Recent advances in software engineering 32039 Laboratory exercises: Week 5

Question 1 Write these out without any λ .

1.
$$elim = \lambda x.x \ \lambda y \rightarrow y$$

$$\begin{array}{ccc} 2. & \mathtt{equal} = \lambda x. \\ & x \to \mathtt{true} \\ & \mid \lambda y.\mathtt{false} \end{array}$$

3.
$$\begin{array}{ccc} \mathtt{elim*} = \lambda x. \\ & x \ \lambda y \to \mathtt{elim*} \ y \\ & | \ \lambda y \to y \end{array}$$

4. update-c =
$$\lambda x \rightarrow \lambda f \rightarrow x \ \lambda y \rightarrow x \ (f \ y)$$

| $\lambda y \ \lambda z \rightarrow (\text{update-c} \ x \ f \ y) \ (\text{update-c} x \ f \ z)$
| $\lambda y \rightarrow y$

Question 2 Evaluate

- 1. elim Leaf (Leaf 3).
- 2. elim Leaf (Node 3).
- 3. elim singleton (singleton 3) (as defined in Lecture 5)
- 4. equal Nil Nil
- 5. equal (Cons 3 Nil) (Cons 3 Nil) (assume that 3 is a constructor)
- 6. equal Nil (Cons 3 Nil)
- 7. equal $(\lambda x.x)$ $(\lambda x.x)$
- 8. elim* Leaf (Leaf 4)
- 9. elim* Leaf (Pair (Leaf 4) (Leaf 5))
- 10. elim* Leaf (Leaf (Leaf 4))

- 11. update-c Leaf $(\lambda x.x + 1)$ (Pair (Leaf 4) (Leaf 5))
- 12. update-c Dept (update-c Leaf $(\lambda x.x+1)$) (Pair (Dept (Leaf 4)) (Leaf 5))

Question 2 3

Define the free matchables and free variables of a term t.

Question 4 Use update-c to define a function that will update the salaries of employees in departments in divisions, where

- a salary is of the form Salary x where x is a floating point number.
- an employee is of the form $Employee \ n \ s$ where n is a string (the name) and s is the salary.
- a department is of the form Department s es where s is its name and es is a list of employees.
- ullet a division is of the form Division ds where ds is a list of departments.

Provide an example.

Question 5 Solve Question 4 using apply2all instead of update-c. Encode your answer in **bondi**. Does this mean that apply2all can do anything that update-c can?