

## Part 2 -- Written Assignment

1. Convert the following two decimal numbers into 8-bit 2's complement codes.

$$\begin{array}{rcl}
 125 & 125/2 = 62.5 & 1 \\
 & 62/2 = 31 & 0 \\
 & 31/2 = 15.5 & 1 \\
 & 15/2 = 7.5 & 1 \\
 & 7/2 = 3.5 & 1 \\
 & 3/2 = 1.5 & 1 \\
 & 1/2 = .5 & 1
 \end{array}$$

01111101

-125

01111101  $\rightarrow$  10000010  $\rightarrow$  +1  $\rightarrow$  10000011

2. Identify the decimal numbers for the following two 8-bit 2's complement codes.

0101 1101

64 16 8 4 1

Signed and unsigned

$$64 + 16 + 8 + 4 + 1 = 93$$

1100 1101

128 64 32 16 8 4 2 1

Signed

Unsigned

$$11001101 \rightarrow -1 \rightarrow 11001100 \rightarrow 00110011 \rightarrow$$

-51

241

3. Do 8-bit unsigned binary addition for  $45 + 242$ . Do not worry that you have no space for the topmost carry bit (simply discard it as if it did not occur -- we will learn how CPU signal this later).

Show your work.

$$\begin{array}{rcl}
 45/2 = 22.5 & 1 & 242/2 = 121 & 0 \\
 22/2 = 11 & 0 & 121/2 = 60.5 & 1 \\
 11/2 = 5.5 & 1 & 60/2 = 30 & 0 \\
 5/2 = 2.5 & 1 & 30/2 = 15 & 0 \\
 2/2 = 1 & 0 & 15/2 = 7.5 & 1 \\
 1/2 = .5 & 1 & 7/2 = 3.5 & 1 \\
 & & 3/2 = 1.5 & 1 \\
 & & 1/2 = .5 & 1
 \end{array}$$

$$45 = 00101101$$

$$242 = 11110010$$

$$\begin{array}{r}
 00101101 \\
 + 11110010 \\
 \hline
 00011111
 \end{array}$$

$$00011111 = 31$$

4. Do 8-bit 2's complement addition for  $45 + (-14)$ . Note 2's complement addition is done as if both numbers were unsigned. So there is no real difference between 2's complement addition and unsigned addition.

Show your work and confirm the result is correct. Briefly state what you learn here.

$$45 = 00101101$$

$$14/2 = 7 \quad 0$$

$$7/2 = 3.5 \quad 1$$

$$3/2 = 1.5 \quad 1$$

$$1/2 = .5 \quad 1$$

$$14 = 00001110 \quad -14 = 11110010$$

$$\begin{array}{r} 00101101 \\ + 11110010 \\ \hline 00011111 \end{array}$$

$$00011111 = 31$$

This problem demonstrates that 2's Complement elegantly handles positive and negative integer addition. Regular addition between a positive and negative value in two's complement will always be correct.

5. Do the following math the C way:

$$5 * 4 =$$

$$5 = 00000101$$

$$5 * 4 \rightarrow 5 * 2^2 \rightarrow 5 \ll 2 \rightarrow 00000101 \ll 2 = 00010100 \rightarrow$$

$$00010100 = 20$$

$$18 / 4 =$$

$$18 = 00010010$$

$$18 / 4 \rightarrow 18 \cdot 2^{-2} \rightarrow 18 \gg 2 \rightarrow 00010010 \gg 2 = 0000100 = 4$$

Then show how the following C operations are done in binary and the results in decimal?

$$5 \ll 2:$$

$$00000101 \ll 2 = 00010100 = 20$$

$$18 \gg 2:$$

$$00010010 \gg 2 = 0000100 = 4$$

What do you learn from this exercise?

I learned that C is capable of multiplication and division by powers of two using only bit shifting to the left and to the right.