

# Metrics Summary

## Metrics

### 1. Sleep Metrics

#### 1.1 Sleep Efficiency (SE)

**Definition:** Ratio of total sleep time to time spent in bed.

**Formula:**

$$SE = \frac{\text{Total Sleep Time}}{\text{Time in Bed}}$$

**Insights:** High SE ( $> 85\%$ ) indicates efficient sleep; low SE ( $< 85\%$ ) suggests fragmented or poor sleep quality.

#### 1.2 Total Sleep Time (TST)

**Definition:** Cumulative duration of sleep during a 24-hour period.

**Formula:**

$$TST = \text{Sleep Offset Time} - \text{Sleep Onset Time}$$

**Insights:** Evaluates whether participants meet recommended sleep durations.

#### 1.3 Wake After Sleep Onset (WASO)

**Definition:** Total time spent awake after initially falling asleep.

**Formula:**

$$WASO = \text{Sum of Awake Durations (after Sleep Onset)}$$

**Insights:** High WASO reflects restless or fragmented sleep.

#### 1.4 Sleep Midpoint

**Definition:** Average time between sleep onset and offset.

**Formula:**

$$\text{Sleep Midpoint} = \frac{\text{Sleep Onset Time} + \text{Wake Time}}{2}$$

**Insights:** Provides circadian rhythm alignment information.

#### 1.5 Sleep Latency

**Definition:** Time between going to bed and falling asleep.

**Formula:**

$$\text{Sleep Latency} = \text{Sleep Onset Time} - \text{Bedtime}$$

**Insights:** Longer sleep latency often indicates difficulty initiating sleep.

## 1.6 Sleep Fragmentation Index

**Definition:** Measures frequency of awakenings during sleep.

**Formula:**

$$\text{Fragmentation Index} = \frac{\text{Number of Awakenings}}{\text{Total Sleep Time}}$$

## 1.7 Intra-Individual Standard Deviation of Sleep Duration

**Definition:** Measures variability in sleep duration across nights.

**Formula:**

$$\text{Standard Deviation} = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n}}$$

**Insights:** High variability may indicate irregular sleep schedules.

## 1.8 Interdaily Stability (IS)

**Definition:** Quantifies regularity of sleep-wake cycles across days.

**Formula:**

$$IS = 1 - \frac{\text{Variance of Daily Sleep Durations}}{\text{Mean Daily Sleep Duration}^2}$$

## 1.9 Sleep Regularity Index (SRI)

**Definition:** Probability of being asleep or awake at the same time on consecutive days.

**Formula:**

$$SRI = \frac{\text{Consistent States Across Consecutive Days}}{\text{Total States Compared}}$$

## 1.10 Social Jet Lag (SJJ)

**Definition:** Difference in sleep timing between weekdays and weekends.

**Formula:**

$$SJJ = |\text{Weekend Sleep Midpoint} - \text{Weekday Sleep Midpoint}|$$

# 2. Physical Activity Metrics

## 2.1 Total Daily Steps

**Definition:** Sum of steps recorded per day.

**Formula:**

$$\text{Total Daily Steps} = \sum \text{Step Counts Over a Day}$$

## 2.2 Activity Intensity Distribution

**Definition:** Proportion of time spent in different activity levels (sedentary, light, moderate, vigorous).

**Formula:**

$$\text{Intensity Distribution} = \frac{\text{Time in Intensity Level}}{\text{Total Time}}$$

**Insights:** Highlights time distribution among activity intensities.

## 2.3 Energy Expenditure

**Definition:** Daily caloric burn estimate based on activity levels and accelerometer data.

**Formula:**

$$\text{Energy Expenditure} = \text{Activity Coefficient} \times \text{Total ENMO}$$

## 2.4 Non-Wear Time Analysis

**Definition:** Periods when the device was not worn.

**Formula:**

$$\text{Non-Wear Time} = \sum (\text{Non-Wear Flag})$$

**Insights:** Helps exclude invalid data points.

## 2.5 Circadian Rhythm Consistency

**Definition:** Regularity of activity levels at the same times across days.

**Formula:**

$$\text{Consistency} = \text{Correlation of Activity Levels Across Days}$$

# 3. Behavioral Metrics

## 3.1 Screen Time Patterns

**Definition:** Average daily internet/computer use hours.

**Formula:**

$$\text{Average Screen Time} = \frac{\text{Total Hours Online}}{\text{Number of Days}}$$

## 3.2 Digital Dependency Score

**Definition:** Composite of PCIAT scores and internet usage hours.

**Formula:**

$$\text{Dependency Score} = \text{PCIAT Score} + \text{Internet Use Hours}$$

## 3.3 Sleep and Internet Use Mismatch

**Definition:** Difference between screen time before bed and average sleep onset latency.

**Formula:**

$$\text{Mismatch} = \text{Screen Time Before Bed} - \text{Sleep Latency}$$

## 3.4 Internet Use Impact

**Definition:** Correlation between internet use and sleep quality metrics.

# 4. Combined Metrics

## 4.1 Physical and Mental Health Composite Index

**Definition:** Combines CGAS, BMI, and sleep quality scores.

**Formula:**

$$\text{Composite Index} = \frac{\text{CGAS} + \text{BMI} + \text{Sleep Quality Score}}{3}$$

## 4.2 Internet Use vs. Activity Tradeoff

**Definition:** Ratio of screen time to physical activity time.

**Formula:**

$$\text{Tradeoff Ratio} = \frac{\text{Screen Time}}{\text{Physical Activity Time}}$$

## 5. Social and Environmental Context

### 5.1 Impact of Ambient Light

**Definition:** Correlation between ambient light exposure and sleep onset/offset.

### 5.2 Quarterly Variations

**Definition:** Trends in activity and sleep metrics across seasons.

**Formula:**

$$\text{Quarterly Variation} = \text{Difference in Metrics Across Quarters}$$

## 6. Predictive Modeling Features

### Feature Engineering

**Examples:**

- Temporal patterns in actigraphy (morning vs. evening activity).
- High-risk binary indicators based on thresholds (e.g., high PCIAT, low SE).