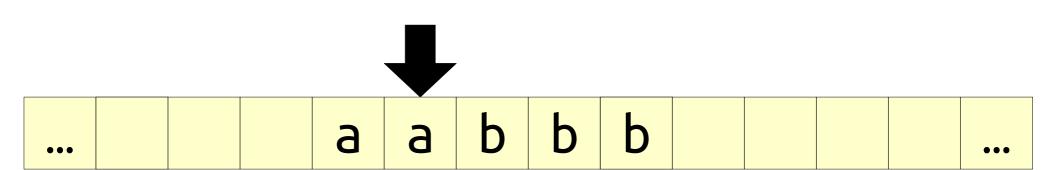
A Recursive Approach

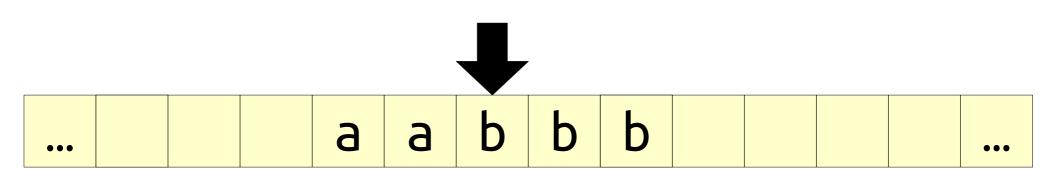
- We can process our string using this recursive approach:
 - The string ε is in L.
 - The string awb is in L if and only if w is in L.
 - Any string starting with **b** is not in *L*.
 - Any string ending with a is not in L.
- All that's left to do now is write a TM that implements this.

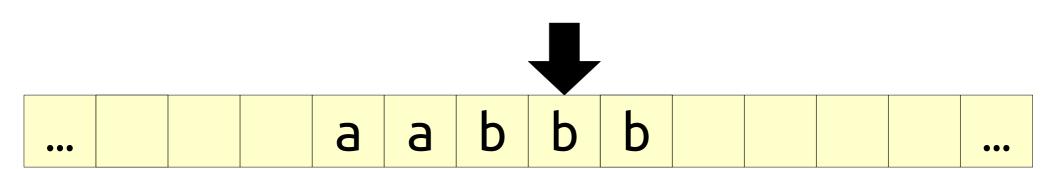


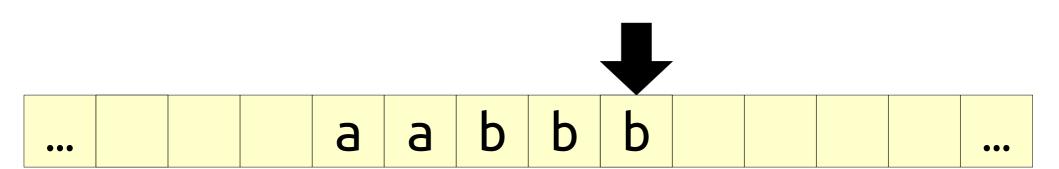


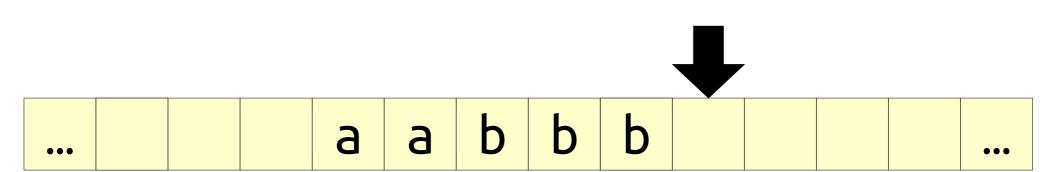


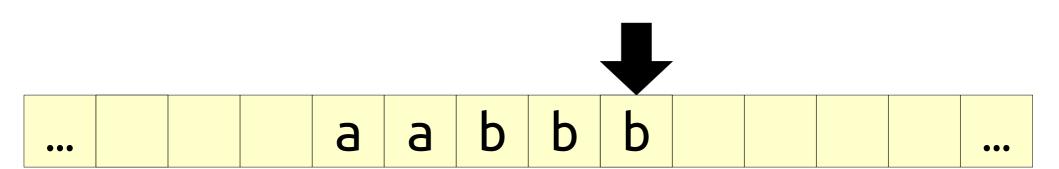


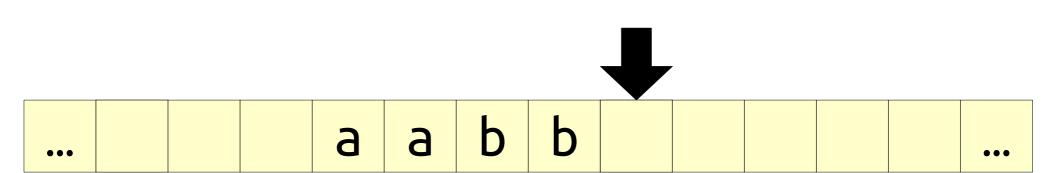


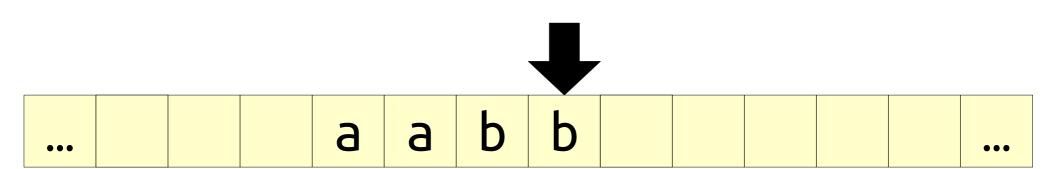


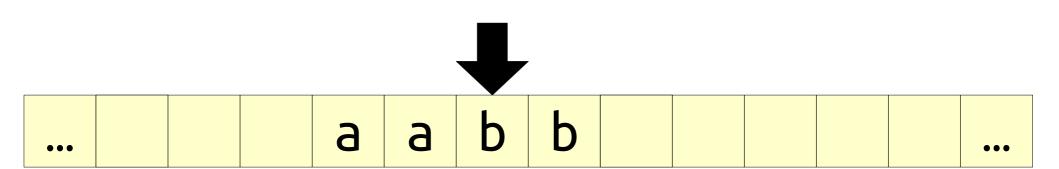


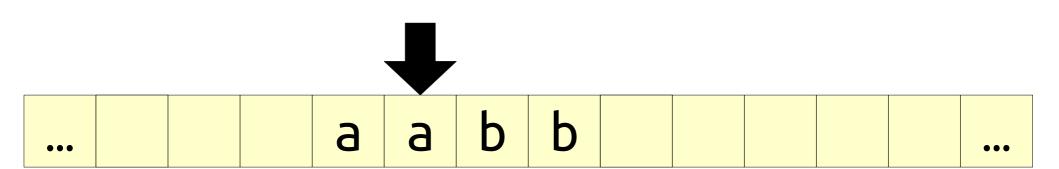


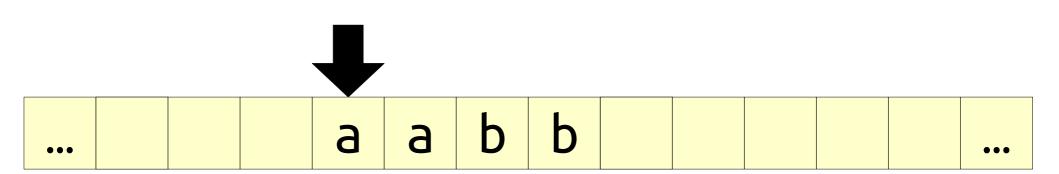


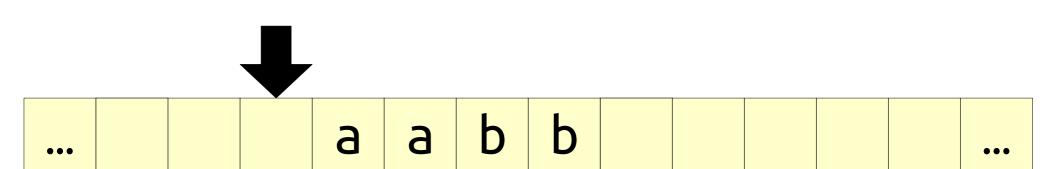


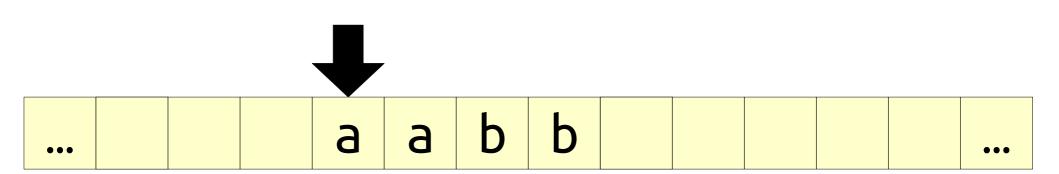


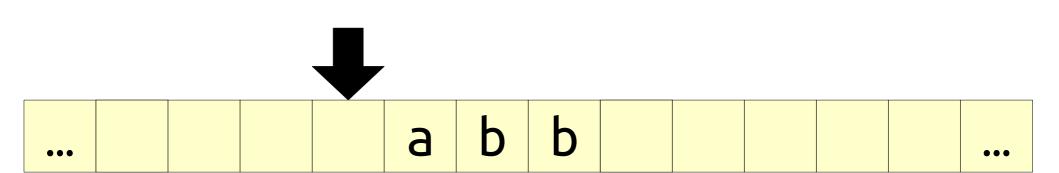


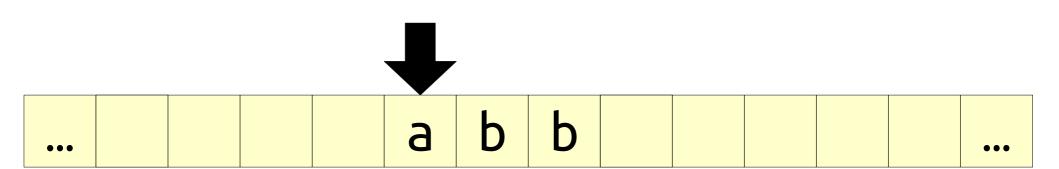


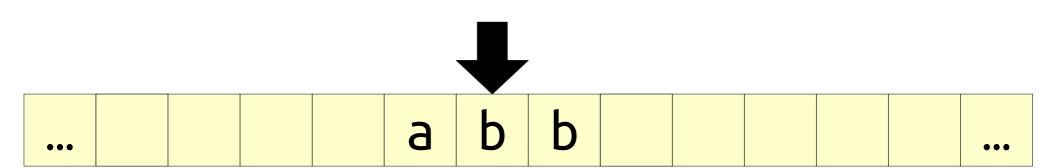


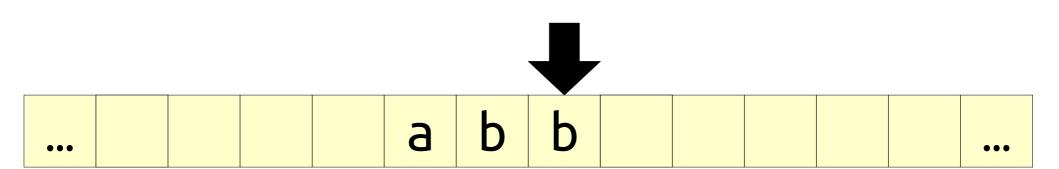


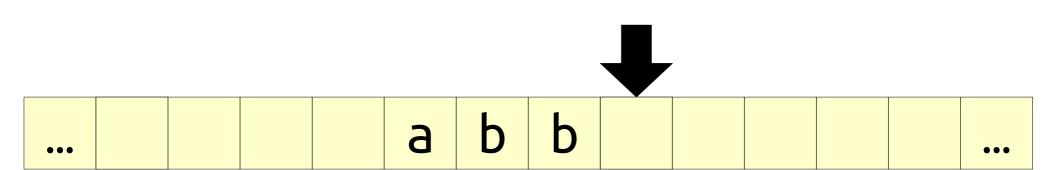


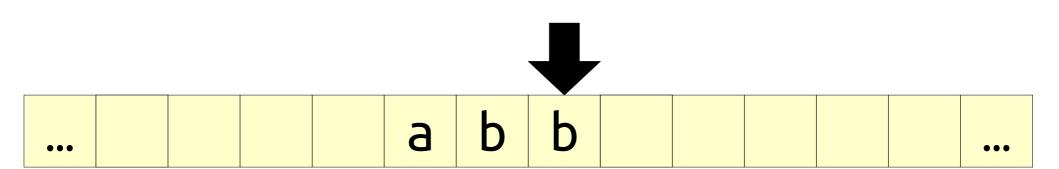


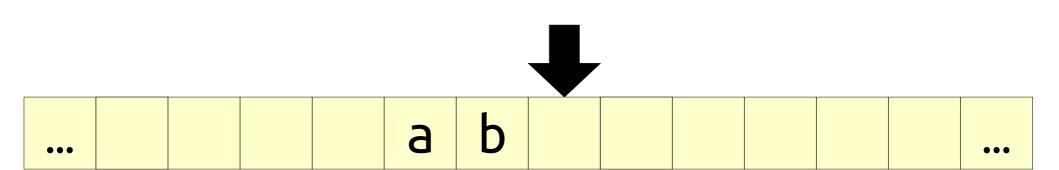


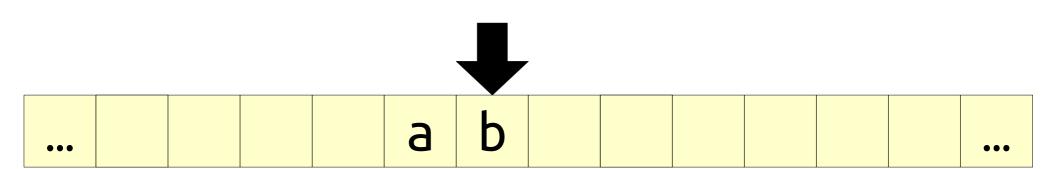


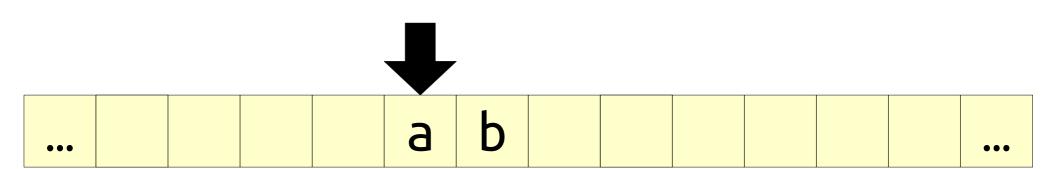


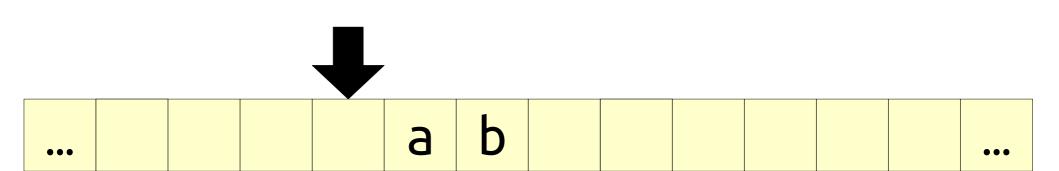


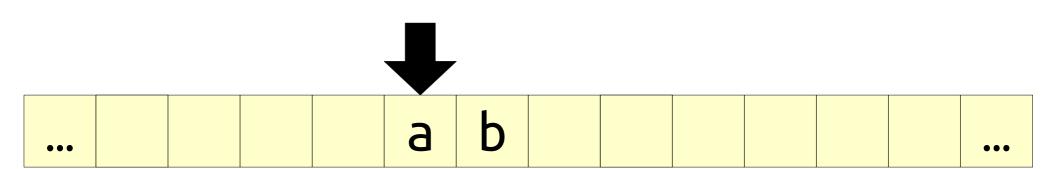


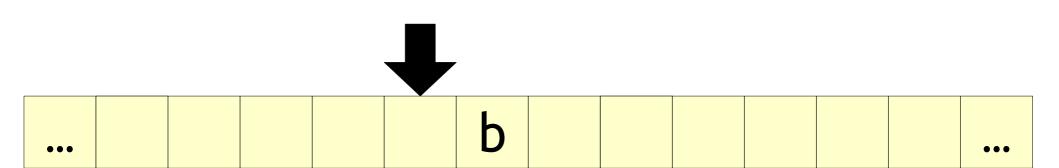


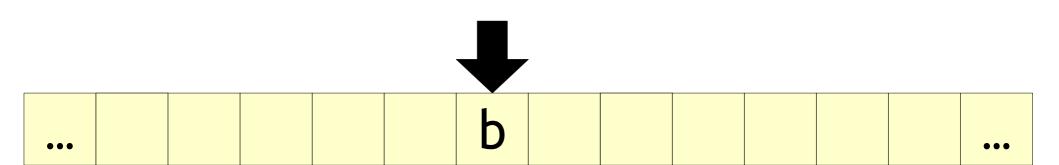


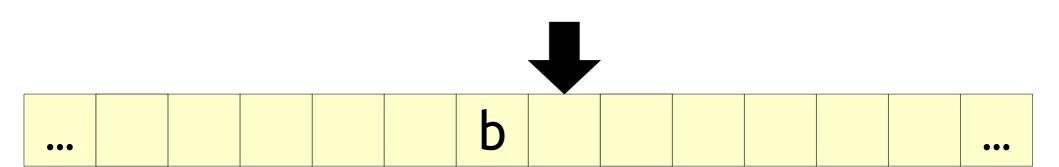


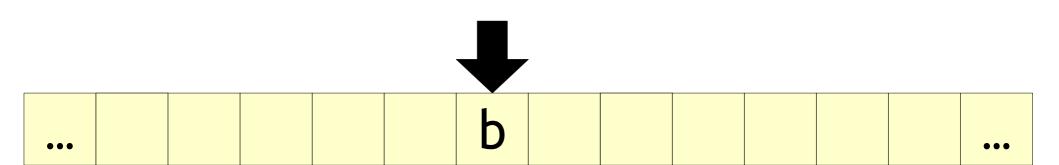


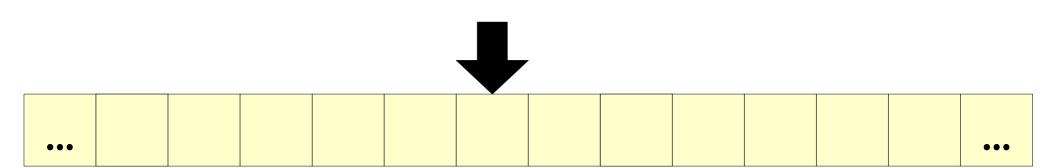


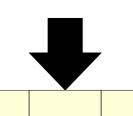




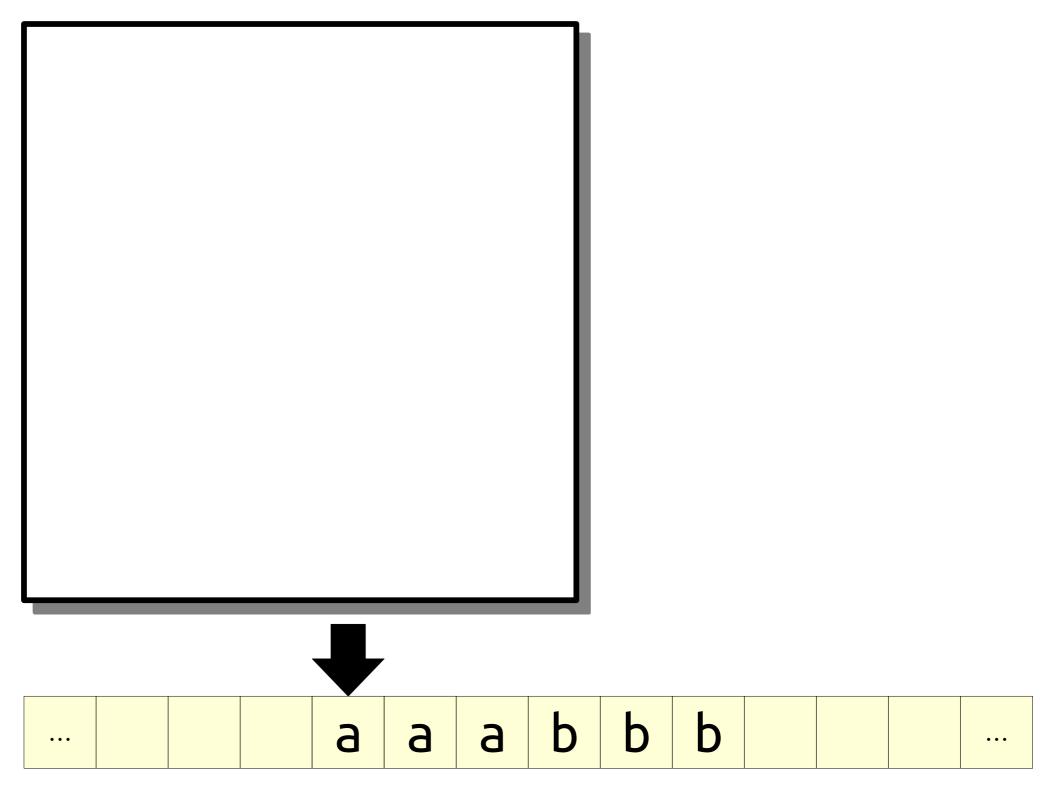


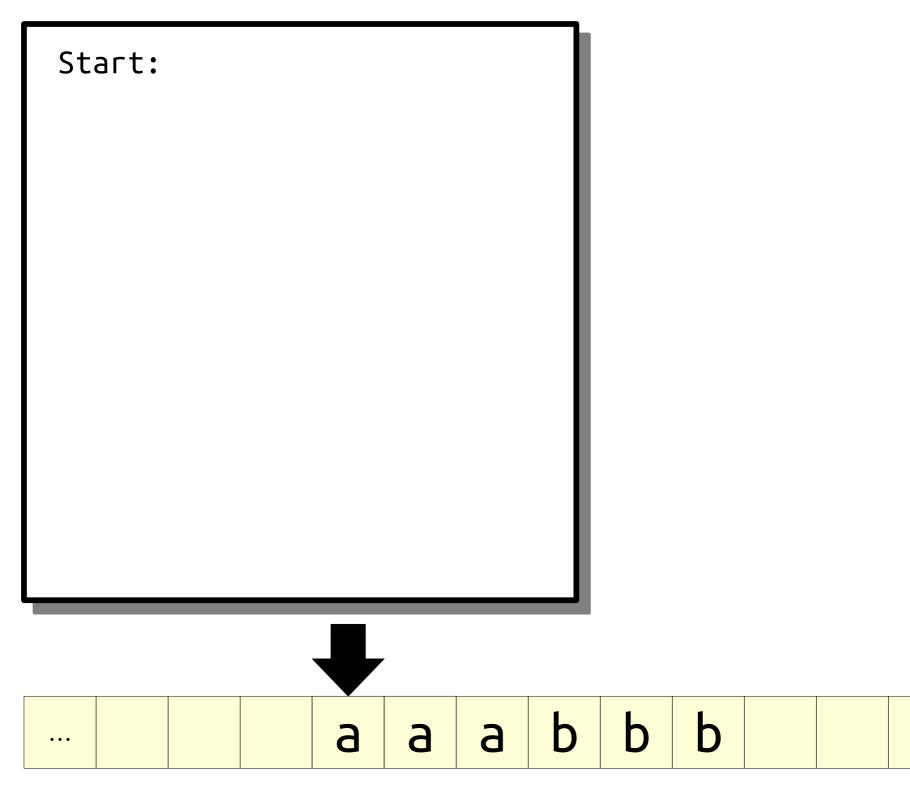


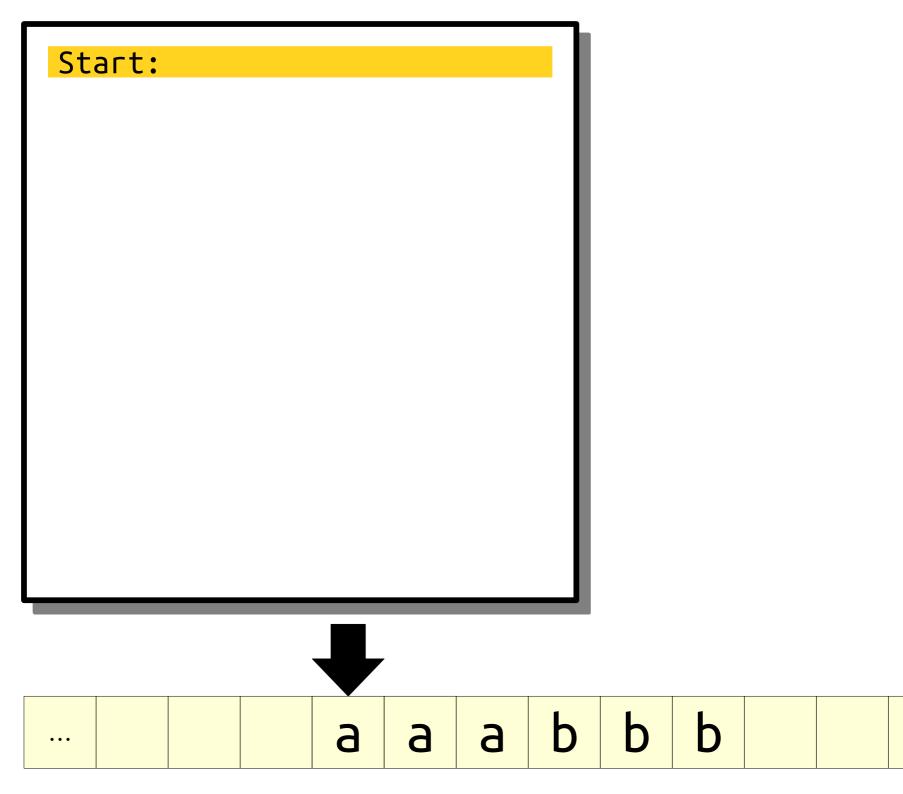


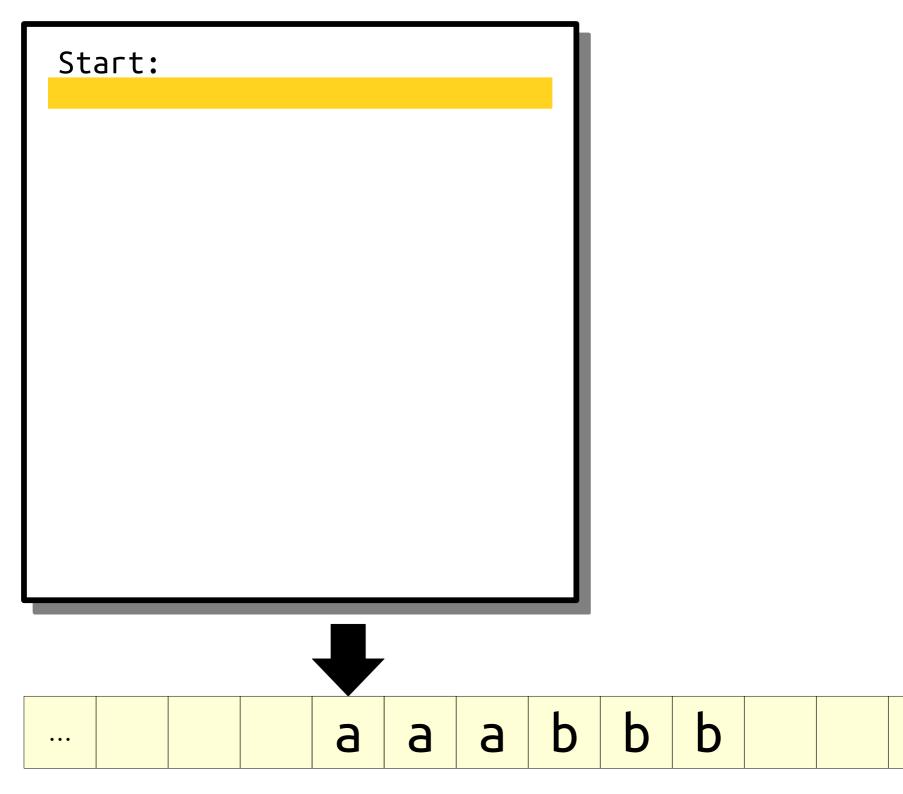


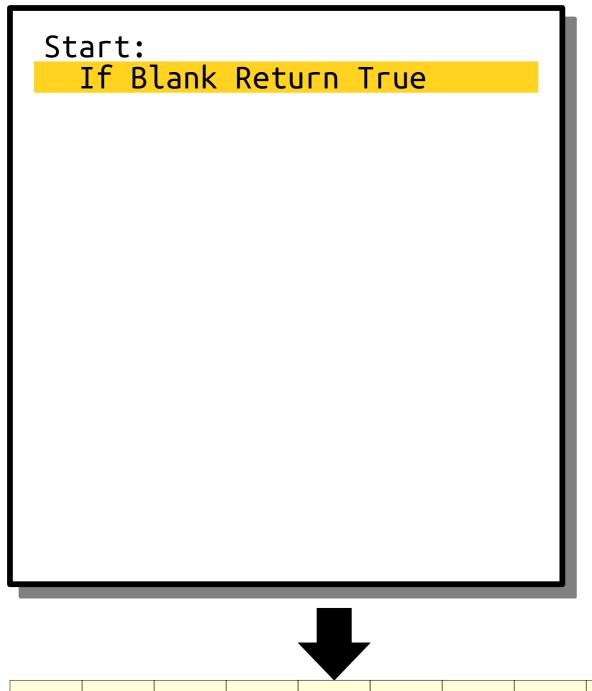
... a a b b b ...



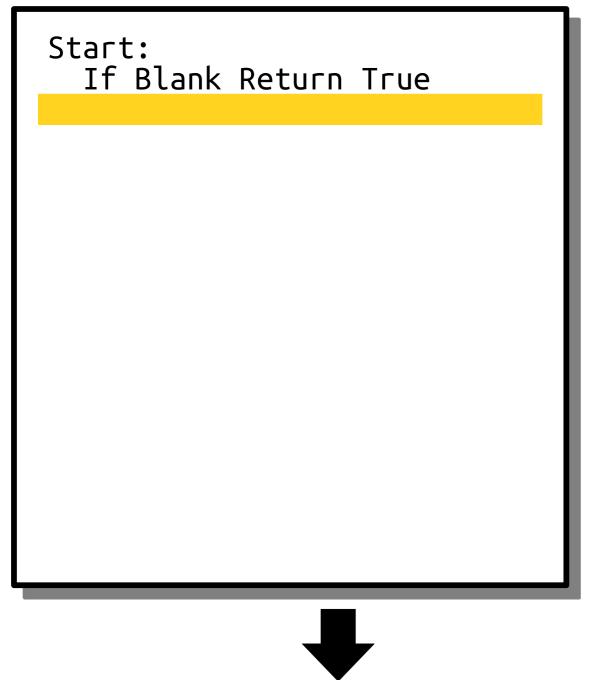




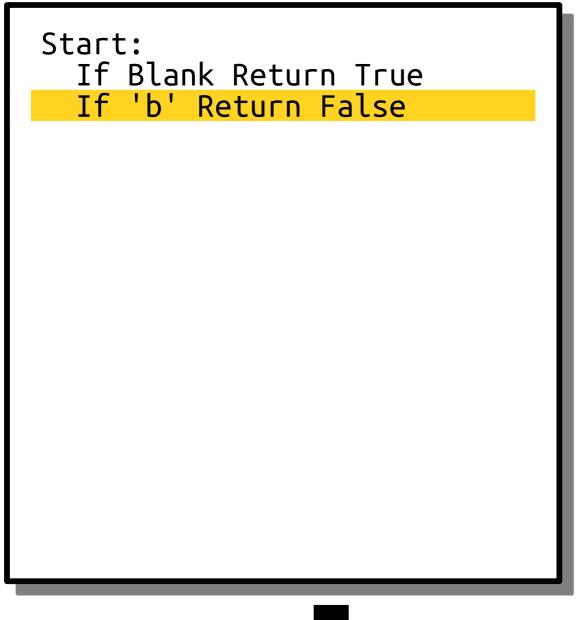




... a a b b b ...

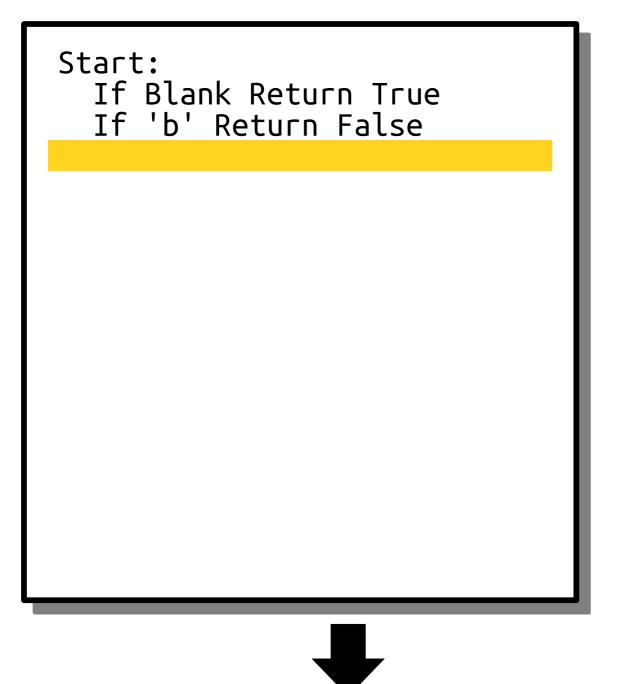


m a a b b b ...

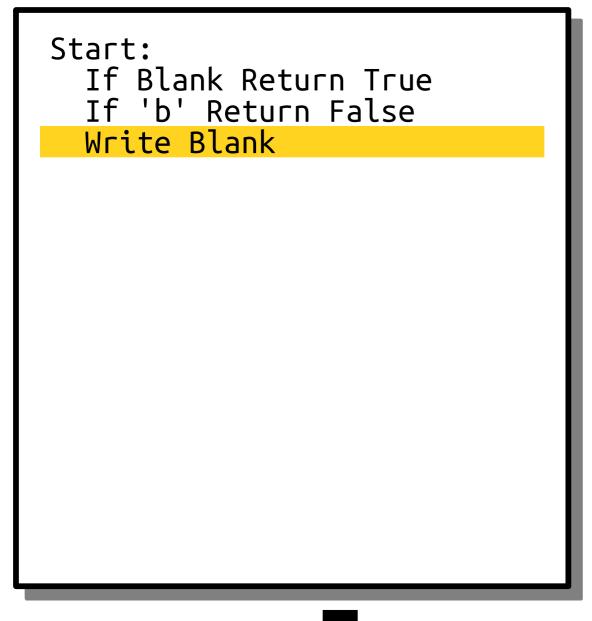


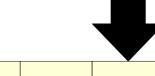


... | a a a b b b

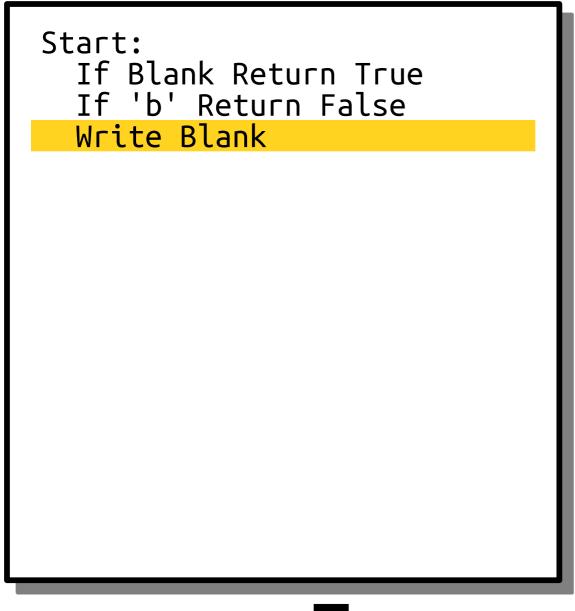


... a a b b b ...



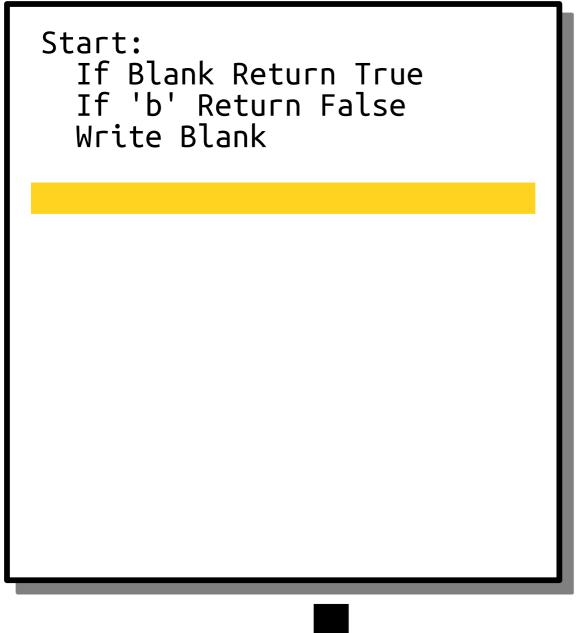


... | a a b b b



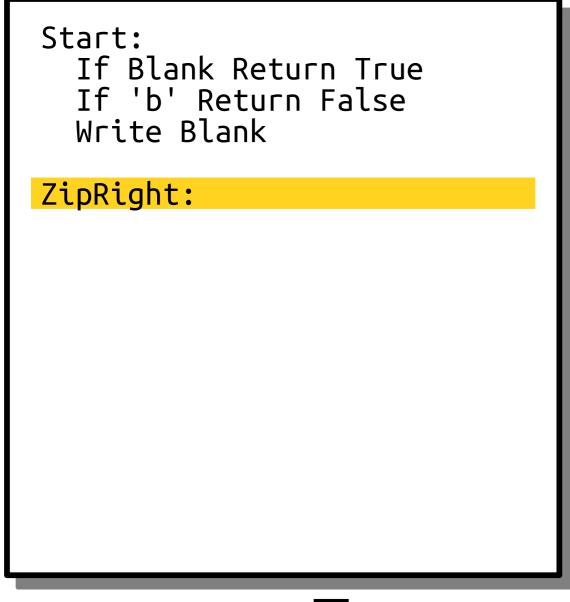


... | a a b b b ...



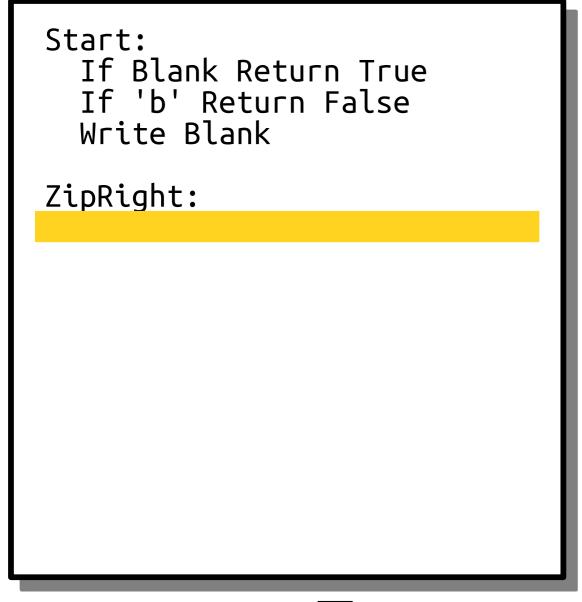


... | a a b b b





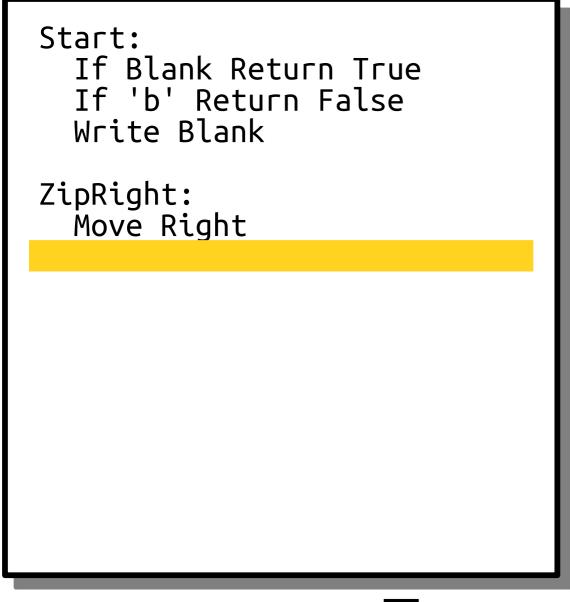
... | a a b b b



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
```

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
```







```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
```

1

Start:

If Blank Return True
If 'b' Return False
Write Blank

ZipRight:

Move Right If Not Blank Goto ZipRight

1



... a a b b ...

1

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
```

1

Start: If Blank Return True If 'b' Return False Write Blank

ZipRight:

Move Right If Not Blank Goto ZipRight



1

```
Start:
    If Blank Return True
    If 'b' Return False
    Write Blank

ZipRight:
    Move Right
    If Not Blank Goto ZipRight
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
```

1

Start: If Blank Return True If 'b' Return False Write Blank

ZipRight:

Move Right If Not Blank Goto ZipRight

9

```
Start:
    If Blank Return True
    If 'b' Return False
    Write Blank

ZipRight:
    Move Right
    If Not Blank Goto ZipRight
```



						+	•		
•••			а	а	b	b	b		•••

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
```



Start: If Blank Return True If 'b' Return False Write Blank ZipRight: Move Right

Move Right If Not Blank Goto ZipRight

1

						+	•		
•••			а	а	b	b	b		•••

							-	•		
• • •			а	а	b	b	Ь			•••

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
```

							-		
•••			а	а	b	b	b		•••

Start: If Blank Return True If 'b' Return False Write Blank ZipRight: Move Right

Move Right
If Not Blank Goto ZipRight

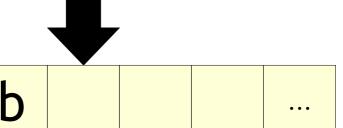
							1	•		
•••			а	а	b	b	b			•••

							-	•		
•••			а	а	b	b	b			•••

								1	•	
•••			а	а	b	b	b			•••

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
```

9

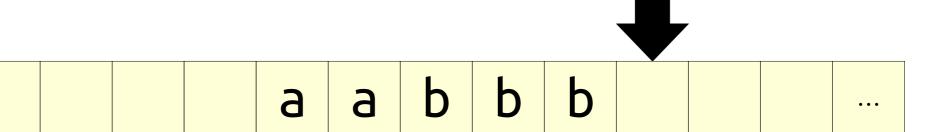


```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
If Not Blank Goto ZipRight
```

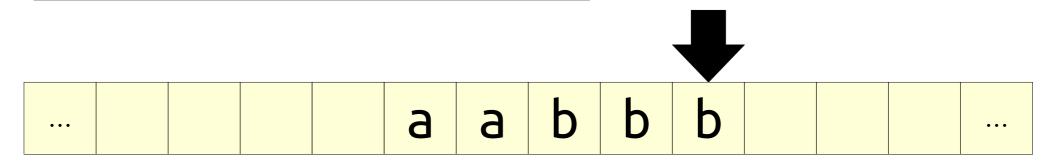


a a b b b ...

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
```



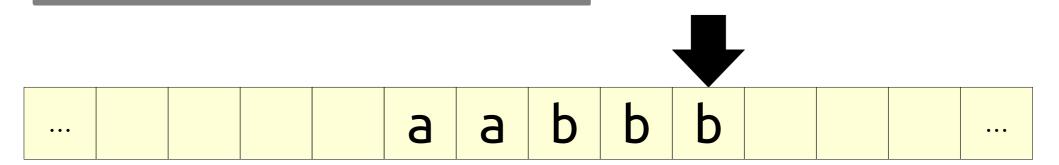
```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
```



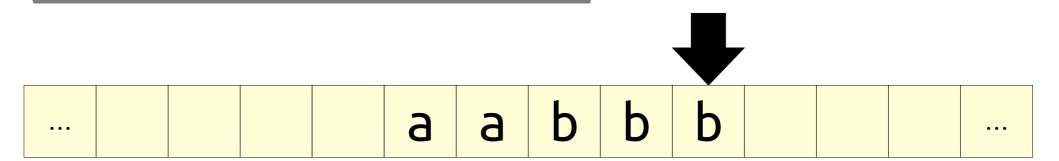
```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
```

... a a b b ...

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
```

							1	-		
•••			а	а	b	b	b			•••

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
```



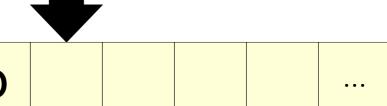
a a b b = ---

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
```

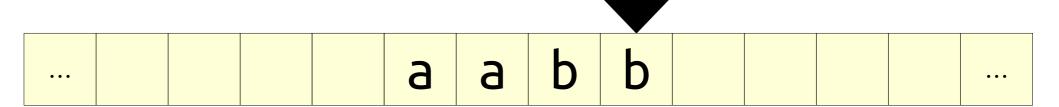


```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
```

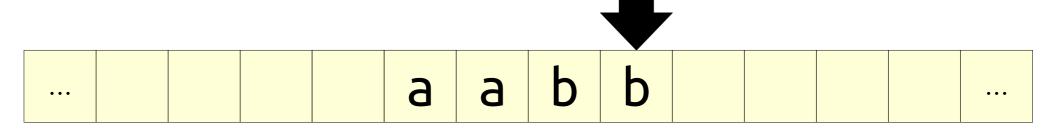
a



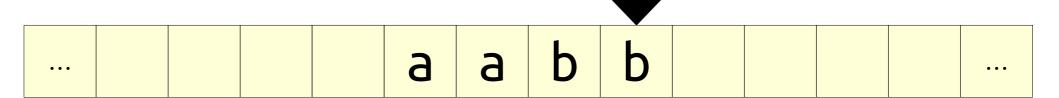
```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
```



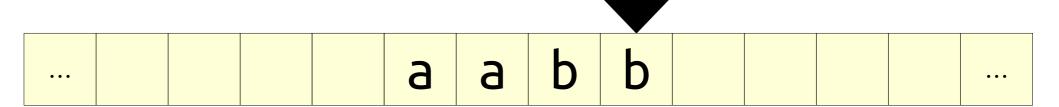
```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
```

... a a b b ...

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
```



m a a b b ...

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
```

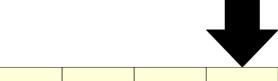
... a a b b ...

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
```





```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
```



... a a b b ...

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
```





```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
```



... a a b b ...

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
```



a a b b ...

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
```



a a b b - - -

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
```



| a a b b = | ...

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```







a a b b ...

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



. | a a b b ...

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```





```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



| a b b | ...



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```







```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



.... | a | b | b | ...

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



... | a b b

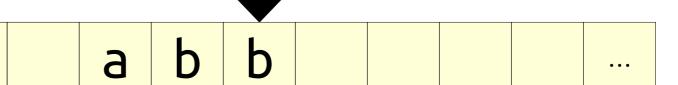
```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



... | a b b

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



| | a | b | b | ...

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



1

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```





```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



Start: If Blank Return True If 'b' Return False Write Blank ZipRight: Move Right If Not Blank Goto ZipRight Move Left If Not 'b' Return False Write Blank

ZipLeft:

Move Left
If Not Blank Goto ZipLeft
Move Right
Goto Start







... | | | a | b | | ...

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



| a b | | | | | | | | |

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```







```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```





Start: If Blank Return True If 'b' Return False Write Blank ZipRight: Move Right If Not Blank Coto 7:

If Not Blank Goto ZipRight Move Left If Not 'b' Return False Write Blank

ZipLeft: Move Left If Not Blank Goto ZipLeft Move Right Goto Start





... | **b** | |

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



Start: If Blank Return True If 'b' Return False Write Blank ZipRight: Move Right

Move Right
If Not Blank Goto ZipRight
Move Left
If Not 'b' Return False
Write Blank

ZipLeft:
 Move Left
 If Not Blank Goto ZipLeft
 Move Right
 Goto Start

Ţ

J

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



.... | b | ...

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



... | b | ...

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



.... | b | ...

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



• • •

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



J

Start:

If Blank Return True
If 'b' Return False
Write Blank

ZipRight:

Move Right
If Not Blank Goto ZipRight
Move Left
If Not 'b' Return False
Write Blank

ZipLeft:

Move Left
If Not Blank Goto ZipLeft
Move Right
Goto Start

...

. . .



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



...

```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```



```
Start:
  If Blank Return True
  If 'b' Return False
  Write Blank
ZipRight:
  Move Right
  If Not Blank Goto ZipRight
  Move Left
  If Not 'b' Return False
  Write Blank
ZipLeft:
  Move Left
  If Not Blank Goto ZipLeft
  Move Right
  Goto Start
```

Start: If Blank Return True If 'b' Return False Write Blank ZipRight: Move Right

Move Right
If Not Blank Goto ZipRight
Move Left
If Not 'b' Return False
Write Blank

ZipLeft: Move Left If Not Blank Goto ZipLeft Move Right Goto Start

Time-Out for Announcements!

Second Midterm Complete

- You're done with the second midterm exam
 - congratulations!
- We're going to do our best to get the second midterm graded before Friday. However, as of now we can't promise "yes, it will definitely be graded by then."
- Have any questions about the exam? Post them on EdStem or come chat with us in person.

Your Questions

"What class at Stanford were you most surprised by (i.e. you didn't think you would like it/had to take it and ended up loving it)?"

Without a doubt, ENGR 50 (Intro to Materials Science and Engineering). I signed up for the course because it was required and was floored by how interesting and useful it was. I still remember some of the demos the professor and the TAs did in lecture and am surprised by how helpful it's been to know the basic concepts from that class.

"whats your favorite cuisine / food / comfort food"

It's really hard for me to just pick one, so I won't. I'm a huge fan of just about everything spanning from the Eastern Mediterranean through the Indian subcontinent. But in terms of straight—up comfort food, probably a bowl of French lentils cooked with aromatics and bok choy.

"What software do you use for your slides?"

It's LibreOffice, the default presentation software that comes with Ubuntu Linux. It's free, and I get what I pay for.

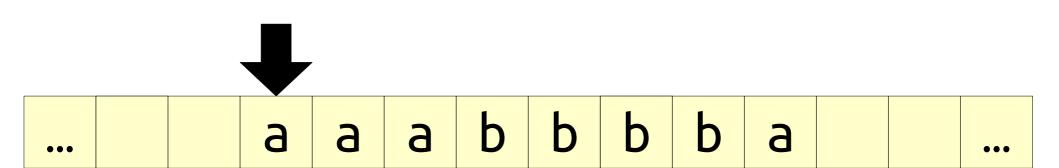
Back to CS103!

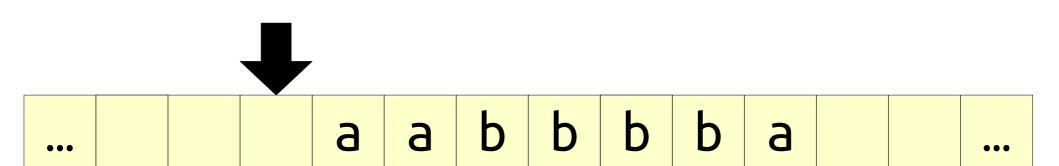
Our Next Challenge

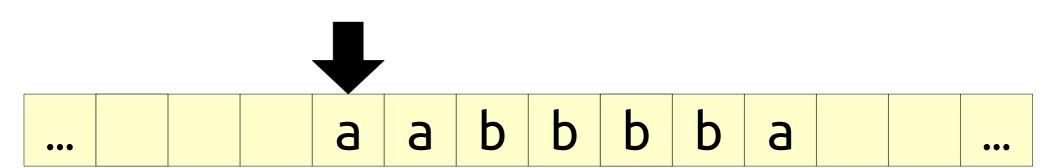
 Let's now take aim at this more general language:

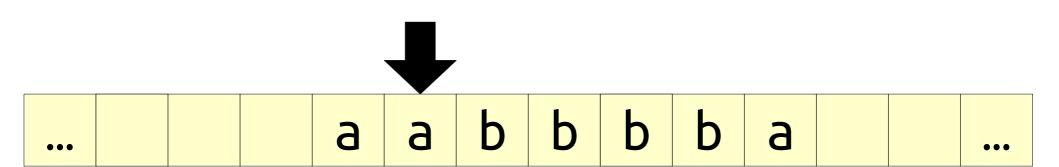
```
\{ w \in \{a, b\}^* \mid w \text{ has an equal number of } a's \text{ and } b's \}
```

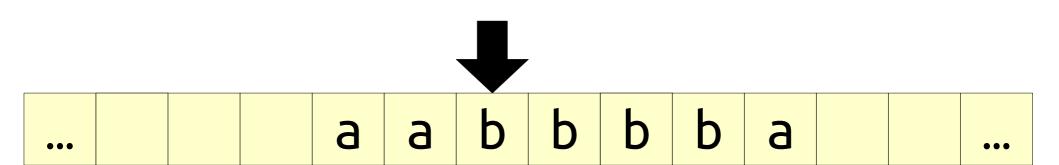
- This language is not regular (do you see why?)
- It is context-free, but it's a bit tricky to write a CFG for it. (This is a great exercise!)
- Let's see how to design a TM for it.

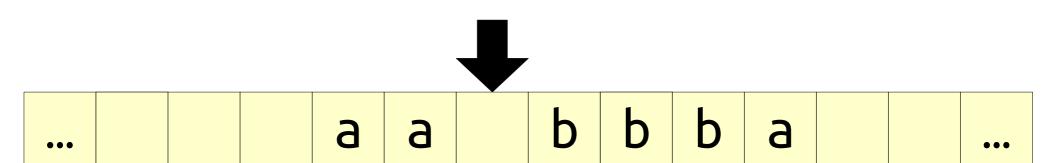


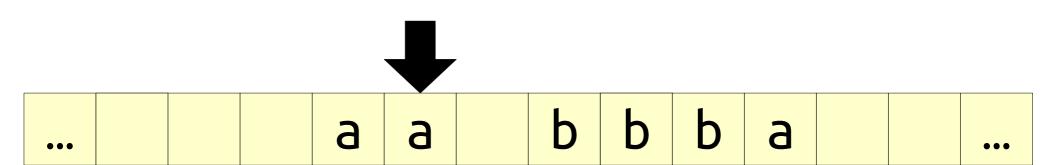


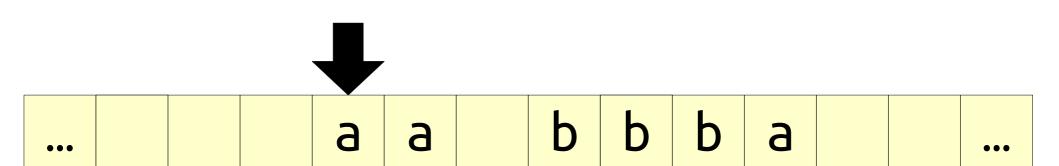


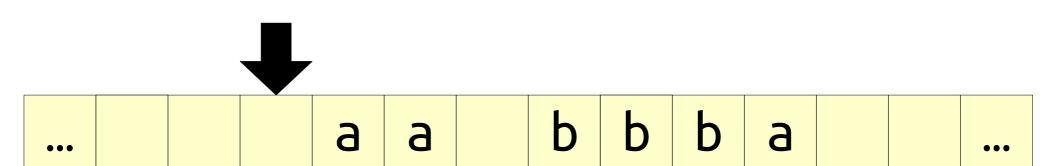


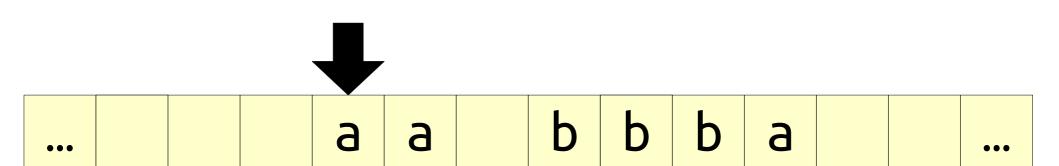


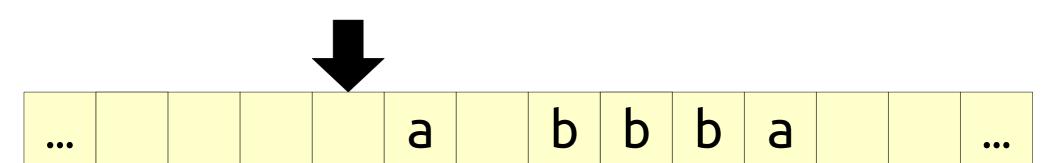


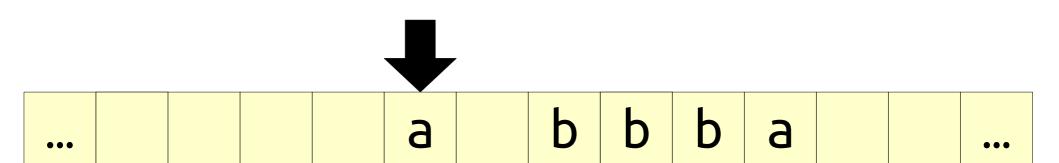


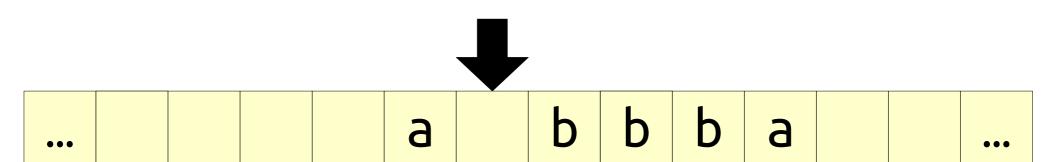


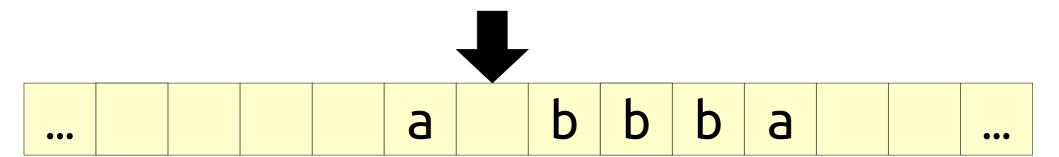


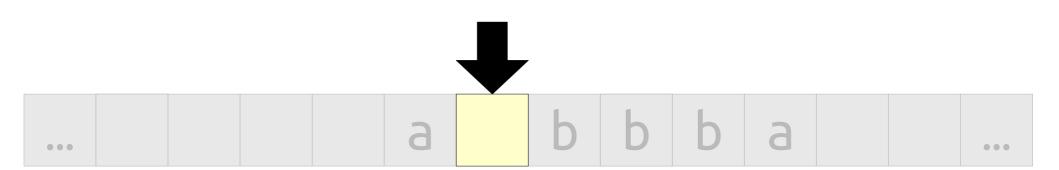


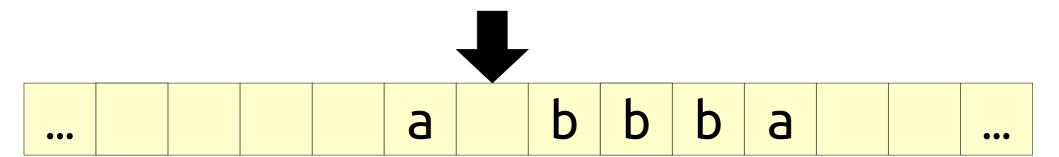


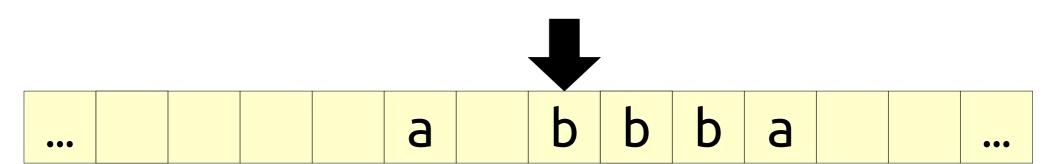


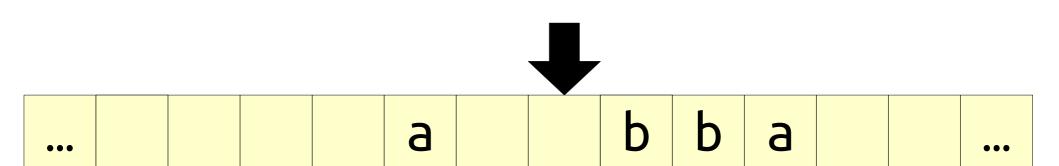


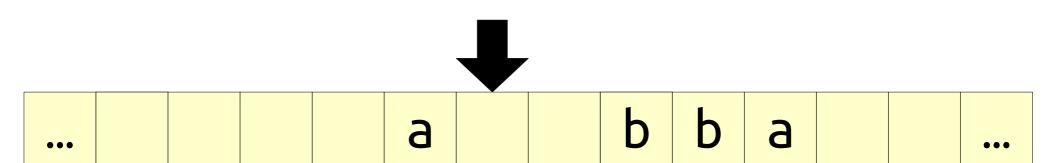


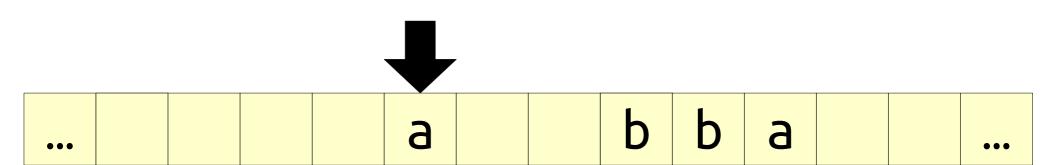


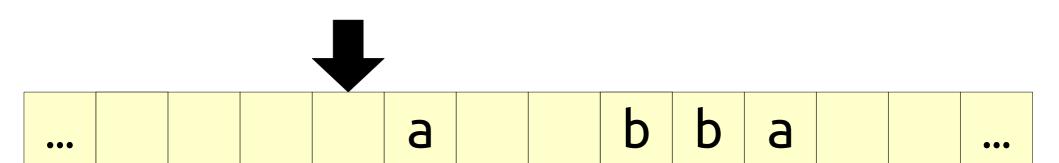


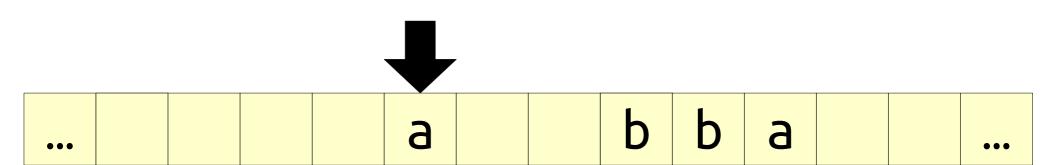


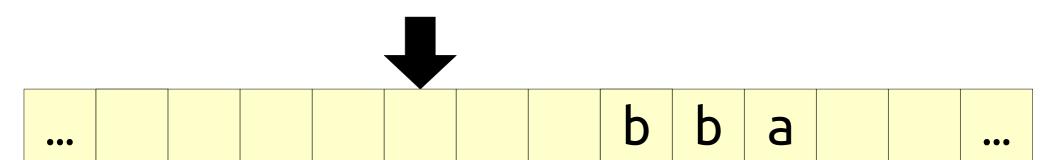


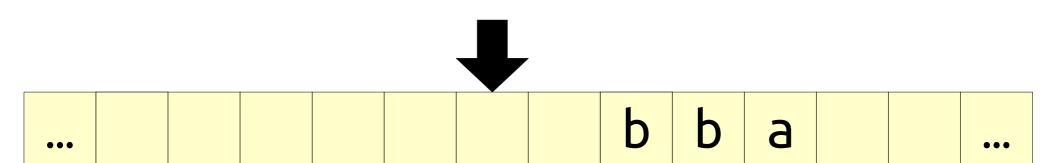


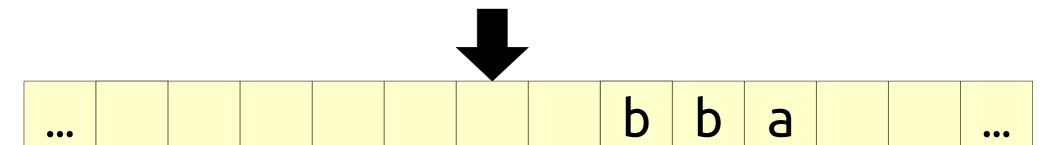


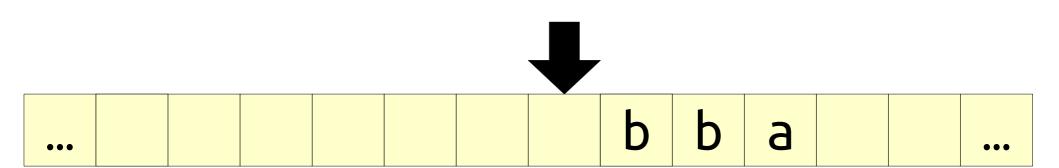


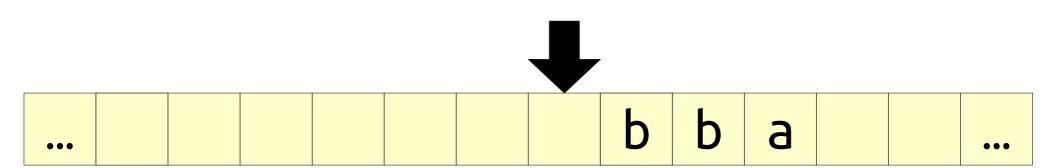


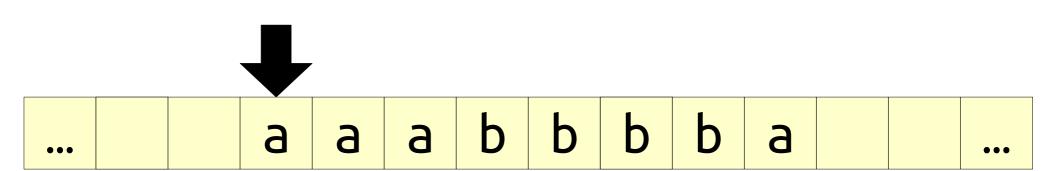


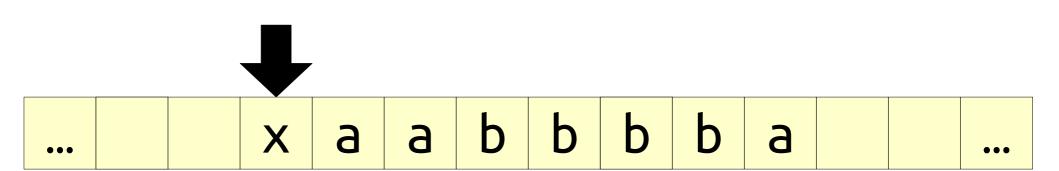


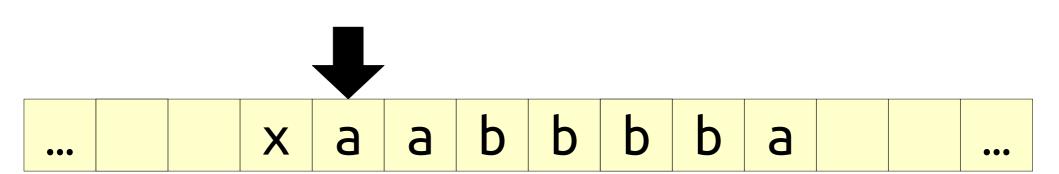


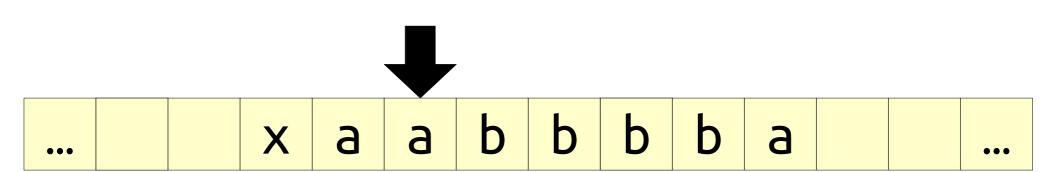


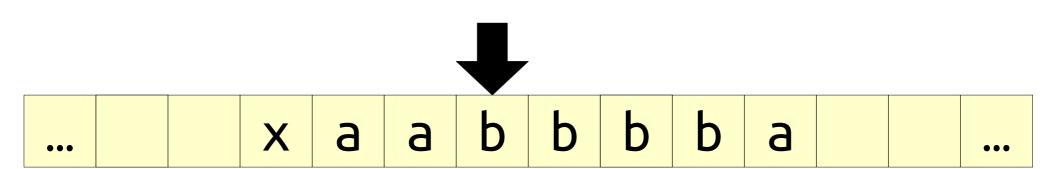


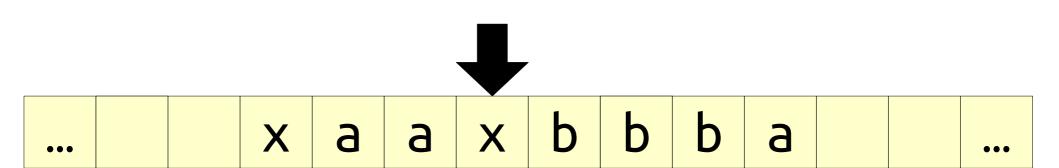


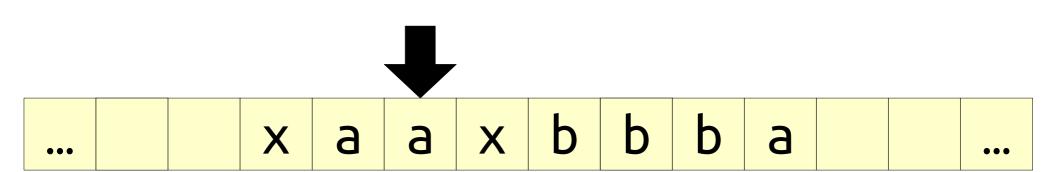


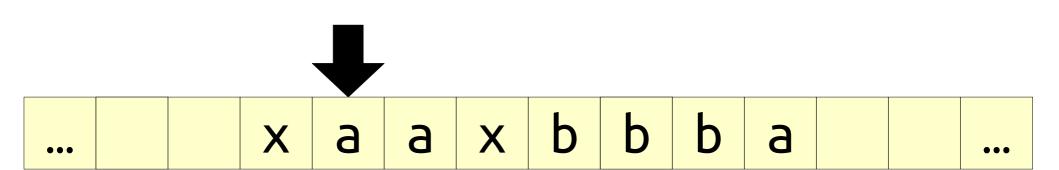


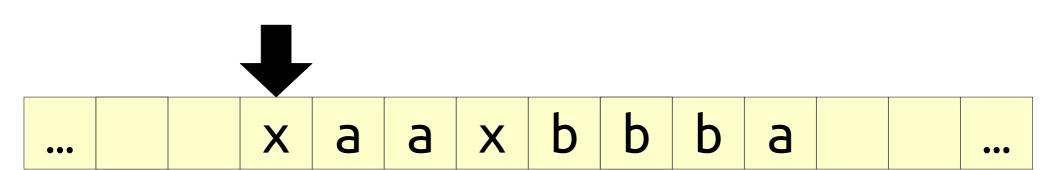


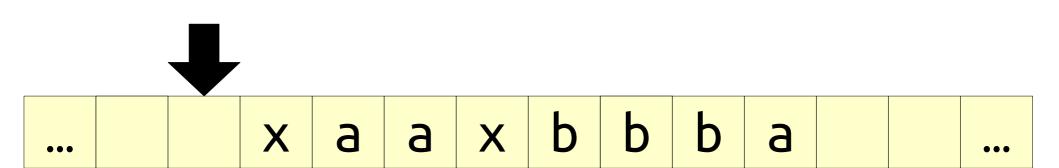


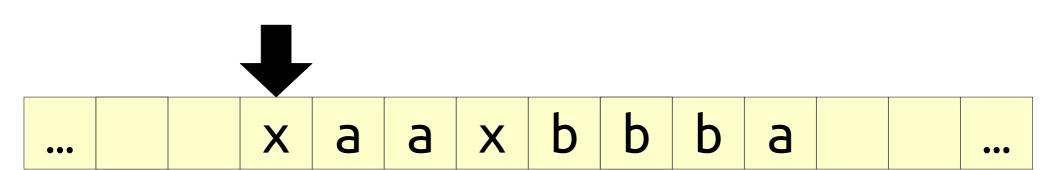


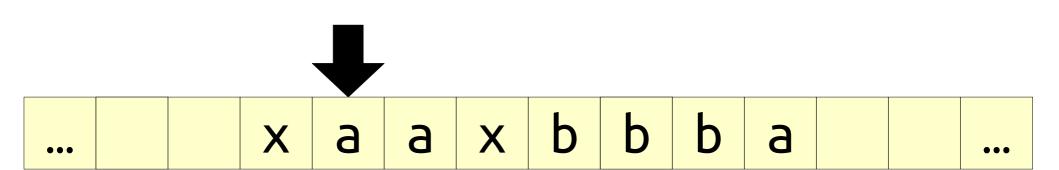


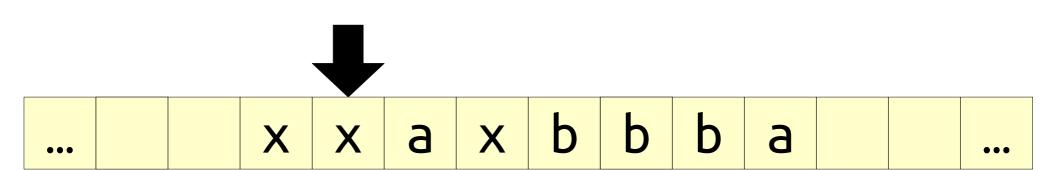


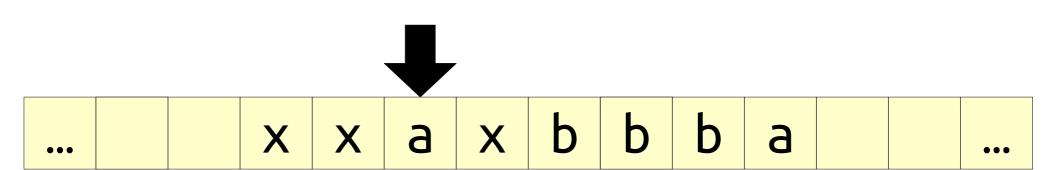


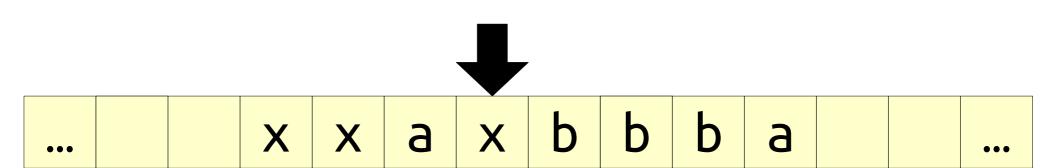


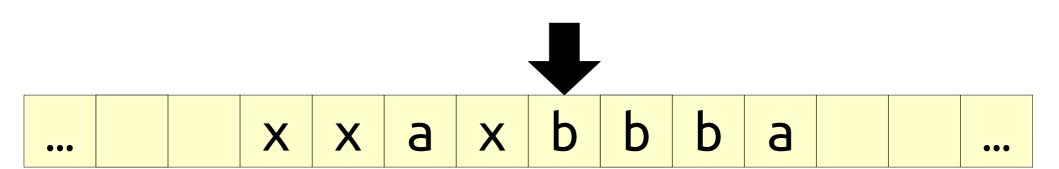


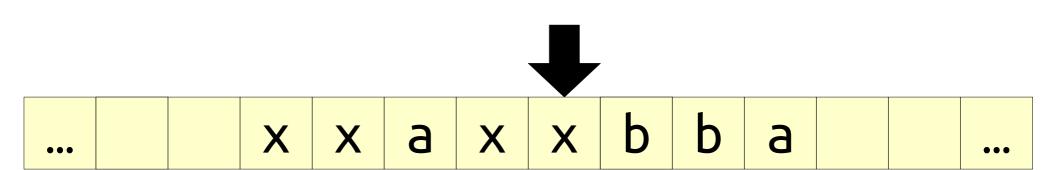


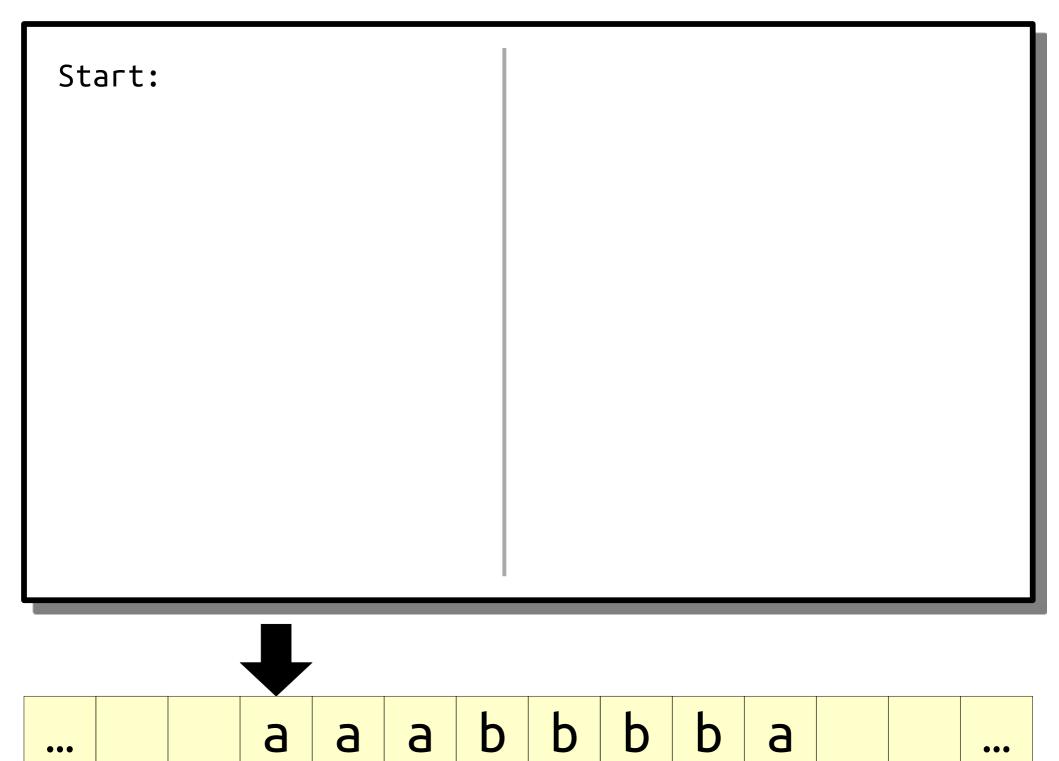


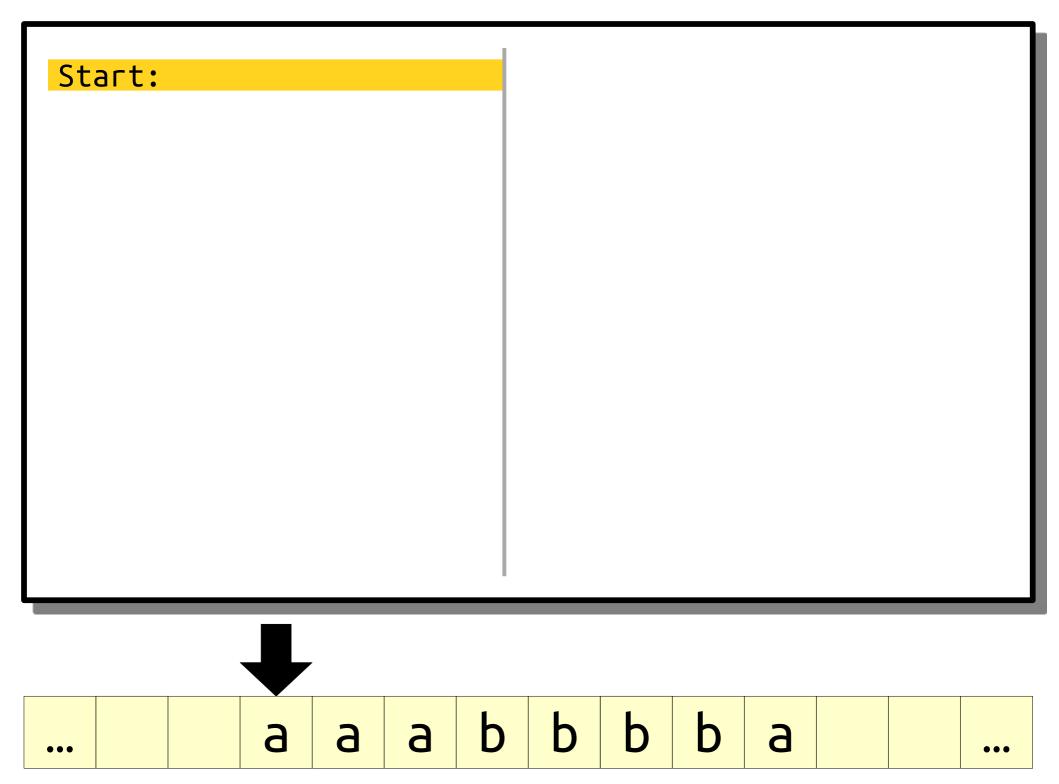


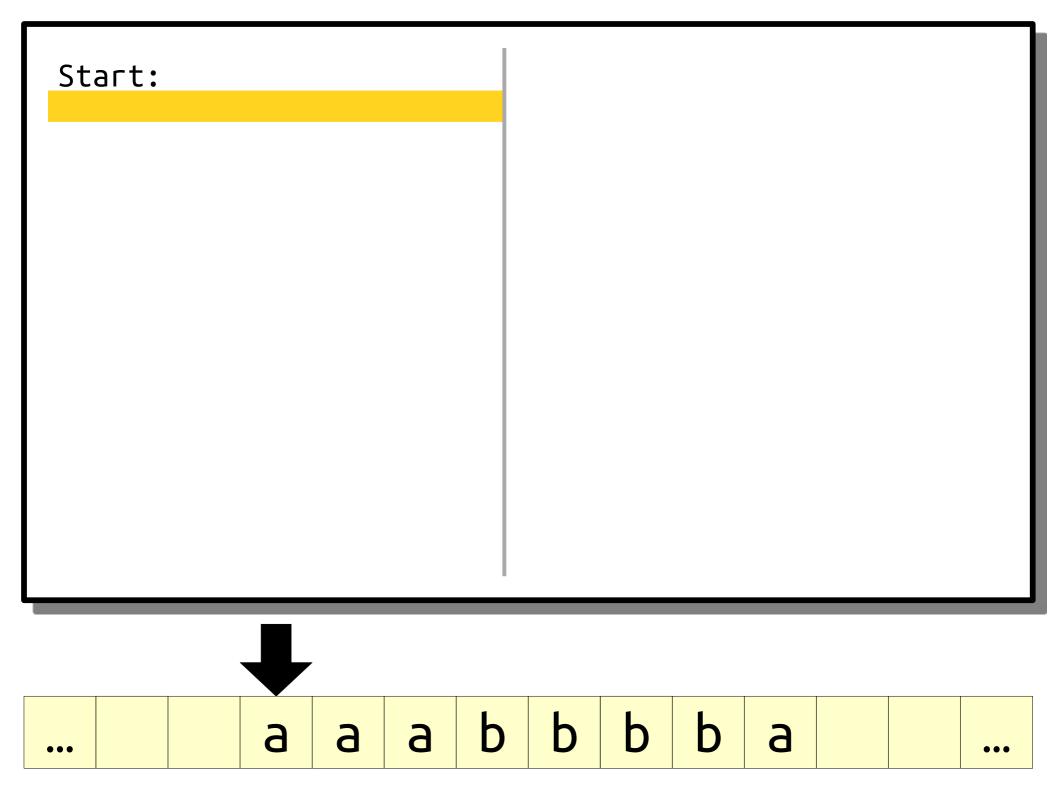


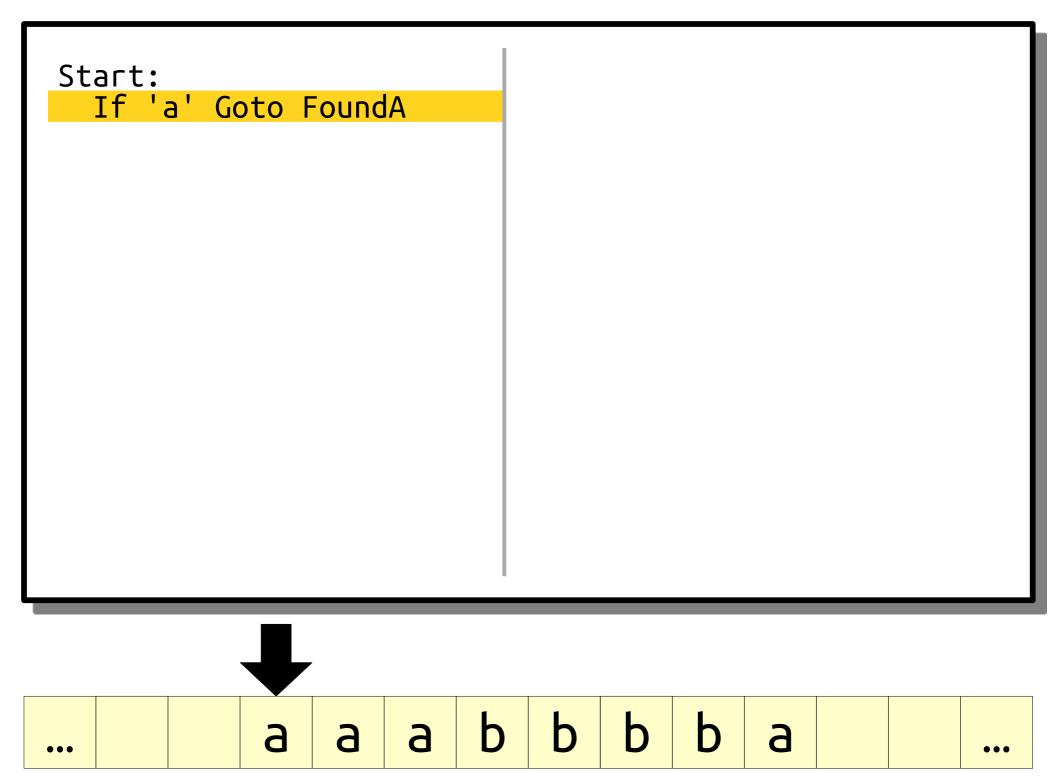


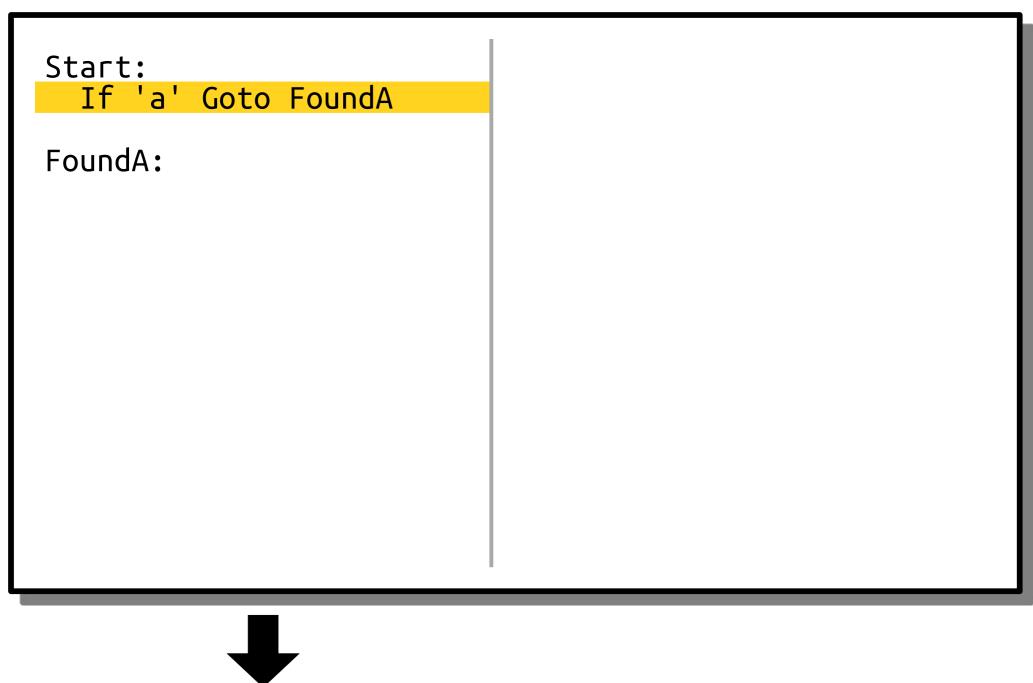




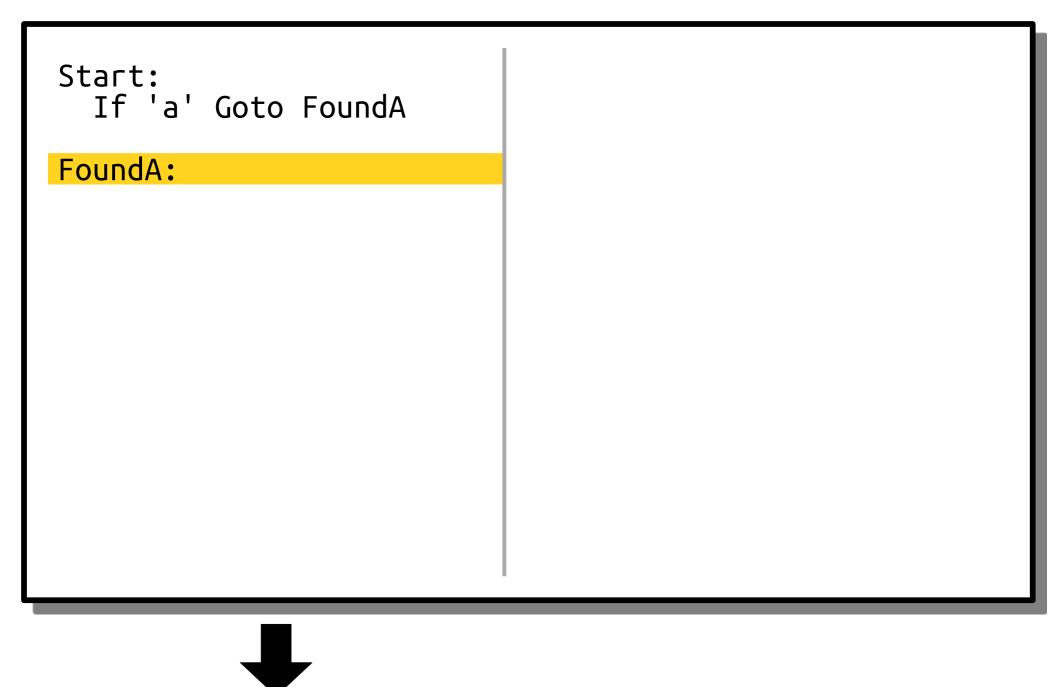


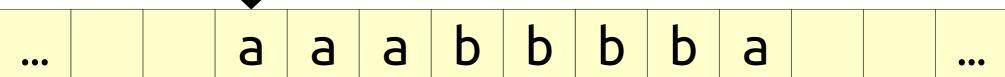


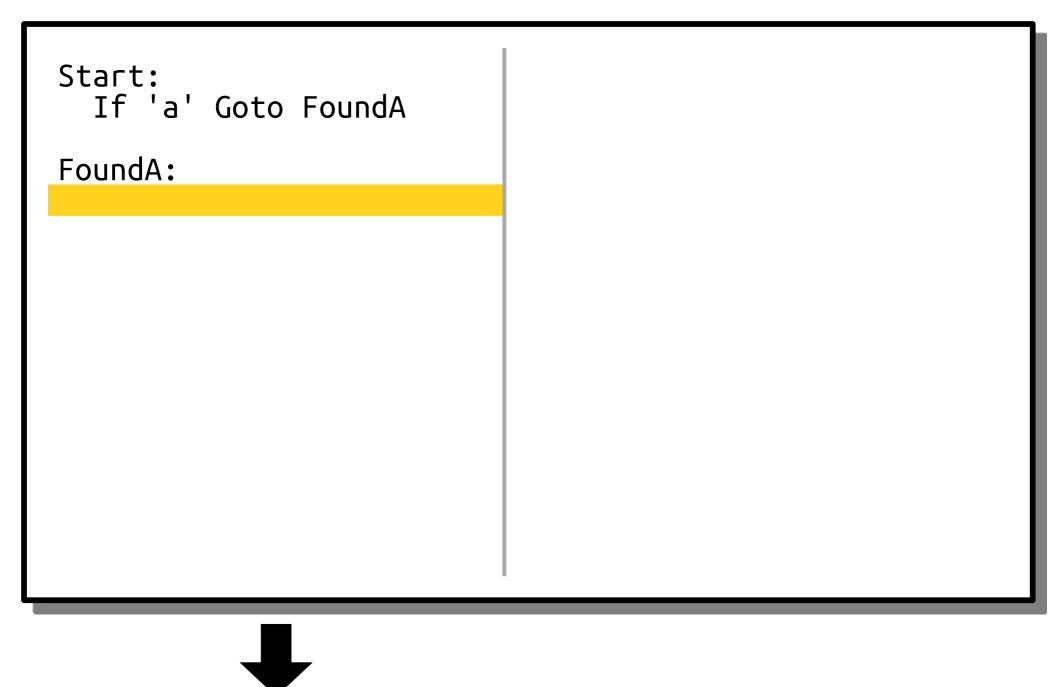


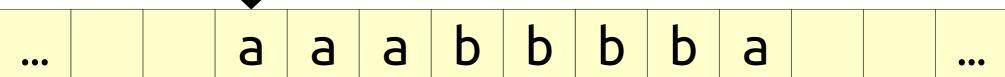


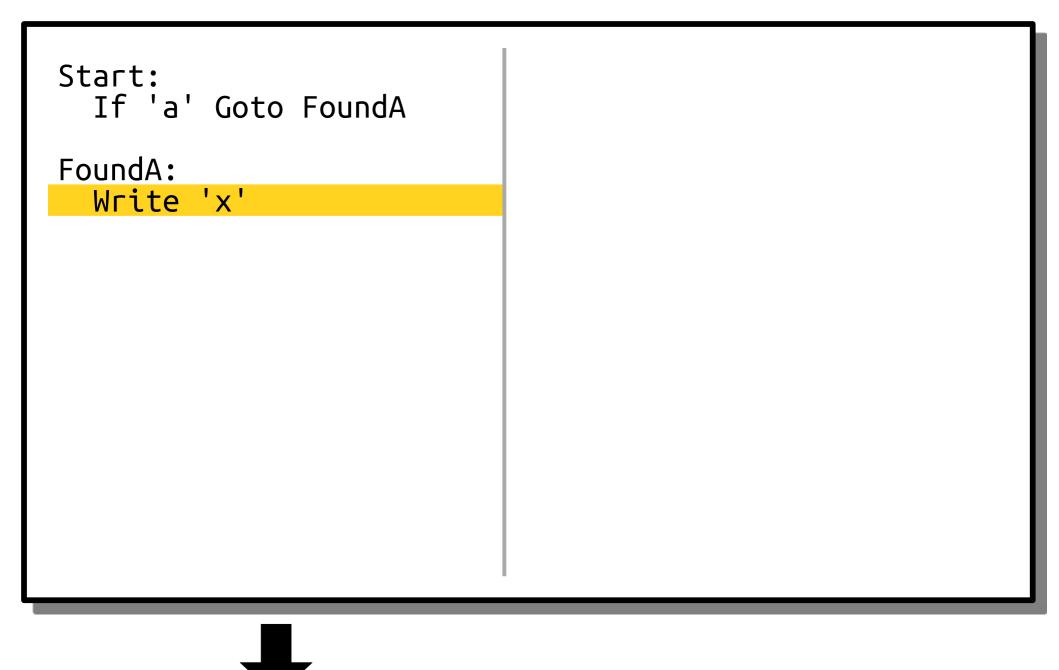
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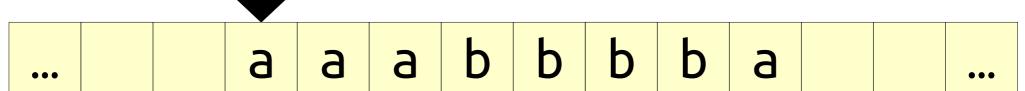


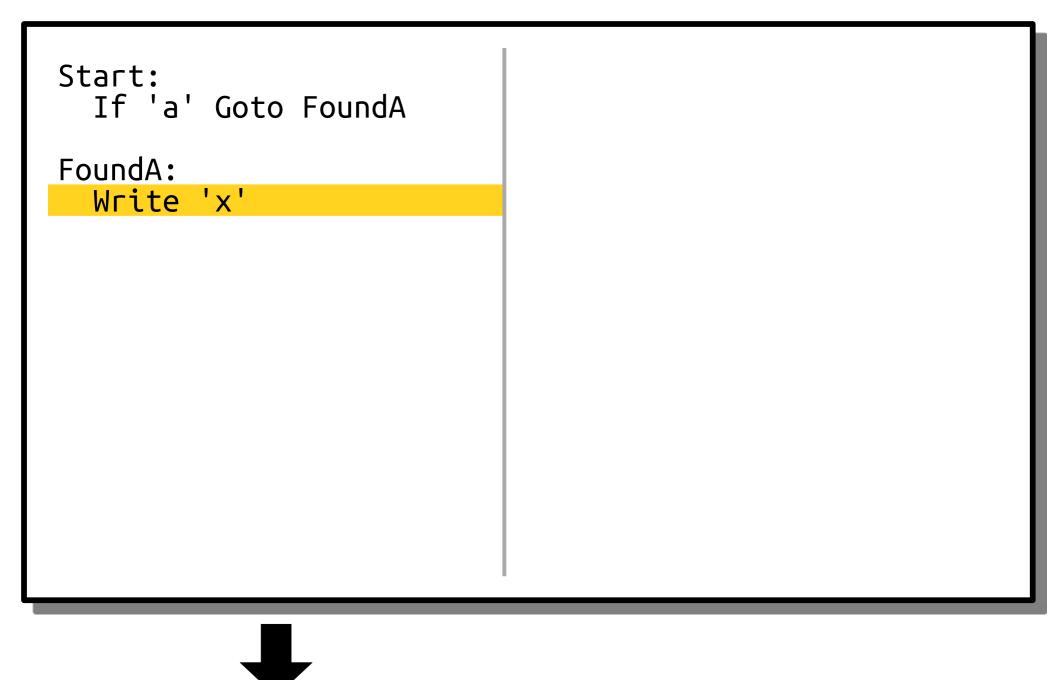


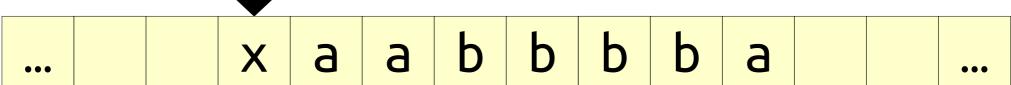


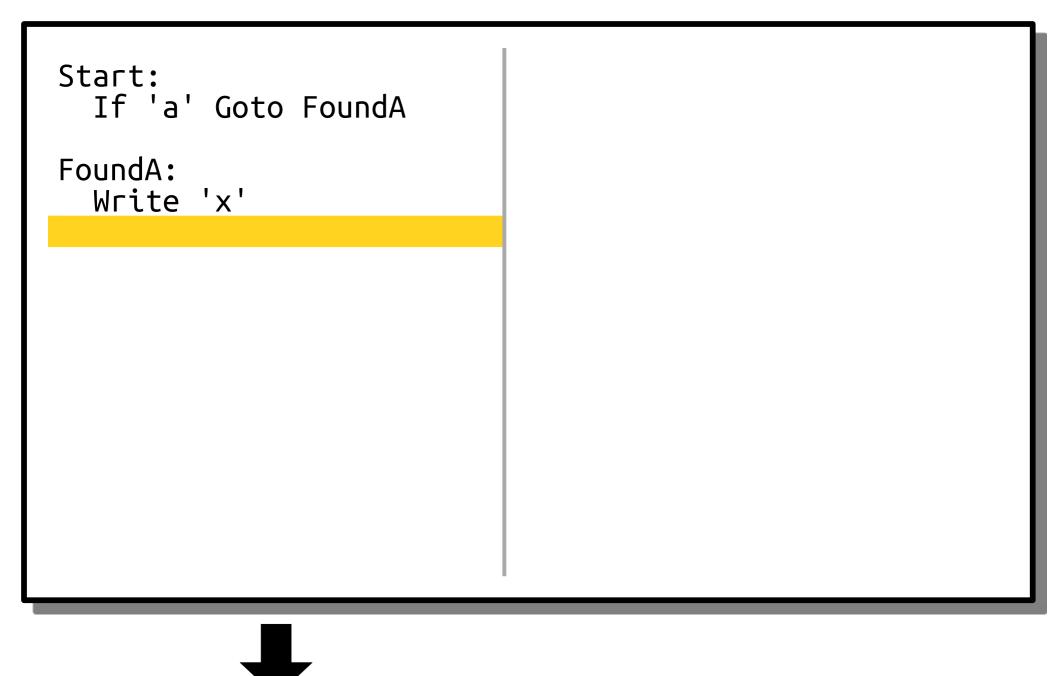


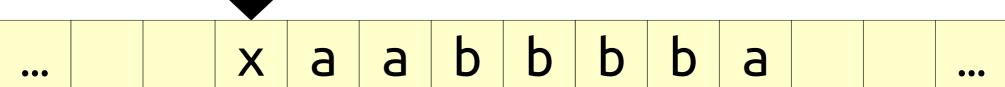




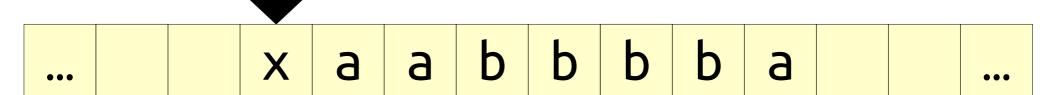




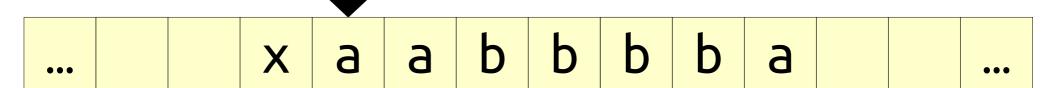




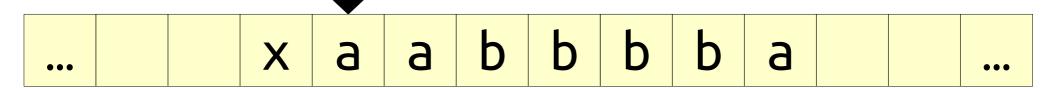
```
Start:
 If 'a' Goto FoundA
FoundA:
 Write 'x'
  Move Right
```



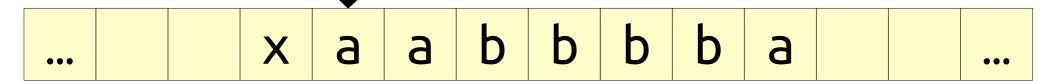
```
Start:
 If 'a' Goto FoundA
FoundA:
 Write 'x'
  Move Right
```



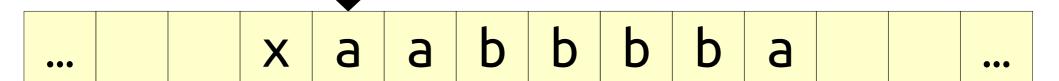
```
Start:
  If 'a' Goto FoundA
FoundA:
  Write 'x'
  Move Right If 'a' ?
```



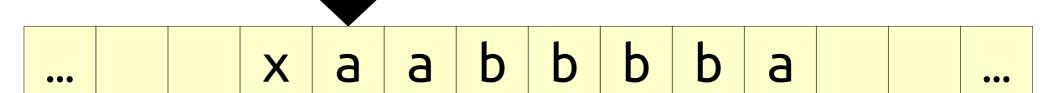
```
Start:
  If 'a' Goto FoundA
FoundA:
  Write 'x'
  Move Right If 'a' ?
```



```
Start:
  If 'a' Goto FoundA
FoundA:
  Write 'x'
LoopA:
 Move Right If 'a' ?
```



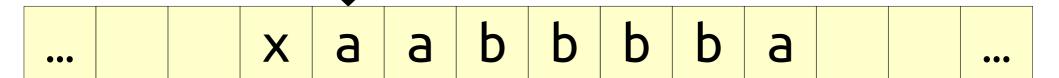
```
Start:
 If 'a' Goto FoundA
FoundA:
 Write 'x'
LoopA:
 Move Right
 If 'a' Goto LoopA
```



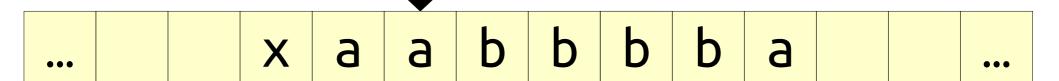
```
Start:
 If 'a' Goto FoundA
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
```

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```
Start:
 If 'a' Goto FoundA
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
```



```
Start:
 If 'a' Goto FoundA
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
```



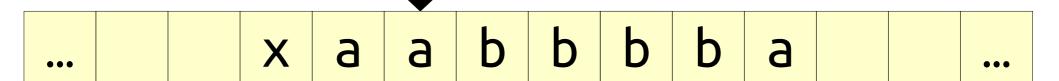
```
Start:
 If 'a' Goto FoundA
FoundA:
 Write 'x'
LoopA:
 Move Right
 If 'a' Goto LoopA
```



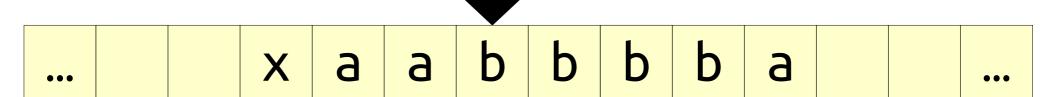
```
Start:
 If 'a' Goto FoundA
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
```

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```
Start:
 If 'a' Goto FoundA
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
```



```
Start:
 If 'a' Goto FoundA
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
```

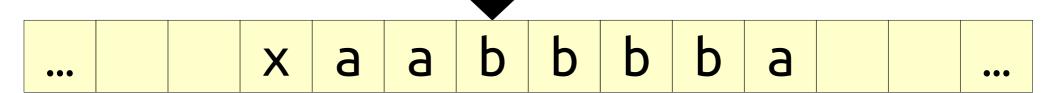


```
Start:
   If 'a' Goto FoundA

FoundA:
   Write 'x'
LoopA:
   Move Right
   If 'a' Goto LoopA
```

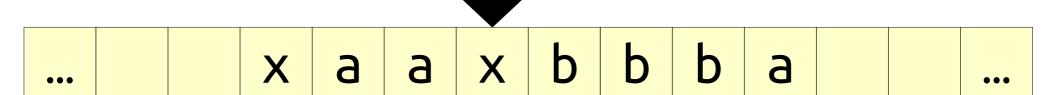


```
Start:
 If 'a' Goto FoundA
FoundA:
 Write 'x'
LoopA:
 Move Right
 If 'a' Goto LoopA
```

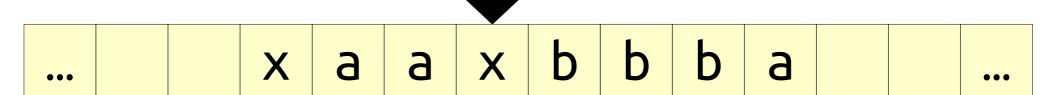


```
Start:
 If 'a' Goto FoundA
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  Write 'x'
```

```
Start:
 If 'a' Goto FoundA
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  Write 'x'
```



```
Start:
 If 'a' Goto FoundA
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  Write 'x'
```



```
Start:
 If 'a' Goto FoundA
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
   If 'a' Goto FoundA

FoundA:
   Write 'x'
LoopA:
   Move Right
   If 'a' Goto LoopA
   Write 'x'
   Goto GoHome
```

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



```
Start:
  If 'a' Goto FoundA

FoundA:
    Write 'x'
LoopA:
    Move Right
    If 'a' Goto LoopA
    Write 'x'
    Goto GoHome
```

GoHome:

Move Left
If Not Blank Goto GoHome
Move Right
Goto Start



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```
Start:
   If 'a' Goto FoundA

FoundA:
   Write 'x'
LoopA:
   Move Right
   If 'a' Goto LoopA
   Write 'x'
   Goto GoHome
```

GoHome:

Move Left

If Not Blank Goto GoHome Move Right Goto Start



```
Start:
   If 'a' Goto FoundA

FoundA:
   Write 'x'
LoopA:
   Move Right
   If 'a' Goto LoopA
   Write 'x'
   Goto GoHome
```

GoHome:

Move Left

If Not Blank Goto GoHome

If Not Blank Goto GoHome Move Right Goto Start



```
Start:
  If 'a' Goto FoundA

FoundA:
    Write 'x'
LoopA:
    Move Right
    If 'a' Goto LoopA
    Write 'x'
    Goto GoHome
```

```
GoHome:
   Move Left
   If Not Blank Goto GoHome
   Move Right
   Goto Start
```



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```
Start:
   If 'a' Goto FoundA

FoundA:
   Write 'x'
LoopA:
   Move Right
   If 'a' Goto LoopA
   Write 'x'
   Goto GoHome
```

GoHome:

Move Left
If Not Blank Goto GoHome
Move Right
Goto Start



•••		X	а	а	X	b	b	b	а		•••

```
Start:
   If 'a' Goto FoundA

FoundA:
   Write 'x'
LoopA:
   Move Right
   If 'a' Goto LoopA
   Write 'x'
   Goto GoHome
```

GoHome:

Move Left

If Not Blank Goto GoHome

If Not Blank Goto GoHome Move Right Goto Start



```
Start:
   If 'a' Goto FoundA

FoundA:
   Write 'x'
LoopA:
   Move Right
   If 'a' Goto LoopA
   Write 'x'
   Goto GoHome
```

Move Left

If Not Blank Goto GoHome Move Right Goto Start



```
Start:
   If 'a' Goto FoundA

FoundA:
   Write 'x'
LoopA:
   Move Right
   If 'a' Goto LoopA
   Write 'x'
   Goto GoHome
```



	•••			X	а	а	X	b	b	b	а			•••	
--	-----	--	--	---	---	---	---	---	---	---	---	--	--	-----	--

```
Start:
   If 'a' Goto FoundA

FoundA:
   Write 'x'
LoopA:
   Move Right
   If 'a' Goto LoopA
   Write 'x'
   Goto GoHome
```

Move Left
If Not Blank Goto GoHome
Move Right
Goto Start



•••		X	а	а	X	b	b	b	а		•••

```
Start:
   If 'a' Goto FoundA

FoundA:
   Write 'x'
LoopA:
   Move Right
   If 'a' Goto LoopA
   Write 'x'
   Goto GoHome
```

Move Left

If Not Blank Goto GoHome Move Right Goto Start



```
Start:
  If 'a' Goto FoundA

FoundA:
    Write 'x'
LoopA:
    Move Right
    If 'a' Goto LoopA
    Write 'x'
    Goto GoHome
```

Move Left

If Not Blank Goto GoHome Move Right Goto Start



```
Start:
   If 'a' Goto FoundA

FoundA:
   Write 'x'
LoopA:
   Move Right
   If 'a' Goto LoopA
   Write 'x'
   Goto GoHome
```



•••		X	а	а	X	Ь	Ь	Ь	а		•••

```
Start:
   If 'a' Goto FoundA

FoundA:
   Write 'x'
LoopA:
   Move Right
   If 'a' Goto LoopA
   Write 'x'
   Goto GoHome
```

Move Left
If Not Blank Goto GoHome
Move Right
Goto Start



	•••			X	а	а	X	b	b	b	а			•••
--	-----	--	--	---	---	---	---	---	---	---	---	--	--	-----

```
Start:
  If 'a' Goto FoundA

FoundA:
    Write 'x'
LoopA:
    Move Right
    If 'a' Goto LoopA
    Write 'x'
    Goto GoHome
```

Move Left

If Not Blank Goto GoHome Move Right Goto Start



```
Start:
   If 'a' Goto FoundA

FoundA:
   Write 'x'
LoopA:
   Move Right
   If 'a' Goto LoopA
   Write 'x'
   Goto GoHome
```

Move Left

If Not Blank Goto GoHome Move Right Goto Start



```
Start:
   If 'a' Goto FoundA

FoundA:
   Write 'x'
LoopA:
   Move Right
   If 'a' Goto LoopA
   Write 'x'
   Goto GoHome
```



```
Start:
   If 'a' Goto FoundA

FoundA:
   Write 'x'
LoopA:
   Move Right
   If 'a' Goto LoopA
   Write 'x'
   Goto GoHome
```



```
Start:
   If 'a' Goto FoundA

FoundA:
   Write 'x'
LoopA:
   Move Right
   If 'a' Goto LoopA
   Write 'x'
   Goto GoHome
```

```
GoHome:
   Move Left
   If Not Blank Goto GoHome
   Move Right
   Goto Start
```



```
Start:
   If 'a' Goto FoundA

FoundA:
   Write 'x'
LoopA:
   Move Right
   If 'a' Goto LoopA
   Write 'x'
   Goto GoHome
```



•••		X	а	а	X	Ь	b	b	а		•••

```
Start:
  If 'a' Goto FoundA

FoundA:
    Write 'x'
LoopA:
    Move Right
    If 'a' Goto LoopA
    Write 'x'
    Goto GoHome
```



```
Start:
   If 'a' Goto FoundA

FoundA:
    Write 'x'
LoopA:
    Move Right
    If 'a' Goto LoopA
    Write 'x'
    Goto GoHome
```



```
Start:
   If 'a' Goto FoundA
```

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



```
Start:
   If 'a' Goto FoundA
   Move Right
```



•••		X	а	а	X	b	b	b	а		•••
											1

```
Start:
   If 'a' Goto FoundA
   Move Right
```



•••		X	а	а	X	b	b	b	а		•••

```
Start:
    If 'a' Goto FoundA
    Move Right
```



	•••			X	а	а	X	b	b	b	а			•••
--	-----	--	--	---	---	---	---	---	---	---	---	--	--	-----

```
Start:
   If 'a' Goto FoundA
   Move Right
   Goto Start
```

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



Start: If 'a' Goto FoundA Move Right Goto Start FoundA: Write 'x' LoopA: Move Right If 'a' Goto LoopA Write 'x' Goto GoHome

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  Write 'x'
  Goto GoHome
```



•••		X	а	а	X	b	b	b	а		•••

Start:
 If 'a' Goto FoundA
 Move Right
 Goto Start

FoundA:

Write 'x'
LoopA:
 Move Right
 If 'a' Goto LoopA
 Write 'x'
 Goto GoHome

GoHome:

Move Left
If Not Blank Goto GoHome
Move Right
Goto Start



```
Start:
    If 'a' Goto FoundA
    Move Right
    Goto Start

FoundA:
    Write 'x'
LoopA:
    Move Right
```

If 'a' Goto LoopA

Write 'x'

Goto GoHome

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



```
Start:
   If 'a' Goto FoundA
   Move Right
   Goto Start
```

FoundA:

Write 'x'

LoopA:

Move Right
If 'a' Goto LoopA
Write 'x'
Goto GoHome

GoHome:

Move Left
If Not Blank Goto GoHome
Move Right
Goto Start



Start:
 If 'a' Goto FoundA
 Move Right
 Goto Start

FoundA:
Write 'x'

LoopA:

Move Right
If 'a' Goto LoopA
Write 'x'
Goto GoHome

GoHome:

Move Left
If Not Blank Goto GoHome
Move Right
Goto Start



```
Start:
   If 'a' Goto FoundA
   Move Right
   Goto Start

FoundA:
   Write 'x'
```

LoopA:

Move Right
If 'a' Goto LoopA
Write 'x'
Goto GoHome



x x a x b b a .

```
Start:
    If 'a' Goto FoundA
    Move Right
    Goto Start

FoundA:
    Write 'x'
LoopA:
    Move Right
```

If 'a' Goto LoopA Write 'x' Goto GoHome



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
   If 'a' Goto FoundA
   Move Right
   Goto Start
```

FoundA:
Write 'x'

LoopA:

Move Right
If 'a' Goto LoopA
Write 'x'
Goto GoHome

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



```
Start:
    If 'a' Goto FoundA
    Move Right
    Goto Start

FoundA:
    Write 'x'
LoopA:
    Move Right
```

If 'a' Goto LoopA Write 'x' Goto GoHome



```
Start:
   If 'a' Goto FoundA
   Move Right
   Goto Start

FoundA:
   Write 'x'
LoopA:
```

Move Right
If 'a' Goto LoopA
Write 'x'
Goto GoHome



• • •			X	X	а	X	Ь	b	Ь	а			•••
-------	--	--	---	---	---	---	---	---	---	---	--	--	-----

```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  Write 'x'
  Goto GoHome
```



	•••			X	X	а	X	Ь	b	Ь	а			•••
--	-----	--	--	---	---	---	---	---	---	---	---	--	--	-----

```
Start:
   If 'a' Goto FoundA
   Move Right
   Goto Start

FoundA:
   Write 'x'
```

Move Right
If 'a' Goto LoopA

Write 'x'
Goto GoHome

LoopA:

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



	•••			X	X	а	X	b	b	b	а			•••
--	-----	--	--	---	---	---	---	---	---	---	---	--	--	-----

```
Start:
    If 'a' Goto FoundA
    Move Right
    Goto Start

FoundA:
    Write 'x'
LoopA:
```

Move Right
If 'a' Goto LoopA
If 'x' Goto LoopA
Write 'x'
Goto GoHome



```
Start:
    If 'a' Goto FoundA
    Move Right
    Goto Start

FoundA:
    Write 'x'
LoopA:
    Move Right
    If 'a' Goto LoopA
    If 'x' Goto LoopA
```

Write 'x'

Goto GoHome

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



```
Start:
    If 'a' Goto FoundA
    Move Right
    Goto Start

FoundA:
    Write 'x'
```

LoopA:

Move Right
If 'a' Goto LoopA
If 'x' Goto LoopA
Write 'x'
Goto GoHome

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left
If Not Blank Goto GoHome
Move Right
Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

GoHome: Move Left If Not Blank Goto GoHome

Move Right Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left
If Not Blank Goto GoHome
Move Right
Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left
If Not Blank Goto GoHome
Move Right
Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left
If Not Blank Goto GoHome
Move Right
Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left

If Not Blank Goto GoHome Move Right Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left
If Not Blank Goto GoHome
Move Right
Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left

If Not Blank Goto GoHome Move Right Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left

If Not Blank Goto GoHome Move Right Goto Start



•••		X	X	а	X	X	b	b	а			•••	
-----	--	---	---	---	---	---	---	---	---	--	--	-----	--

```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



x x a x b b a

```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left
If Not Blank Goto GoHome
Move Right
Goto Start



•••		X	X	а	X	X	b	b	а		•••
			-								

```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left

If Not Blank Goto GoHome Move Right Goto Start



•••		X	X	а	X	X	b	b	а			•••	
-----	--	---	---	---	---	---	---	---	---	--	--	-----	--

```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left

If Not Blank Goto GoHome Move Right Goto Start



•••			X	X	а	X	X	Ь	Ь	а			•••
-----	--	--	---	---	---	---	---	---	---	---	--	--	-----

```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left
If Not Blank Goto GoHome
Move Right
Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left

If Not Blank Goto GoHome Move Right Goto Start



•••			X	X	а	X	X	Ь	Ь	а			•••
-----	--	--	---	---	---	---	---	---	---	---	--	--	-----

```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left

If Not Blank Goto GoHome Move Right Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



•••		X	X	а	X	X	b	b	а		•••

```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



•••		X	X	а	X	X	b	b	а		•••

```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



x x a x x b b a		•••
-----------------	--	-----

```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
    If 'a' Goto FoundA
    Move Right
    Goto Start
```

FoundA:
 Write 'x'
LoopA:
 Move Right
 If 'a' Goto LoopA
 If 'x' Goto LoopA
 Write 'x'
 Goto GoHome

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



x x a x x	b b	a	•••
-----------	-----	---	-----

```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
   If 'a' Goto FoundA
   Move Right
   Goto Start
```

FoundA:
 Write 'x'
LoopA:
 Move Right
 If 'a' Goto LoopA
 If 'x' Goto LoopA
 Write 'x'
 Goto GoHome



•••		X	X	а	X	X	b	b	а		•••

```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
    If 'a' Goto FoundA
    Move Right
    Goto Start
```

FoundA:

Write 'x'
LoopA:
 Move Right
 If 'a' Goto LoopA
 If 'x' Goto LoopA
 Write 'x'
 Goto GoHome



	•••			X	X	а	X	X	b	b	а			•••	
--	-----	--	--	---	---	---	---	---	---	---	---	--	--	-----	--

```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



•••			X	X	а	X	X	Ь	Ь	а			•••
-----	--	--	---	---	---	---	---	---	---	---	--	--	-----

```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



x x x x b b a	X X	($X \mid X$			•••	
---------------	-----	----------	------------	--	--	-----	--

```
Start:
   If 'a' Goto FoundA
   Move Right
   Goto Start

FoundA:
   Write 'x'
LoopA:
```

Move Right
If 'a' Goto LoopA
If 'x' Goto LoopA
Write 'x'
Goto GoHome

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



```
Start:
    If 'a' Goto FoundA
    Move Right
    Goto Start

FoundA:
    Write 'x'
LoopA:
    Move Right
    If 'a' Goto LoopA
    If 'x' Goto LoopA
```

Write 'x'

Goto GoHome



•••		X	X	X	X	X	b	b	а		•••

```
Start:
    If 'a' Goto FoundA
    Move Right
    Goto Start

FoundA:
    Write 'x'
LoopA:
    Move Right
    If 'a' Goto LoopA
    If 'x' Goto LoopA
```

Write 'x'

Goto GoHome



X X X X X	b b	a	•••
-----------	-----	---	-----

```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



•••			X	X	X	X	X	b	Ь	а			•••
-----	--	--	---	---	---	---	---	---	---	---	--	--	-----

```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



• (•		X	X	X	X	X	Ь	b	а			•••
-----	---	--	---	---	---	---	---	---	---	---	--	--	-----

```
Start:
    If 'a' Goto FoundA
    Move Right
    Goto Start

FoundA:
    Write 'x'
```

LoopA:

Move Right
If 'a' Goto LoopA
If 'x' Goto LoopA
Write 'x'
Goto GoHome



•••	X	X	X	X	X	b	b	а		•••

```
Start:
    If 'a' Goto FoundA
    Move Right
    Goto Start

FoundA:
    Write 'x'
LoopA:
    Move Right
    If 'a' Goto LoopA
    If 'x' Goto LoopA
```

Write 'x'

Goto GoHome



X X X X X	b b	a	•••
-----------	-----	---	-----

```
Start:
   If 'a' Goto FoundA
   Move Right
   Goto Start

FoundA:
   Write 'x'
```

Move Right

LoopA:

If 'a' Goto LoopA
If 'x' Goto LoopA
Write 'x'
Goto GoHome

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
   If 'a' Goto FoundA
   Move Right
   Goto Start

FoundA:
   Write 'x'
```

LoopA:

Move Right
If 'a' Goto LoopA
If 'x' Goto LoopA
Write 'x'
Goto GoHome

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



```
Start:
   If 'a' Goto FoundA
   Move Right
   Goto Start

FoundA:
   Write 'x'
```

Move Right

LoopA:

If 'a' Goto LoopA
If 'x' Goto LoopA
Write 'x'
Goto GoHome

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



```
Start:
    If 'a' Goto FoundA
    Move Right
    Goto Start

FoundA:
    Write 'x'
```

Move Right
If 'a' Goto LoopA
If 'x' Goto LoopA
Write 'x'
Goto GoHome

LoopA:

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left
If Not Blank Goto GoHome
Move Right
Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left

If Not Blank Goto GoHome Move Right Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left

If Not Blank Goto GoHome Move Right Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left
If Not Blank Goto GoHome
Move Right
Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left

If Not Blank Goto GoHome Move Right Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

GoHome: Move Left

If Not Blank Goto GoHome Move Right Goto Start



x x x x x b a	•••
---------------	-----

```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left
If Not Blank Goto GoHome
Move Right
Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

GoHome: Move Left

If Not Blank Goto GoHome Move Right Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left
If Not Blank Goto GoHome
Move Right
Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

GoHome: Move Left

If Not Blank Goto GoHome Move Right Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left

If Not Blank Goto GoHome Move Right Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left
If Not Blank Goto GoHome
Move Right
Goto Start



•••		X	X	X	X	X	X	b	а		•••

```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left

If Not Blank Goto GoHome Move Right Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left

If Not Blank Goto GoHome Move Right Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left
If Not Blank Goto GoHome
Move Right
Goto Start



•••		X	X	X	X	X	X	b	а		•••

```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left

If Not Blank Goto GoHome Move Right Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

Move Left
If Not Blank Goto GoHome
Move Right
Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



Start: If 'a' Goto FoundA Move Right Goto Start FoundA: Write 'x' LoopA: Move Right If 'a' Goto LoopA If 'x' Goto LoopA Write 'x'

Goto GoHome

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



```
Start:
  If 'a' Goto FoundA
 Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
   If 'a' Goto FoundA
   Move Right
   Goto Start
```

FoundA:
 Write 'x'
LoopA:
 Move Right
 If 'a' Goto LoopA
 If 'x' Goto LoopA
 Write 'x'
 Goto GoHome

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



Start: If 'a' Goto FoundA Move Right Goto Start FoundA: Write 'x' LoopA: Move Right If 'a' Goto LoopA If 'x' Goto LoopA Write 'x'

Goto GoHome

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



•••		X	X	X	X	X	X	b	а		•••

```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
   If 'a' Goto FoundA
   Move Right
   Goto Start
```

FoundA:
 Write 'x'
LoopA:
 Move Right
 If 'a' Goto LoopA
 If 'x' Goto LoopA
 Write 'x'
 Goto GoHome

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
 Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
   If 'a' Goto FoundA
   Move Right
   Goto Start
```

FoundA:
 Write 'x'
LoopA:
 Move Right
 If 'a' Goto LoopA
 If 'x' Goto LoopA
 Write 'x'
 Goto GoHome

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



Start: If 'a' Goto FoundA Move Right Goto Start FoundA: Write 'x' LoopA: Move Right If 'a' Goto LoopA If 'x' Goto LoopA Write 'x' Goto GoHome

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



•••		X	X	X	X	X	X	b	а		•••

```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
   If 'a' Goto FoundA
   Move Right
   Goto Start
```

FoundA:
 Write 'x'
LoopA:
 Move Right
 If 'a' Goto LoopA
 If 'x' Goto LoopA
 Write 'x'
 Goto GoHome

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



Start: If 'a' Goto FoundA Move Right Goto Start FoundA: Write 'x' LoopA: Move Right If 'a' Goto LoopA If 'x' Goto LoopA Write 'x' Goto GoHome

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



```
Start:
  If 'a' Goto FoundA
 Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
   If 'a' Goto FoundA
   Move Right
   Goto Start
.
```

FoundA:
 Write 'x'
LoopA:
 Move Right
 If 'a' Goto LoopA
 If 'x' Goto LoopA
 Write 'x'
 Goto GoHome

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
 Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
   If 'a' Goto FoundA
   Move Right
   Goto Start
```

FoundA:
 Write 'x'
LoopA:
 Move Right
 If 'a' Goto LoopA
 If 'x' Goto LoopA
 Write 'x'
 Goto GoHome

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
 Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



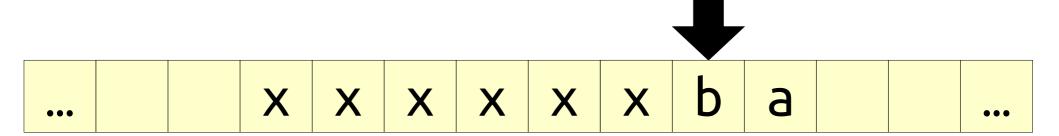
```
Start:
  If 'a' Goto FoundA
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

FoundB:
Write 'x'
LoopB:
Move Right
If 'b' Goto LoopB
If 'x' Goto LoopB
Write 'x'
Goto GoHome



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
 Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
                               Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
  Write 'x'
                               If 'x' Goto LoopB
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



... x x x x x b a

•••

```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
                               Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
  Write 'x'
                               If 'x' Goto LoopB
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



... | x x x x x x x a | ...

```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
 Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
  Write 'x'
                               If 'x' Goto LoopB
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



... | x x x x x x x a | ...

```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
 Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
                               Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```

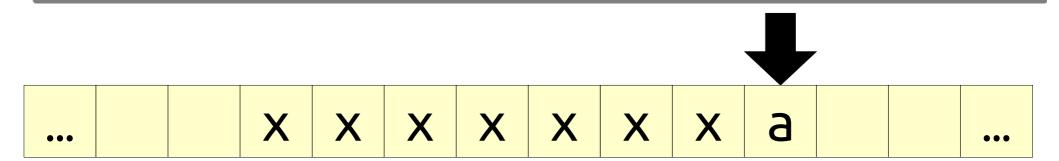


```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
 Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
                               Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
                               If 'b' Goto LoopB
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```

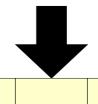


... | x x x x x x x a ...

```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
 Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
  Write 'x'
                               If 'x' Goto LoopB
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



... | x x x x x x x a | ...

```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
  If 'x' Goto LoopA
                               If 'b' Goto LoopB
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

GoHome: Move Left If Not Blank Goto GoHome Move Right Goto Start FoundB:

Write 'x'
LoopB:
 Move Right
 If 'b' Goto LoopB
 If 'x' Goto LoopB
 Write 'x'
 Goto GoHome



... X X X X X X X

```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



... X X X X X X X

```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
```



Goto GoHome

```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

GoHome: Move Left If Not Blank Goto GoHome Move Right Goto Start FoundB: Write 'x' LoopB: Move Right If 'b' Goto LoopB If 'x' Goto LoopB Write 'x' Goto GoHome

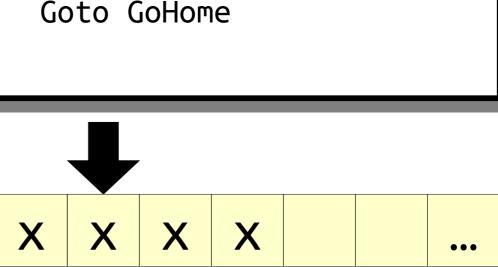


... | X X X X X X X X | ...

```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```

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X



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

GoHome: Move Left If Not Blank Goto GoHome Move Right Goto Start FoundB:

Write 'x'
LoopB:
 Move Right
 If 'b' Goto LoopB
 If 'x' Goto LoopB
 Write 'x'
 Goto GoHome



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

GoHome: Move Left If Not Blank Goto GoHome Move Right Goto Start FoundB:

Write 'x'
LoopB:
 Move Right
 If 'b' Goto LoopB
 If 'x' Goto LoopB
 Write 'x'
 Goto GoHome



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
Move Left
If Not Blank Goto GoHome
Move Right
Goto Start

FoundB:
```

Write 'x'
LoopB:
 Move Right
 If 'b' Goto LoopB
 If 'x' Goto LoopB
 Write 'x'
 Goto GoHome



... X X X X X X X

```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



... X X X X X X X

```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
                             FoundB:
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
Move Left
If Not Blank Goto GoHome
Move Right
Goto Start
Write 'x'
Move Right
If 'b' Goto LoopB
If 'x' Goto LoopB
Write 'x'
Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

GoHome: Move Left If Not Blank Goto GoHome Move Right Goto Start FoundB:

Write 'x'
LoopB:
 Move Right
 If 'b' Goto LoopB
 If 'x' Goto LoopB
 Write 'x'
 Goto GoHome



•••		X	X	X	X	X	X	X	X		•••
•••		•									•••

```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

GoHome: Move Left If Not Blank Goto GoHome Move Right Goto Start FoundB:

Write 'x'
LoopB:
 Move Right
 If 'b' Goto LoopB
 If 'x' Goto LoopB
 Write 'x'
 Goto GoHome



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



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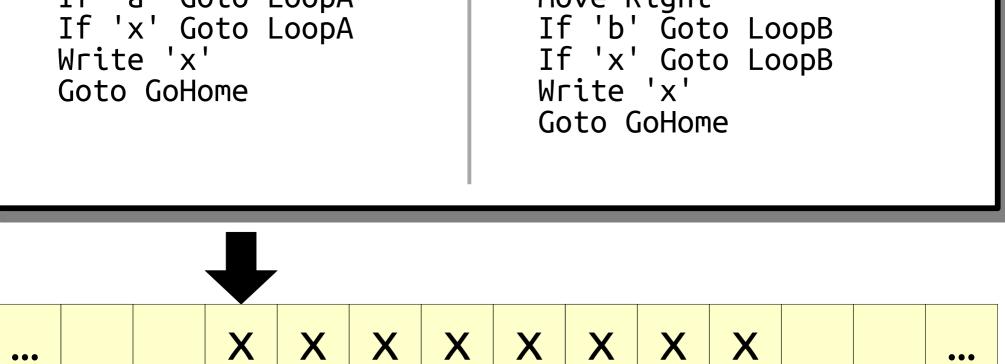
```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
  Write 'x'
                               If 'x' Goto LoopB
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
  If 'x' Goto LoopA
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
   Move Left
   If Not Blank Goto GoHome
   Move Right
   Goto Start
```

FoundB:
 Write 'x'
LoopB:
 Move Right
 If 'b' Goto LoopB
 If 'x' Goto LoopB
 Write 'x'
 Goto GoHome



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start

FoundB:

Write 'x'
LoopB:
 Move Right
 If 'b' Goto LoopB
 If 'x' Goto LoopB
 Write 'x'
 Goto GoHome



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
  Write 'x'
                               If 'x' Goto LoopB
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
                             FoundB:
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```

Move Left If Not Blank Goto GoHome Move Right Goto Start Write 'x' Move Right If 'b' Goto LoopB If 'x' Goto LoopB



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
  Write 'x'
                               If 'x' Goto LoopB
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
  Write 'x'
                               If 'x' Goto LoopB
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
    If 'a' Goto FoundA
    If 'b' Goto FoundB
    Move Right
    Goto Start

FoundA:
    Write 'x'
LoopA:
```

oundA:
Write 'x'
oopA:
Move Right
If 'a' Goto LoopA
If 'x' Goto LoopA
Write 'x'
Goto GoHome

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start

FoundB:
 Write 'x'
LoopB:
 Move Right
 If 'b' Goto LoopB
 If 'x' Goto LoopB
 Write 'x'
 Goto GoHome



... X X X X X X X

```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

GoHome: Move Left If Not Blank Goto GoHome Move Right Goto Start FoundB: Write 'x' LoopB: Move Right If 'b' Goto LoopB If 'x' Goto LoopB



.. | X X X X X X X X

Write 'x'

Goto GoHome

```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
  Write 'x'
                               If 'x' Goto LoopB
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
  Write 'x'
                               If 'x' Goto LoopB
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
  Write 'x'
                               If 'x' Goto LoopB
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
   Move Left
   If Not Blank Goto GoHome
   Move Right
   Goto Start

FoundB:
```

Write 'x'
LoopB:
 Move Right
 If 'b' Goto LoopB
 If 'x' Goto LoopB
 Write 'x'
 Goto GoHome



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
  Write 'x'
                               If 'x' Goto LoopB
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
  Write 'x'
                               If 'x' Goto LoopB
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
  Write 'x'
                               If 'x' Goto LoopB
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
```

Write 'x'

Goto GoHome



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
                               Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
  Write 'x'
                               If 'x' Goto LoopB
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
  Write 'x'
                               If 'x' Goto LoopB
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
 Write 'x'
                             FoundB:
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
                               Goto GoHome
```

Move Left If Not Blank Goto GoHome Move Right Goto Start Write 'x' Move Right If 'b' Goto LoopB If 'x' Goto LoopB Write 'x'



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
  Write 'x'
                               If 'x' Goto LoopB
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
  Write 'x'
                               If 'x' Goto LoopB
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

GoHome: Move Left If Not Blank Goto GoHome Move Right Goto Start FoundB: Write 'x' LoopB: Move Right If 'b' Goto LoopB If 'x' Goto LoopB Write 'x' Goto GoHome



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
                               Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
  Write 'x'
                               If 'x' Goto LoopB
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

GoHome:
 Move Left
 If Not Blank Goto GoHome
 Move Right
 Goto Start

FoundB:

Write 'x'
LoopB:
 Move Right
 If 'b' Goto LoopB
 If 'x' Goto LoopB
 Write 'x'
 Goto GoHome

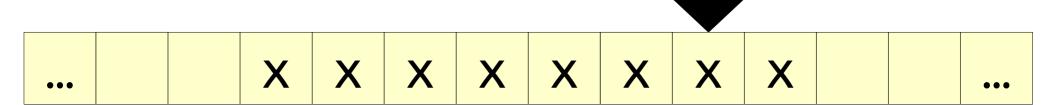


```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

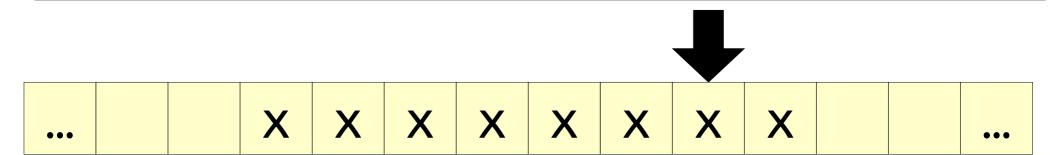
GoHome: Move Left If Not Blank Goto GoHome Move Right Goto Start FoundB: Write 'x' LoopB: Move Right If 'b' Goto LoopB If 'x' Goto LoopB Write 'x' Goto GoHome



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
  Write 'x'
                               If 'x' Goto LoopB
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
   Move Left
   If Not Blank Goto GoHome
   Move Right
   Goto Start

FoundB:
```

Write 'x'
LoopB:
 Move Right
 If 'b' Goto LoopB
 If 'x' Goto LoopB
 Write 'x'
 Goto GoHome



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
   Move Left
   If Not Blank Goto GoHome
   Move Right
   Goto Start

FoundB:
```

Write 'x'
LoopB:
 Move Right
 If 'b' Goto LoopB
 If 'x' Goto LoopB
 Write 'x'
 Goto GoHome



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



... X X X X X X X

```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  Move Right
                               Move Right
  Goto Start
                               Goto Start
FoundA:
  Write 'x'
                             FoundB:
                               Write 'x'
LoopA:
  Move Right
                             LoopB:
  If 'a' Goto LoopA
                               Move Right
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



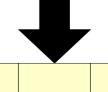
```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
  Move Left
  If Not Blank Goto GoHome
  Move Right
  Goto Start
FoundB:
  Write 'x'
LoopB:
  Move Right
  If 'b' Goto LoopB
  If 'x' Goto LoopB
  Write 'x'
  Goto GoHome
```



| X X X X X X X X | X | .

```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
                               Move Right
  Move Right
                               Goto Start
  Goto Start
FoundA:
                             FoundB:
 Write 'x'
                               Write 'x'
LoopA:
                             LoopB:
                               Move Right
  Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  If Blank Return True
                               Move Right
  Move Right
                               Goto Start
  Goto Start
FoundA:
                             FoundB:
 Write 'x'
                               Write 'x'
LoopA:
                             LoopB:
                               Move Right
  Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  If Blank Return True
                               Move Right
  Move Right
                               Goto Start
  Goto Start
FoundA:
                             FoundB:
 Write 'x'
                               Write 'x'
LoopA:
                             LoopB:
  Move Right
                               Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  If Blank Return True
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
   Move Left
   If Not Blank Goto GoHome
   Move Right
   Goto Start

FoundB:
   Write 'x'
```

HoundB:
Write 'x'
LoopB:
Move Right
If 'b' Goto LoopB
If 'x' Goto LoopB
Write 'x'
Goto GoHome

```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  If Blank Return True
                               Move Right
  Move Right
                               Goto Start
  Goto Start
FoundA:
                             FoundB:
 Write 'x'
                               Write 'x'
                             LoopB:
LoopA:
                               Move Right
  Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



a a

```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  If Blank Return True
  Move Right
  Goto Start
FoundA:
  Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

```
GoHome:
   Move Left
   If Not Blank Goto GoHome
   Move Right
   Goto Start

FoundB:
   Write 'x'
```

Write 'x'
LoopB:
 Move Right
 If 'b' Goto LoopB
 If 'x' Goto LoopB
 Write 'x'
 Goto GoHome



ala

```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  If Blank Return True
                               Move Right
                               Goto Start
  Move Right
  Goto Start
FoundA:
                             FoundB:
 Write 'x'
                               Write 'x'
                             LoopB:
LoopA:
                               Move Right
  Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



aa

```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  If Blank Return True
                               Move Right
  Move Right
                               Goto Start
  Goto Start
FoundA:
                             FoundB:
 Write 'x'
                               Write 'x'
                             LoopB:
LoopA:
                               Move Right
  Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



aa

```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  If Blank Return True
                               Move Right
  Move Right
                               Goto Start
  Goto Start
FoundA:
                             FoundB:
  Write 'x'
                               Write 'x'
                             LoopB:
LoopA:
                               Move Right
  Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



aa

```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  If Blank Return True
                               Move Right
  Move Right
                               Goto Start
  Goto Start
FoundA:
                             FoundB:
  Write 'x'
                               Write 'x'
                             LoopB:
LoopA:
                               Move Right
  Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



x a

```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  If Blank Return True
                               Move Right
  Move Right
                               Goto Start
  Goto Start
FoundA:
                             FoundB:
                               Write 'x'
  Write 'x'
LoopA:
                             LoopB:
 Move Right
                               Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



x a

```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  If Blank Return True
                               Move Right
                               Goto Start
  Move Right
  Goto Start
FoundA:
                             FoundB:
 Write 'x'
                               Write 'x'
                             LoopB:
LoopA:
  Move Right
                               Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



x a

```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  If Blank Return True
                               Move Right
                               Goto Start
  Move Right
  Goto Start
FoundA:
                             FoundB:
 Write 'x'
                               Write 'x'
                             LoopB:
LoopA:
  Move Right
                               Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



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```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  If Blank Return True
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
 Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  Write 'x'
  Goto GoHome
```

GoHome: Move Left If Not Blank Goto GoHome Move Right Goto Start FoundB: Write 'x' LoopB: Move Right If 'b' Goto LoopB If 'x' Goto LoopB Write 'x'

Goto GoHome



x a

```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  If Blank Return True
                               Move Right
  Move Right
                               Goto Start
  Goto Start
FoundA:
                             FoundB:
                               Write 'x'
  Write 'x'
LoopA:
                             LoopB:
 Move Right
                               Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



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```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  If Blank Return True
                               Move Right
                               Goto Start
  Move Right
  Goto Start
FoundA:
                             FoundB:
 Write 'x'
                               Write 'x'
                             LoopB:
LoopA:
  Move Right
                               Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



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```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  If Blank Return True
                               Move Right
                               Goto Start
  Move Right
  Goto Start
FoundA:
                             FoundB:
 Write 'x'
                               Write 'x'
                             LoopB:
LoopA:
  Move Right
                               Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



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```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  If Blank Return True
                               Move Right
                               Goto Start
  Move Right
  Goto Start
FoundA:
                             FoundB:
 Write 'x'
                               Write 'x'
                             LoopB:
LoopA:
 Move Right
                               Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
                               If 'x' Goto LoopB
  If 'x' Goto LoopA
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



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```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  If Blank Return True
                               Move Right
                               Goto Start
  Move Right
  Goto Start
FoundA:
                             FoundB:
 Write 'x'
                               Write 'x'
                             LoopB:
LoopA:
                               Move Right
  Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



... X a

```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  If Blank Return True
                               Move Right
  Move Right
                               Goto Start
  Goto Start
FoundA:
                             FoundB:
 Write 'x'
                               Write 'x'
                             LoopB:
LoopA:
 Move Right
                               Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
                               If 'x' Goto LoopB
  If 'x' Goto LoopA
                               Write 'x'
  Write 'x'
                               Goto GoHome
  Goto GoHome
```



... | X | a

```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  If Blank Return True
                               Move Right
  Move Right
                               Goto Start
  Goto Start
FoundA:
                             FoundB:
 Write 'x'
                               Write 'x'
                             LoopB:
LoopA:
                               Move Right
  Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
                               If 'x' Goto LoopB
  If 'x' Goto LoopA
                               Write 'x'
  Write 'x'
                               Goto GoHome
  Goto GoHome
```



```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  If Blank Return True
                               Move Right
  Move Right
                               Goto Start
  Goto Start
FoundA:
                             FoundB:
 Write 'x'
                               Write 'x'
                             LoopB:
LoopA:
                               Move Right
  Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  If Blank Return False
                               Write 'x'
  Write 'x'
                               Goto GoHome
  Goto GoHome
```



... | X a

```
Start:
  If 'a' Goto FoundA
  If 'b' Goto FoundB
  If Blank Return True
  Move Right
  Goto Start
FoundA:
 Write 'x'
LoopA:
  Move Right
  If 'a' Goto LoopA
  If 'x' Goto LoopA
  If Blank Return False
  Write 'x'
  Goto GoHome
```

GoHome: Move Left If Not Blank Goto GoHome Move Right Goto Start FoundB: Write 'x' LoopB: Move Right If 'b' Goto LoopB If 'x' Goto LoopB Write 'x' Goto GoHome



| X | 8

```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  If Blank Return True
                               Move Right
  Move Right
                               Goto Start
  Goto Start
FoundA:
                             FoundB:
 Write 'x'
                               Write 'x'
                             LoopB:
LoopA:
                               Move Right
  Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  If Blank Return False
                               If Blank Return False
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



. | X | 8

```
Start:
                             GoHome:
  If 'a' Goto FoundA
                               Move Left
  If 'b' Goto FoundB
                               If Not Blank Goto GoHome
  If Blank Return True
                               Move Right
  Move Right
                               Goto Start
  Goto Start
FoundA:
                             FoundB:
 Write 'x'
                               Write 'x'
                             LoopB:
LoopA:
                               Move Right
  Move Right
  If 'a' Goto LoopA
                               If 'b' Goto LoopB
  If 'x' Goto LoopA
                               If 'x' Goto LoopB
  If Blank Return False
                               If Blank Return False
  Write 'x'
                               Write 'x'
  Goto GoHome
                               Goto GoHome
```



... | X a | | | | | | | | | |

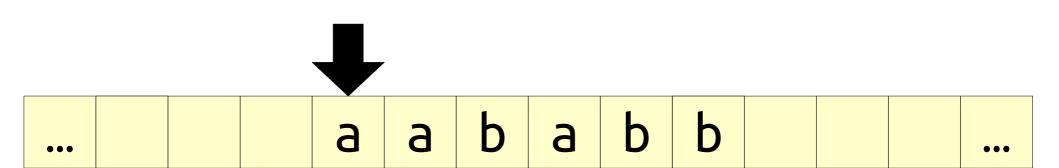
Another Idea

We just built a TM for the language

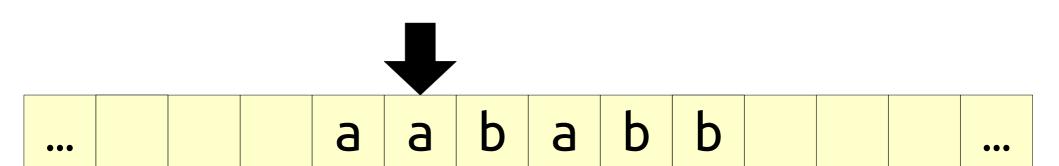
```
\{ w \in \{a, b\}^* \mid w \text{ has the same number of a's and b's } \}.
```

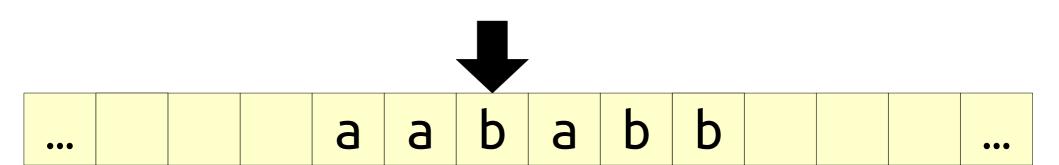
- An observation: this would be a *lot* easier to test for if all the a's came before all the b's.
 - In fact, that would turn this into checking if the string has the form $\mathbf{a}^n\mathbf{b}^n$, which we already know how to do!
- *Idea*: Could we sort the characters of our input string?

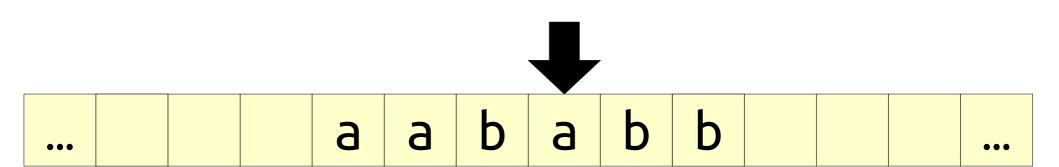
The Idea

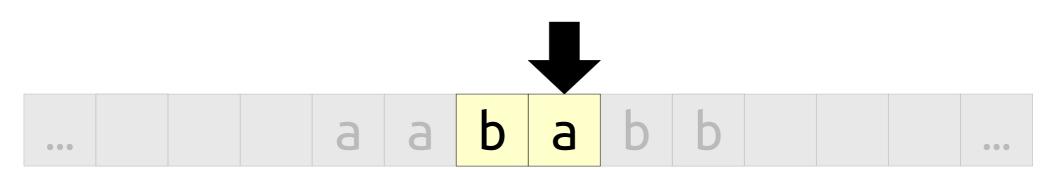


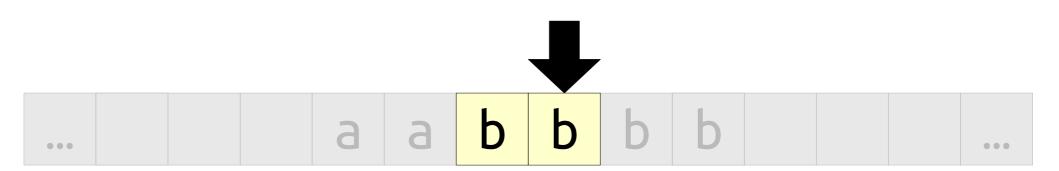
The Idea

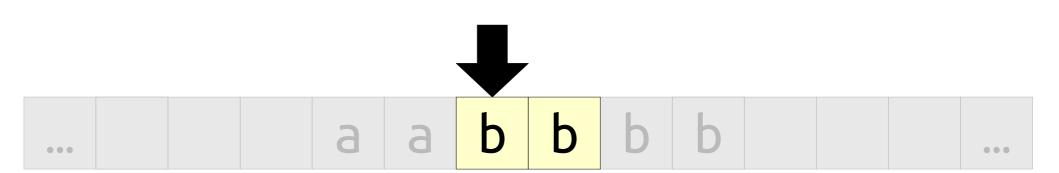


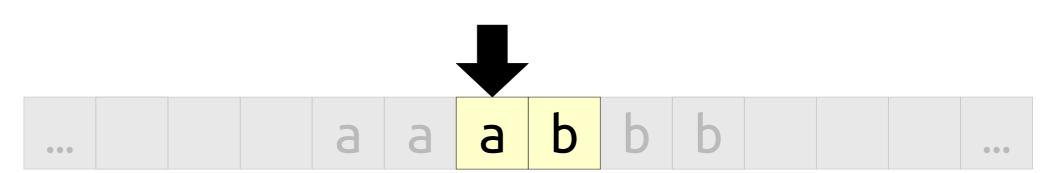


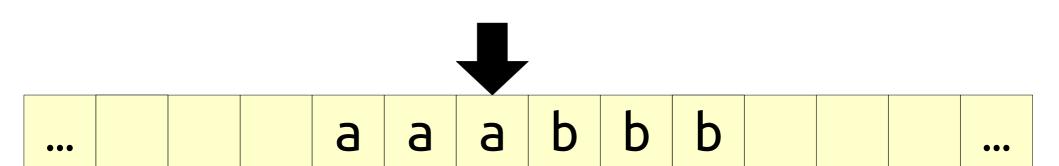








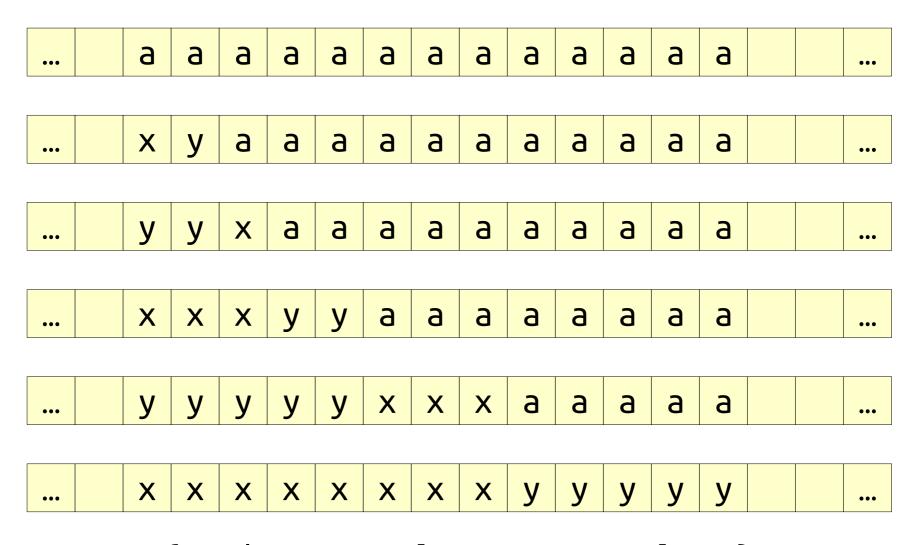




Exploring This Idea



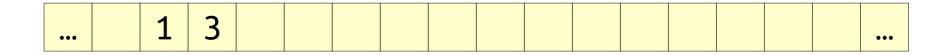
Fibonacci Numbers



{ $\mathbf{a}^n \mid n \text{ is a Fibonacci number }$ }
0, 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, ...



Decimal Fibonacci



```
... a a a a a a a a a a a ... ...
```

```
{ w \in \{0, 1, 2, ... 9\}^* \mid w, interpreted as a base-10 number, is a Fibonacci number. }
```

Summary for Today

- Turing machines are abstract computers that issue commands to an infinite tape subdivided into cells.
- Each step of the TM can move the tape head, change what's on the tape, or jump to a different part of the program.
- TMs can be composed together to build larger TMs out of smaller ones.

Next Time

- The Church-Turing Thesis
 - How powerful are Turing machines?
- Decidability and Recognizability
 - Two notions of "solving a problem."