

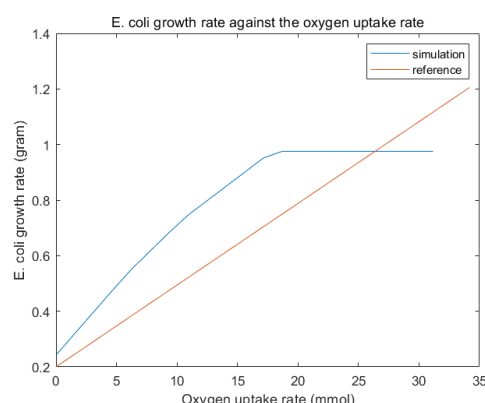
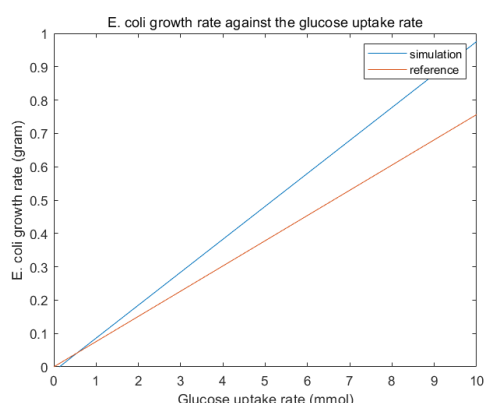
In the modeling part, we are mainly working on simulating the function of the fermentation system at different levels and serving suggestions for future implementation. The work consists of two parts, flux balance analysis (FBA) and diffusion model of alginate beads considering bacterial metabolism, specifically, the photosynthesis of *Synechococcus sp.*, the formaldehyde degradation function, and sucrose hydrolysis by two types of *e. coli*.

## 1. Flux Balance Analysis (FBA)

The first part is about flux balance analysis, an approach for studying a genome-scale metabolic network, containing almost all known metabolic reactions, genes, and related enzymes for an organism (Orth, 2010). The reason we chose this approach as the simulation part is not only there were existed reconstructed microorganism models, but through dynamic FBA and some well-developed toolboxes such as COBRA and COMETs, we can track the changes in metabolite concentrations in the presence of complex reactions within microbial bodies, and even simulate the co-cultivation of blue algae and *e. coli*.

### 1.1 Verification

First of all, we need to verify the model.

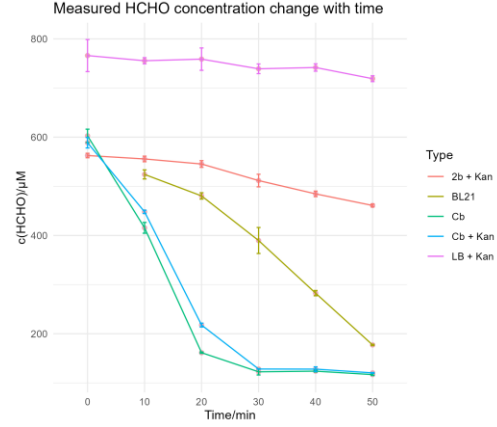
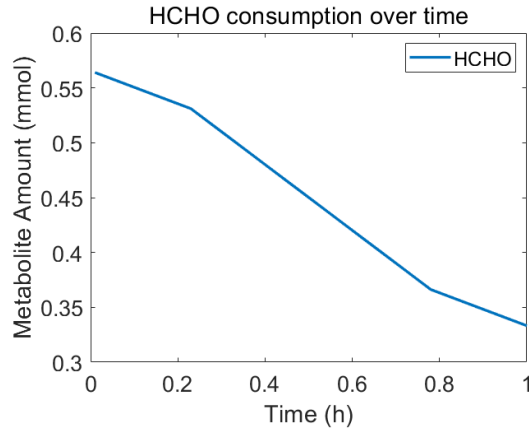


### 1.2 Modification

Then, we modify the model according to the metabolite pathway.

### 1.3 Dynamic-FBA

After that, we adjusted the parameters to fit the experiment data, and the simulation result of *E. coli*'s HCHO consumption is presented below.



#### 1.4 Multi-species dFBA (dynamic FBA)

This part gives a general idea of how the coculture system works.

## 2. Diffusion Model

This model is aimed at giving an insight into how alginate beads affect the metabolite of the microorganism embedded. In our project, we make three types of beads, one with blue algae for sucrose production, one with e. coli for sucrose degradation, and one with e. coli for formaldehyde degradation. During the development, we realized that we could increase the accuracy by the embedding ODE system description of the formaldehyde degradation pathway.

The model can be separated into two parts: diffusion and metabolite. We first developed the diffusion model and started a rough simulation, then combined the metabolite part with the diffusion model.

### 2.1 Metabolite function

Before we start, notice that one bead will only have one function, and we will not simulate multiple beads together for now.

#### 2.1.1 Photosynthesis

We describe photosynthesis with the Michaelis-Menten equation and obtain the parameters through curve fitting with data from the wet lab.

#### 2.1.2 Sucrose hydrolysis

#### 2.1.3 Formaldehyde degradation

### 2.2 Diffusion model

The diffusion model is based on Fick's second law

$$\frac{\partial c}{\partial t} = \frac{\partial^2 c}{\partial x^2} D \quad (1)$$

In three dimension space, the formula can be rewrote with laplacian operator

$$\frac{\partial c}{\partial t} = \nabla^2 c D \quad (2)$$

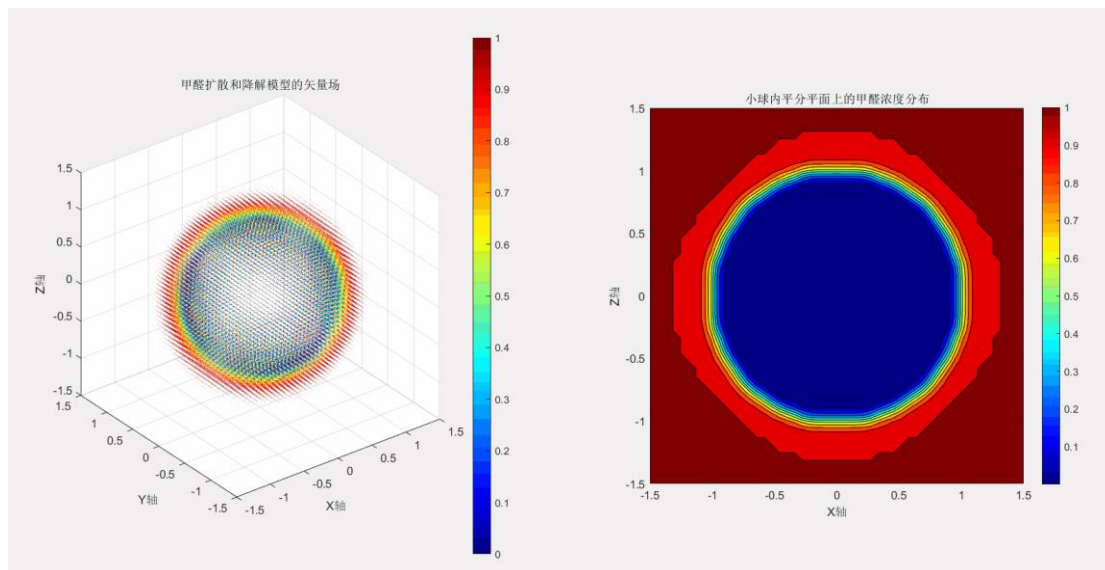
Where

$$\nabla^2 = \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2} \quad (3)$$

Which means for a point, the unit change of concentration within unit time equals the point's divergence times original concentration times the diffusion coefficient of the substance in a specific matter, in this case, the alginate is the matter.

This formula tells us how a substance diffuses into another quantitatively, and more importantly, we could set up a simulation based on that with the finite element method (FEM).

This is the pure alginate bead simulation.



## 2.3 Result

The simulation was done with MATLAB.

The reason we did not further do the simulation of multiple beads is based on an assumption, that with the pump, the solution is well mixed in every moment.

## 2.4 Discussion

We developed an “alginate beads with microorganism embedded” model, and set up a mathematical simulation with the finite element method. The result showed that after a sufficient time, the system will reach homeostasis, and the diffusion rate equals the consumption/production rate.

There are still much things to be done in the future. The cell growth is limited due to the volume of the beads, and the distribution inside the beads is uneven. There are still bricks left aside, thus we upload our commented MATLAB code and served it as a rough

framework for teams want to give FEM a try.

