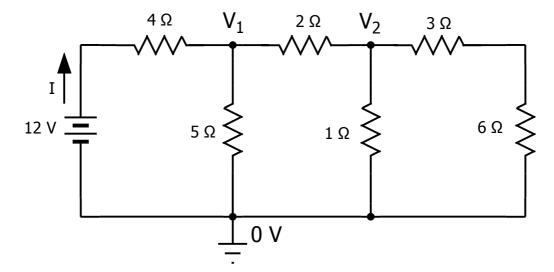
EE3 Fall 2021

Practice Problems 2



- 1. This is a similar circuit to that in Lecture 1. Only the resistor values are different. It can be solved using series-parallel equivalents. But solve it using the NVA process below.
 - a. Assuming that all of the currents at Node 1 (where V_1 is) are *leaving* the node, write an Ohm's Law expression for the current going through the 4 Ω resistor.
 - b. Under the same assumption, write an Ohm's Law expression for the current through the $5\,\Omega$ resistor.
 - c. Continuing, write an expression for the current through the 2 Ω resistor.
 - d. Now, following the same procedure, write Ohm's Law expressions for the three currents leaving Node 2.
 - e. Now, combine the answers to 1a,b,c into a KCL equation.
 - f. Combine the three answers to 1d into a KCL equation.
- 2. You now have 2 equations in 2 unknowns. Solve them for V_1 and V_2 .
- 3. Now that you know V_1 , you can compute I.

Currents leaving a node are given + signs. By the Passive Sign Convention, the end of the resistor where the current enters must be the + end.

1a.
$$\frac{V_1 - 12}{4}$$
1b.
$$\frac{V_1 - 0}{5}$$
1c.
$$\frac{V_1 - V_2}{2}$$
1d.
$$\frac{V_2 - V_1}{2}; \frac{V_2 - 0}{1}; \frac{V_2 - 0}{3 + 6}$$
1e.
$$\frac{V_1 - 12}{4} + \frac{V_1}{5} + \frac{V_1 - V_2}{2} = 0$$
1f.
$$\frac{V_2 - V_1}{2} + \frac{V_2 - 0}{1} + \frac{V_2 - 0}{3 + 6} = 0$$

2. From 1e:
$$19V_1 - 10V_2 = 60$$

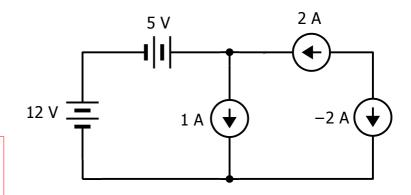
From 1f: $-9V_1 + 29V_2 = 0$
 $V_1 = 3.7744 \text{ V}; V_2 = 1.1714 \text{ V}$

3.
$$I = \frac{12 - 3.77}{4} = 2.06 \text{ A}$$

4. Is this a "legal" circuit? If not, why not?

Circuit is legal.

KVL is satisfied in all three loops. KCL is satisfied at both nodes.



5. Is this a "legal" circuit? If not, why not?

12 V = 1 V = -2 A

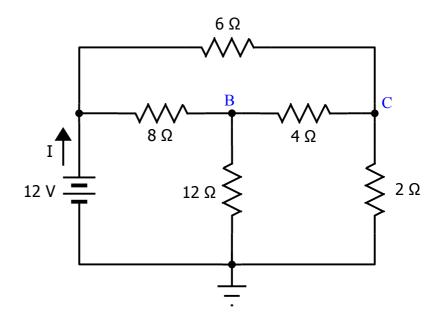
5 V

2 A

Circuit is illegal. KVL not satisfied in left loop.

Using your knowledge of Node Voltage Analysis (NVA), find the current I.

$$I = 2.24 A$$



Node B:
$$\frac{V_B - 12}{8} + \frac{V_B}{12} + \frac{V_B - V_C}{4} = 0$$

Node C:
$$\frac{V_C - V_B}{4} + \frac{V_C}{2} + \frac{V_C - 12}{6} = 0$$

Node B:
$$\left(\frac{1}{8} + \frac{1}{12} + \frac{1}{4}\right) V_B - \left(\frac{1}{4}\right) V_C = \left(\frac{1}{8}\right) 12$$

Node C:
$$\left(\frac{-1}{4}\right)V_B + \left(\frac{1}{4} + \frac{1}{2} + \frac{1}{6}\right)V_C = \left(\frac{1}{6}\right)12$$

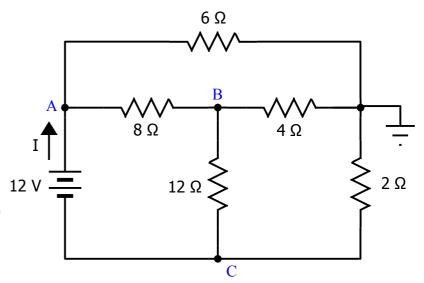
2x2 matrix to get V_B and V_C .

$$V_B = 5.243 \text{ V}; V_C = 3.612 \text{ V}.$$

KCL at top of battery:
$$-I + \frac{12 - V_B}{8} + \frac{12 - V_C}{6} = 0$$

I = 2.24 A

7. This is the same circuit as Problem 6.
Using your knowledge of Node Voltage
Analysis (NVA),find the current I. HINT:
Use I as an unknown fourth variable.
(Note: with the reference node at a
different location, you now have 3
unknown nodes. But you also know the
voltage relationship between 2 of them.)



I = 2.24 A

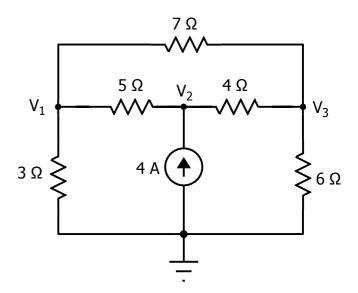
Node A:
$$-I + \frac{V_A - V_B}{8} + \frac{V_A - 0}{6} = 0$$

Node B: $\frac{V_B - V_A}{8} + \frac{V_B - V_C}{12} + \frac{V_B - 0}{4} = 0$
Node C: $+I + \frac{V_C - V_B}{12} + \frac{V_C - 0}{2} = 0$
 $V_A = V_C + 12$
 $-24I + 7V_A - 3V_B + 0V_C = 0$
 $0I - 3V_A + 11V_B - 2V_C = 0$
 $12I + 0V_A - V_B + 7V_C = 0$
 $0I + V_A + 0V_B - V_C = 12$
 $I = 2.24$ A; $V_A = 8.39$ V; $V_B = 1.63$ V; $V_C = -3.61$ V

Note that $V_B - V_C = 5.24$ V (compare to V_B in Problem 6).

Try the other equivalencies.

8. This is almost the circuit that we studied in Problem 1. This time, we have replaced the battery with a current source. Find the three voltages. You may need to dig a little to work this problem.



$$\frac{V_1 - V_2}{5} + \frac{V_1}{3} + \frac{V_1 - V_3}{7} = 0$$

$$\frac{V_2 - V_1}{5} - 4 + \frac{V_2 - V_3}{4} = 0$$

$$\frac{V_3 - V_1}{7} + \frac{V_3 - V_2}{4} + \frac{V_3}{6} = 0$$

$$21 V_1 - 21 V_2 + 35 V_1 + 15 V_1 - 15 V_3 = 0$$

$$4 V_2 - 4 V_1 - 80 + 5 V_2 - 5 V_3 = 0$$

$$24 V_3 - 24 V_1 + 42 V_3 - 42 V_2 + 28 V_3 = 0$$

$$71 V_1 - 21 V_2 - 15 V_3 = 0$$

$$-4 V_1 + 9 V_2 - 5 V_3 = 80$$

$$-24 V_1 - 42 V_2 + 94 V_3 = 0$$

$$V_1 = 7.2 \text{ V}$$

$$V_2 = 17.4 \text{ V}$$

$$V_3 = 9.6 \text{ V}$$