

Typesystems For DSLs

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Typesystem (from Wikipedia)

In computer science, a type system may be defined as a tractable syntactic framework for classifying phrases according to the kinds of values they compute.

A type system associates types with each computed value. By examining the flow of these values, a type system attempts to prove that no type errors can occur.

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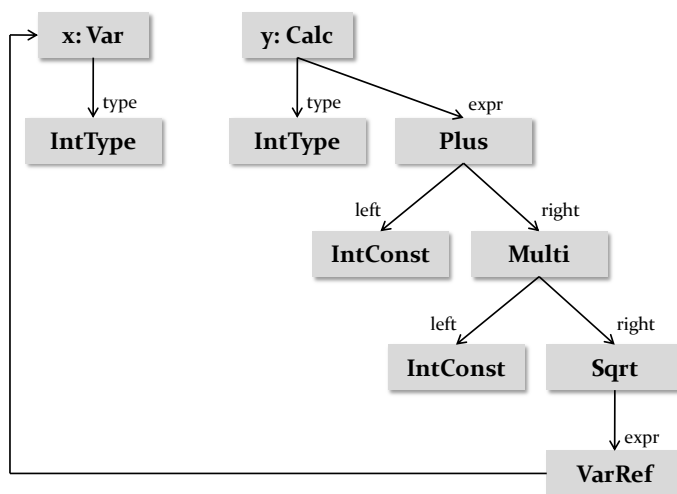
The type system in question **determines what constitutes a type error**, but a type system generally seeks to guarantee that operations expecting a certain kind of value are not used with values for which that operation makes no sense.



var x : int;
calc y : int = 1 + 2 * \sqrt{x}

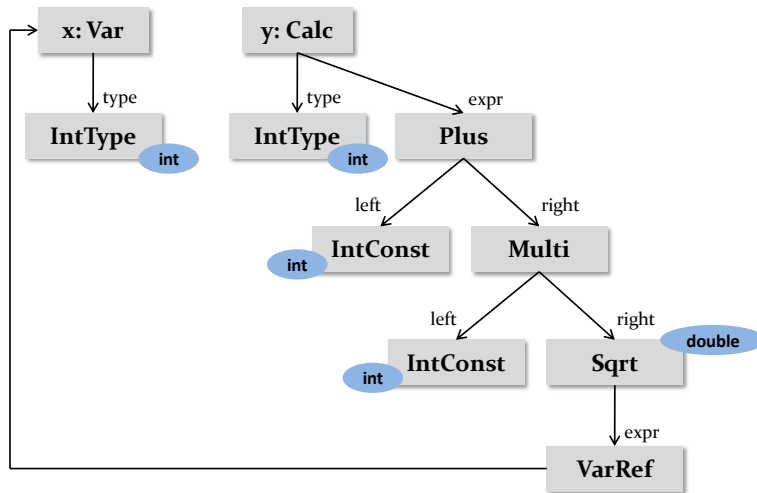


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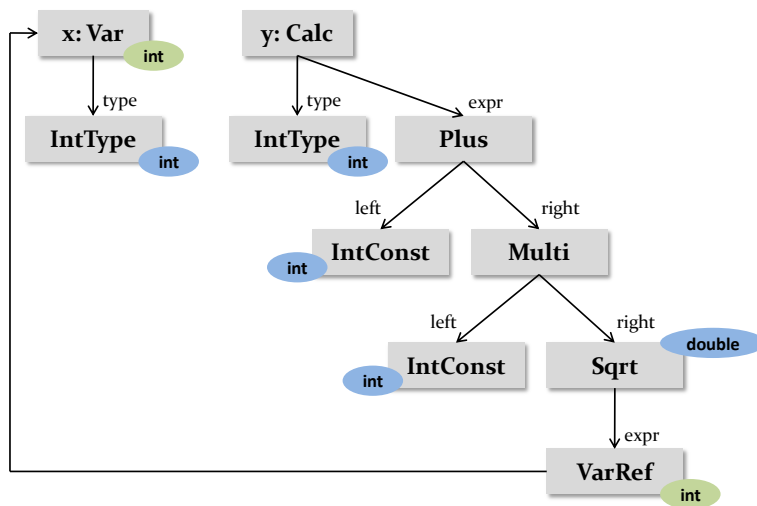
declare fixed types

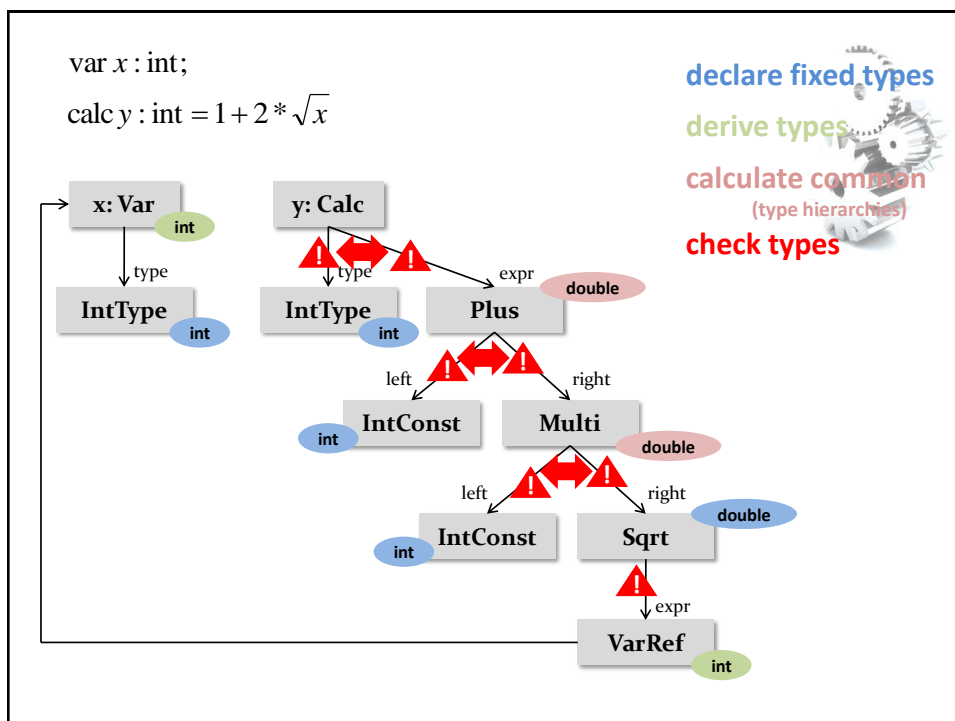
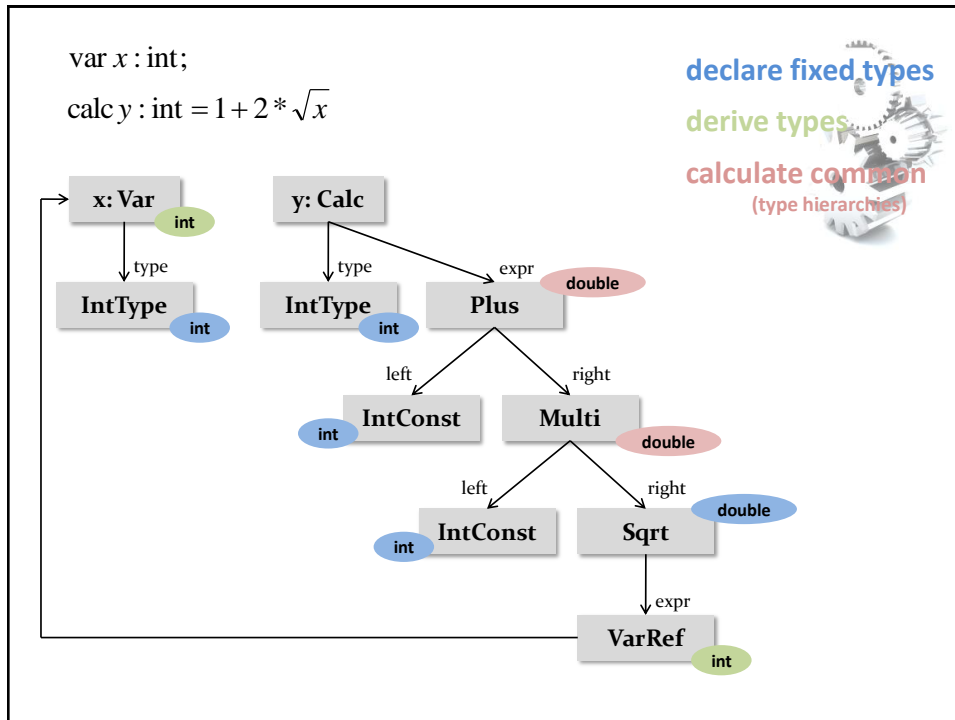


var x : int;
calc y : int = 1 + 2 * \sqrt{x}

declare fixed types

derive types





By the way:

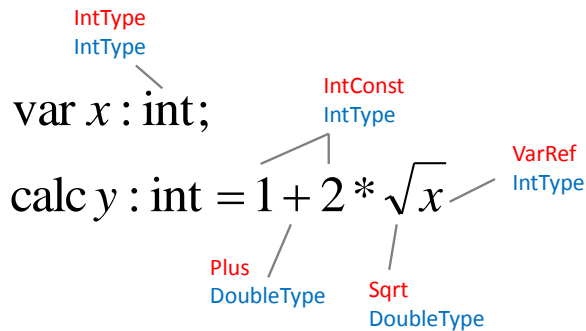
Type != Meta Class

```
var x : int;
```

```
calc y : int = 1 + 2 *  $\sqrt{x}$ 
```

By the way:

Type != Meta Class



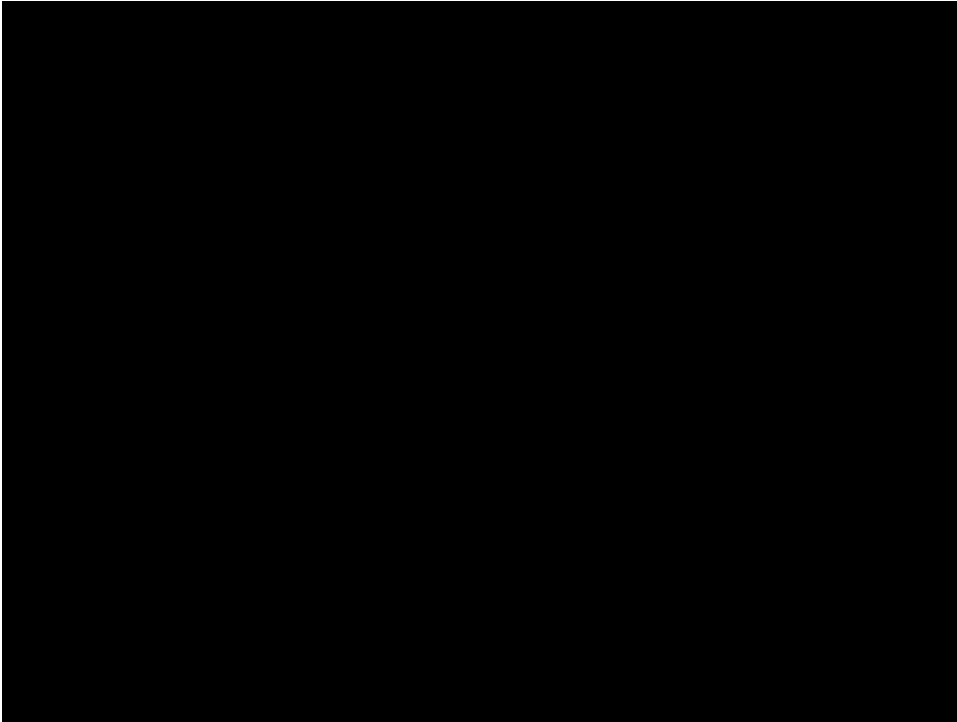
Aren't
Typesystems
just another set of
Constraints?



Aren't
Typesystems
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Constraints?



Yes, but:
way more complicated;
special approach useful



Context

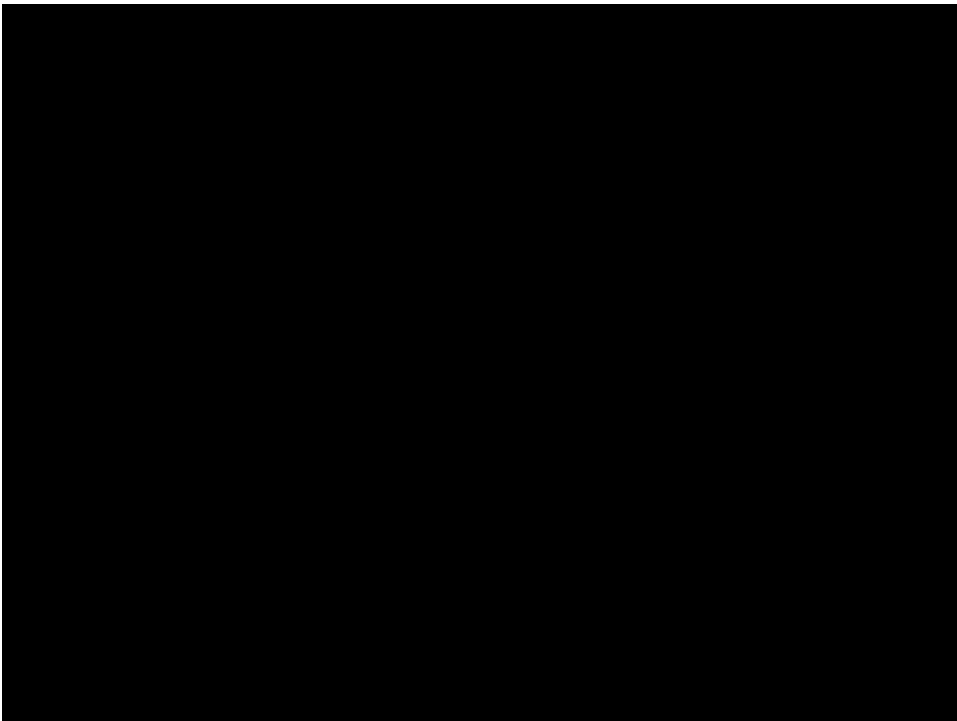
Intended for
static
Typesystems



Context

Especially useful
for languages
with

Expressions

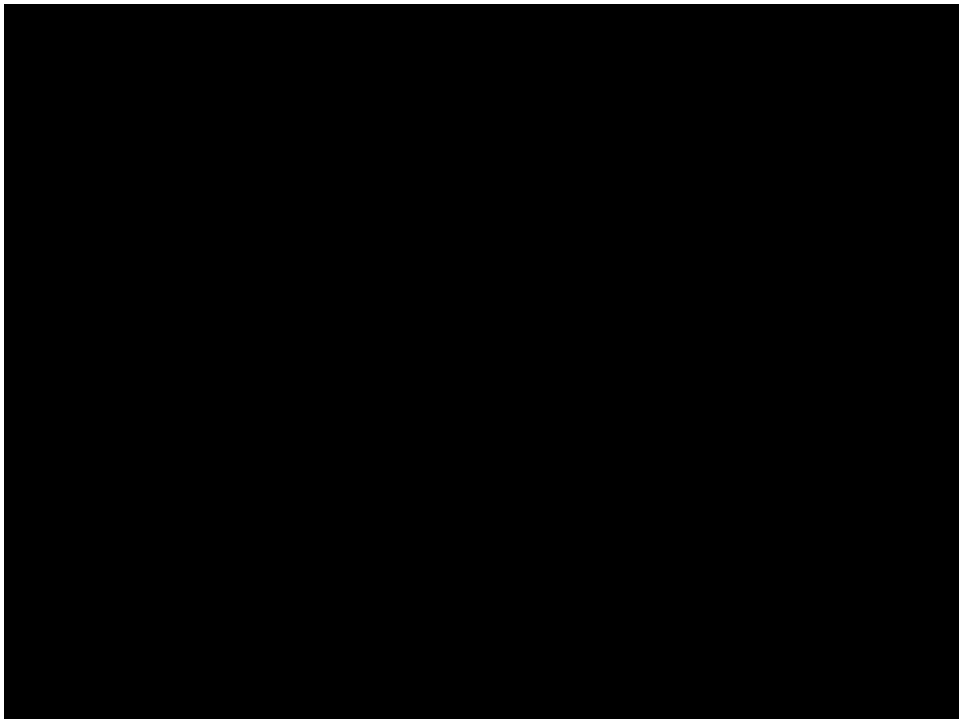


Three main approaches:

1 Recursion

2 Unification

3 Pattern Matching



1 Recursion

general:

Recursion is the process of repeating items in a self-similar way

computer science:


in which it refers to a method of defining functions in which the function being defined is applied within its own definition

1 Recursion

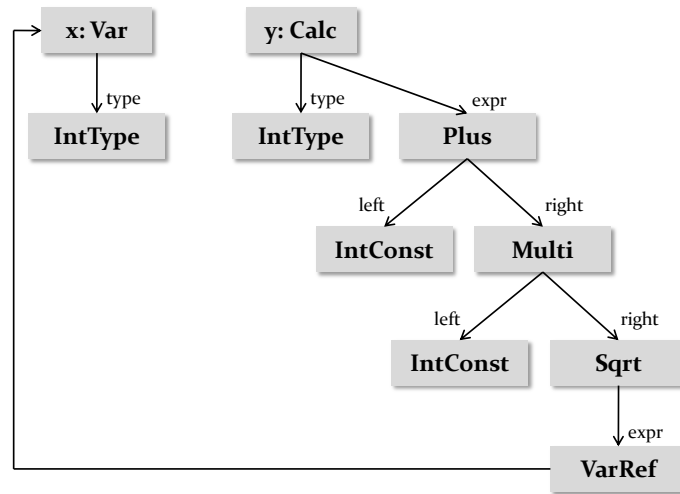
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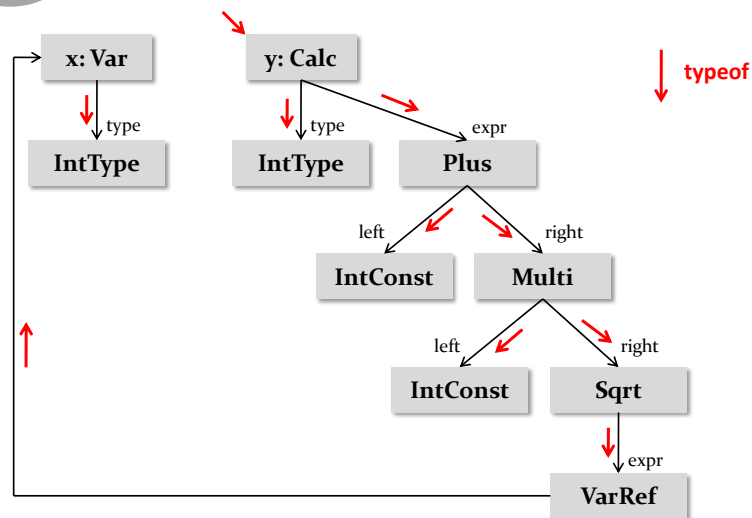
```
unsigned int factorial(unsigned int n)
{
    if (n <= 1)
        return 1;
    else
        return n * factorial(n-1);
}
```



1 Recursion



1 Recursion



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typeof := function that returns the type of
an element for a given element

typeof := element -> type-of-the-element

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typeof := function that returns the type of
an element for a given element

typeof := element -> type-of-the-element

In the **recursive** approach, it does it by drawing
on the types of „related“ elements $p_1 \dots p_n$

typeof(e) := $f(\text{typeof}(p_1), \text{typeof}(p_2) \dots \text{typeof}(p_n))$

1 Recursion

```
var i: int
var i: int = 42
var i: int = 33.33
var i = 42
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} LocalVarDecl:
`var` name=ID `:` type=Type (`=` init=Expr)?

1 Recursion

```
var i: int
var i: int = 42
var i: int = 33.33
var i = 42
```

} LocalVarDecl:
`var` name=ID `:` type=Type (`=` init=Expr)?

```
typeof( LocalVarDecl ) {
  if ( type != null && init != null ) {
    ensure typeof( init ) is-same-as typeof( type ) ||
      typeof( init ) is-subtype-of typeof( type )
    return typeof( type )
  }
  ...
}
```

1 Recursion

LocalVarDecl:
`var` name=ID `:` type=Type (`=` init=Expr)?

```
typeof( LocalVarDecl ) {
  if ( type != null && init != null ) {
    ensure typeof( init ) is-same-as typeof( type ) ||
      typeof( init ) is-subtype-of typeof( type )
    return typeof( type )
  }
  if ( type == null && init != null ) { return typeof( init ) }
  if ( type != null && init == null ) { return typeof( type ) }
  if ( type == null && init == null ) { raise error }
}
```


1 Recursion

LocalVarDecl:

``var` name=ID `:` type=Type (`=` init=Expr)?`

```
ensureSameOrSub( LocalVarDecl.init, LocalVarDecl.type )
useTypeOfFeature( LocalVarDecl, LocalVarDecl.type)
else useTypeOfFeature( LocalVarDecl, LocalVarDecl.init )
else error
```

(do nothing if C.x == null)

1 Recursion

LocalVarDecl:

``var` name=ID `:` type=Type (`=` init=Expr)?`

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ensureSameOrSub( LocalVarDecl.init, LocalVarDecl.type )
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Derivation and Propagation

Constraints

(do nothing if C.x == null)

1 Recursion

LocalVarDecl:

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Derivation and Propagation

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Constraints

(do nothing if C.x == null)

Xtext/TS

1 Recursion

Now for Xtext 2.0

With new typing DSL

Static consistency
checks, custom navigation,
templates, etc.

```
typesystem expr.typesys.ExprTypesystem
ecore file "platform:/resource/expr/src-gen/expr/ExprDemo.ecore"
language package expr.exprDemo.ExprDemoPackage

@section "Basics"

// float is a subtype of string
subtype IntType base FloatType

// primitive types use clones of themselves as their type
typeof Type + -> clone
// string literals have string type
typeof StringLiteral -> StringType
typeof Equals -> BoolType
typeof NumberLiteral -> javacode
// variable declarations and formulas use have the type of their type
typeof VarDecl -> feature type {
  ensureCompatibility type <=: init
}
typeof Formula -> feature type {
  ensureCompatibility type <=: expr
}
typeof Symbol -> abstract
// a symbol reference has the type of the symbol it references
typeof SymbolRef -> feature symbol
// plus must have ints or floats on either side, and the two
// have to be compatible. Type of Plus is the common supertype
// of left and right
typeof Plus -> common left right {
  ensureType left <=: IntType, FloatType
  ensureType right <=: IntType, FloatType
  ensureCompatibility left <=: right
}
// same for multi...
typeof Multi -> common left right {
  ensureType left <=: IntType, FloatType
  ensureType right <=: IntType, FloatType
  ensureCompatibility left <=: right
}
```

Xtext

<http://code.google.com/a/eclipselabs.org/p/xtext-typesystem/>

Demo



Xtext/TS

1 Recursion

Xtypes

*a DSL for writing type systems for
Xtext languages*

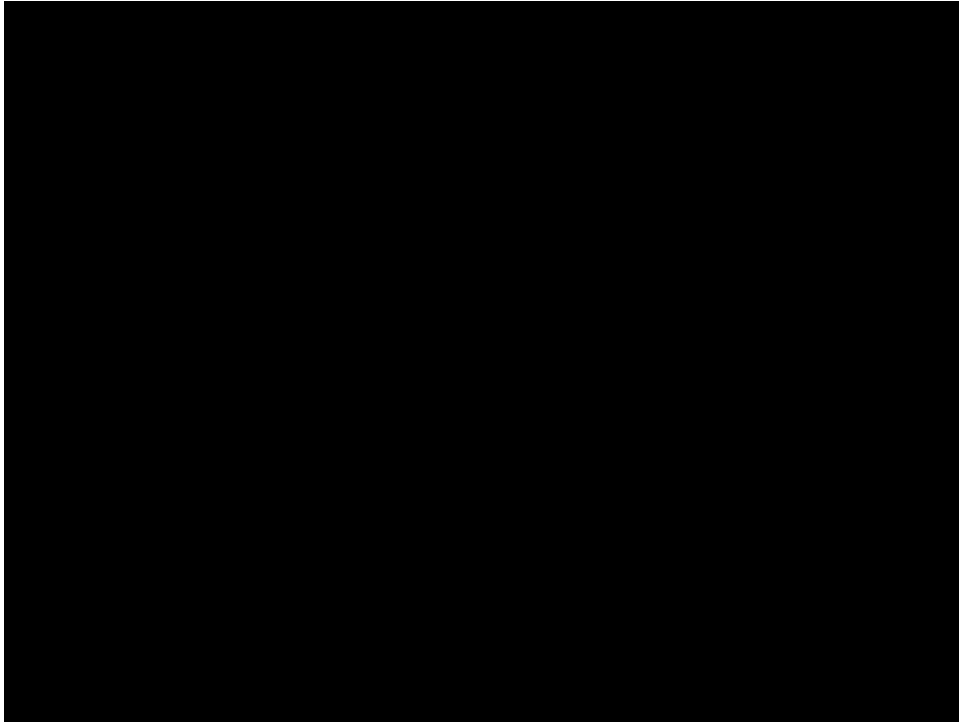
Lorenzo Bettini

<http://xtypes.sourceforge.net/>

```
rule TIntConstant
derives
  G |- var IntConstant i : var Type int
from
  var IntType intType
  $int := $intType

rule TStringConstant
derives
  G |- var StringConstant s : var Type string
from
  var StringType stringType
  $string := $stringType
```

```
rule TFieldOk
derives
  G |- var Field f : 'OK'
from
  // checks that there are no duplicate field in the hierarchy
  var Class C := (Class) container($f)
  !exists inheritedField in getall($C.extends, fields, extends) {
    $inheritedField.name = $f.name
  } error='duplicate field in base class'
  !exists otherField in $C.fields {
    $otherField.name = $f.name
    $otherField != $f
  } error='duplicate field in the same class'
```



2 Unification

Unification is an operation [..] which produces from [..] logic terms a substitution which [..] makes the terms equal modulo some equational theory.

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- (1) $2 * x == 10$
- (2) $x + x == 10$
- (3) $x + y == 2 * x + 5$

set of linear equations

2 Unification

Unification is an operation $[..]$ which produces from $[..]$ logic terms a substitution which $[..]$ makes the terms equal modulo some equational theory.

```
(1) 2 * x == 10
(2) x + x == 10
(3) x + y == 2 * x + 5
```

set of linear equations

```
x := 5
y := 10
```

```
(1) 2 * 5 == 10
(2) 5 + 5 == 10
(3) 5 + 10 == 2 * 5 + 5
```

2 Unification

```
var i: int
var i: int = 42
var i: int = 33.33
var i = 42
```



LocalVarDecl:

``var` name=ID `:` type=Type (`=` init=Expr)?`

2 Unification

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} LocalVarDecl:
`var` name=ID `:` type=Type (`=` init=Expr)?

typeof(LocalVarDecl.type) **<::** **typeof**(LocalVarDecl.init)
typeof(LocalVarDecl) **::=** **typeof**(LocalVarDecl.type)

(do nothing if C.x == null)

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(do nothing if C.x == null)

Constraints and Derivation Rules
at the same time!

2 Unification

typeof(LocalVarDecl.type) **<::=** **typeof**(LocalVarDecl.init)

typeof(LocalVarDecl) **<::=** **typeof**(LocalVarDecl.type)

var i: int	typeof (int) <::= typeof (-null-)	→ ignore
	typeof (T) <::= typeof (int)	→ T := int

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	typeof (T) <::= typeof (int)	→ T := int

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typeof(LocalVarDecl.type) **<::=** **typeof**(LocalVarDecl.init)

typeof(LocalVarDecl) **==:** **typeof**(LocalVarDecl.type)

var i: int	typeof (int) <::= typeof (-null-)	→ ignore
	typeof (T) ==: typeof (int)	→ T := int

var i: int = 42	typeof (int) <::= typeof (int)	→ ok
	typeof (T) ==: typeof (int)	→ T := int

var i: int = 33.33	typeof (int) <::= typeof (double)	→ error!
	typeof (T) ==: typeof (int)	→ T := int

2 Unification

typeof(LocalVarDecl.type) **<::=** **typeof**(LocalVarDecl.init)

typeof(LocalVarDecl) **==:** **typeof**(LocalVarDecl.type)

var i: int	typeof (int) <::= typeof (-null-)	→ ignore
	typeof (T) ==: typeof (int)	→ T := int

var i: int = 42	typeof (int) <::= typeof (int)	→ ok
	typeof (T) ==: typeof (int)	→ T := int

var i: int = 33.33	typeof (int) <::= typeof (double)	→ error!
	typeof (T) ==: typeof (int)	→ T := int

var i = 42	typeof (U) <::= typeof (int)	→ U := int
	typeof (T) ==: typeof (U)	→ T := int

2 Unification

typeof(LocalVarDecl.type) **<::=** **typeof**(LocalVarDecl.init)

typeof(LocalVarDecl) **==:** **typeof**(LocalVarDecl.type)

var i: int **typeof**(int) **<::=** **typeof**(-null-) → ignore
 typeof(T) **==:** **typeof**(int) → T := int

var i: int = 42 **typeof**(int) **<::=** **typeof**(int) → ok
 typeof(T) **==:** **typeof**(int) → T := int

var i: int = 33.33 **typeof**(int) **<::=** **typeof**(do
 typeof(T) **==:** **typeof**(int)

var i = 42 **typeof**(U) **<::=** **typeof**(int)
 typeof(T) **==:** **typeof**(U)



Meta Programming System

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2 Unification

var i: int[]

var i: int[] = {1, 2, 3}

var i = {1, 2, 3}

2 Unification

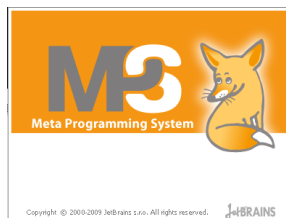
```

var i: int[]
var i: int[] = {1, 2, 3}
var i = {1, 2, 3}

type var t
init.elements.foreach{ e | t <=: typeof(e) }
typeof( LocalVarDecl.type ) <=: t
typeof( LocalVarDecl ) ::= typeof( LocalVarDecl.type )

```

Demo



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2 Unification

Unification is more powerful:

```
factorial( int i ) {  
    if ( i == 0 ) return 1;  
    return i * factorial(i-1);  
}
```

Recursion cannot be used to derive the return type of factorial, since it calls itself.

2 Unification

Unification is more powerful:

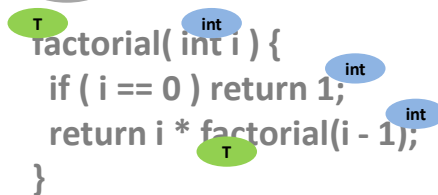
```
int factorial( int i ) {  
    if ( i == 0 ) return 1;  
    return i * factorial(i-1);  
}
```

Recursion cannot be used to derive the return type of factorial, since it calls itself, so recursive functions need a type specification.

2 Unification

```
factorial( int i ) {  
  if ( i == 0 ) return 1;  
  return i * factorial(i - 1);  
}
```

2 Unification

```
  
factorial( int i ) {  
  if ( i == 0 ) return 1;  
  return i * factorial(i - 1);  
}
```

2 Unification

```

  T      int
factorial( int i ) {
    if ( i == 0 ) return 1;
    return i * factorial(i - 1);
}

```

typeof(BinOp) <=: **typeof**(BinOp.left)
typeof(BinOp) <=: **typeof**(BinOp.right)

2 Unification

```

  T      int      int      int
factorial( int i ) {
    if ( i == 0 ) return 1;
    return i * factorial(i - 1);
}

```

typeof(BinOp) <=: **typeof**(BinOp.left)
typeof(BinOp) <=: **typeof**(BinOp.right)
typeof(Return) <=: **typeof**(Return.expr)

2 Unification

```

  int factorial( int i ) {
    if ( i == 0 ) return 1;
    return i * factorial(i - 1);
  }

```

```

typeof( BinOp ) <=: typeof( BinOp.left )
typeof( BinOp ) <=: typeof( BinOp.right )
typeof( Return ) <=: typeof( Return.expr )

```

```

type var t_ret;
for (Return r in FunctionDecl.allReturns):
  t_ret <=: typeof( r );

```

3 Pattern Matching

```

var i: int
var i: int = 42
var i: int = 33.33
var i = 42

```

} LocalVarDecl:
`var` name=ID `:` type=Type (`=` init=Expr)?

3 Pattern Matching

```

var i: int
var i: int = 42
var i: int = 33.33
var i = 42

```

} LocalVarDecl:
`var` name=ID `:` type=Type (`=` init=Expr)?

typeof(init)	typeof(type)	typeof(LocalVarDecl)
int	int	int
int	-	int
-	int	int
-	-	<error>
int	double	int
double	int	<error>

3 Pattern Matching

```

var i: int
var i: int = 42
var i: int = 33.33
var i = 42
  
```

} LocalVarDecl:
`var` name=ID `:` type=Type (`=` init=Expr)?

typeof(init)	typeof(type)	typeof(LocalVarDecl)
t	-	t
-	t	t
t	u :<= t	u
-	-	<error>

upper case: unbound, free type vars

lower case: bound type vars

3 Pattern Matching

```

var i: int
var i: int = 42
var i: int = 33.33
var i = 42
  
```

} LocalVarDecl:
`var` name=ID `:` type=Type (`=` init=Expr)?

typeof(init)	typeof(type)	typeof(LocalVarDecl)
t	-	t
-	t	t
t	u :<= t	u
-	-	<error>

upper case: unbound, free type vars

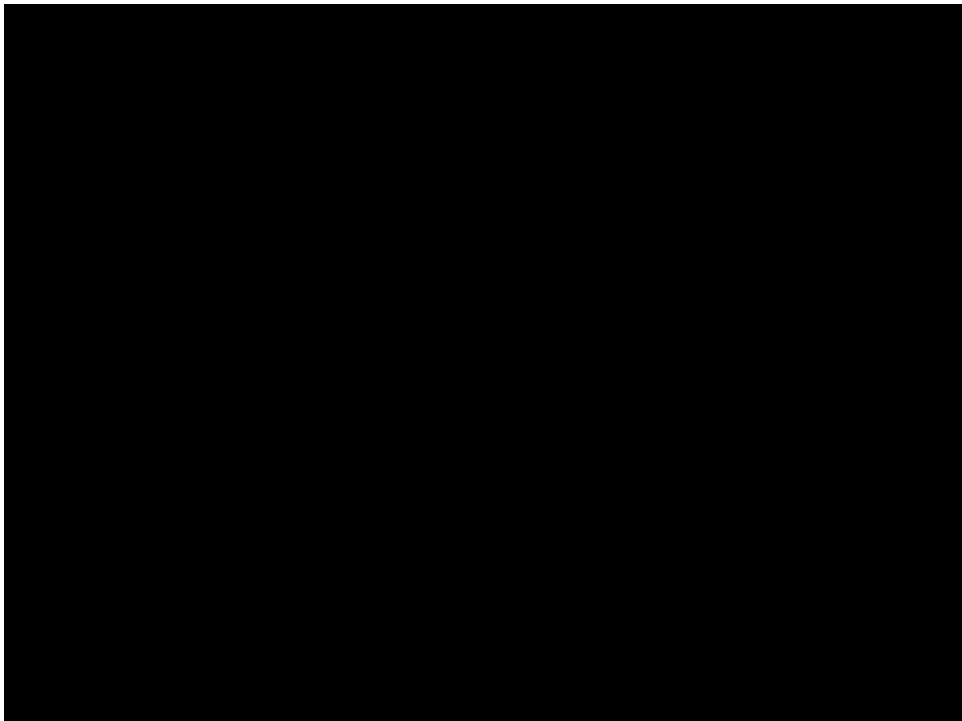
lower case: bound type vars

Spoofox

No Demo ☺



SpooFax



THE END.

.coordinates

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