Note on Change Detection

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?? solve the change detection problem with i.i.d in Bayesian setup. But he didn't show the asymptotic property of his proposal. Notation in the paper follows ?.

1 Problem formulation

The observed sequence of random variables $X_1, X_2, ...$ are i.i.d., untile a change occurs, the observations are again i.i.d., but with another distribution. General guideline for math notations:

- use lower case Greek letter for parameters, β , α
- use capital letters for random variables, X,Y, sometime for matrix
- use lower case letter for realization of random variables, x,y, or individual observation.
- use \mathbb{R} denote space and \mathcal{F} to denote σ -algebra on the space.

2 Measure

A measure is a set function, a mapping which associates a real number with a set. ?

3 Expectation

Corollary 3.1. Let $g : \mathbb{R} \to \mathbb{R}$ be a function with that property that $x \geq a$ implies $g(x) \geq g(a) > 0$, for a given constant a. Then

$$P(X \ge a) \le \frac{E(g(X))}{g(a)}.$$

Proof.

$$g(a)P(X \ge a) = g(a) \int_{x \ge a} dF(x)$$

$$\le \int_{x \ge a} g(x)dF(x)$$

$$\le E(g(X).$$

Appendix

Notations	Description
λ	structural breaking time
au	stopping time
Ω	sample space
$\omega \in \Omega$	a point in the sample space
\mathbb{R}	real number space
Q	rational number space
$(\Omega, \mathcal{F}, \mu)$	measurable space

Table 1: Table of Notations