Basic Concept of Probability

- Today's Class
 - Sample Space
 - Events
 - Venn Diagram
 - Set Theory





Sample Space

- Outcome: Each possible result of such an experiment that we perform
- Sample space (S): the set of all possible outcomes of an experiment
 - Discrete
 - Continuous

• • •

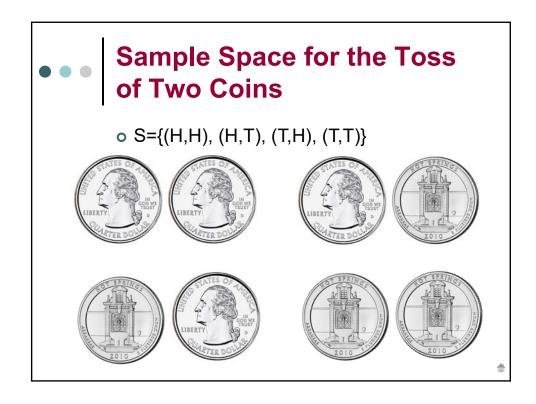
Sample Space for the Toss of a Single Coin

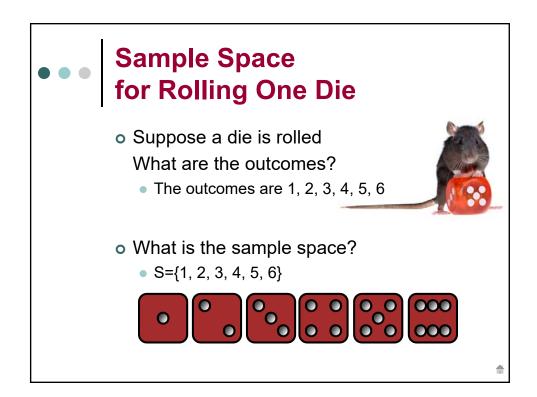
o S={head, tail}

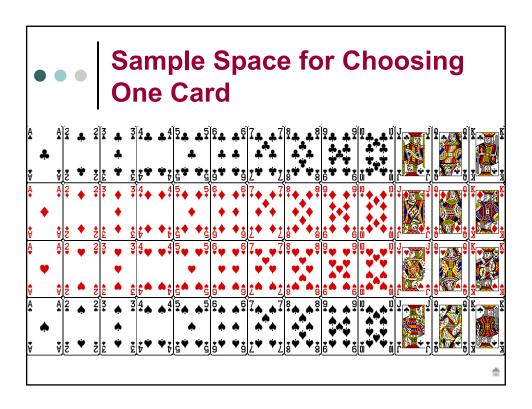




ì







Events

- Event: any subset of outcomes contained in the sample space, S
- What is the event that an even score when rolling a die?
 - Even= {2, 4, 6}









Events Example

• What is the events that the sum of the scores of two dice is equal to 6?







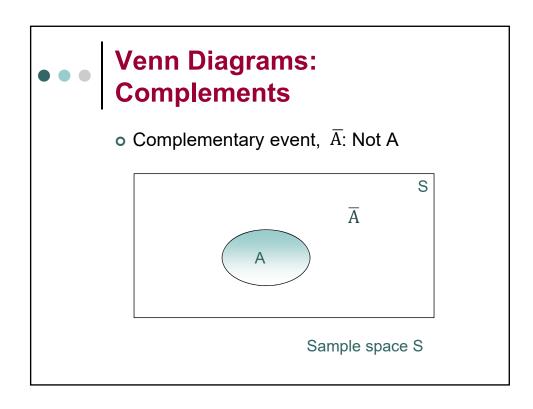


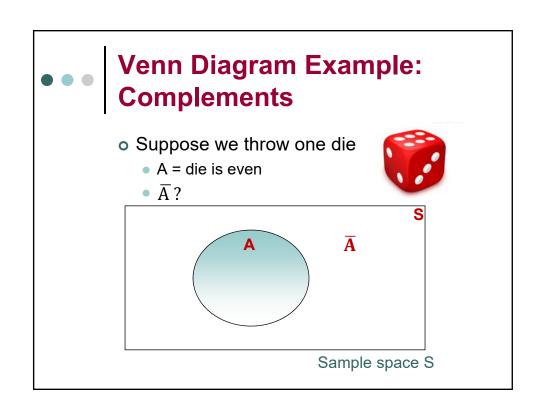


• • •

Combination of Events

- Union: event consisting of all outcomes of both events, e.g. A ∪ B
- Intersection: event of outcomes that are part of both events, e.g. A ∩ B
- Complement: event of all outcomes not part of the event, e.g. A', A^c or \overline{A}
- Contained: one event is a subset of another event, e.g. A ⊂ B

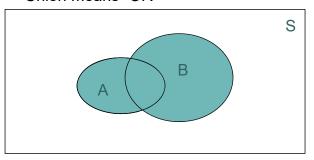






Venn Diagrams: Union

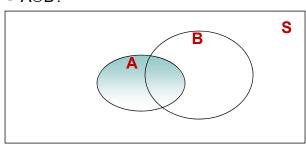
- \bullet The union of two events, A \cup B
 - includes all sample points from A and B
 - Union means "OR"



• • •

Venn Diagram Example: Union

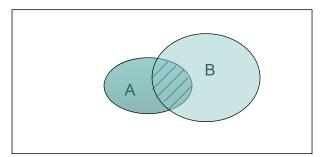
- o Suppose we throw one die
 - A = die is even
 - B = die is less than 4
 - A∪B?





Venn Diagrams: Intersection

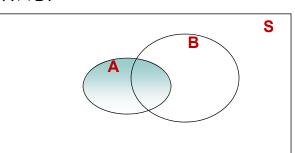
- The intersection of two events, $A \cap B$
 - includes all sample points that are in both A and B
 - Intersection means "AND"



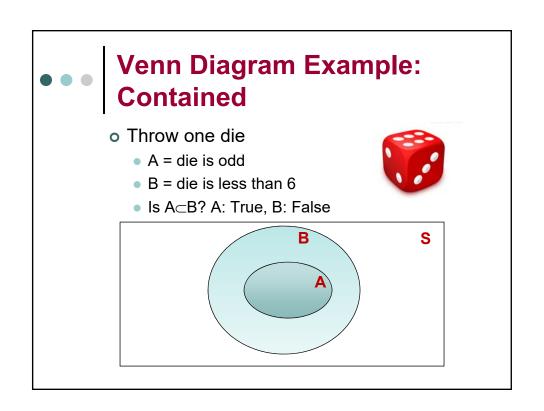
• • •

Venn Diagram Example: Intersection

- o Suppose we throw one die
 - A = die is even
 - B = die is less than 4
 - A ∩ B?

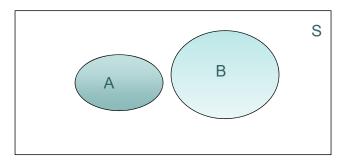


• • • • Venn Diagrams: Contained • • • • A is a subset of B, A⊂B S S



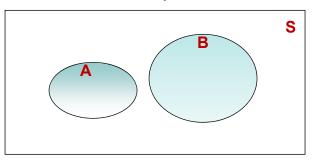
Venn Diagrams: Mutually Exclusive Events

• A and B are mutually exclusive if there is no overlap: $A \cap B = \emptyset$

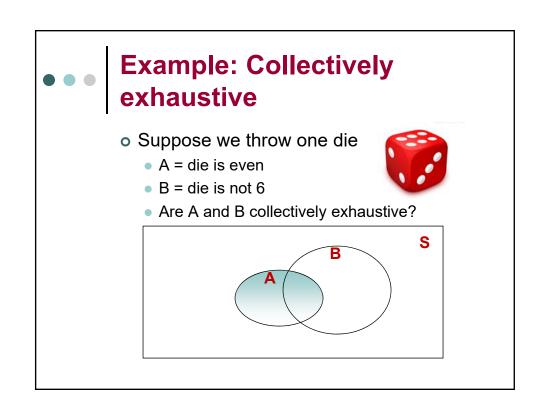


Venn Diagram Example: Mutually Exclusive

- o Suppose we throw one die
 - A = die is even
 - B = die is odd
 - Are A and B mutually exclusive?



Venn Diagrams: Collectively exhaustive • A and B are collectively exhaustive if all sample points are contained within their union A A B B



Venn Diagrams: Mutually Exclusive & Collectively Exhaustive • A and B, are mutually exclusive and collectively exhaustive A B

Set Theory Associative Rule (A ∪ B) ∪ C = A ∪ (B ∪ C) (A ∩ B) ∩ C = A ∩ (B ∩ C) Distributive Rule (A ∪ C) ∩ (B ∪ C) = (A ∩ B) ∪ C (A ∩ C) ∪ (B ∩ C) = (A ∪ B) ∩ C De Morgan's Rule

• $\overline{A \cup B} = \overline{A} \cap \overline{B}$