1 Mathematics

Sound & Light (1)

1.1 Miscellaneous

$$\% \text{ error} = \frac{\text{observed - theoretical}}{\text{theoretical}} * 100\%$$

1.2 Kinematics

$$x = \frac{a}{2}(\Delta t)^2 + v_0 \Delta t + x_0 \qquad v = v_0 + a \Delta t$$
$$v^2 = v_0^2 + 2a \Delta x \qquad \Delta x = \frac{v_0 + v}{2} * \Delta t$$

1.3 Simple Harmonic Motion

$$x = A\cos(\omega t + \varphi)$$
 $v = -\omega A\cos(\omega t + \varphi)$ $a = -\omega^2 A\cos(\omega t + \varphi)$
 $x_{\text{max}} = A$ $v_{\text{max}} = \omega A$ $a_{\text{max}} = \omega^2 A$ $F_{\text{max}} = m\omega^2 A$

1.3.1 Springs and Slinkies

$$F_s = kx \qquad F_{s_{\max}} = kx_0 = mg$$

$$f = \frac{1}{2\pi} \sqrt{\frac{k}{m}} \qquad T = 2\pi \sqrt{\frac{m}{k}} \qquad \omega = 2\pi f = \sqrt{\frac{m}{k}}$$

$$SPE = \frac{1}{2}kx^2 \qquad KE = \frac{1}{2}mv^2$$

$$TME = \frac{1}{2}kx^2 + \frac{1}{2}mv^2 = \frac{1}{2}kA^2 = \frac{1}{2}mv_{\max}^2$$

1.3.2 Pendulums

$$f = \frac{1}{2\pi} \sqrt{\frac{g}{L}}$$
 $T = 2\pi \sqrt{\frac{L}{g}}$

1.4 Waves

$$T = \frac{1}{f}$$
 $v = \lambda f$ $v = \frac{\Delta x}{\Delta t}$

1.4.1 Slinkies and strings with fixed ends

$$F_T = F_s = kx$$
 $\mu = \frac{m}{L}$ $v = \sqrt{\frac{F_T}{\mu}}$

Given mass m_T hanging below a pulley, $F_T = m_T g$.

1.5 Standing waves

1.5.1 Open-open, closed-closed

n is the number of antinodes, or the n^{th} harmonic.

$$f_n = f_1 n = \frac{nv}{2L}$$
 $f_1 = \frac{v}{2L}$ $\lambda_n = \frac{2L}{n}$

1.5.2 Open-closed

$$f_n = f_1 n = \frac{nv}{4L}$$
 $f_1 = \frac{v}{4L}$ $\lambda_n = \frac{2L}{n}$

1.6 Sound

1.6.1 Speed of sound

$$v = 331\sqrt{\frac{T_{^{\circ}\text{C}} + 273}{273}}$$
 $v \approx 331 + 0.59T$

1.6.2 Sound intensity

$$I = \frac{\text{Power (W)}}{\text{Area}} = \frac{\text{Power (W)}}{4\pi r^2}$$

$$I_{\text{dB}} = 10 \log_{10} \left(\frac{I}{10^{-12}} \right) \qquad I = 10^{\frac{I_{\text{dB}}}{10} - 12}$$

1.6.3 Doppler effect

$$S \rightarrow O$$
 $f_o = f_s \frac{v}{v - v_s}$ O $S \rightarrow f_o = f_s \frac{v}{v + v_s}$

$$\boxed{S} \rightarrow \leftarrow \boxed{O} \quad f_o = f_s \frac{v + v_o}{v - v_s} \qquad \boxed{O} \rightarrow \boxed{S} \rightarrow \quad f_o = f_s \frac{v + v_o}{v + v_s}$$

$$\boxed{S} \rightarrow \boxed{O} \rightarrow \quad f_o = f_s \frac{v - v_o}{v - v_s} \qquad \leftarrow \boxed{O} \boxed{S} \rightarrow \quad f_o = f_s \frac{v - v_o}{v + v_s}$$