COSC 3340

Examination 3 Wednesday, April 9, 2008, 1 – 2:30 pm Open Book and Notes

Prove that the following language L is not contextfree:	
$L = \{ 0^{k} 1^{j} 2^{i} i > j > k \ge 0 \}.$	
Construct a pda \mathbb{P} for the following language: $L = \{ 0^{i} 1^{3i} \mid i \geq 0 \} \text{ where } L = L_{f}(\mathbb{P}) \text{ (acceptance by final state)}.$ State on which side you write the top of the stack, left: or right	
Hint: Put three markers on the stack for every 0.	
Construct a pda \mathbb{P} that accepts the following language by <u>empty stack</u> : $L = L(G) \text{ where } G = (T, N, P, S) \text{ with } T = \{ \le >, [,] \},$ $N = \{S,A\}, \text{ and } P = \{ S \rightarrow \le A \mid [A]A, A \rightarrow [A]S \mid \le S \le E \}.$	
State on which side you write the top of the stack, left: or right Note: You <u>must</u> use the construction "cfg → pda" given in class. Get G into GNF first!	
Construct a grammar for L(G) for the language N(F): $\mathbb{P} = (\{p,q\}, \{a,b\}, \{Z,X\}, \delta, p, Z, \emptyset) \text{ where the move function } \delta \text{ is given by } \delta(p,a,Z) = \{(p,X,Z)\} \qquad \delta(p,\epsilon,Z) = \{(p,\epsilon)\} \qquad \delta(p,a,X) = \{(p,X,X)\} \delta(q,a,Z) = \{(q,\epsilon)\} \qquad \delta(p,b,X) = \{(q,X)\} \qquad \delta(q,b,Z) = \{(p,Z)\}.$	40
$\delta(q,a,Z) = \{(q,\epsilon)\} \qquad \delta(p,b,X) = \{(q,X)\} \qquad \delta(q,b,Z) = \{(p,Z)\}.$ Here, the top of the stack is on the left.	
 Construct a Turing machine for the language in Question 1, L = { 0^k1^j2ⁱ i>j>k≥0 }. Describe first in words what you are doing, then formulate the formal Turing machine. 	
Points: 1: 20 2: 12 3: 18 4: 30 5: 20	
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test 1	

Test 1

test 1 16

Name: Alex Metry L= {0 k | 2 2 | 2 > 0 > K > 0 } assume LisefL = Hen 3 G(N,T,P,S) in CNF s.b./ L=L(G) assure t= no. ofwirds, assure award Z = 02t 12t+1 22t+2 / 121>2t by pumping Lemma Z=UVWXY where IVXI>1 & UVWXYY & L(6) 12 for allizo Case 11. V&X areall O's => for i=2 noof zero can be equil no of 1 5 L(6), \$L 100 cox 22 V&x are all is -> for i'=2 (LG) &L cose 32 VEXare all i's => for i'=0 ELG, &L casely. No 2's in vorx => for i'=2 ELG), &L because No of 1's can be equal to no. of 2's cose 5: No 1s in Vorx => for i'=2 EL(G), &L Cose 6: No O's in Vorx => for i=0 EL(6), & L becase No of \$'s decrease to be equal No of zeros cose 7: at less one 0, me 1, pre 2 in vorx for it >1 the pattern will change IRL zous can follow 25 which is not acceptable by L here is contradiction in each case He language Lis not Content free

*
$$(p, \epsilon) \in \delta(p, \epsilon, z)$$

$$[p, z, p] \rightarrow \epsilon$$
* $(q, x) \in \delta(p, b, x)$

$$[p, x, p] \rightarrow b[q, x, p]$$

$$[p, x, p] \rightarrow b[q, x, p]$$

$$[p, x, p] \rightarrow b[q, x, q]$$
* $(q, \epsilon) \in \delta(q, \alpha, z)$
* $(p, z) \in \delta(q, \alpha, z)$

$$[q, z, q] \rightarrow a \rightarrow 0$$
* $(p, z) \in \delta(q, b, z)$

$$[q, z, p] \rightarrow b[p, z, p]$$

$$[q, z, p] \rightarrow b[p, z, p]$$

$$[q, z, q] \rightarrow b[p, z, q]$$
The $L(6)$ is observed with $[p, z, q]$

first I'll construct a pda let accepts by exptystack the class it to one that accepts by fluid state

Le \{0\; 3\; 1\; 100 \\

Le \{\(0\, 1\}\), \{\(20\, 2\), \{\(20\, 2\)}\}, \{\(20\, 2\)}\}, \{\(20\, 2\)}\}, \{\(20\, 2\)}\}, \{\(20\, 2\)}\}, \{\(20\, 2\)}\}

The topofthe stack ison the left) {(q, zzzz)} {(q, E)} # [, = ({0,1}, {9,9,9,1,{2',2,2},8,9',9,2) {(q,, E)} Zo 7. 8(9,, €)(lind state

3
$$S \rightarrow \langle S \rangle A | [A]A$$
 $A \rightarrow [A]S | \langle S \rangle S | \mathcal{E}$
 $S \rightarrow \langle S \rangle A | \langle S \rangle | [A]A | [A] | [A]A | [A]$



