analysis

May 25, 2023

1 Imports and Setup

```
[62]: import pandas as pd
      import numpy as np
[63]: df = pd.read_csv('data/starcraft_player_data.csv')
[64]: df
[64]:
             GameID
                      LeagueIndex Age HoursPerWeek TotalHours
                                                                        APM
                                    27
                 52
                                                  10
                                                            3000
                                                                   143.7180
      1
                 55
                                    23
                                                  10
                                                            5000
                                                                   129.2322
      2
                 56
                                 4
                                    30
                                                             200
                                                                    69.9612
                                                  10
      3
                 57
                                 3
                                    19
                                                  20
                                                             400
                                                                   107.6016
      4
                 58
                                 3
                                    32
                                                  10
                                                             500
                                                                   122.8908
                                     ?
                                                   ?
                                                                   259.6296
      3390
              10089
                                 8
                                     ?
                                                   ?
                                                                   314.6700
      3391
              10090
                                 8
              10092
                                     ?
                                                   ?
      3392
                                                                   299.4282
                                                   ?
      3393
                                 8
                                                                   375.8664
              10094
      3394
              10095
                                                   ?
                                                                   348.3576
                               AssignToHotkeys
                                                  UniqueHotkeys
                                                                   MinimapAttacks
             SelectByHotkeys
                    0.003515
                                                                7
      0
                                       0.000220
                                                                         0.000110
      1
                    0.003304
                                       0.000259
                                                                4
                                                                          0.000294
      2
                    0.001101
                                       0.000336
                                                                4
                                                                         0.000294
      3
                    0.001034
                                       0.000213
                                                                1
                                                                          0.000053
      4
                    0.001136
                                       0.000327
                                                                2
                                                                          0.000000
                    0.020425
      3390
                                       0.000743
                                                               9
                                                                          0.000621
      3391
                    0.028043
                                       0.001157
                                                              10
                                                                          0.000246
                                                                7
      3392
                    0.028341
                                       0.000860
                                                                          0.000338
      3393
                                                                5
                    0.036436
                                       0.000594
                                                                          0.000204
      3394
                    0.029855
                                       0.000811
                                                                4
                                                                          0.000224
             MinimapRightClicks
                                   {\tt NumberOfPACs}
                                                  {\tt GapBetweenPACs}
                                                                    ActionLatency
                        0.000392
      0
                                       0.004849
                                                          32.6677
                                                                           40.8673
```

1	0.0	00432	0.00430	7	32.9194	42.3454
2	0.0	00461	0.00292	6	44.6475	75.3548
3	0.0	00543	0.00378	3	29.2203	53.7352
4	0.0	01329	0.00236	8	22.6885	62.0813
•••			•••	•••		•••
3390	0.0	00146	0.00455	5	18.6059	42.8342
3391	0.0	01083	0.00425	9	14.3023	36.1156
3392	0.0	00169	0.00443		12.4028	39.5156
3393		00780	0.00434		11.6910	34.8547
3394	0.0	01315	0.00556	6	20.0537	33.5142
	ActionsInPAC	Total	MapExplored	WorkersMa	de Unio	queUnitsMade \
0	4.7508		28	0.0013	97	6
1	4.8434		22	0.0011	93	5
2	4.0430		22	0.0007	45	6
3	4.9155		19	0.0004	26	7
4	9.3740		15	0.0011	74	4
					77	
3390	6.2754		46	0.0008		5
3391 3392	7.1965 6.3979		16 19	0.0007 0.0012		4 4
3393	7.9615		15	0.0012		6
3394	6.3719		27	0.0000		7
333 4	0.3719		21	0.0013	00	,
	ComplexUnitsM		omplexAbilit			
0	0.000			.000000		
1	0.000			.000208		
2	0.000000			0.000189		
3	0.000000			0.000384		
4	0.000	000	0	.000019		
 3390	 0.000	000				
3391	0.000			.000000		
3392	0.000			.000000		
3393	0.000			.000631		
3394	0.000			.000895		
2301	3.300	-0.	O			

2 Cleaning Data

[3395 rows x 20 columns]

```
[65]: df_without_question_mark = df[df != '?'].dropna()
    string_cols = ['TotalHours', 'HoursPerWeek', 'Age']
    for s in string_cols:
        df_without_question_mark[s] = df_without_question_mark[s].astype(int)
        df_without_question_mark
```

[65]:	GameID	LeagueIndex	Age	HoursPe	erWeek	TotalHours	s APM \	
0	52	5	27		10	3000		
1	55	5	23		10	5000		
2	56	4	30		10	200		
3	57	3	19		20	400		
4	58	3	32		10	500		
•••	00	Ö	OZ				122.0000	
 3335	 9261	 4	20	•••	 8	 400	158.1390	
3336	9264	5	16		56	1500		
3337		4	21		8	100		
3338	9270	3	20		28	400		
3339	9270	4	22		28 6	400		
3339	9211	4	22		6	400	00.0240	
	Select	ByHotkeys As	signTo	Hotkeys	Unique	Hotkeys M	MinimapAttacks	\
0		0.003515	0	.000220	_	7	0.000110	
1		0.003304	0	.000259		4	0.000294	
2		0.001101	0	.000336		4	0.000294	
3		0.001034		.000213		1	0.000053	
4		0.001136		.000327		2	0.000000	
-						_		
3335		0.013829		.000504		7	0.000217	
3336		0.006951		.000360		6	0.000083	
3337		0.002956		.000241		8	0.000055	
3338		0.005424		.000211		5	0.000000	
3339		0.000424		.000102		2	0.000000	
5555		0.000044	O	.000100		2	0.000000	
	Minimap	RightClicks	Numbe	rOfPACs	GapBet	weenPACs	ActionLatency	\
0		0.000392	0	.004849		32.6677	40.8673	
1		0.000432	0	.004307		32.9194	42.3454	
2		0.000461	0	.002926		44.6475	75.3548	
3		0.000543	0	.003783		29.2203	53.7352	
4		0.001329	0	.002368		22.6885	62.0813	
•••		•••		.		•	•••	
3335		0.000313	0	.003583		36.3990	66.2718	
3336		0.000166	0	.005414		22.8615	34.7417	
3337		0.000208	0	.003690		35.5833	57.9585	
3338		0.000480	0	.003205		18.2927	62.4615	
3339		0.000341		.003099		45.1512	63.4435	
	Actions		MapExp		lorkers1	-	ieUnitsMade \	
0		1.7508		28	0.001		6	
1		1.8434		22	0.001		5	
2		1.0430		22	0.000		6	
3	4	1.9155		19	0.000)426	7	
4	Ş	9.3740		15	0.001	174	4	
•••		•••	•••			••	•	
3335	4	1.5097		30	0.001	1035	7	

3336	4.9309	38	0.001343	7
3337	5.4154	23	0.002014	7
3338	6.0202	18	0.000934	5
3339	5.1913	20	0.000476	8
	${\tt ComplexUnitsMade}$	ComplexAbilit	iesUsed	
0	0.0	0	.000000	
1	0.0	0	.000208	
2	0.0	0	.000189	
3	0.0	0	.000384	
4	0.0	0	.000019	
•••	•••		•••	
3335	0.0	0	.000287	
3336	0.0	0	.000388	
3337	0.0	0	.000000	
3338	0.0	0	.000000	
3339	0.0	0	.000054	

[3338 rows x 20 columns]

3 Exploring Correlations

```
[66]: corr = df_without_question_mark.corr()
[67]:
      corr.columns
[67]: Index(['GameID', 'LeagueIndex', 'Age', 'HoursPerWeek', 'TotalHours', 'APM',
             'SelectByHotkeys', 'AssignToHotkeys', 'UniqueHotkeys', 'MinimapAttacks',
             'MinimapRightClicks', 'NumberOfPACs', 'GapBetweenPACs', 'ActionLatency',
             'ActionsInPAC', 'TotalMapExplored', 'WorkersMade', 'UniqueUnitsMade',
             'ComplexUnitsMade', 'ComplexAbilitiesUsed'],
            dtype='object')
[68]: league_index_corr = corr['LeagueIndex']
[69]: league_index_corr
[69]: GameID
                              0.024974
                              1.000000
     LeagueIndex
      Age
                             -0.127518
      HoursPerWeek
                              0.217930
      TotalHours
                              0.023884
      APM
                              0.624171
      SelectByHotkeys
                              0.428637
      AssignToHotkeys
                              0.487280
      UniqueHotkeys
                              0.322415
```

```
MinimapAttacks
                              0.270526
      MinimapRightClicks
                              0.206380
      NumberOfPACs
                              0.589193
      GapBetweenPACs
                             -0.537536
      ActionLatency
                             -0.659940
      ActionsInPAC
                              0.140303
      TotalMapExplored
                              0.230347
      WorkersMade
                              0.310452
      UniqueUnitsMade
                              0.151933
      ComplexUnitsMade
                              0.171190
      ComplexAbilitiesUsed
                              0.156033
      Name: LeagueIndex, dtype: float64
     indices = np.where(abs(league_index_corr) > 0.5)
[71]: indices
[71]: (array([ 1, 5, 11, 12, 13]),)
[72]: corr.columns[indices]
[72]: Index(['LeagueIndex', 'APM', 'NumberOfPACs', 'GapBetweenPACs',
             'ActionLatency'],
            dtype='object')
```

From the **above** it appears that the categories with a relatively significant correlation to LeagueIndex (>0.5), which is our 1-8 code for rank, are **APM**, **NumberOfPACs**, **GapBetweenPACs**, and **ActionLatency**

So, it makes sense to continue by creating a classification model trained on this data. It is possible that adding in other features would only make our model worse because they are so uncorrelated with our output variable and could cause overfitting.

These variables make intuitive sense because APM, ActionLatency, NumberOfPACs, and Gap-BetweenPACs all correlate to how fast a player is and it makes sense that quicker players would have a higher rank because they have better reactions and more practice, developing their faster movement.

For further confirmation, I will also use scikit-learn's SelectKBest to see if selecting the 5 best features aligns with what we have above. I will use the f_classif because it is suitale for numerical classification.

```
[73]: features = list(df.columns)
features.pop(1)
print(features)
```

```
['GameID', 'Age', 'HoursPerWeek', 'TotalHours', 'APM', 'SelectByHotkeys', 'AssignToHotkeys', 'UniqueHotkeys', 'MinimapAttacks', 'MinimapRightClicks', 'NumberOfPACs', 'GapBetweenPACs', 'ActionLatency', 'ActionsInPAC',
```

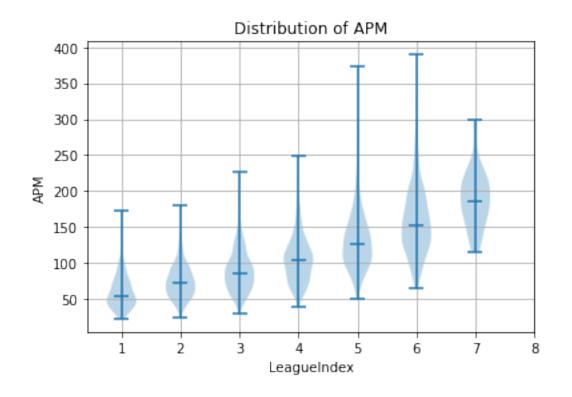
```
'TotalMapExplored', 'WorkersMade', 'UniqueUnitsMade', 'ComplexUnitsMade', 'ComplexAbilitiesUsed']
```

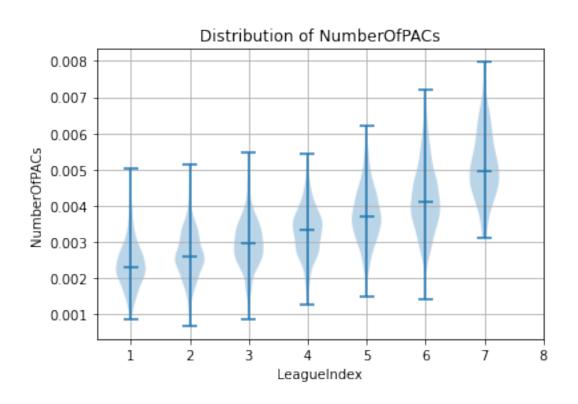
```
[74]: from sklearn.feature_selection import SelectKBest, f_classif
X = df_without_question_mark[features]
y = df_without_question_mark['LeagueIndex']
kbest = SelectKBest(score_func=f_classif, k=5)
kbest.fit(X, y)
selected_features = kbest.get_support(indices=True)
print(df.columns[selected_features])
```

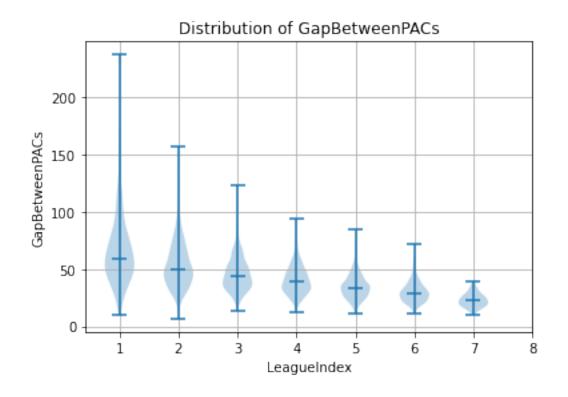
Performing this check we see that **TotalHours**, which was not included in the correlation matrix, is a good predictor for LeagueIndex, so this is an additional feature worth exploring. Scikit-Learn also suggests **MinimapRightClicks** is a good predictor, which makes sense because a more skilled player will check the minimap more often. Also, **SelectByHotkeys** measures some efficiency of game play, so also makes sense to correlate with skill

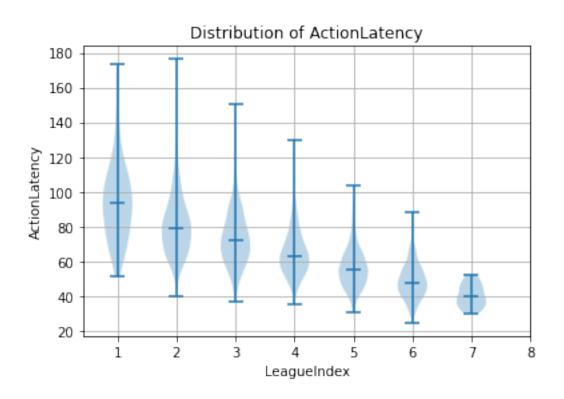
4 Visualizing Variables of Interest

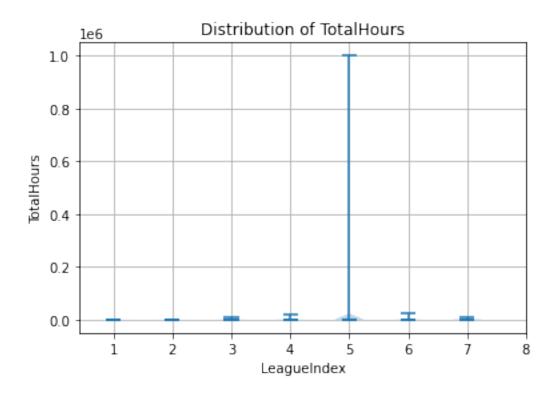
```
[57]: import matplotlib.pyplot as plt
[75]: var = ['APM', 'NumberOfPACs', 'GapBetweenPACs',
             'ActionLatency', 'TotalHours', 'SelectByHotkeys', 'MinimapRightClicks']
      for v in var:
          data_list = []
          for i in range (1,8):
              data = df_without_question_mark[df_without_question_mark['LeagueIndex']_
       →== i][v]
              data list.append(data)
          plt.violinplot(data_list, showmedians=True)
          plt.xlabel('LeagueIndex')
          plt.ylabel(v)
          plt.title(f'Distribution of {v}')
          plt.xticks(range(1, 9), range(1, 9))
          plt.grid(True)
          plt.show()
```

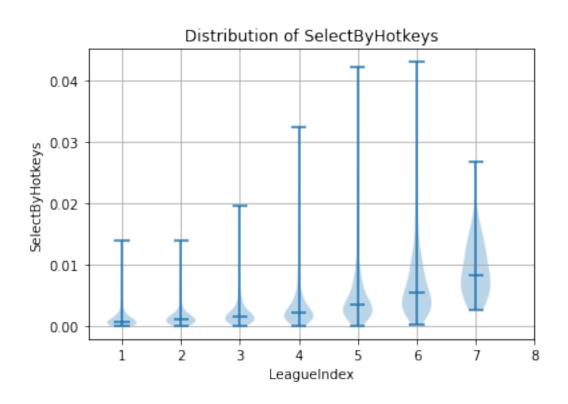


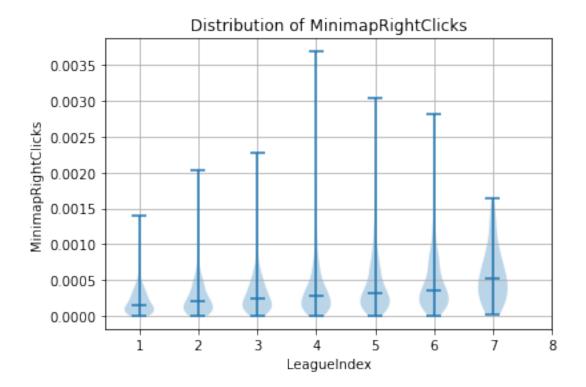




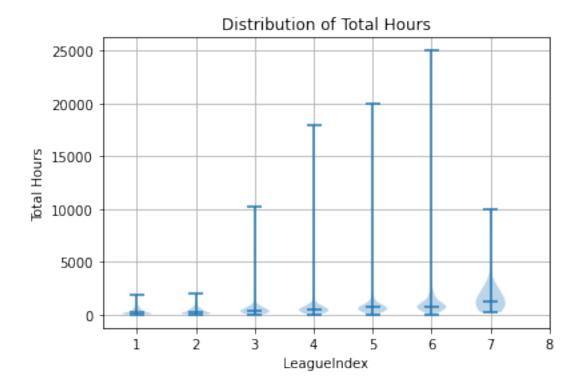








Looking at this we see an outlier in **TotalHours** that makes it hard to visualize so I'll remove that to see if there is a clear relation with our target variable



Now some relation does appear to be pressent when you follow the medians, so I will train the model on the classification model on these features with that row removed.

5 Train/Test Split For Classification Model

Based on the nature of the classification task (distinct integer categories) I will first try using a Decision Tree classifier. This is because it has good interpretability and may fit the data will, but it is possible to overfit, so I will also try a Random Forest, and see if that gives better performance on the test data. If overfitting does not appear to be a problem, the Decision Tree is preferable because of its interpretability. Otherwise, the Random Forest will be the solution to overfitting.

```
[125]: from sklearn.tree import DecisionTreeClassifier
    from sklearn.metrics import mean_squared_error
    model = DecisionTreeClassifier()
    model.fit(X_train, y_train)
    y_pred = model.predict(X_test)
    mse = mean_squared_error(y_test, y_pred)
    rmse = np.sqrt(mse)
    print("RMSE for DT:", rmse)
```

RMSE for DT: 1.3430905463031382

```
[126]: from sklearn.ensemble import RandomForestClassifier
model = RandomForestClassifier()
model.fit(X_train, y_train)
y_pred = model.predict(X_test)
mse = mean_squared_error(y_test, y_pred)
rmse = np.sqrt(mse)
print("RMSE for RF:", rmse)
```

RMSE for RF: 1.124708877834722

It appears that the Random Forest gives better perfomance than the Decision Tree. However, because both are not great, and average being off by a bit more than 1 whole rank, I will try some other models.

```
[127]: from sklearn.linear_model import LogisticRegression
  model = LogisticRegression()
  model.fit(X_train, y_train)
  y_pred = model.predict(X_test)
  mse = mean_squared_error(y_test, y_pred)
  rmse = np.sqrt(mse)
  print("RMSE for Logistic Regression:", rmse)
```

RMSE for Logistic Regression: 1.0943513103291655

/Users/ethan/miniconda3/envs/data/lib/python3.9/sitepackages/sklearn/linear_model/_logistic.py:814: ConvergenceWarning: lbfgs failed to converge (status=1): STOP: TOTAL NO. of ITERATIONS REACHED LIMIT.

Increase the number of iterations (max_iter) or scale the data as shown in:
 https://scikit-learn.org/stable/modules/preprocessing.html
Please also refer to the documentation for alternative solver options:

```
https://scikit-learn.org/stable/modules/linear_model.html#logistic-
regression
    n_iter_i = _check_optimize_result(

[128]: from sklearn.svm import SVC
    model = SVC()
    model.fit(X_train, y_train)
    y_pred = model.predict(X_test)
    mse = mean_squared_error(y_test, y_pred)
    rmse = np.sqrt(mse)
    print("RMSE for SVC:", rmse)
```

RMSE for SVC: 1.2118427597058525

```
[129]: from sklearn.ensemble import GradientBoostingClassifier
model = GradientBoostingClassifier()
model.fit(X_train, y_train)
y_pred = model.predict(X_test)
mse = mean_squared_error(y_test, y_pred)
rmse = np.sqrt(mse)
print("RMSE for Gradient Boosting Classifier:", rmse)
```

RMSE for Gradient Boosting Classifier: 1.1153528482269206

5.0.1 To get a better sense of the different classification models I will test on multiple train-test splits and plot the RMSE's

```
[131]: group_labels = ['Decision Tree', 'Random Forest', 'Logistic Regression', 'SVC', __
       dt_rmse = []
      for i in range(50):
          X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2,__
       →random state=42)
          model = DecisionTreeClassifier()
          model.fit(X_train, y_train)
          y_pred = model.predict(X_test)
          mse = mean_squared_error(y_test, y_pred)
          rmse = np.sqrt(mse)
          dt_rmse.append(rmse)
      rf_rmse = []
      for i in range(50):
          X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2,_
       ⇒random state=42)
          model = RandomForestClassifier()
          model.fit(X_train, y_train)
```

```
rmse = np.sqrt(mse)
    rf_rmse.append(rmse)
lr_rmse = []
for i in range(50):
    X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2,_
 ⇒random state=42)
    model = LogisticRegression()
    model.fit(X_train, y_train)
    y_pred = model.predict(X_test)
    mse = mean_squared_error(y_test, y_pred)
    rmse = np.sqrt(mse)
    lr_rmse.append(rmse)
svc_rmse = []
for i in range(50):
    X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2,_
 →random state=42)
    model = SVC()
    model.fit(X_train, y_train)
    y_pred = model.predict(X_test)
    mse = mean_squared_error(y_test, y_pred)
    rmse = np.sqrt(mse)
    svc_rmse.append(rmse)
gb_rmse = []
for i in range(50):
    X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2,__
 →random_state=42)
    model = GradientBoostingClassifier()
    model.fit(X_train, y_train)
    y_pred = model.predict(X_test)
    mse = mean_squared_error(y_test, y_pred)
    rmse = np.sqrt(mse)
    gb_rmse.append(rmse)
/Users/ethan/miniconda3/envs/data/lib/python3.9/site-
packages/sklearn/linear_model/_logistic.py:814: ConvergenceWarning: lbfgs failed
to converge (status=1):
STOP: TOTAL NO. of ITERATIONS REACHED LIMIT.
```

y_pred = model.predict(X_test)

mse = mean_squared_error(y_test, y_pred)

Increase the number of iterations (max_iter) or scale the data as shown in:

https://scikit-learn.org/stable/modules/preprocessing.html
Please also refer to the documentation for alternative solver options:
https://scikit-learn.org/stable/modules/linear_model.html#logistic-

```
regression
 n_iter_i = _check_optimize_result(
/Users/ethan/miniconda3/envs/data/lib/python3.9/site-
packages/sklearn/linear_model/_logistic.py:814: ConvergenceWarning: lbfgs failed
to converge (status=1):
STOP: TOTAL NO. of ITERATIONS REACHED LIMIT.
Increase the number of iterations (max_iter) or scale the data as shown in:
   https://scikit-learn.org/stable/modules/preprocessing.html
Please also refer to the documentation for alternative solver options:
   https://scikit-learn.org/stable/modules/linear_model.html#logistic-
regression
 n_iter_i = _check_optimize_result(
/Users/ethan/miniconda3/envs/data/lib/python3.9/site-
packages/sklearn/linear_model/_logistic.py:814: ConvergenceWarning: lbfgs failed
to converge (status=1):
STOP: TOTAL NO. of ITERATIONS REACHED LIMIT.
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   https://scikit-learn.org/stable/modules/preprocessing.html
Please also refer to the documentation for alternative solver options:
   https://scikit-learn.org/stable/modules/linear_model.html#logistic-
regression
 n_iter_i = _check_optimize_result(
/Users/ethan/miniconda3/envs/data/lib/python3.9/site-
packages/sklearn/linear_model/_logistic.py:814: ConvergenceWarning: lbfgs failed
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regression
 n_iter_i = _check_optimize_result(
/Users/ethan/miniconda3/envs/data/lib/python3.9/site-
packages/sklearn/linear_model/_logistic.py:814: ConvergenceWarning: lbfgs failed
to converge (status=1):
STOP: TOTAL NO. of ITERATIONS REACHED LIMIT.
Increase the number of iterations (max_iter) or scale the data as shown in:
   https://scikit-learn.org/stable/modules/preprocessing.html
Please also refer to the documentation for alternative solver options:
   https://scikit-learn.org/stable/modules/linear_model.html#logistic-
regression
 n_iter_i = _check_optimize_result(
/Users/ethan/miniconda3/envs/data/lib/python3.9/site-
packages/sklearn/linear_model/_logistic.py:814: ConvergenceWarning: lbfgs failed
```

```
to converge (status=1):
STOP: TOTAL NO. of ITERATIONS REACHED LIMIT.
Increase the number of iterations (max_iter) or scale the data as shown in:
   https://scikit-learn.org/stable/modules/preprocessing.html
Please also refer to the documentation for alternative solver options:
   https://scikit-learn.org/stable/modules/linear model.html#logistic-
regression
 n_iter_i = _check_optimize_result(
/Users/ethan/miniconda3/envs/data/lib/python3.9/site-
packages/sklearn/linear model/ logistic.py:814: ConvergenceWarning: lbfgs failed
to converge (status=1):
STOP: TOTAL NO. of ITERATIONS REACHED LIMIT.
Increase the number of iterations (max_iter) or scale the data as shown in:
   https://scikit-learn.org/stable/modules/preprocessing.html
Please also refer to the documentation for alternative solver options:
   https://scikit-learn.org/stable/modules/linear_model.html#logistic-
regression
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Please also refer to the documentation for alternative solver options:

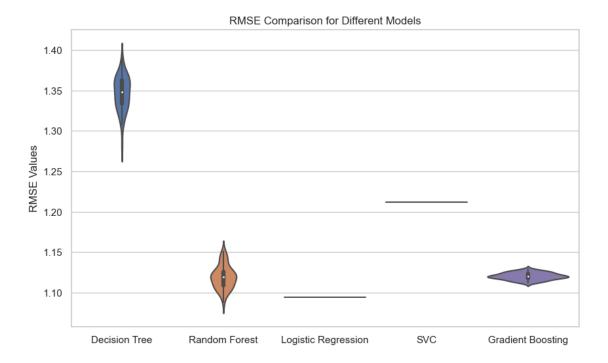
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        n_iter_i = _check_optimize_result(
[135]: import seaborn as sns
      import matplotlib.pyplot as plt
      rmse_values = [dt_rmse, rf_rmse, lr_rmse, svc_rmse, gb_rmse]
      sns.set(style="whitegrid")
      fig, ax = plt.subplots(figsize=(10, 6), dpi=100)
      ax = sns.violinplot(data=rmse_values)
      ax.set_xticklabels(group_labels)
      ax.set_ylabel("RMSE Values")
      ax.set_title("RMSE Comparison for Different Models")
```

[135]: Text(0.5, 1.0, 'RMSE Comparison for Different Models')



6 Conclusion

It appears that the best model in terms of performance is the logistic regression. Although the performance is similar for many of the classification models, notably Logistic Regression performs the best and a Random Forest performs better than the Decision Tree classifier on the test set, so overfitting appears to not be an issue.

I would recommend the use of the logistic regression model, specified below because it has the lowest RMSE, and it also has very good interpretability, because it is easy to understand the logistic regression function and what the probability outputs mean.

```
[114]: model = LogisticRegression()
      model.fit(X_train, y_train)
      coefficients = model.coef_
      intercept = model.intercept_
      print("Coefficients:", coefficients)
      print("Intercept:", intercept)
      Coefficients: [[-3.97320020e-02 -1.15202002e-06 2.83030320e-02 3.42274734e-02
        -2.64148820e-03 -2.01214191e-06 -1.48514127e-07]
       [-1.67540557e-02 -5.11403476e-07 1.74990088e-02
                                                      2.79831344e-02
        -1.56508736e-03 -1.95864396e-06 -1.59310977e-08]
       [-5.12243720e-03 -3.11215896e-07 4.21422373e-03 2.23381862e-02
       -8.53615791e-05 -1.68413988e-06 2.44393605e-08]
       [ 6.84625077e-03  9.55242512e-08  7.18671839e-03
                                                      4.90093157e-03
        5.04184438e-04 -1.28843521e-06 7.99465771e-08]
       [ 1.93061163e-02 3.38182409e-07 -1.13087052e-02 -1.44690293e-02
         1.12683397e-03 1.19024052e-06 8.01249152e-08]
       [ 2.75528230e-02 1.79623176e-06 -2.27566303e-02 -3.93508327e-02
         1.27938236e-03 3.61855671e-06 1.08678378e-09]
       [ 7.90330492e-03 -2.55299036e-07 -2.31376475e-02 -3.56298635e-02
         1.38153637e-03 2.13456373e-06 -2.11524114e-08]]
      -1.41906968e-05 -1.18956177e-04 -3.54075320e-04]
      /Users/ethan/miniconda3/envs/data/lib/python3.9/site-
      packages/sklearn/linear_model/_logistic.py:814: ConvergenceWarning: lbfgs failed
      to converge (status=1):
      STOP: TOTAL NO. of ITERATIONS REACHED LIMIT.
      Increase the number of iterations (max iter) or scale the data as shown in:
         https://scikit-learn.org/stable/modules/preprocessing.html
      Please also refer to the documentation for alternative solver options:
         https://scikit-learn.org/stable/modules/linear_model.html#logistic-
      regression
       n_iter_i = _check_optimize_result(
```

6.1 For non-technical stake holders

By exploring the data, I found that several factors would be useful predictors of LeagueIndex i.e. rank. These factors were: APM, NumberOfPACs, GapBetweenPACs, ActionLatency, TotalHours, SelectByHotkeys, MinimapRightClicks. Most of these factors make sense because they relate to the speed of the player, and faster players probably have higher ranks, while others are good indicators of how much information a player is gathering or how much experience they have, which are both good ways to learn about the score. I chose to focus on this subset of factors to avoid over-fitting, which is where our model is trained so closely on training data, it struggles in the future to make accurate predictions. I ended up with a model that is both straight forward, as we can see its mathematical definition below, and in testing had a root mean squared error of only slightly greater than 1, which means we are on average roughly around 1 rank off, so it is a fairly good predictor. It also has no variability, which is better than the models with similar performance, as seen above.

Thus, the logistic regression model above is a suitable predictor of LeagueIndex.