

# CS M151B HW3

539 14. 8 bit Integer Each step - 4 time units

Hardware

① Product = Product + multiplicand (4 time units)

② shift multiplicand left, multiplier right (simultaneous) (4)

8 iterations for 8 bit integer  $\rightarrow 8 \times (4 + 4) = 64$

Software

① Product = Product + multiplicand (4)

② shift multiplicand left (4)

③ Shift multiplier right (4)

8 iterations  $\rightarrow 8 \times (4 + 4 + 4) = 96$

Hardware: 64 time units Software: 96 time units

540 15. 31 adders stacked vertically 8 bit integer 4 time units/adder

Adding two 8-bit integers means you need 7 adders

$7 \text{ adders} \times \frac{4 \text{ time units}}{\text{adder}} = 28 \text{ time units}$

16. 8-bit integer 4 time units/adder Fast multiplication

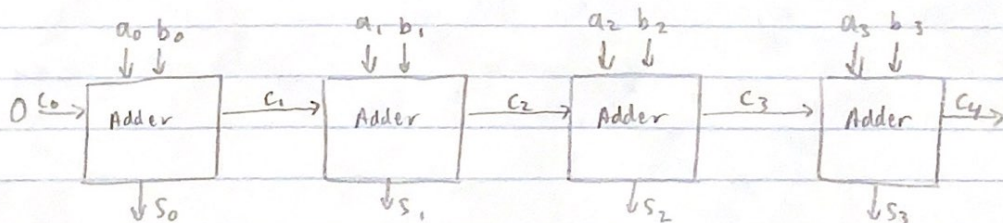
The idea behind this approach is to use the adders in parallel to be more efficient - we use  $\log_2(n)$  time units where  $n$  is the number of bits.

$4 \cdot \log_2(8) = 4 \cdot 3 = 12$  12 time units

1653 25. only OR or AND terms - T

OR of several AND terms - 2T

Ripple Carry



T0:  $a_0 a_1 a_2 a_3 b_0 b_1 b_2 b_3 C_0$

T6:  $s_2 C_3$

T2:  $s_0 C_1$

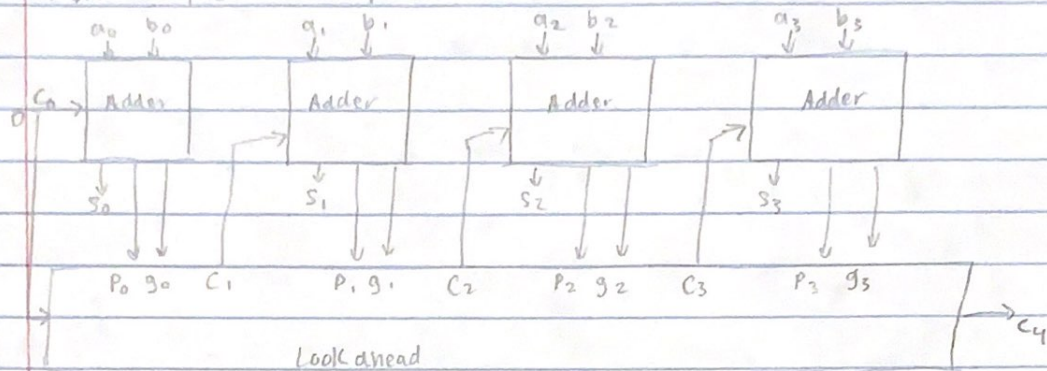
T8:  $s_3 C_4$

T4:  $s_1 C_2$

The total time needed for the 4-bit Ripple-carry adder is  $8T$ .

The path is from  $a_0, b_0, C_0 \rightarrow S_3, C_4$  and this takes 8 time units.

#### 4-bit Carry Lookahead Adder



$T_0: a_0, a_1, a_2, a_3, b_0, b_1, b_2, b_3, C_0$

$T_1: p_0, p_1, p_2, p_3, g_0, g_1, g_2, g_3$

$T_2: S_0$

$T_3: C_1, C_2, C_3, C_4$

$T_5: S_1, S_2, S_3$

The total time needed for the 4-bit Carry Lookahead adder is  $5T$ .

The path is from the  $p$  (propagate) and  $g$  (generate) signals to the  $S_0$ , then all the carries, then finally all the sums.

#### 29. 16-bit Ripple Carry Adder

→ For ripple carry adder, time required is  $2 \times \# \text{ Bits}$

There will be a  $32T$  delay.

?

Ripple Carry of 4-bit groups that use carry lookahead

→ For ripple carry adder, time required is  $2 \times \# \text{ Bits}$

Each 4-bit block takes  $8T$ , and all 4 blocks perform in parallel

It takes  $4T$  for the carry-lookahead stuff (see bracket above)

There will be a  $12T$  delay

?

16 bit carry lookahead adder

→ Same as  $28$ , but connected (4)

There will be a  $8T$  delay.



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31.

Full Carry - Lookahead adders (4 4-bit Carry Lookaheads)

- As we saw in #28, it takes  $5T$  for a single 4-bit Carry lookahead adder.
- Connecting them all together into 4 consecutive ones means that the Total Delay is  $8T$ .

Carry Save

- According to the diagram, carry save would take  $6T$ . The first level would take  $3T$ , the second level  $2T$ , and the third level  $1T$ . Thus, the total time would be  $6T$ .