| _ | ons in the boxes provided on the question sheets. If you run out of room or an answer, add a page to the end of the document. | |
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| Name: | Wisc id: | |
| More Greedy | f Algorithms | |
| 1. Kleinberg, Jon. Algoria | hm Design (p. 189, q. 3). | |
| between New York and each day between the they are allowed to car weight w_i . The trucking Company policy requirements upon seeing a is using a simple greed. | a trucking company that does a large amount of business shipping packal Boston. The volume is high enough that they have to send a number of truetwo locations. Trucks have a fixed limit W on the maximum amount of weignery. Boxes arrive at the New York station one by one, and each package i has a station is quite small, so at most one truck can be at the station at any times that boxes are shipped in the order they arrive; otherwise, a customer might box that arrived after his make it to Boston faster. At the moment, the company algorithm for packing: they pack boxes in the order they arrive, and whene fit, they send the truck on its way. | cks ght as a me. ght |
| | set of boxes with specified weights, the greedy algorithm currently in use actual of trucks that are needed. Hint: Use the stay ahead method. | ally |
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| 2. | Kleinberg, Jon. Algorithm Design (p. 192, q. 8). Suppose you are given a connected graph G with edge costs that are all distinct. Prove that G has a unique minimum spanning tree. |
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3. Kleinberg, Jon. Algorithm Design (p. 193, q. 10). Let G = (V, E) be an (undirected) graph with costs

| | aning tree. Give a st spanning tree. | |
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4. In class, we saw that an optimal greedy strategy for the paging problem was to reject the page the

| FWF IS a S | trategy that, or | n a page fault, | if the cache i | s full, it evict | s all the pages | |
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| | trategy that, if | the cache is fu | ıll, evicts the | least recently | used page wh | en there is a |
| LRU is a stault. | trategy that, if | the cache is fu | all, evicts the | least recently | used page wh | en there is a |
| | trategy that, if | the cache is fu | all, evicts the | least recently | used page wh | en there is a |
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 $^{^{-1}}$ An interesting note is that both of these strategies are k-competitive, meaning that they are equivalent under the standard theoretical measure of online algorithms. However, FWF really makes no sense in practice, whereas LRU is used in practice.

Coding Problem

5. For this question you will implement Furthest in the future paging in either C, C++, C#, Java, Python, or Rust.

The input will start with an positive integer, giving the number of instances that follow. For each instance, the first line will be a positive integer, giving the number of pages in the cache. The second line of the instance will be a positive integer giving the number of page requests. The third and final line of each instance will be space delimited positive integers which will be the request sequence.

Note: a naïve solution doing repeated linear searches will timeout.

A sample input is the following:

```
3
2
7
1 2 3 2 3 1 2
4
12
12 3 33 14 12 20 12 3 14 33 12 20
3
20
1 2 3 4 5 1 2 3 4 5 1 2 3 4 5 1 2 3 4 5
```

The sample input has three instances. The first has a cache which holds 2 pages. It then has a request sequence of 7 pages. The second has a cache which holds 4 pages and a request sequence of 12 pages. The third has a cache which holds 3 pages and a request sequence of 15 pages.

For each instance, your program should output the number of page faults achieved by furthest in the future paging assuming the cache is initially empty at the start of processing the page request sequence. One output should be given per line. The correct output for the sample input is

4 6 12