# 6\_17\_2020 all genes

Ethan Ashby

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#### Overview

According to Saptarshi, bootstrapping the frequencies (as performed in '06\_15\_2020\_4\_genes.Rmd') works for generating SE estimates for seen mutations, but does not extend to SE for unseen mutations. Thus, if we chose to pursue a bootstrap method, we would have to conduct a parametric bootstrap, which assumes that each of the  $N_r$ 's are modeled. by a Poisson distribution.

We know that the Good-Turing Probabilities for at least one variant is directly a function of  $N_1$ . What about the SE?

Goal: generate Good-Turing estimates for all genes in the TCGA dataset (non-hypermutated samples) that appear at some frequency threshold (relative freq>0.1 or >10 occurrences). Keep track of SE's and plot against  $N_1$  or rare variants ( $\sum N_r$  for r=1,2,3). Also keep track of the number of times we achieve a problematic slope estimate (b>-1).

## Installing new variantprobs package

Took some finagling. I updated R, the commandline tools. But ultimately it took deleting a 'Makevars' file from ' $\sim$ /usr/.R' to get the package to compile.

## goodTuring\_SE function

I wrote a function which takes in a gene name, and then outputs a list with four elements: (i) a vector of good-turing probabilities for all seen and unseen variants, (ii) the Chao estimate of N0, (iii) the SE of the Good-Turing estimates, (iv) whether the smoothing algorithm provided a logical beta estimate. I used the function 'mclapply' with 8 cores to apply this function over a list of genes with a mutation rate >0.03 (as in the original Somatic Variant richness paper). Runtime was fast and the output was a list containing all the above information.

```
#####
#Filter genes w/ frequency>0.03
#####

num_samps<-length(unique(tcga_nh$patient_id))
#filter variants where mutation rate (num_variants/num_samples)>0.03
filtered_variants<-tcga_nh %>% dplyr::group_by(Hugo_Symbol) %>% dplyr::filter(dplyr::n()/num_samps>0.03
#this produces 858 genes
```

```
filtered_variants$Hugo_Symbol %>% unique() %>% length()

#now define your gene list as these filtered genes
genelist<-filtered_variants$Hugo_Symbol %>% unique()

#takes ~10 seconds to run
variant_stats<-c(mclapply(genelist, goodTuring_SE, mc.cores=8))
names(variant_stats)<-genelist</pre>
```

### Exploring results

Of our 45 genes with adequate mutation rate, 45 achieved acceptable Good-Turing estimates ( $\beta < -1$ ).

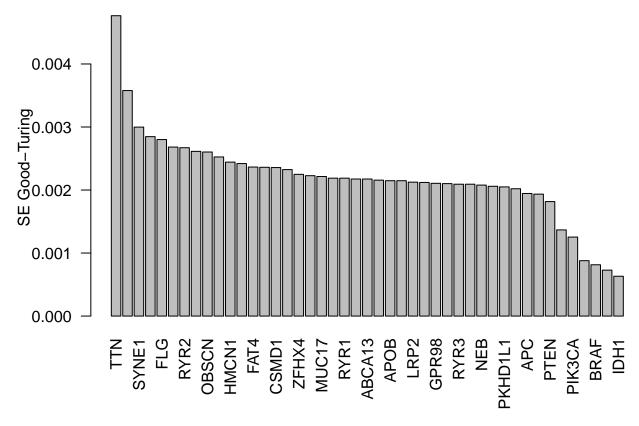


Figure 1: Barplot of ordered Good-Turing standard errors for 45 genes that met mutation frequency criteria

The majority of Good-Turing standard errors fell within [0.002, 0.003] (Figure 1). A density plot of the Good-Turing standard errors shows positive kurtosis 3.3529303(relatively less weight in tails) a slight right-skew 0.5401474 (Figure 2.)

A plot of the Good-Turing standard errors against the gene-wise  $N_1$  values indicated that these standard errors are a logarithmic function of  $N_1$  (Figure 3).

To further investigate this, I fit a variety of logarithmic functions to these data using the package in R. The best fit I obtained was a Log-logistic function with 3 parameters, that practically interpolated the data (sum of squared residuals= $1.8560061 \times 10^{-8}$ ).

$$f(x) = 0 + \frac{d - 0}{1 + \exp(b * (\log(x) - e))}$$

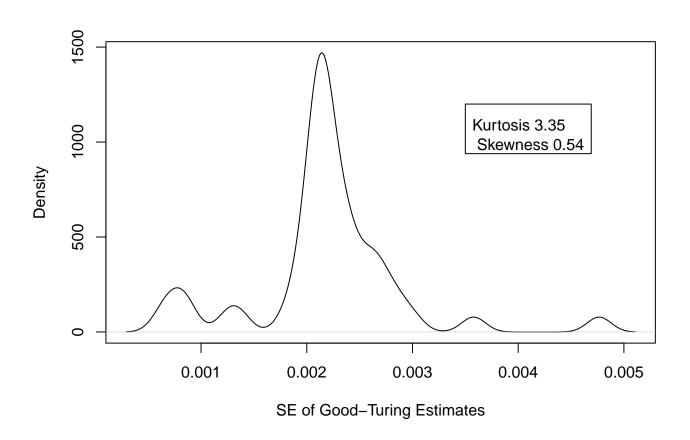


Figure 2: Right-skewed density of Good-Turing Standard Errors

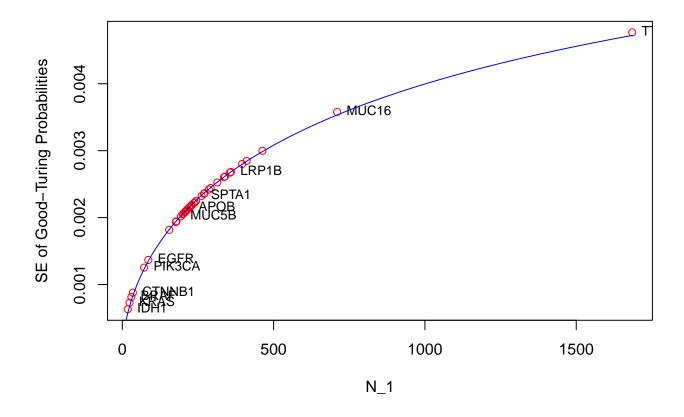


Figure 3: Relationship between N\_1 and SE of Good-Turing Unseen Variants Probabilities

The parameter values for log-logistic function are shown in the table below.

I validated that my bootstrap method which samples variant frequencies does not perform well at capturing the SE of P(one or more unseen variant).