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Bachelor Thesis

Econometrics meets AI:
Predicting Airbnb prices using Machine Learning

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Abstract

Predictive models for Airbnb rental prices are built using Data Mining techniques and Machine Learning algorithms. The goal is to provide an accurate and scalable statistical toolkit for economic agents to make optimal decisions. It is found that Artificial Intelligence models outperform traditional econometric methods at the expense of interpretability, for which a solution is proposed.

Keywords: Algorithms, ML Modeling, Bayesian Statistics, XAI

Mediante técnicas de minería de datos y algoritmos de Machine Learning, se estiman diferentes modelos predictivos para precios de Airbnb. El objetivo es proveer a los agentes económicos de una herramienta estadística precisa y escalable para tomar decisiones óptimas. Se encuentra que los modelos de Inteligencia Artificial superan en rendimiento predictivo a los métodos econométricos clásicos al precio de una menor interpretabilidad, para lo cual se propone una solución.

Keywords: Algoritmos, Modelización ML, Estadística Bayesiana, XAI

1 Introduction

Economic agents face various utility optimization problems on a daily basis. For instance, firms seek to maximize revenue subject to a cost function and input constraints. Households, on the other hand, choose optimal consumption bundles given a specific budget and individual preferences. Likewise, central banks conduct monetary policy by setting interest rates to attain price stability, maximizing social welfare (Herrero and del Río, 2003).

Nowadays, society is immersed in the Big Data era, where numerous data sources are available for agents to make informed decisions. Pernagallo and Torrisi (2019) argue that real time communication networks and continuous technological breakthroughs result in information overload, ultimately overwhelming economic agents. What used to be scarce data has become massively accessible to the public.

Hardly any market is resilient to this issue and even experienced users may struggle to effectively process data to make profitable transactions. Agents might benefit from applying Machine Learning (ML) to large datasets, automating decision-making as shown by Bajari et al. (2015).

Consequently, Artificial Intelligence (AI) could be used to overcome agents' limited computational capacity in the form of ML and Deep Learning (DL) models. However, predictive models that stem from sophisticated algorithms suffer from the so-called 'black box' problem. Said issue is a longstanding concern related with the lack of interpretability of AI models. Rudin (2019) reviewed the tradeoffs of favoring such models over interpretable ones and concluded that the former are not always necessary to successfully fulfill predictive tasks.

In this paper predictive accuracy and model interpretability commutation is studied for the real estate market. An AI framework for solving economic agents' utility optimization problem is proposed using online Airbnb listings data. Several ML and DL models will be built to accurately predict rental pricing in Los Angeles for June 2022, providing eXplainable Artificial Intelligence (XAI) methods to understand contributing factors to final predictions.

The paper is structured as follows: Section II briefly introduces concepts and definitions related to AI. Section III reviews AI applications in Econometrics. Section IV presents the utility maximization problem that is solved for real estate economic agents, describes the relevant dataset and presents Statistical Inference results. Section V explains ML notation and methodological aspects. Section VI provides insights into modeling and XAI. Finally, Section VII concludes and identifies some limitations of the AI framework.

2 Basic Concepts of AI

Grewal (2014) defines AI as “*the mechanical simulation system*” of human intelligence that collects knowledge and information for “*processing intelligence of universe and disseminating it to the eligible in the form of actionable intelligence*”. Indeed, what has made AI stand out is the ability to build intelligent systems that reproduce human cognition.

Machine Learning, as expounded by Mithell (1997), is a subfield of AI “*concerned with the question of how to construct computer programs that automatically improve with experience*”. When the family of learning algorithms used for predictive tasks are Neural Networks, ML is called Deep Learning. DL specifically focuses on developing various model architectures that mimic biological neural networks.

Despite being used almost interchangeably, AI models and algorithms are not identical concepts. An algorithm is “*a procedure that is run on data to create a model*” (Brownlee, 2020). Algorithms *learn* by being fit to datasets. Contrastingly, a model is the output of AI algorithms, as well as the set of assumptions and restrictions on the joint distribution of the predictors and target variable. Thus, an AI model encompasses several algorithms and defines theoretical and empirical rules followed by the latter.

Even though ML and DL are usually linked with Data Science rather than Statistics, a considerable number of AI algorithms are built upon the latter (if not the vast majority). Not coincidentally, as it will be rapidly noticed by Data Analytics professionals such as econometricians and statisticians when reading Section V, AI algorithms extend or slightly change ‘traditional’ quantitative methods.

3 Econometrics and AI

In fact, econometricians have been using ML and DL algorithms for some time. For example, Angrist and Frandsen (2019) resorted to ML for automating the selection of control variables, reducing bias in the reduced form equation of the Two-Stage Least Squares (TSLS) estimator. With respect to policy evaluation, Dube et al. (2021) estimated the impact of minimum wages on employment and income with Classification And Regression Tree (CART) algorithms, greedy function approximations and regularized logistic regression. Hansen et al. (2018) studied how external communication of internal deliberation impacted monetary policy decisions of the Federal Open Market Committee (FOMC) using Natural Language Processing. These are instances of how econometricians can benefit from adopting ML.

With respect to the specific study of rental prices, econometricians have largely focused on hedonic models, a class of linear regression models that estimates the monetary value contribution of different variables such as location, air pollution and number of rooms to prices. Apart from deriving causal effects, sheer prediction was also in the interest of certain research.

Recently, ML and DL algorithms have been widely adopted by econometricians, showing a considerable improvement in predictive performance over OLS estimation method. Limsombunchai et al. (2004) compared Artificial Neural Networks with classical hedonic price models and concluded that DL algorithms outperformed the latter in predictive terms. Embaye et al. (2021) resorted to algorithms such as Random Forest and Gradient Boosting Machine, procuring better results than OLS estimation. It was noted, however, that the explanatory capacity of ML algorithms was scarce.

Even though AI algorithms clearly ousted OLS, this is not to say that it is possible to adopt them for every purpose. Econometrics is the “*the application of mathematics and statistical methods to the analysis of economic data*” (Kayode and Tang, 2013), mainly aiming to establish causality between economic variables. ML and DL are mostly about finding functions that best map covariates with the target variable. Optimal data fitting is not enough to explain relationships between variables, let alone derive causal effects.

Moreover, lack of interpretability is hindering human capacity to oversight and understand the predictions of AI models. While econometricians have developed numerous statistical tests and draw much of their attention to correctly interpreting model outputs, the AI community’s focalpoint has been refining performance of algorithms. Nevertheless, there is growing interest in building mathematical tools for model interpretability and XAI methods will be applied to the champion model (best performing algorithm) in section V.

4 Utility Maximization Problem & Airbnb Data

4.1 Utility function

The statistical toolkit to be built with AI algorithms serves the purpose of assisting economic agents in making optimal decisions. Naturally, a utility function has to be defined to understand how predictive models can contribute to such goal.

Let the i^{th} agent’s problem be expressed as:

$$\begin{aligned} \arg \max_{\hat{p}_i} u_i(\mathbf{x}_i, \hat{p}_i, s_{ij}) &= \sum_{j=1}^n \beta_j u_i(s_{ij}) - |p_i - \hat{p}_i| \\ \text{s.t. } \hat{p}_i &= f(y_i | \mathbf{x}_i; \mathbf{w}_i) \end{aligned} \tag{1}$$

Where $\beta_j \in (0, 1)$ is the importance given by the agent to $u_i(s_{i,j})$, a function dependent on unobservable subjective factors, p_i is the actual listing price and \hat{p}_i is the predicted price. Note that if either data or prior beliefs were available for $u_i(s_{ij})$, it could be incorporated into AI algorithms and thus estimated.

Since the first term of the utility maximization problem cannot be tackled by AI, predictive models optimize agents’ utility by providing accurate predictions in the sense that $|p_i - \hat{p}_i|$ is minimized.

In economic terms, an Airbnb guests benefit from identifying fair priced listings, while real estate firms and Airbnb hosts obtain price margins for their marketing strategy.

4.2 Listings Data

To solve the optimization problem above data is needed to calculate \hat{p}_i . The datasets used in this paper were created by Inside Airbnb, a mission driven project that seeks to debate the role of renting residential homes to tourists with data. Inside Aibnb collects quarterly information about Airbnb listings across different countries via web scrapping and makes it available for the public.

Concretely, the city of Los Angeles was chosen to be analyzed during June 2022. A total of 42,041 listings are included with 74 different characteristics. After some data cleaning and feature engineering steps to be expounded in the next section 41,853 listings and 75 predictors were used for modeling. Although the reader may check the appendix for further details, the variables of the listings dataset can be generally classified into four groups: geographical data, personal information about hosts (name, profile picture, total active time in Airbnb, etc), residential houses characteristics (number of bathrooms, amenities, availability, etc) and rating metrics of listings (cleanliness, communication ...).

Additionally, a specific dataset of Airbnb guests' reviews was incorporated into the analysis, amounting to 1,511,891 opinions about 32,413 distinct listings. Only comments written in the English language were considered, so the final dataset ended up with 1,460,047 records. The dimensions of the listings and reviews datasets considerably vary, making it imperative to perform Data Mining before combining both into a joint database. For such purpose, different data preprocessing techniques have to be applied to the reviews dataset in order to turn originally unstructured data into an acceptable format for predictive modeling.

4.3 Feature Engineering

Feature Engineering is the “*process of using domain knowledge to select and transform the most relevant variables from raw data*” (Ng, 2019). For instance, the target variable price was transformed by taking logarithms to address skewed data. Also, since some information originally available in the datasets was of no predictive use, several predictors were ruled out. For an explanation of the final data matrix please refer to the appendix.

4.3.1 Data Imputation Algorithms

One of the drawbacks of web scrapping is that it may not be possible to retrieve all the data about specific individuals. Additionally, sometimes hosts simply do not post complete information about listings.

Although generally perceived as an analytical obstacle, missing data can be indicative of certain patterns. Indeed, creating features by one-hot encoding the presence of null values has proven to be highly effective in Kaggle competitions (Pandey, 2020).

Once missing data is accounted for with one-hot encoding, data imputation comes into play. Estimating null values is much preferable over eliminating observations that lack some variables since a considerable information loss would be caused. Nonetheless, it is sometimes justified to directly delete some data rows if their number is negligible. Actually, in this paper inactive users were directly discarded.

A custom k-nearest neighbor algorithm (k-NN) and MICE algorithm (Multivariate Imputation by Chained Equations) were applied to impute data.

For the custom k-NN algorithm, three statistical distance matrices were computed on non-missing data: Mahalanobis distance for quantitative predictors, Jaccard distance for binary variables and Hamming distance for the rest of categorical features. Following Chomboon et al. (2015), Mahalanobis distance was preferred over commonly used Euclidean distance since the former accounts for correlation between covariates and remains unchanged after scale changes. As for Jaccard and Hamming distance matrices, they were suitable metrics for non-continuous data. Based on a combination of these distances (called Gower distance matrix), the six nearest neighbors were identified for each listing in the dataset. Leveraging such information, missing data was imputed by taking the median value of the neighbors.

As for MICE algorithm, it was implemented as described by van Buuren and Groothuis-Oudshoorn (2011). MICE combines predicted values for missing data from m copies of the original incomplete dataset into a pooled estimate. Prediction is flexible since different estimators are allowed (Bayesian Ridge Regression and Random Forest were chosen). Pseudo-code was written as a summary of how the algorithm works in the appendix.

4.3.2 Natural Language Processing

Natural Language Processing (NLP) techniques were used to extract information from the unstructured reviews dataset. Emojis, symbols, punctuation and internet links were removed to clean the data. Then text was forced to lowercase and non-English comments were eliminated as to maximize homogeneity among users' comments. Most importantly, the opinion expressed by Airbnb guests was extracted by performing Sentiment Analysis.

Unfortunately, no score rating metric was available so training a NLP model was unfeasible since there were no labels. However, by defining regular expressions (regex) and tweaking VADER (Valence Aware Dictionary and sEntiment Reasoner), a lexicon and rule-based sentiment analysis tool attuned to social media created by developers Hutto and Gilbert (2014), sentiment was estimated in an unsupervised manner.

Gender was guessed based on a database containing 40,000 first names collected by Michael (2006), since hosts' names were available.

4.3.3 Computer Vision

The original dataset provided personal information about hosts, among which an internet link to their profile picture was available. For those hosts that did upload a photograph, a Computer Vision (CV) model was passed to predict their gender.

Resorting to transfer learning, a pre-trained model built by Serengil (2020) was used to guess hosts' gender. Firms and couples were assigned a third category within the gender feature. Sample images displaying the CV model performance are shown:

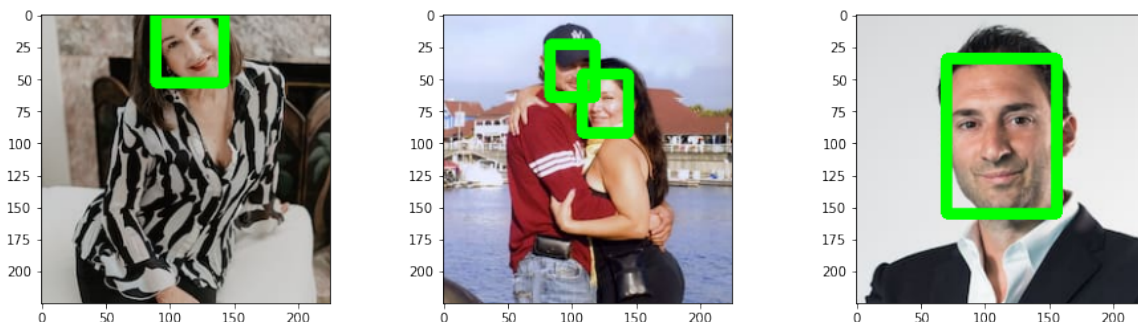


Figure 1: Face Recognition with CV

4.4 Tackling online myths: Statistical Inference

According to The Conversation (2022), the wage gap persists even in the sharing economy. Statistical analysis can shed light on the truth of such statement. A hypothesis test is proposed to verify whether the median price set by women is truly lower than their male counterpart. Let y_m denote the transformed median price, formally we seek to test:

$$H_0 : y_m^{\varphi} < y_m^{\sigma}$$

$$H_1 : y_m^{\varphi} = y_m^{\sigma}$$

Probability distributions for describing the likelihood function and prior beliefs of y^i for $i \in \{\varphi, \sigma\}$ are needed. Five continuous density functions were fit to female and male prices to identify which one modeled such variables best.

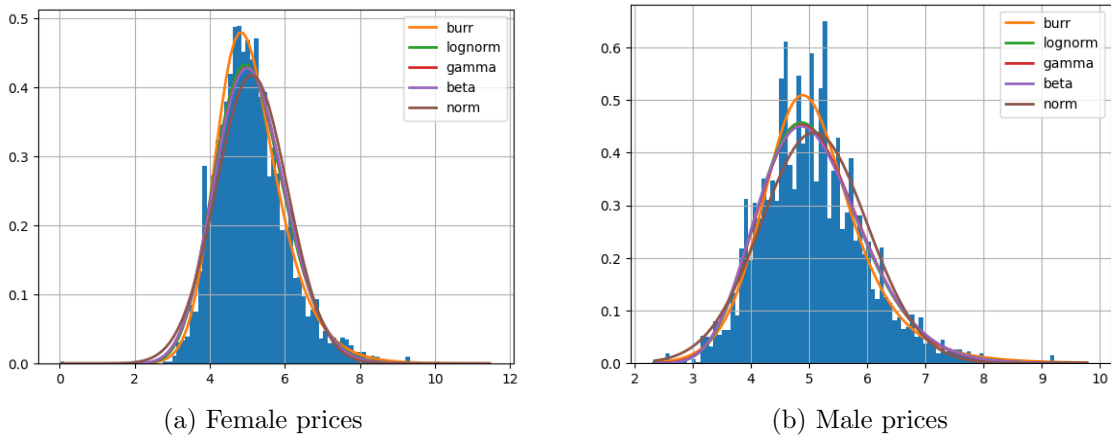


Figure 2: Probability distributions

According to goodness of fit metrics such as sum of squared error, Akaike's Information Criteria (AIC) and Bayesian Information Criteria (BIC), the Burr Type III distribution was the preferred density function (details provided in the appendix).

Now a prior belief has to be defined for a parameter of the Burr distribution. Let $y^i | \theta \sim \text{Burr}(\omega, \theta)$, then a conjugate prior is $\theta \sim \text{Gamma}(\alpha, \beta)$.

It is proved in the appendix that the marginal distribution of y^i after obtaining the posterior distribution $p(\theta | y_1^i, \dots, y_n^i)$ takes the form $y^i \sim \text{Pareto}(\alpha + n, \beta + \sum_{i=1}^n \ln(1 + y_i^{-\omega}))$.

Thus, we can obtain the probability that the median female price is less than the median male price by sampling from the predictive distribution for each gender.

After 300 Monte Carlo simulations, it was noted that results were sensitive to a tolerance threshold $|y_m^{\text{♀}} - y_m^{\text{♂}}| \geq \varepsilon$. For $\varepsilon = 0$, the probability of the female median price being smaller than the male median price was 1. Nevertheless, differences were not significantly large and so if ε was set to the median difference value between gender prices across all Monte Carlo simulations it was obtained that $\Pr(H_1|y) = 0.5$. Furthermore, the remaining 0.5 probability is evenly distributed among $\Pr(H_0|y)$ and $\Pr(y_m^{\text{♀}} > y_m^{\text{♂}})$, so there is no evidence of a wage gap in Airbnb. A frequentist sign test revealed the same outcome.

5 Methodology

5.1 Machine Learning notation

Despite mutually sharing various concepts, ML has adopted new terminology for well-established labels in Econometrics. Athey and Imbens (2019) name a few:

- Regression in ML is only applied in cases where the ‘*target*’ (dependent variable or regressand) is continuous. For discrete targets ‘*classification*’ is performed (even though logistic regression might be used for such tasks).
- The sample data to estimate parameters is renamed to ‘*training set*’.
- Regressors, predictors or covariates become ‘*features*’ and parameters are often referred to as ‘*weights*’.

For the sake of consistency, ML nomenclature will be used, although when necessary the econometric analogues will be mentioned.

Thus, the listings dataset $\mathcal{D} = \{\mathbf{x}_i, y_i\}_{i=1}^n$ is composed of feature vectors $\mathbf{x}_i \in \mathfrak{R}^n$ and a target vector $\mathbf{y} \in \mathfrak{R}^n$. Each \mathbf{x}_i contains data for the i^{th} listing, concretely p random variables or features for n total observations. If stacked together, feature vectors lead to feature matrix $\mathbf{X} \in \mathfrak{R}^{n \times p}$.

Since there exists a target vector \mathbf{y} and $y_i \in \mathfrak{R} \forall i$, predicting Airbnb prices is a *supervised learning* task (specifically a *regression* problem). Such problem will be solved by estimating the target function $f(\mathbf{y}|\mathbf{X}; \mathbf{w})$, which maps feature vectors \mathbf{x}_i to target vector \mathbf{y} through weights $\mathbf{w} \in \mathfrak{R}^p$ (non-parametric models are not considered).

Dataset \mathcal{D} will be randomly partitioned into three sets: training set \mathcal{T} , validation set \mathcal{V} and test set \mathcal{F} so that $\mathcal{T}, \mathcal{V}, \mathcal{F} \subseteq \mathcal{D}$. Specifically, these sets amount to 77%, 14%, 9% of total data (training, validation and test, respectively).

Algorithms learn from the training set \mathcal{T} optimizing a cost function (sum of individual loss functions) $J(\mathbf{w}, \boldsymbol{\lambda}) = \frac{1}{n} \sum_i L_i(\mathbf{w}_i, \boldsymbol{\lambda}_i)$ and \hat{w}_i are obtained by performing cross-validation. This entails that hyperparameters $\boldsymbol{\lambda}$ (user-specified values to control the learning process) are tuned on the validation set and then assessed in \mathcal{F} so as to obtain an unbiased estimate of model performance.

Root Mean Squared Error (RMSE) is the chosen model performance metric to select the champion model. Chai (2014) lists some desirable properties such as sharing in the same measurement units as the target and satisfying the triangle inequality requirement for a distance metric.

A graphical illustration of the AI framework to be followed is available in the appendix.

5.2 Cross-Validation

After having learned from the training set and been refined with the validation set, the AI algorithm can be assessed in the test set and study its performance.

During the refining process, not only weights are optimized to attain accurate results but hyperparameters $\boldsymbol{\lambda}$ are also included in the cost function. These hyperparameters serve the purpose of regularizing AI algorithms, acting as “*penalty terms in the loss function*” (Bishop, 1995). Shrinking \mathbf{w} during the learning process through $\boldsymbol{\lambda}$ leads to better generalization on test data. Otherwise AI algorithms tend to *overfit* the training data, procuring noticeable worse results when exposed to non-training instances.

Finding optimal hyperparameters is no trivial task since $\boldsymbol{\lambda}$ is manually selected by the AI practitioner. Some popular methods are Grid Search and Random Search, where a

vector of user-defined hyperparameter values are tried during training. Although for some tasks such approaches are sufficient, they are highly inefficient. Bergstra et al. (2011) developed a series of greedy algorithms that leverage past evaluations of hyperparameter values to select the most promising λ to evaluate in $J(\mathbf{w}, \lambda)$. For that purpose, Bayesian Inference is performed on a probabilistic model (surrogate model).

Two probability distributions are defined based on the following rule: values of λ that increase model accuracy are part of $l(\lambda)$, whereas poor performing values of hyperparameters belong to $g(\lambda)$. Tree Parzen Estimator (TPE) is a greedy algorithm that maximizes the expected improvement in model performance based on hyperparameter values drawn from these probability distributions. Clearly, the ratio $\frac{g(\lambda)}{l(\lambda)}$ is desired to be minimized, since optimal hyperparameter values λ^* should be drawn from probability distribution $l(\lambda)$ rather than $g(\lambda)$. Prior beliefs $p(\lambda)$ are updated at each evaluation, yielding posterior distribution $p(\lambda^*|\mathbf{y})$. The following pseudo-code gives additional details on how TPE works to find the best hyperparameter values.

Algorithm 1: Tree Parzen Estimator

Input: Prior probability distribution $p(\lambda)$

Output: Optimal hyperparameters λ^*

1 Set probabilistic domain of hyperparameters: $\lambda \sim p(\lambda)$

2 Define $J(\mathbf{w}, \lambda) = \sum_{i=1}^n L_i(\mathbf{w}_i, \lambda_i)$

3 Construct probability distributions $p(\lambda|\mathbf{y}) = \begin{cases} l(\lambda) & \text{if } y < y^* \\ g(\lambda) & \text{if } y \geq y^* \end{cases}$

4 Build surrogate model $p(\mathbf{y}|\lambda) = \frac{p(\lambda|\mathbf{y})p(\mathbf{y})}{p(\lambda)}$

5 **for** $t = 1, \dots, n$ **do**

/* Update $\lambda^{(t)}$ */

$$\lambda^{(t+1)} = \arg \max_{y^*} \int_{-\infty}^{y^*} (y^* - y) \frac{p(\lambda^{(t)}|\mathbf{y})p(\mathbf{y})}{p(\lambda^{(t)})} \partial y$$

6 Obtain optimal weights $\hat{\mathbf{w}} = \arg \min_{\mathbf{w}} \frac{1}{n} \sum_{i=1}^n L_i(\mathbf{w}_i, \lambda_i^*)$

A graphical representation is available in the appendix.

6 Machine Learning Modeling

6.1 Bayesian Ridge Regression

An empirical Bayesian learning framework is proposed as the baseline model. Given prior knowledge on weights \mathbf{w} , Bayes' Theorem will be used to update such distribution of beliefs over the model space. Bayesian modeling offers some advantages (Bishop, 2006):

- **Measurability of prediction uncertainty:** Bayesian Inference procures a probability distribution for weights, allowing to quantify uncertainty around model outputs by estimating conditional distribution $p(\mathbf{y}|\mathbf{x})$.
- **Good generalization performance:** Facilitated by imposing a complexity penalty term in the form of a conditional prior probability distribution $p(\mathbf{w}|\boldsymbol{\lambda})$.
- **Sparsity of inferred predictors:** Many of the weights exhibit posterior distributions $p(\mathbf{w}, \boldsymbol{\lambda}, \alpha|\mathbf{y})$ that are sharply peaked around zero, so the learned algorithm makes predictions based on the most relevant features. Thus, feature selection is carried out in a similar fashion to Least Absolute Shrinkage and Selection Operator (LASSO) Regression.

The Bayesian Ridge Regression Model to be estimated is expressed as:

$$\mathbf{y} = f(\mathbf{y}|\mathbf{X}; \mathbf{w}) + \boldsymbol{\varepsilon} \quad (2)$$

For which a set of restrictions on the joint distribution of $\{\mathbf{x}_i, y_i\}$ is imposed:

- Stochastic process $\{\mathbf{x}_i, y_i\}$ originates from random sampling.
- The parametrized conditional density function is linear $f(\mathbf{y}|\mathbf{X}; \mathbf{w}) = \mathbf{X}\mathbf{w}$
- The prior distribution of target vector \mathbf{y} is $p(\mathbf{y}|\mathbf{X}, \mathbf{w}, \boldsymbol{\alpha}) = \mathcal{N}(\mathbf{X}\mathbf{w}, \sigma^2\mathbf{I}_p)$
- The prior distribution of coefficient vector \mathbf{w} is $p(\mathbf{w}|\boldsymbol{\lambda}) = \mathcal{N}(\mathbf{0}, \boldsymbol{\lambda}^{-1}\mathbf{I}_p)$
- ε_i are samples drawn from a noise process such that $\boldsymbol{\varepsilon} \stackrel{\text{i.i.d}}{\sim} \mathcal{N}(\mathbf{0}, \sigma^2\mathbf{I}_p)$

Even if an economic agent has no real estate market expertise knowledge, Bayesian Inference allows the parameters of a prior distribution to be estimated from data by building hierarchical models (Gelman et al., 2021). In order to do that, marginal probability functions have to be defined for hyperpriors $\boldsymbol{\lambda}$ and σ^2 , introducing an additional level of beliefs. Specifically:

$$p(\boldsymbol{\lambda}) = \prod_{i=0}^n \frac{\beta^\alpha}{\Gamma(\alpha)} \lambda_i^{\alpha-1} e^{-\lambda_i/\beta}, \quad p(\sigma^2) = \frac{\theta^\delta}{\Gamma(\delta)} \sigma^{2(\delta-1)} e^{-\sigma^2\theta} \quad (3)$$

Note that hyperpriors follow a Gamma distribution, a selection justified by the fact that when operating with the previously assumed distributions $p(\mathbf{y}|\mathbf{X}, \mathbf{w}, \boldsymbol{\alpha})$ and $p(\mathbf{w}|\boldsymbol{\lambda})$, an analytical result can be derived thanks to conjugate priors. Consequently, there is no need to resort to Markov Chain Monte Carlo (MCMC) algorithms for sampling posterior distributions. As an example, the first three weight posterior distribution plots are presented:

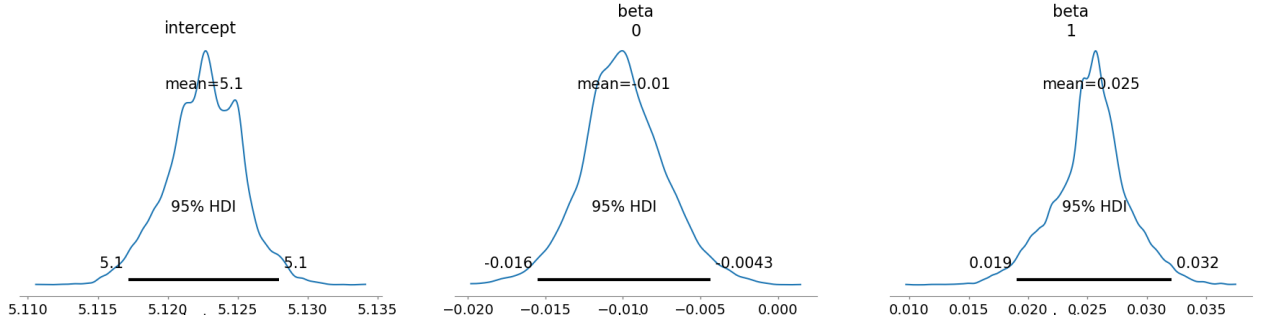


Figure 3: Posterior distribution of \mathbf{w}

Note how a credible interval is given for each w_i , allowing to analyze predictive uncertainty rather than obtaining unequivocal point estimates. Furthermore, the interpretation of credible intervals is far clearer than confidence intervals: it can be seen that the first three weights are statistically significant with 95% chance. The null hypothesis that zero is contained within the credible interval is rejected with probability 95% for these weights.

It is possible to test whether all weights really contribute to enhance predictive performance. A second specification was estimated using only the most relevant features

according to the champion model (to be uncovered in the following subsections). Consequently, model comparison is carried out between a complete model (using all 75 features) and a restricted one (top 20 relevant features). For such purpose, Deviance Information Criterion (DIC) is used. Let DIC be expressed as $D(\theta) = -2 \ln(p(y|\theta)) + C$, where y is the data, θ represents unknown parameters and $p(y|\theta)$ is the likelihood function. Just like AIC and BIC, a lower DIC is associated with higher predictive performance. After estimating the expected log pointwise predictive density using Pareto-smoothed importance sampling leave-one-out cross-validation, it was found that the full model is the preferred specification (50,195.4 vs 54,910.2 DIC). Evidence was found in favor of the statistical significance of features different from the most relevant ones.

6.2 Elastic Net Regression

For comparison purposes, a Linear Regression Model is estimated in a frequentist fashion. The weight vector \mathbf{w} is obtained by solving the following optimization problem:

$$\hat{\mathbf{w}} = \arg \min_{\tilde{\mathbf{w}}} (\mathbf{y} - \mathbf{X}\tilde{\mathbf{w}})'(\mathbf{y} - \mathbf{X}\tilde{\mathbf{w}}) + \lambda_1 \|\tilde{\mathbf{w}}\|_1 + \lambda_2 \|\tilde{\mathbf{w}}\|_2^2 \quad (4)$$

Where $\tilde{\mathbf{w}}$ is a running parameter, $\|\mathbf{w}\|_1$ is the ℓ_1 -norm of the weight vector and λ_1 is the associated regularization term. Likewise, $\|\mathbf{w}\|_2^2$ is the ℓ_2 -norm of \mathbf{w} and λ_2 is its regularization term.

Zou and Hastie (2005) combined ℓ_1 and ℓ_2 -norm regularization to overcome some drawbacks of LASSO, obtaining a new regularization and feature selection method. The result is that few non-zero weights are left while maintaining properties of Ridge Regression.

Note that some restrictions on the joint distribution of $\{\mathbf{x}_i, y_i\}$ can be relaxed for this model: heteroskedasticity is allowed, there is no need to define prior distributions and random sampling can be reduced to ergodic stationarity.

Despite being a notably less restrictive model in terms of assumptions, Elastic Net Regression performs worse than Bayesian Ridge Regression (0.5232 vs 0.5104 RMSE, respectively). Thus, as of now the best performing model is Bayesian Regression.

6.3 Random Forest

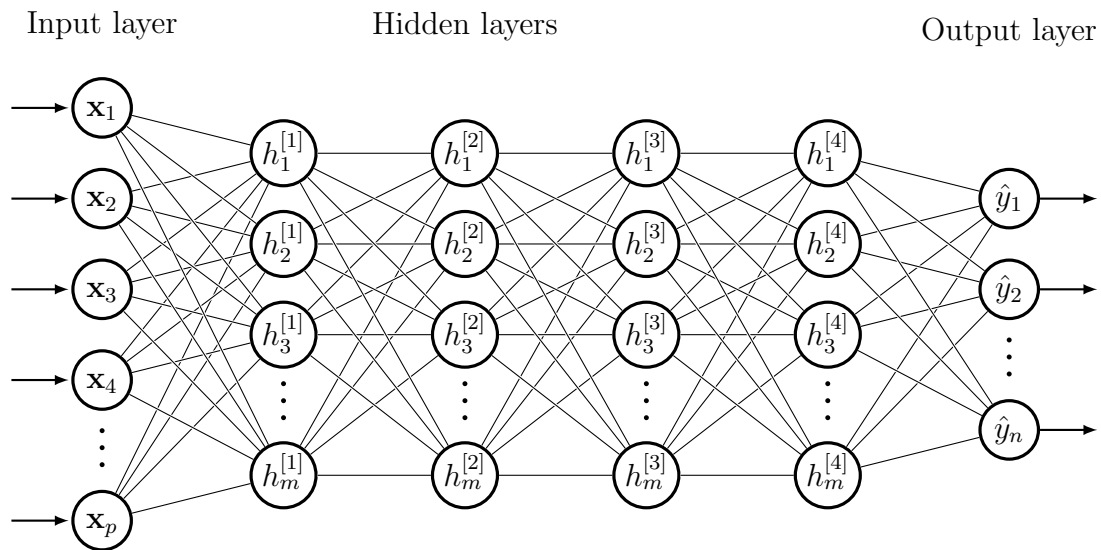


Figure 4: Artificial Neural Network Architecture

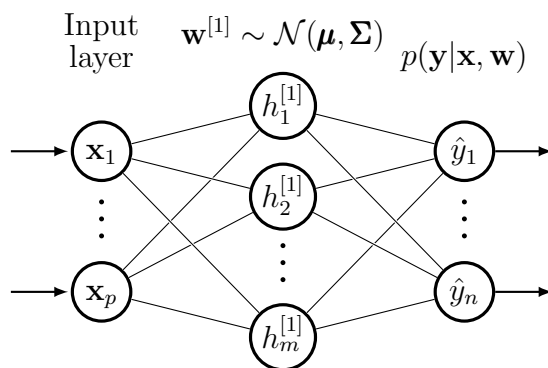


Figure 5: Bayesian Neural Network Architecture

6.4 XGBoost

6.5 Neural Network

7 Conclusion

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Appendix

Algorithm 2: Iterative Imputer Algorithm

Input: Incomplete dataset \mathcal{D}

Output: Imputed dataset \mathcal{D}^*

1 Create m copies of $\mathcal{D} = \{\mathcal{D}_1, \dots, \mathcal{D}_m\}$

2 Iteratively sample $p(\mathbf{y}_i | \mathbf{y}_{-i}, \boldsymbol{\theta}_i)$ from each \mathcal{D}_j

3 Draw $(\boldsymbol{\theta}^{(t)}, \mathbf{y}^{(t)})$ with Gibbs sampler:

4 **for** $t = 1, \dots, n$ **do**

$$\begin{aligned} \boldsymbol{\theta}_1^{(t)} &\sim p(\boldsymbol{\theta}_1 | \mathbf{y}_1^{\text{obs}}, \mathbf{y}_2^{(t-1)}, \dots, \mathbf{y}_p^{(t-1)}) \\ \mathbf{y}_1^{(t)} &\sim p(\mathbf{y}_1 | \mathbf{y}_1^{\text{obs}}, \mathbf{y}_2^{(t-1)}, \dots, \mathbf{y}_p^{(t-1)}, \boldsymbol{\theta}_1^{(t)}) \\ &\vdots \\ \boldsymbol{\theta}_p^{(t)} &\sim p(\boldsymbol{\theta}_p | \mathbf{y}_p^{\text{obs}}, \mathbf{y}_1^{(t)}, \dots, \mathbf{y}_{p-1}^{(t)}) \\ \mathbf{y}_p^{(t)} &\sim p(\mathbf{y}_p | \mathbf{y}_p^{\text{obs}}, \mathbf{y}_1^{(t)}, \dots, \mathbf{y}_p^{(t)}, \boldsymbol{\theta}_p^{(t)}) \end{aligned}$$

5 Estimate $Q^{(1)}, \dots, Q^{(m)}$ and pool results: $\bar{Q} = \text{pool}(\hat{Q}^{(1)}, \dots, \hat{Q}^{(m)})$

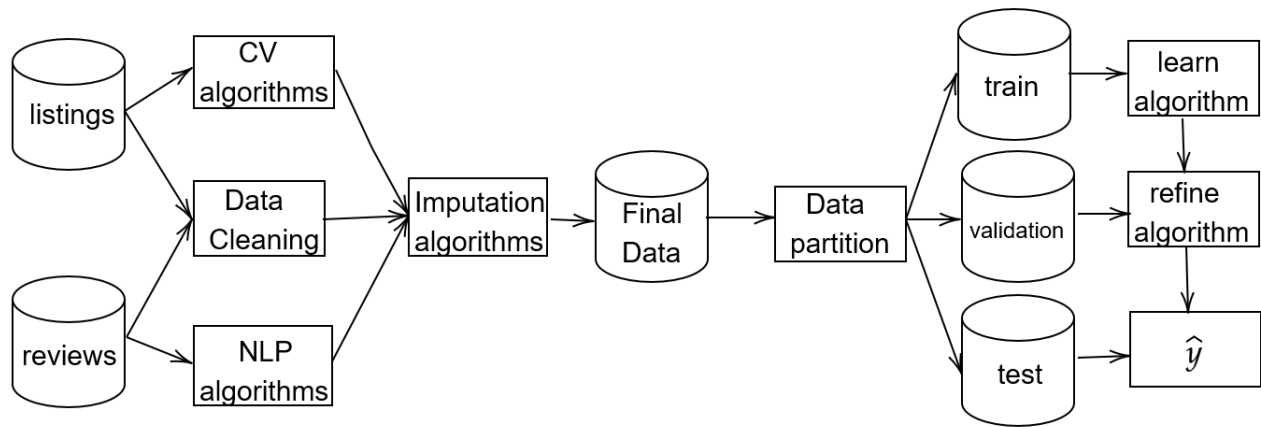


Figure 6: AI Framework

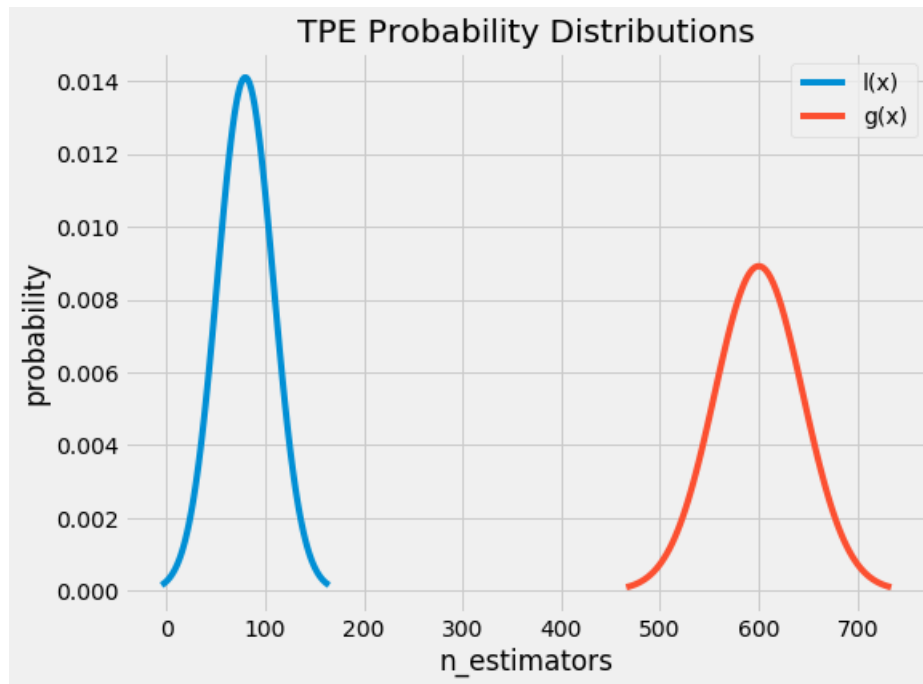


Figure 7: TPE Algorithm

Marginal probability distribution $f(y)$

$$\begin{aligned}
f(y) &= \int_0^{+\infty} f(y|\theta) f(\theta) \partial\theta \\
&= \int_0^{+\infty} \frac{\omega \theta y^{-(\omega+1)}}{(1+y^{-\omega})^{\theta+1}} \frac{\beta^\alpha}{\Gamma(\alpha)} \theta^{\alpha-1} e^{-\theta\beta} \partial\theta \\
&= \frac{\omega y^{-(\omega+1)} \beta^\alpha}{\Gamma(\alpha)} \int_0^{+\infty} \theta^\alpha e^{-\theta\beta} \frac{1}{(1+y^{-\omega})^{\theta+1}} \partial\theta \\
&= \frac{\omega y^{-(\omega+1)} \beta^\alpha}{\Gamma(\alpha)} \int_0^{+\infty} \theta^\alpha e^{-\theta\beta} \exp \left\{ \ln \left[\frac{1}{(1+y^{-\omega})^{\theta+1}} \right] \right\} \partial\theta \\
&= \frac{\omega y^{-(\omega+1)} \beta^\alpha}{\Gamma(\alpha)} \int_0^{+\infty} \theta^\alpha e^{-\theta\beta} \exp \left\{ -(\theta+1) \ln (1+y^{-\omega}) \right\} \partial\theta \\
&= \frac{\omega y^{-(\omega+1)}}{1+y^{-\omega}} \frac{\beta^\alpha}{\Gamma(\alpha)} \int_0^{+\infty} \theta^\alpha \exp \left\{ -\theta[\beta + \ln (1+y^{-\omega})] \right\} \partial\theta \\
&= \frac{\omega y^{-(\omega+1)}}{1+y^{-\omega}} \frac{\beta^\alpha}{\Gamma(\alpha)} \frac{\Gamma(\alpha^*)}{\beta^{\alpha^*}} \int \frac{\beta^{\alpha^*}}{\Gamma(\alpha^*)} \theta^{\alpha^*-1} e^{-\theta\beta^*} \partial\theta \\
&= \frac{\omega y^{-(\omega+1)}}{1+y^{-\omega}} \frac{\beta^\alpha}{\Gamma(\alpha)} \frac{\alpha\Gamma(\alpha)}{[\beta + \ln (1+y^{-\omega})]^{\alpha+1}} \\
&= \frac{\alpha\beta^\alpha}{[\beta + \ln (1+y^{-\omega})]^{\alpha+1}} \left(-\frac{\omega y^{-(\omega+1)}}{1+y^{-\omega}} \right) \quad \text{Let } z := \ln (1+y^{-\omega}) \\
&= \frac{\alpha\beta^\alpha}{(\beta+z)^{\alpha+1}} \left(-\frac{\partial z(y)}{\partial y} \right) \implies y \sim \text{Pareto}(\alpha, \beta)
\end{aligned}$$

Posterior probability distribution $f(\theta|\{y_i\}_{i=1}^n)$

$$f(\theta|\{y_i\}_{i=1}^n) = \frac{l(y|\theta)f(\theta)}{\int_0^{+\infty} f(y|\theta)f(\theta) \partial\theta}$$

$$\propto \prod_{i=1}^n \frac{\omega\theta y_i^{-(\omega+1)}}{(1+y_i^{-\omega})^{\theta+1}} \frac{\beta^\alpha}{\Gamma(\alpha)} \theta^{\alpha-1} e^{-\theta\beta}$$

$$\propto \theta^{\alpha+n-1} e^{-\theta\beta} \prod_{i=1}^n \exp \left\{ \ln \left[\frac{1}{(1+y_i^{-\omega})^{\theta+1}} \right] \right\}$$

$$\propto \theta^{\alpha+n-1} e^{-\theta\beta} \prod_{i=1}^n \exp \left\{ -(\theta+1) \ln(1+y_i^{-\omega}) \right\}$$

$$\propto \theta^{\alpha+n-1} e^{-\theta\beta} \exp \left\{ -\sum_{i=1}^n (\theta+1) \ln(1+y_i^{-\omega}) \right\}$$

$$\propto \theta^{\alpha+n-1} e^{-\theta\beta} \exp \left\{ -\sum_{i=1}^n \theta \ln(1+y_i^{-\omega}) \right\}$$

$$\propto \theta^{\alpha+n-1} \exp \left\{ -\theta \left(\beta + \sum_{i=1}^n \ln(1+y_i^{-\omega}) \right) \right\}$$

$$= \frac{\left(\beta + \sum_{i=1}^n \ln(1+y_i^{-\omega}) \right)^{\alpha+n}}{\Gamma(\alpha+n)} \theta^{\alpha+n-1} \exp \left\{ -\theta \left(\beta + \sum_{i=1}^n \ln(1+y_i^{-\omega}) \right) \right\}$$

$$= \frac{\beta^{*\alpha^*}}{\Gamma(\alpha^*)} \theta^{\alpha^*-1} e^{-\theta\beta^*} \implies f(\theta|\{y_i\}_{i=1}^n) = \text{Gamma} \left(\alpha+n, \beta + \sum_{i=1}^n \ln(1+y_i^{-\omega}) \right)$$