0.1 The Compression Rebuttal

This section talks about if a NN can compress¹ data – i.e is it possible to lose information from layer to layer. There is an argument to be made for both sides. We can easily construct a NN that loses information. If we take the layer transition function f_{θ}^{l} to be

$$f_{\theta}^{l}(x) = 0$$

This function would lose information as we are not able to recover the input given the output, hence the NN must have discarded some information. Therefore compression is definitely possible. However, it is equally possible to create a function that preserves all the information about the input. Every layer in a NN is just a number \mathbb{R}^{d_l} , where d_l is the dimension of layer l. We know there is a one to one mapping between \mathbb{R} and \mathbb{R}^d for any dimension d. Therefore we can construct a neural network that loses no information if we take the layer transition function f_{θ}^l to be

$$f_{\theta}^{l}(x) = \text{map} \mathbb{R}_{-} \text{to} \mathbb{R}^{d_{l}} (\text{map} \mathbb{R}^{d_{l-1}} \text{_to} \mathbb{R}(x))$$

That is mapping the value of previous layer to \mathbb{R} and mapping it back to \mathbb{R}^{d_l} . It is important to understand if NN can compress data if we are to study how NN manipulate information.

0.1.1 Viability of compression

Viability of compression inside a NN. Asking if a NN compresses data is equivalent to asking if Equation 1 holds.

$$I(X, T_{e,l}) < H(X) \tag{1}$$

Lets examine the value $I(X, T_{e,l})$ more closely. From ?? we know,

$$I(X, T_{e,l}) = H(X) - H(X|T_{e,l})$$
(2)

Form Equation 1 and Equation 2 we have,

$$I(X, T_{e,l}) < H(X) \Leftrightarrow H(X|T_{e,l}) > 0 \tag{3}$$

Consider the value $H(X|T_{e,l})$. $H(X|T_{e,l})$ is 0 iff the value of $T_{e,l}$ uniquely identifies the value of X i.e

$$H(X|T_{e,l}) = 0 \Leftrightarrow P(X = x|T_{e,t} = t) = \begin{cases} 1, & \text{if } t = F_{\theta(e)}^l(x). \\ 0, & \text{otherwise.} \end{cases}$$
 (4)

Equation 4 holds iff $F_{\theta}^{l}(x)$ is an invertible function. Recall the definition of $F_{\theta}^{l}(x)$

$$F_{\theta}^{l}(x) = f_{\theta}^{l}(f_{\theta}^{l-1}(...(f_{\theta}^{1}(x))))$$
(5)

Equation 5 implies

$$F_{\theta}^{l}$$
 is invertible $\Leftrightarrow \forall i \in \{1...l\}.f_{\theta}^{i}$ is invertible

Putting it all together we get the bi implications

$$I(X, T_{e,l}) < H(X) \Leftrightarrow \neg(\forall i \in \{1...l\}, f_{\theta}^{i} \text{ is invertible})$$

$$\Leftrightarrow \exists i \in \{1...l\}, f_{\theta}^{i} \text{ is not invertible}$$

$$\Leftrightarrow \exists i \in \{1...l\} \exists u, v \in \{x_{1}, ..., x_{N}\}, f_{\theta}^{t}(u) = f_{\theta}^{t}(v) \land u \neq v$$

$$(6)$$

 $^{^{1}}$ N.B This section does not talk about the compression phase, just about compression in the network for a single epoch

and

This implies that compression can only happen if at least on transition function f_{θ}^{l} is not invertible.

0.1.2 Determinism of the Transition Function

Decomposing the Transition Function Lets break away from our NN abstraction and consider the transition function f_{θ}^{l} and how it is defined in concrete implementations of NNs – recall the ??.

$$n_{l+1,i} = g\left(\sum_{j=0}^{\text{layer } l \text{ size}} w_{l,j,i} * n_{l,j}\right)$$

Where g is an invertible function such as Leaky ReLu, Sigmoid, Tanh. This means we can consider the function f_{θ}^{l} to be a composition of two different functions:

- A matrix multiplication which is responsible for the weighted sum of previous layers activations $\sum_{j=0}^{\text{layer } l \text{ size}} w_{l,j,i} * n_{l,j}$. Let us call this matrix m_{θ}^{l} .
- \bullet An application of the invertible function g to every element of the vector produced by the matrix multiplication.

This function decomposition implies that

$$f_{\theta}^{l}$$
 is invertible $\Leftrightarrow m_{\theta}^{l}$ is invertible (7)

A Note on Invertible Matrices

Let M be a matrix and M^{-1} be the inverse, then;

$$M^{-1}$$
 is defined $\Leftrightarrow det(M) \neq 0$ (8)

Let M be a random matrix, then;

$$P(\det(M) = 0) = 0 \tag{9}$$

Let M be random matrix, then from Equation 8 and Equation 9 we have

$$P(M^{-1} \text{ is defined}) = 1 \tag{10}$$

i.e every random matrix has an inverse.

Randomness in SGD Consider the matrix m_{θ}^{l} . The Matrix is defined by the parameters θ which are controlled by Stochastic Gradient Descent (SGD). At the start of the training period the parameters θ are initialized to random values. Every iteration of SGD we update the parameters – this update can also be considered random due to the Stochastic nature of the algorithm. From this we can treat the parameters θ and consequently the matrix m_{θ}^{l} as random throughout the training process.

Having m_{θ}^{l} be an instance of a random matrix would mean that Equation 10 holds – which would imply that every transition function is invertible, which in turn means that there cannot be any compression in a NN.

This would mean having discussion about Information in NN is moot. However, we can still have a meaningful discussion about neural networks if consider the parameters θ to be a random distribution rather than an instance of a concrete value. This is not agreed upon fully within the scientific community – Tishby assumes this is inherent in SGD, while Saxe has contested the claim.

Let us refer to the parameters as probability distribution with notation $\hat{\theta}$. $\hat{\theta}$ is a sequence of probability distributions that depend s.t $\hat{\theta}(e+1)$ depends on $\hat{\theta}(e)$, where e is the epoch.

Let us formally define $\hat{\theta}$. Since at the start of the training period SGD initializes parameters at random – let the start of the sequence $\hat{\theta}(1)$ be defined by Equation 11, where: \mathcal{N}_k – is the Multivariate Normal distribution with dimension k, μ – is a vector in k'th dimension defining the mean of the distribution, Σ – is a k*k matrix defining the variance of the distribution.

$$\hat{\theta}(1) \sim \mathcal{N}_k(\mu, \Sigma) \tag{11}$$

Let the sequence be defined as;

$$P(\hat{\theta}(e+1) = t|\hat{\theta}(e) = \hat{t}) = P(\phi = t),$$
 (12)

where
$$\phi$$
 is $\hat{\theta}(e)$ with one SGD step applied, we can assume $\phi \sim \mathcal{N}_k$ (13)

We have shown that parameters of a NN can be though as being a probability distribution.

Impact of $\hat{\theta}$ – parameters as probability distributions. With the idea that parameters $\hat{\theta}$ are a probability distribution let us again consider the question of compression in neural networks. From subsection 0.1.1 we know that no compression in NN is equivalent to

$$I(X, T_{e,l}) = H(X)$$

which is equivalent

$$H(X|T_{e,l}) = 0$$

 $H(X|T_{e,l})=0$ means by observing $T_{e,l}$ we can deduce the exact value of X. i.e

$$(\forall t. \ P(T_{e,l} = t) > 0 \implies P(X = x | T_{e,l} = t) = 1)$$

$$\implies (\forall t. \ P(T_{e,l} = t) > 0 \implies P(T_{e,l} = t | X \neq x) = 0)$$

$$(14)$$

Notice from Equation 11 and Equation 13 that

$$\forall e. \, \hat{\theta}(e) \sim \mathcal{N}_k$$
, where e is an epoch (15)

Equations 14 and 15 are unsatisfiable together. Proof: Consider x and \hat{x} s.t $\hat{x} \neq x$. Let ϕ be s.t. $f_{\phi}^{1}(x) = t$

$$f_{\phi}^{1}(x) = t,$$

$$\Rightarrow P(T_{e,1} = t) > 0,$$

$$\Rightarrow P(T_{e,1} = t | X \neq x) = 0, \text{ by Equation 14}$$

$$\Rightarrow P(T_{e,1} = t | X = \hat{x}) = 0$$
(16)

however, we can construct $\hat{\phi}$ s.t $f_{\hat{\phi}^1}(\hat{x}) = t$

$$P(T_{e,1} = t | X = \hat{x}) = P(\hat{\theta}(e) = \hat{\phi}) > 0$$
, by Equation 15 (17)

hence, we get a contradiction

$$P(T_{e,1} = t | X = \hat{x}) = 0 \land P(T_{e,1} = t | X = \hat{x}) > 0$$
(18)

and Equation 14 is unsatisfiable, this implies

$$H(X|T_{e,l}) > 0 (19)$$

which finally implies

$$I(X, T_{e,l}) < H(X)$$

and proves that if we consider parameters to be random distributions the compression happens inside NN.

0.1.3 Recap

There is contention if NN are actually capable of compressing information. I have shown that if we assume the parameters of a NN to be concrete values compression is not possible and discussion about Information within them is moot. However, if we make the assumptions that parameters are actually random variables then compression does happen.

- MIE is hard, how can we measure it rewrite
 - Discrete
 - KDE
 - Advanced
 - AIR
- project structure

0.2 Mutual Information Estimation

As stated before we are trying to validate the fact that compression is happening within the hidden layers in a neural network as such having robust tools to measure mutual information is of utmost importance.

0.2.1 Mutual Information Definition

Mutual information is a measure of dependence between two variables X and Y, it quantifies the number of bits obtained about one when observing the other.

Suppose we have two random variables X and Y if we want to measure mutual information between the two of them we usually refer to one of the following equations:

Using the entropy of the distributions to infer the value

$$I(X,Y) = H(X) - H(X|Y) \tag{20}$$

$$I(X,Y) = H(X) + H(Y) - H(X,Y)$$
(21)

Or calculating the mutual information explicitly from probabilities, for discrete and continuous distributions respectively

$$I(X;Y) = \sum_{y \in \mathcal{Y}} \sum_{x \in \mathcal{X}} p(x,y) \log \left(\frac{p(x,y)}{p(x) p(y)} \right)$$
 (22)

$$I(X;Y) = \int_{\mathcal{V}} \int_{\mathcal{X}} p(x,y) \log \left(\frac{p(x,y)}{p(x)p(y)} \right) dx dy$$
 (23)

0.2.2 Theoretically undefined

Calculating mutual information is mathematically defined for both continuous and discrete distributions by using one of the functions above. However since we are looking at neural networks we do not have the full distribution – only an empirical sample of the unknown joint distribution P(X,Y). As such we cannot use conventional methods to calculate the mutual information and instead have to use tools to estimate it.

The field of estimating mutual information is relatively new as a result the tools that are available are quite primitive. There has been some papers published that use more advanced techniques to tackle the problem, we will talk about in subsection 0.3.4

0.3 Calculating Mutual Information

0.3.1 Experimental setup

```
Algorithm: Generate Information Plane Data
1
2
    T = number of layers
    X = training data
    Y = label data
    N = number of epochs
6
    Output:
    I_x(epoch, layer), # mutual information with X
    I_{y}(epoch, layer) # mutual information with Y
9
    Algorithm:
10
    NN = setup\_neural\_network(T, X, Y)
11
    for e in 0..N:
12
      NN.run_SGD_once()
13
      for t in 0...T:
14
        data = []
15
        for x \in X:
16
           \hat{t} = NN.predict(x).layer_activation(t)
17
           data.append(\hat{t})
18
         I_x(e, t) = calculate_mutual_information(data, X)
19
         I_{y}(e, t) = calculate_mutual_information(data, Y)
20
```

Figure 1: The general algorithm for calculating mutual information inside a neural network.

- X input is an empirical sample of all possible inputs.
- Y label data. Every $x \in X$ has a corresponding label $y \in Y$.
- $T_{e,i}$ data for a specific epoch e and specific layer i in the neural network. The dataset is generated by feeding every $x \in X$ trough the neural network and recording the activations.

0.3.2 Discrete method

The method used by Tishby in his paper. The method estimates mutual information between the X or Y and the hidden layer T by assuming the observed empirical distribution of input samples is the true distribution. We use this assumption to compute entropies of T and varying subsets as outlined in Equation 24

$$I(X,Y) = H(X) - H(X|Y) = H(X) - \sum_{y \in Y} H(X|Y = y)p(Y = y)$$
 (24)

However just calculating mutual information for a discrete distribution is not enough as this yields mutual information equal to 0, in order to sidestep this issue we need to simulate randomness Tishby achieves this by grouping multiple values together, which he calls binning. A more detailed explanation why this is done is given in ??

Figure 2 trough to Figure 4 outline the full algorithm.

```
Algorithm: Mutual Information
1
    Input:
2
    X = x_1, x_2, ..., x_n
3
    Y = y_1, y_2, ..., y_n
    Output: I(X:Y)
5
    X = Bin close values of X together
6
    Y = Bin close values of Y together
    H(X) = Calculate entropy of X
8
    H(X|Y) = Calculate conditional entropy of X given Y
9
    I = H(X) - H(X|Y)
10
```

Figure 2: Pseudo code for computing mutual information refer to Figure 3 and Figure 4 for entropy computation.

```
Algorithm: Entropy - Discrete Method Input: X = x_1, x_2, ..., x_n Output: H(X) for \hat{x} \in Unique(X): count = 0 for x \in X:

if \hat{x} = x:

count = count + 1

P_x = \text{count} / \text{len}(X)

H(X) = -\sum_{x \in Unique(X)} P_x log(P_x)
```

Figure 3: Algorithm for computing entropy – Discrete method

```
Algorithm: Conditional Entropy
1
     Input:
2
     X = x_1, x_2, ..., x_n
     Y = y_1, y_2, ..., y_n
4
     Output: H(X|Y)
5
     H(X|Y) = H(X)
6
     for \hat{y} \in Unique(Y):
        \hat{X} = \prod
8
        for x, y \in zip(X, Y):
           if \hat{y} = y:
10
             \hat{X}.append(x)
11
           H(X|Y) = H(X|Y) - H(\hat{X})
12
```

Figure 4: Algorithm for computing conditional entropy

When computing mutual information between a hidden layer T and the input set X we can abuse the fact that every element $x \in X$ is unique and uniquely identifies an element $t \in T$ hence

$$H(T|X) = 0 (25)$$

$$I(T,X) = H(T) - H(T|X) = H(T)$$
 (26)

This does not affect the result but increases performance of our algorithm.

0.3.3 Kernel Density Estimation

The KDE method used in Saxe's paper but originally devised by Kolchinsky & Tracey (2017); Kolchinsky et al. (2017). As well as the Discrete method KDE assumes that the observed empirical distribution in the hidden layer T is the true distribution.

However, instead of binning values together KDE assumes the distribution is a mixture of Gaussians. Using this fact we can get an upper bound when calculating entropy for a collection of data points.

The algorithm closely follows figures: Figure 2, Figure 3, and Figure 4, however there is a change the way entropy is calculated so instead of Figure 3 we have Figure 5 below.

```
Algorithm: Entropy - KDE
1
    Input:
2
    X = x_1, x_2, ..., x_n
    var = noise variance 0.05 by default
4
    Output: H(X)
5
    dists = compute distance matrix of X
6
    dists = dists / 2*var # divide every distance by a value
    # an x is an observation of a hidden layer so, hence it's a vector
8
    # which has an associated dimension
9
    dim = x_1.dimension
10
    normconst = (\dim / 2)*log(2*\pi*var)
11
    lprobs = []
12
    for row in dists:
13
      lprobs.append(log(sum(exp(-row))) - log(n) - normconst
14
    H(X) = mean(lprobs) + (dim / 2)
15
```

Figure 5: Algorithm for computing entropy – Kernel Density Estimation method. The same algorithm as used by Saxe.

As before when computing mutual information between a hidden layer T and the input set X we can use the fact that every element $x \in X$ is unique and hence uniquely identifies an element in $t \in T$.

0.3.4 Advanced methods

Since mutual information estimation is a contentious part of the project we wanted to experiment with more advanced techniques however we were not able to adopt the methods for this project, the methods that we have tried are outlined below.

Mutual Information by Gaussian approximation

"Estimating Mutual Information by Local Gaussian Approximation" (Shuyang Gao). A promising way to estimate mutual information. However the implementation proved to be to difficult and time consuming so we abandoned it. I contacted out to the author but he was not able to provide any concrete code.

Geometrical Adaptive Entropy Estimation

"Breaking the Bandwidth Barrier: Geometric Adaptive Entropy Estimation" (Weihao Gao). We were pointed to this paper by S. Gao the author of the previous method, as previously this looked like a promising method to measure entropy and mutual information. Furthermore, the code was available online unfortunately we were not able to adapt the code for multidimensional values as a result we were getting wrong and inconsistent results. We decided making this method work would require too much time and is out of scope of this project.

0.4 Implementation Optimizations

Producing data for the information plane requires a substantial amount of computational power and memory, in order for the computation to complete in a reasonable amount of time we have to utilize all the available resources and minimize the amount of work we are doing.

0.4.1 Maximising Resource Utilization

The obvious way to maximise the resource usage is to parllelize the workload. If we refer to Figure 1, we can see two main ways we can do this.

The first way is to parallelize one of the two outer loops and run mutual information calculations in parallel, this is easy to do, however an issue occurs if we need a lot of memory since every instance of mutual information calculation manipulates the datasets creating copies, this is an issue for bigger datasets such as MNIST.

The second way is to parallelize the mutual information calculation itself, this is nice since we use minimal amounts of memory, however might be hard or impossible to implement as it depends on the method.

The second way is to parallelize the mutual information calculation itself, this method has a bonus that uses minimal amounts of memory improving performance for bigger datasets such as MNIST. However implementing this option might be hard as it heavily depends on the maths of the method, or impossible if the method has an inherently linear part to it. In our case KDE parallel performance is very good, however Tishby's Discrete method has some bottlenecks that I wasn't able to remove.

0.4.2 Minimising the Workload

Even when using all the systems resources the calculations take a very long time to complete as such we need to find a way to speed it up. If we consider an information plane graph for ex. ??, we see that from epoch to epoch there is very little change that is occurring, skipping some epochs might be a good way to reduce workload while keeping the overall result unchanged. We have implemented a couple of ways to skip the epochs

Simple Skip

A very simple simple way to skip epochs calculates mutual information for every n'th epoch.

It's quite effective and is fast to implement and easy to parallelize, however it yields subpar results. At the beginning of the training period during the fitting phase the step sizes are too big and yields gaps in data as there are big changes between consecutive epochs. Toward the end of the training period during the compression phase the step size becomes too small and we are wasting computation as the changes between epochs is negligible. The next two methods address this problem, but have their own drawbacks.

Delta Skip – Exact

The Exact Delta Skip method introduces a distance metric which measures mutual information distance between two epochs. Using the distance metric the method tries to skip as many epochs

as possible while still guaranteeing that the distance is at most delta δ , and backtracks when necessary.

The Algorithm starts by measuring every consecutive epoch (skip = 1) as at the start of the training epochs are far apart – distance between them is more than δ . When the distance become smaller there is no need to measure every epoch so we exponentially increase skip until the difference between consecutively measured epochs is larger than δ . At this point we run into the issue of backtracking since we made a guarantee that every measured epoch will be at most δ apart.

We can consider the backtracing problem as an array of unknown – let's call this array a section. Every unknown in a section corresponds to the saved state of the neural network, revealing the unknown is equivalent to computing mutual information for the epoch. In this context we can rephrase the problem of backtracking as finding a subset of the section such that the difference between every consecutive number is less than or equal δ .

Consider an example with $\delta = 2$. At the start all the values are unknown

We measure values at the start and the end of the section to get the range.

We continue to split the section and measure the middle element until the difference between consecutive elements is less than or equal to δ or there are no more elements left.

2	?	?	?	10	?	?	?	14
2	?	6	?	10	?	12	?	14
2	5	6	8	10	?	12	?	14

The algorithm stops at this stage as:

- The distances between 10, 12 and 14 are 2 and $\delta \le 2$ holds.
- There is no cell between 2 and 5, even though the distance is $3 > \delta$.

Every unknown has to save the state of the neural network, that means that every unknown contains |X|*|nodes| float numbers. To put it into perspective if we use the MNIST dataset which has 240,000 samples into a small network of 128 nodes every unknown would contain 0.25GB of data. As such this method is unsuited for large datasets in that case Delta Skip Approximate is more suited for the job. A way to remedy the problem is instead of saving all the activations, just save the neural network weights and compute the activations just before calculating Mutual Information for the epoch

Parallelizing The entire single threaded algorithm is described in Figure 6 and Figure 7. However there are two main ways how we can parallelize the algorithm.

- Parallelize Backtracking every time we need to backtrack we can launch two threads to do the computation, it's quite easy to implement however we need to be careful as we don't want to change the global *skip* value.
- Compute Multiple sections consider a section as before. Once we compute the latest epoch of the array we can launch backtracking and the next section computation in parallel as separate threads. We need to wait until the latest epoch is computed before computing the next section as we might need to update the *skip* value.

```
Algorithm: DeltaSkipExact
    Input:
2
    prev = mutual information result of the previous epoch
3
    curr = mutual information result of the current epoch
    \delta = user specified maximum "distance" between epochs
5
    multiplier = how much to multiply skip by
6
    Output:
    Algorithm:
    dist = Distance(prev, curr)
9
    if dist > \delta:
10
      Backtrack(prev, curr) # Figure 7
11
    else:
12
      skip = skip*multiplier
13
```

Figure 6: Delta Skip Exact. The skip value is assumed to be global it specifies how many epochs to skip until we measure again

```
Algorithm: Backtrack
2
    prev = mutual information result of the previous epoch
    curr = mutual information result of the current epoch
4
    \delta = user specified maximum "distance" between epochs
5
    Output:
    if prev.epoch + 1 < curr.epoch:</pre>
      mid_epoch = average(prev.epoch, curr.epoch)
8
      mid = Calculate Mutual Information of mid_epoch
      DeltaSkipExact(prev, mid, \delta, 1)
10
      DeltaSkipExact(mid, curr, \delta, 1)
11
```

Figure 7: Backtrack Algorithm

Distance Metric Every epoch that we measure yields us with a vector of mutual information values, that is for every layer T we receive two values I(X,T) and I(Y,T). Given the information vectors for two epochs we need to find a reasonable way to measure distance between them.

The distance is used for the purposes of speeding up the computation and won't meaningfully impact the results. I've chosen to define the distance as the maximum shift between the two epochs refer to Equation 27 how to compute it or to Figure 8 for a graphical representation.

$$D = \max_{t \in T} [\max(I_e(X, t) - I_{\hat{e}}(X, t), I_e(Y, t) - I_{\hat{e}}(Y, t))]$$
(27)

The equation reduces the vector to a single value that is easy to compare and to track.

If we consider the Figure 8 we can see that the axis are different in scale this is due to input X and label Y having different entropy values H(X) = 12 and H(Y) = 1. As such we might wish to adjust Equation 27, and scale mutual information values by the entropy as in Equation 28.

$$D = \max_{s \in \{X,Y\}} \max_{t \in T} [(I_e(s,t) - I_{\hat{e}}(s,t))/H(s)]$$
 (28)

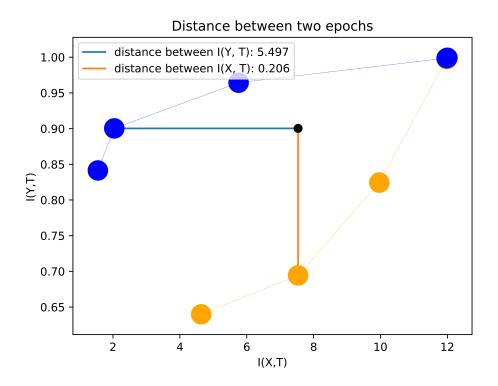


Figure 8: Example how distance between two epochs is measured.

Delta Skip – Approximate

The Exact method suffers the same problem as when we try to instantiate too many mutual information calculation instances, namely it runs out of memory if our dataset is too big. In order to solve this we use the approximate method which follows closely the Exact method.

The Algorithm – refer to Figure 9, as previously, in the Exact method it uses a distance metric and measures every n'th epoch where n is adaptive and depends on how close the

epochs are. The critical difference between Exact and Approximate method happens when the distance between epochs is more than δ , the Exact method attempts to backtrack and fill in the gap whereas the Approximate doesn't backtrack and just continues to the next epoch, this is justified because the approximate method assumes that distance between epochs only shrinks and never increases.

This method does not suffer from memory issues but cannot be parallelized as in order to compute next epoch we need to know the distance between current epoch and the previous one. Delta Approximate method performs best when paired with highly parallel Mutual Information Estimator.

```
Algorithm: Delta Skip - Approximate
2
    prev = mutual information result of the previous epoch
3
    curr = mutual information result of the current epoch
    \delta = user specified estimated "distance" between epochs
5
    Output:
6
    Algorithm:
    dist = Distance(prev, curr)
    if dist > \delta:
9
      skip = skip
10
    else:
11
      skip = skip*2
12
```

Figure 9: Delta Skip Approximate

0.5 As-If-Random Experiment

Tishby's paper relies heavily on the notion that weights of a neural network behave 'as if' they are random, however his and Saxe's experiments don't capture this idea as much as they could – refer to ??.

An experiment that better captures the ideas of random is instead of

- Tishby and Saxe didn't capture randomness incredibly well
- We have a bettter way
- How we've done it, only measure compression at the end of the training period when the network is stable and only "brownian randomness happens" (refer paper what randomness).
- the problem is every x in X is unique, if we sample multiple epochs instead of only one we have more compression
- we rely on the property of the network that there is very little change at the end of the training period

• Achieves compression even with ReLu yay!!!!!!!!

We believe that Tishby's experiments Saxe's experiments could be improved, with introducing a better notion of randomness. blah blah blah blah not finished.

0.6 Repository Structure