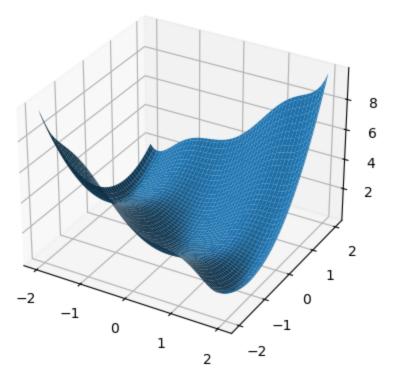
## **Tutorial 2**

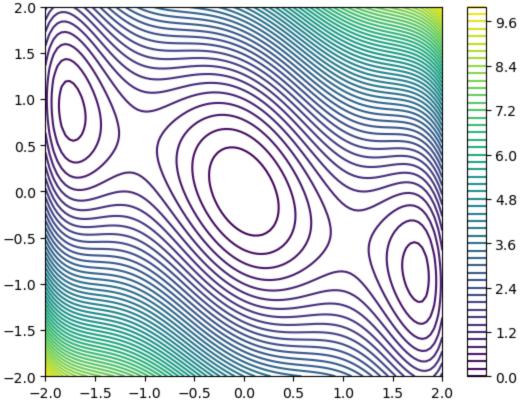
### **Outline**

- Simulated Annealing (for HW#2)
- Pandas
- Numba

## Simulated Annealing

```
In [1]: import numpy as np
        import matplotlib.pyplot as plt
        def Camel(X):
            x, y = X
            return 2 * x**2 - 1.05 * x**4 + x**6 / 6 + x * y + y**2
        def plot_surface(func, x_min=-2, x_max=2, y_min=-2, y_max=2):
            a = np.linspace(x_min, x_max, 100)
            b = np.linspace(y_min, y_max, 100)
            x,y = np.meshgrid(a, b)
            z = func((x, y))
            fig = plt.figure()
            ax = fig.add_subplot(projection='3d')
            ax.plot_surface(x, y, z)
        plot_surface(Camel)
        def draw_path(func, path=None, x_min=-2, x_max=2, y_min=-2, y_max=2):
            a = np.linspace(x_min, x_max, 100)
            b = np.linspace(y_min, y_max, 100)
            x, y = np.meshgrid(a, b)
            z = func((x, y))
            fig, ax = plt.subplots()
            contour = ax.contour(x, y, z, 50)
            plt.colorbar(contour)
            if path:
                 ax.plot(path[:, 0], path[:, 1], color='red')
                 print(len(path))
        draw_path(Camel)
```





No description has been provided for this image

• Random Displacement:

$$X_{i+1} = X_i + \Delta*(2*\mathrm{URN}-1)$$

• Metropolis Rule:

$$P( ext{accept}) = \exp\left(-rac{\Delta E}{T}
ight)$$

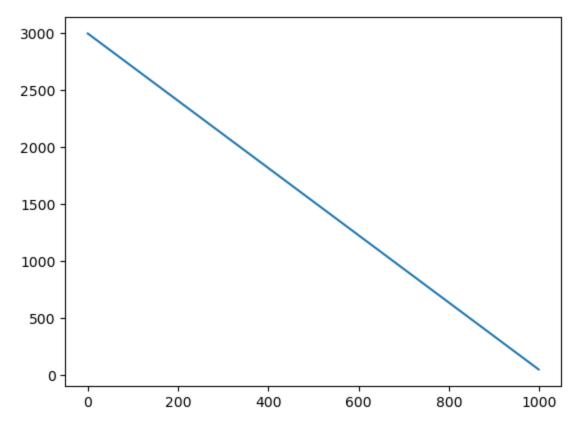
```
In [2]: def SA(solution, func, schedule, delta, boundary, n_iter, report_interval=None):
            Simulated Annealing for minimization
            Parameters
             _____
            solution: np.ndarray
                Initial guess
            func: Callable
                 Function to minimize
            schedule: np.ndarray
                An array of temperatures for simulated annealing
            delta: float
                Magnitude of random displacement
            boundary: tuple
                 Boundary of the variables to minimize. (lowerbound, upperbound)
            n_iter: int
                Number of random displacement move in each temperature
            report_interavl: int
                 Number of temperature steps to report result
            Returns
             _____
            res: dict
                Minimized point and its evaulation value
            best_solution = solution.copy()
            lowest_eval = func(best_solution)
            for idx, temp in enumerate(schedule):
                 if report_interval is not None and ((idx + 1) % report_interval == 0 or idx
                    msg = (
                         f"{idx + 1}/{len(schedule)}, Temp: {temp:.2f}, "
                        f"Best solution: {best_solution}, Value: {lowest_eval:.7f}"
                    print(msg)
                for n in range(n iter):
                    trial = solution.copy()
                    trial += delta * (2 * np.random.random(trial.shape) - 1)
                    if np.all(trial >= boundary[0]) and np.all(trial <= boundary[1]):</pre>
                         # fill in acceptance criterion
                         if np.exp(-(func(trial) - func(solution)) / temp) > np.random.rando
                             solution = trial
                             if func(solution) < lowest_eval:</pre>
                                 # update solution here
                                 best_solution = solution.copy()
                                 lowest_eval = func(best_solution)
```

```
return {"solution":best_solution, "evaluation":lowest_eval}
```

Try linear cooling

```
In [3]: linear_cooling = np.linspace(3000, 50, 1000)
    plt.plot(linear_cooling)
```

Out[3]: [<matplotlib.lines.Line2D at 0x1a54d604710>]



```
In [4]: # Start from a point which is close to local minimum
starting_point = np.array([-1.7, 0.7])
SA(starting_point, Camel, linear_cooling, 0.1, (-2, 2), 5, 100)
1/1000, Temp: 3000.00, Best solution: [-1.7 0.7], Value: 0.3332232
```

100/1000, Temp: 2707.66, Best solution: [ 0.02742354 -0.38066902], Value: 0.1359731 200/1000, Temp: 2412.36, Best solution: [ 0.08827732 0.04828203], Value: 0.0221154 300/1000, Temp: 2117.07, Best solution: [ 0.01358763 -0.03255679], Value: 0.0009868 400/1000, Temp: 1821.77, Best solution: [ 0.01358763 -0.03255679], Value: 0.0009868 500/1000, Temp: 1526.48, Best solution: [ 0.01358763 -0.03255679], Value: 0.0009868 600/1000, Temp: 1231.18, Best solution: [ 0.01358763 -0.03255679], Value: 0.0009868 700/1000, Temp: 935.89, Best solution: [ 0.01358763 -0.03255679], Value: 0.0009868 800/1000, Temp: 640.59, Best solution: [ 0.01358763 -0.03255679], Value: 0.0009868 900/1000, Temp: 345.30, Best solution: [ 0.01358763 -0.03255679], Value: 0.0009868 1000/1000, Temp: 50.00, Best solution: [ 0.01358763 -0.03255679], Value: 0.0009868

In [5]: # Local minimization methods fail to find the global minimum
from scipy.optimize import minimize

### **Pandas**

Documentation

```
In [6]: import pandas as pd

C:\Users\artui\AppData\Local\Temp\ipykernel_12292\4080736814.py:1: DeprecationWarnin
g:
    Pyarrow will become a required dependency of pandas in the next major release of pan
das (pandas 3.0),
    (to allow more performant data types, such as the Arrow string type, and better inte
    roperability with other libraries)
    but was not found to be installed on your system.
    If this would cause problems for you,
    please provide us feedback at https://github.com/pandas-dev/pandas/issues/54466

import pandas as pd
```

### Read CSV file

```
In [7]: df = pd.read_csv("Datasets/titanic.csv")
    print(type(df))
    df
```

<class 'pandas.core.frame.DataFrame'>

				Pclass	Name		1.90	энээр	Parch	Ticket	F
	0	1	0	3	Braund, Mr. Owen Harris	male	22.0	1	0	A/5 21171	7.2!
	1	2	1	1	Cumings, Mrs. John Bradley (Florence Briggs Th	female	38.0	1	0	PC 17599	71.2{
	2	3	1	3	Heikkinen, Miss. Laina	female	26.0	0	0	STON/O2. 3101282	7.9%
	3	4	1	1	Futrelle, Mrs. Jacques Heath (Lily May Peel)	female	35.0	1	0	113803	53.10
	4	5	0	3	Allen, Mr. William Henry	male	35.0	0	0	373450	8.0!
	•••			•••				•••			
8	886	887	0	2	Montvila, Rev. Juozas	male	27.0	0	0	211536	13.00
8	387	888	1	1	Graham, Miss. Margaret Edith	female	19.0	0	0	112053	30.00
8	388	889	0	3	Johnston, Miss. Catherine Helen "Carrie"	female	NaN	1	2	W./C. 6607	23.4!
8	889	890	1	1	Behr, Mr. Karl Howell	male	26.0	0	0	111369	30.00
8	390	891	0	3	Dooley, Mr. Patrick	male	32.0	0	0	370376	7.7!
89	91 ro	ws × 12 colur	nns								
4											•

In [8]: df.head(40)

Out[8]:		Passengerld	Survived	Pclass	Name	Sex	Age	SibSp	Parch	Ticket	
	0	1	0	3	Braund, Mr. Owen Harris	male	22.0	1	0	A/5 21171	7
	1	2	1	1	Cumings, Mrs. John Bradley (Florence Briggs Th	female	38.0	1	0	PC 17599	71
	2	3	1	3	Heikkinen, Miss. Laina	female	26.0	0	0	STON/O2. 3101282	7
	3	4	1	1	Futrelle, Mrs. Jacques Heath (Lily May Peel)	female	35.0	1	0	113803	53
	4	5	0	3	Allen, Mr. William Henry	male	35.0	0	0	373450	}
	5	6	0	3	Moran, Mr. James	male	NaN	0	0	330877	{
	6	7	0	1	McCarthy, Mr. Timothy J	male	54.0	0	0	17463	51
	7	8	0	3	Palsson, Master. Gosta Leonard	male	2.0	3	1	349909	2*
	8	9	1	3	Johnson, Mrs. Oscar W (Elisabeth Vilhelmina Berg)	female	27.0	0	2	347742	1.
	9	10	1	2	Nasser, Mrs. Nicholas (Adele Achem)	female	14.0	1	0	237736	3(
	10	11	1	3	Sandstrom, Miss. Marguerite Rut	female	4.0	1	1	PP 9549	16
	11	12	1	1	Bonnell, Miss. Elizabeth	female	58.0	0	0	113783	26
	12	13	0	3	Saundercock, Mr. William Henry	male	20.0	0	0	A/5. 2151	{

	Passengerld	Survived	Pclass	Name	Sex	Age	SibSp	Parch	Ticket	
13	14	0	3	Andersson, Mr. Anders Johan	male	39.0	1	5	347082	3.
14	15	0	3	Vestrom, Miss. Hulda Amanda Adolfina	female	14.0	0	0	350406	7
15	16	1	2	Hewlett, Mrs. (Mary D Kingcome)	female	55.0	0	0	248706	16
16	17	0	3	Rice, Master. Eugene	male	2.0	4	1	382652	29
17	18	1	2	Williams, Mr. Charles Eugene	male	NaN	0	0	244373	13
18	19	0	3	Vander Planke, Mrs. Julius (Emelia Maria Vande	female	31.0	1	0	345763	18
19	20	1	3	Masselmani, Mrs. Fatima	female	NaN	0	0	2649	7
20	21	0	2	Fynney, Mr. Joseph J	male	35.0	0	0	239865	26
21	22	1	2	Beesley, Mr. Lawrence	male	34.0	0	0	248698	13
22	23	1	3	McGowan, Miss. Anna "Annie"	female	15.0	0	0	330923	{
23	24	1	1	Sloper, Mr. William Thompson	male	28.0	0	0	113788	3;
24	25	0	3	Palsson, Miss. Torborg Danira	female	8.0	3	1	349909	2′
25	26	1	3	Asplund, Mrs. Carl Oscar (Selma Augusta Emilia	female	38.0	1	5	347077	3*
26	27	0	3	Emir, Mr. Farred	male	NaN	0	0	2631	-

	Passengerld	Survived	Pclass	Name	Sex	Age	SibSp	Parch	Ticket	
				Chehab						
27	28	0	1	Fortune, Mr. Charles Alexander	male	19.0	3	2	19950	263
28	29	1	3	O'Dwyer, Miss. Ellen "Nellie"	female	NaN	0	0	330959	7
29	30	0	3	Todoroff, Mr. Lalio	male	NaN	0	0	349216	7
30	31	0	1	Uruchurtu, Don. Manuel E	male	40.0	0	0	PC 17601	27
31	32	1	1	Spencer, Mrs. William Augustus (Marie Eugenie)	female	NaN	1	0	PC 17569	146
32	33	1	3	Glynn, Miss. Mary Agatha	female	NaN	0	0	335677	7
33	34	0	2	Wheadon, Mr. Edward H	male	66.0	0	0	C.A. 24579	1(
34	35	0	1	Meyer, Mr. Edgar Joseph	male	28.0	1	0	PC 17604	82
35	36	0	1	Holverson, Mr. Alexander Oskar	male	42.0	1	0	113789	52
36	37	1	3	Mamee, Mr. Hanna	male	NaN	0	0	2677	7
37	38	0	3	Cann, Mr. Ernest Charles	male	21.0	0	0	A./5. 2152	{
38	39	0	3	Vander Planke, Miss. Augusta Maria	female	18.0	2	0	345764	18
39	40	1	3	Nicola- Yarred, Miss. Jamila	female	14.0	1	0	2651	1.

In [9]: df.tail(10)

]:		Passengerld	Survived	Pclass	Name	Sex	Age	SibSp	Parch	Ticket	
	881	882	0	3	Markun, Mr. Johann	male	33.0	0	0	349257	7
	882	883	0	3	Dahlberg, Miss. Gerda Ulrika	female	22.0	0	0	7552	10
	883	884	0	2	Banfield, Mr. Frederick James	male	28.0	0	0	C.A./SOTON 34068	10
	884	885	0	3	Sutehall, Mr. Henry Jr	male	25.0	0	0	SOTON/OQ 392076	7
	885	886	0	3	Rice, Mrs. William (Margaret Norton)	female	39.0	0	5	382652	29
	886	887	0	2	Montvila, Rev. Juozas	male	27.0	0	0	211536	13
	887	888	1	1	Graham, Miss. Margaret Edith	female	19.0	0	0	112053	30
	888	889	0	3	Johnston, Miss. Catherine Helen "Carrie"	female	NaN	1	2	W./C. 6607	23
	889	890	1	1	Behr, Mr. Karl Howell	male	26.0	0	0	111369	30
	890	891	0	3	Dooley, Mr. Patrick	male	32.0	0	0	370376	7
	4										•

# **Drop columns**

In [10]: df2 = df.drop(['Cabin'], axis=1, inplace=True)

## **Drop NaN values**

Drop the rows where at least one element is missing

In [11]: df.dropna()

]:		PassengerId	Survived	Pclass	Name	Sex	Age	SibSp	Parch	Ticket	Fi
	0	1	0	3	Braund, Mr. Owen Harris	male	22.0	1	0	A/5 21171	7.25
	1	2	1	1	Cumings, Mrs. John Bradley (Florence Briggs Th	female	38.0	1	0	PC 17599	71.28
	2	3	1	3	Heikkinen, Miss. Laina	female	26.0	0	0	STON/O2. 3101282	7.92
	3	4	1	1	Futrelle, Mrs. Jacques Heath (Lily May Peel)	female	35.0	1	0	113803	53.10
	4	5	0	3	Allen, Mr. William Henry	male	35.0	0	0	373450	8.05
8	85	886	0	3	Rice, Mrs. William (Margaret Norton)	female	39.0	0		382652	29.12
8	86	887	0	2	Montvila, Rev. Juozas	male	27.0	0	0	211536	13.00
8	87	888	1	1	Graham, Miss. Margaret Edith	female	19.0	0	0	112053	30.00
8	89	890	1	1	Behr, Mr. Karl Howell	male	26.0	0	0	111369	30.00
8	90	891	0	3	Dooley, Mr. Patrick	male	32.0	0	0	370376	7.75
71	2 ro	ws × 11 colur	mns								
4											•

Drop the columns where at least one element is missing.

In [12]: df.dropna(axis=1) # or axis='columns'

Out[12]:		Passengerld	Survived	Pclass	Name	Sex	SibSp	Parch	Ticket	Fare
	0	1	0	3	Braund, Mr. Owen Harris	male	1	0	A/5 21171	7.2500
	1	2	1	1	Cumings, Mrs. John Bradley (Florence Briggs Th	female	1	0	PC 17599	71.2833
	2	3	1	3	Heikkinen, Miss. Laina	female	0	0	STON/O2. 3101282	7.9250
	3	4	1	1	Futrelle, Mrs. Jacques Heath (Lily May Peel)	female	1	0	113803	53.1000
	4	5	0	3	Allen, Mr. William Henry	male	0	0	373450	8.0500
	•••									
	886	887	0	2	Montvila, Rev. Juozas	male	0	0	211536	13.0000
	887	888	1	1	Graham, Miss. Margaret Edith	female	0	0	112053	30.0000
	888	889	0	3	Johnston, Miss. Catherine Helen "Carrie"	female	1	2	W./C. 6607	23.4500
	889	890	1	1	Behr, Mr. Karl Howell	male	0	0	111369	30.0000
	890	891	0	3	Dooley, Mr. Patrick	male	0	0	370376	7.7500

891 rows × 9 columns

Define in which columns to look for missing values.

In [13]: df.dropna(subset=['Age'])

L3]:		PassengerId	Survived	Pclass	Name	Sex	Age	SibSp	Parch	Ticket	Fi
	0	1	0	3	Braund, Mr. Owen Harris	male	22.0	1	0	A/5 21171	7.25
	1	2	1	1	Cumings, Mrs. John Bradley (Florence Briggs Th	female	38.0	1	0	PC 17599	71.28
	2	3	1	3	Heikkinen, Miss. Laina	female	26.0	0	0	STON/O2. 3101282	7.92
	3	4	1	1	Futrelle, Mrs. Jacques Heath (Lily May Peel)	female	35.0	1	0	113803	53.10
	4	5	0	3	Allen, Mr. William Henry	male	35.0	0	0	373450	8.05
	•••										
	885	886	0	3	Rice, Mrs. William (Margaret Norton)	female	39.0	0	5	382652	29.12
	886	887	0	2	Montvila, Rev. Juozas	male	27.0	0	0	211536	13.00
	887	888	1	1	Graham, Miss. Margaret Edith	female	19.0	0	0	112053	30.00
	889	890	1	1	Behr, Mr. Karl Howell	male	26.0	0	0	111369	30.00
	890	891	0	3	Dooley, Mr. Patrick	male	32.0	0	0	370376	7.75
7	714 rc	ows × 11 colur	mns								
	4										•

## Indexing

```
In [14]: df.loc[0, "Pclass"]
Out[14]: 3
In [15]: df.iloc[0, 2]
Out[15]: 3
In [16]: df[['Pclass', 'Survived']]
Out[16]:
               Pclass Survived
            0
                   3
                            0
                   1
                            1
            2
                   3
                            1
                   1
                            1
                   3
                            0
            4
                   2
                            0
          886
          887
          888
                   3
                            0
          889
                   1
                            1
                   3
                            0
          890
         891 rows × 2 columns
In [17]: df[df['Survived'] == 1]
```

Out[17]:		PassengerId	Survived	Pclass	Name	Sex	Age	SibSp	Parch	Ticket	Fi
	1	2	1	1	Cumings, Mrs. John Bradley (Florence Briggs Th	female	38.0	1	0	PC 17599	71.28
	2	3	1	3	Heikkinen, Miss. Laina	female	26.0	0	0	STON/O2. 3101282	7.92
	3	4	1	1	Futrelle, Mrs. Jacques Heath (Lily May Peel)	female	35.0	1	0	113803	53.1(
	8	9	1	3	Johnson, Mrs. Oscar W (Elisabeth Vilhelmina Berg)	female	27.0	0	2	347742	11.13
	9	10	1	2	Nasser, Mrs. Nicholas (Adele Achem)	female	14.0	1	0	237736	30.07
	•••										
	875	876	1	3	Najib, Miss. Adele Kiamie "Jane"	female	15.0	0	0	2667	7.22
	879	880	1	1	Potter, Mrs. Thomas Jr (Lily Alexenia Wilson)	female	56.0	0	1	11767	83.15
	880	881	1	2	Shelley, Mrs. William (Imanita Parrish Hall)	female	25.0	0	1	230433	26.00
	887	888	1	1	Graham, Miss.	female	19.0	0	0	112053	30.00

	Passengerld	Survived	Pclass	Name	Sex	Age	SibSp	Parch	Ticket	Fi
				Margaret Edith						
889	890	1	1	Behr, Mr. Karl Howell	male	26.0	0	0	111369	30.00

342 rows × 11 columns

#### Other useful methods

Use .values attribute to get values in numpy.ndarray

```
In [18]: df.values
Out[18]: array([[1, 0, 3, ..., 'A/5 21171', 7.25, 'S'],
                  [2, 1, 1, ..., 'PC 17599', 71.2833, 'C'],
                  [3, 1, 3, ..., 'STON/02. 3101282', 7.925, 'S'],
                  [889, 0, 3, ..., 'W./C. 6607', 23.45, 'S'],
                  [890, 1, 1, ..., '111369', 30.0, 'C'],
                  [891, 0, 3, ..., '370376', 7.75, 'Q']], dtype=object)
          Use describe() method to get statistics
In [19]:
          df.describe()
Out[19]:
                  PassengerId
                                 Survived
                                                Pclass
                                                                        SibSp
                                                                                    Parch
                                                             Age
                                                                                                 Far€
                                           891.000000
                                                       714.000000
                                                                   891.000000
          count
                   891.000000
                               891.000000
                                                                               891.000000
                                                                                           891.000000
                   446.000000
                                                                                            32.204208
           mean
                                 0.383838
                                             2.308642
                                                        29.699118
                                                                     0.523008
                                                                                 0.381594
             std
                   257.353842
                                 0.486592
                                                        14.526497
                                                                     1.102743
                                             0.836071
                                                                                 0.806057
                                                                                            49.693429
            min
                     1.000000
                                 0.000000
                                             1.000000
                                                         0.420000
                                                                     0.000000
                                                                                 0.000000
                                                                                             0.000000
            25%
                   223.500000
                                 0.000000
                                             2.000000
                                                        20.125000
                                                                     0.000000
                                                                                 0.000000
                                                                                             7.910400
            50%
                   446.000000
                                 0.000000
                                             3.000000
                                                        28.000000
                                                                     0.000000
                                                                                 0.000000
                                                                                            14.454200
                                                                                 0.000000
            75%
                   668.500000
                                 1.000000
                                             3.000000
                                                        38.000000
                                                                     1.000000
                                                                                            31.000000
                   891.000000
                                 1.000000
                                                                     8.000000
                                                                                           512.329200
            max
                                             3.000000
                                                        80.000000
                                                                                 6.000000
          Use .index or .columns get index/columns
In [20]: for index in df.index:
              print(index)
```

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Tutorial\_2 1/31/24, 10:31 PM

```
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890
```

In [21]: for col in df.columns:
 print(col)

```
PassengerId
        Survived
        Pclass
        Name
        Sex
        Age
        SibSp
        Parch
        Ticket
        Fare
        Embarked
         Use to_csv() to export DataFrame
        df.to_csv("test_export.csv")
In [22]:
         Use sort_values() method to sort the DataFrame according to values in one column.
         df.sort_values(by=["Age"], ascending=False)
In [23]:
```

Out[23]

	Passengerld	Survived	Pclass	Name	Sex	Age	SibSp	Parch	Ticket	F
630	631	1	1	Barkworth, Mr. Algernon Henry Wilson	male	80.0	0	0	27042	30.00
851	852	0	3	Svensson, Mr. Johan	male	74.0	0	0	347060	7.7
493	494	0	1	Artagaveytia, Mr. Ramon	male	71.0	0	0	PC 17609	49.50
96	97	0	1	Goldschmidt, Mr. George B	male	71.0	0	0	PC 17754	34.6
116	117	0	3	Connors, Mr. Patrick	male	70.5	0	0	370369	7.7
•••										
859	860	0	3	Razi, Mr. Raihed	male	NaN	0	0	2629	7.27
863	864	0	3	Sage, Miss. Dorothy Edith "Dolly"	female	NaN	8	2	CA. 2343	69.5
868	869	0	3	van Melkebeke, Mr. Philemon	male	NaN	0	0	345777	9.50
878	879	0	3	Laleff, Mr. Kristo	male	NaN	0	0	349217	7.89
888	889	0	3	Johnston, Miss. Catherine Helen "Carrie"	female	NaN	1	2	W./C. 6607	23.4!
891 r	ows × 11 colur	mns								
4										

## Numba

Use pip install numba or conda install numba -c conda-forge to install numba package.

Numba is a package that help users to accelerate the code.

In [24]: **import** numba

```
In [25]: def test():
    i = 0
    for a in range(100000):
        i += a
    return i

%timeit test()
```

4.98 ms  $\pm$  219  $\mu$ s per loop (mean  $\pm$  std. dev. of 7 runs, 100 loops each)

```
In [26]: @numba.njit()
def test():
    i = 0
    for a in range(100000):
        i += a
    return i

%timeit test()
```

The slowest run took 65.00 times longer than the fastest. This could mean that an in termediate result is being cached.

1.1  $\mu$ s  $\pm$  2.21  $\mu$ s per loop (mean  $\pm$  std. dev. of 7 runs, 1 loop each)