

Distances

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Distances in R

Distance functions are available in at least three packages of the R language.

Package stats

Function `dist` : 6 distances (documentation: `?dist`) The choice of coefficient is done by typing its name in quotes. Example: `dist(data, method="binary")` or `dist(data, "binary")`

euclidean: Usual distance between the two vectors (2 norm aka L_2), $\sqrt{\sum((x_i - y_i)^2)}$.

maximum: Maximum distance between two components of x and y (supremum norm)

manhattan: Absolute distance between the two vectors (1 norm aka L_1).

canberra: $\sum(|x_i - y_i| / |x_i + y_i|)$. Terms with zero numerator and denominator are omitted from the sum and treated as if the values were missing.

binary: (aka asymmetric binary): The vectors are regarded as binary bits, so non-zero elements are ‘on’ and zero elements are ‘off’. The distance is the proportion of bits in which only one is on amongst those in which at least one is on.

minkowski: The p norm, the pth root of the sum of the pth powers of the differences of the components.

```
x <- matrix(rnorm(100), nrow = 5)
dim(x)

## [1] 5 20

dist(x)

##           1           2           3           4
## 2 5.086051
## 3 7.294924 6.686224
## 4 5.702883 6.317966 6.755952
## 5 5.674455 6.605299 7.850960 7.538817

class(dist(x))

## [1] "dist"

dist(x, diag = TRUE)

##           1           2           3           4           5
## 1 0.000000
## 2 5.086051 0.000000
## 3 7.294924 6.686224 0.000000
## 4 5.702883 6.317966 6.755952 0.000000
## 5 5.674455 6.605299 7.850960 7.538817 0.000000

dist(x, upper = TRUE)

##           1           2           3           4           5
## 1           5.086051 7.294924 5.702883 5.674455
## 2 5.086051           6.686224 6.317966 6.605299
```

```
## 3 7.294924 6.686224          6.755952 7.850960
## 4 5.702883 6.317966 6.755952          7.538817
## 5 5.674455 6.605299 7.850960 7.538817
```

```
m <- as.matrix(dist(x))
m
```

```
##           1           2           3           4           5
## 1 0.000000 5.086051 7.294924 5.702883 5.674455
## 2 5.086051 0.000000 6.686224 6.317966 6.605299
## 3 7.294924 6.686224 0.000000 6.755952 7.850960
## 4 5.702883 6.317966 6.755952 0.000000 7.538817
## 5 5.674455 6.605299 7.850960 7.538817 0.000000
```

Package vegan

Function `vegdist` : 10 distances (documentation: `?vegdist`)

The choice of coefficient is done by typing its name in quotes. Example: `vegdist(data, method="bray")` or `vegdist(data, "bray")`

euclidean $d[jk] = \sqrt{\sum (x[ij] - x[ik])^2}$

manhattan $d[jk] = \sum (\text{abs}(x[ij] - x[ik]))$

gower $d[jk] = (1/M) \sum (\text{abs}(x[ij] - x[ik]) / (\max(x[ij]) - \min(x[ij])))$

altGower $d[jk] = (1/NZ) \sum (\text{abs}(x[ij] - x[ik]))$ where NZ is the number of non-zero columns excluding double-zeros (Anderson et al. 2006).

canberra $d[jk] = (1/NZ) \sum (\text{abs}(x[ij] - x[ik]) / (\text{abs}(x[ij]) + \text{abs}(x[ik])))$ where NZ is the number of non-zero entries.

bray $d[jk] = (\sum \text{abs}(x[ij] - x[ik])) / (\sum (x[ij] + x[ik]))$

...

Package ade4

Function `dist.binary` : 10 binary distances (documentation: `?dist.binary`)

These similarities (S) are converted to distances through the transformation $D = \sqrt{1 - S}$ The choice of coefficient is done by typing its number in the list above. Example: `dist.binary(data, method=1)` or `dist.binary(data, 1)` or `dist.binary(data, "1")`

Let be the contingency table of binary data such as $n_{11} = a$, $n_{10} = b$, $n_{01} = c$ and $n_{00} = d$.

1 = Jaccard index (1901) S3 coefficient of Gower & Legendre $s_1 = a / (a+b+c)$

2 = Simple matching coefficient of Sokal & Michener (1958) S4 coefficient of Gower & Legendre $s_2 = (a+d) / (a+b+c+d)$

3 = Sokal & Sneath (1963) S5 coefficient of Gower & Legendre $s_3 = a / (a + 2(b + c))$

4 = Rogers & Tanimoto (1960) S6 coefficient of Gower & Legendre $s_4 = (a + d) / (a + 2(b + c) + d)$

5 = Dice (1945) or Sorensen (1948) S7 coefficient of Gower & Legendre $s_5 = 2a / (2a + b + c)$

6 = Hamann coefficient S9 index of Gower & Legendre (1986) $s_6 = (a - (b + c) + d) / (a + b + c + d)$

7 = Ochiai (1957) S12 coefficient of Gower & Legendre $s_7 = a / \sqrt{(a + b)(a + c)}$

8 = Sokal & Sneath (1963) S13 coefficient of Gower & Legendre $s8 = ad / \sqrt{(a + b)(a + c)(d + b)(d + c)}$
 9 = Phi of Pearson S14 coefficient of Gower & Legendre $s9 = (ad - bc) / \sqrt{(a + b)(a + c)(d + b)(d + c)}$
 10 = S2 coefficient of Gower & Legendre $s10 = a / (a + b + c + d)$

Practice

```
wd<-"C:/Users/User/Documents/docencia/curs17_18/ub/Multivariant/bloc1"
setwd(wd)
data<-read.table("FANGA TAUFA delimitado tabulaciones.txt",sep="\t",header=TRUE) #gastropod species
str(data)
```

```
## 'data.frame': 28 obs. of 14 variables:
## $ GRUP : int 1 1 1 1 1 1 1 3 3 3 ...
## $ Pat.fle: int 95 12 7 9 4 0 0 0 0 0 ...
## $ Tur.set: int 18 5 14 13 5 2 3 0 0 0 ...
## $ Ner.pli: int 0 0 0 0 0 0 0 0 0 0 ...
## $ Tec.gra: int 0 0 0 0 0 0 0 0 0 0 ...
## $ Dru.ric: int 24 13 10 13 25 2 4 2 2 1 ...
## $ Mor.uva: int 0 0 0 0 0 0 0 14 10 3 ...
## $ Mor.gra: int 0 0 0 0 0 0 0 7 0 0 ...
## $ Mit.lit: int 0 0 0 0 0 0 0 1 1 0 ...
## $ Con.ebr: int 0 0 0 0 0 0 0 0 0 0 ...
## $ Con.mil: int 0 0 0 0 0 0 0 0 0 0 ...
## $ Con.spo: int 0 0 0 0 0 0 0 0 0 0 ...
## $ Con.nan: int 0 0 0 0 0 0 0 0 0 0 ...
## $ Con.ver: int 0 0 0 0 0 0 0 3 0 1 ...
```

```
head(data)
```

```
##   GRUP Pat.fle Tur.set Ner.pli Tec.gra Dru.ric Mor.uva Mor.gra Mit.lit
## 1    1    95    18     0     0    24     0     0     0
## 2    1    12     5     0     0    13     0     0     0
## 3    1     7    14     0     0    10     0     0     0
## 4    1     9    13     0     0    13     0     0     0
## 5    1     4     5     0     0    25     0     0     0
## 6    1     0     2     0     0     2     0     0     0
##   Con.ebr Con.mil Con.spo Con.nan Con.ver
## 1      0      0      0      0      0
## 2      0      0      0      0      0
## 3      0      0      0      0      0
## 4      0      0      0      0      0
## 5      0      0      0      0      0
## 6      0      0      0      0      0
```

MDS

The function `cmdscale` of the `stats` package to carry out this analysis. “cmds” is the acronym of classical multidimensional scaling.

Compute the matrix of Bray Curtis distances

```
library(vegan)
```

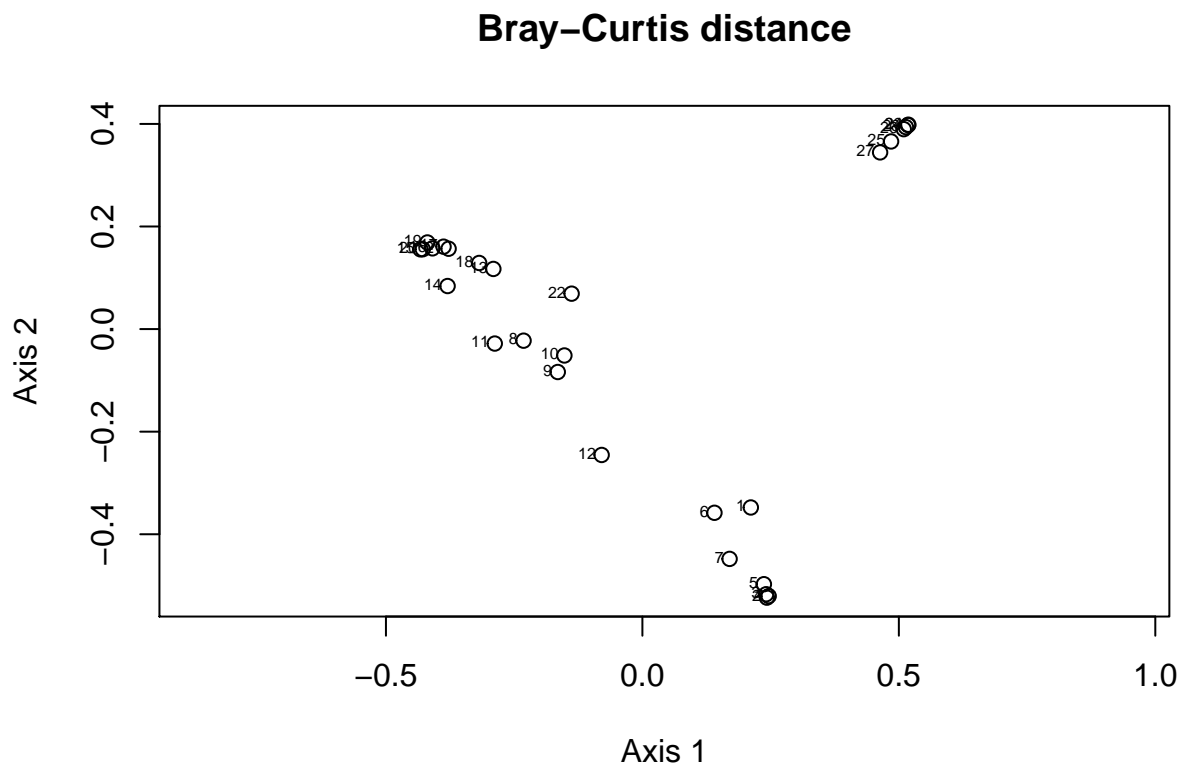
```
## Warning: package 'vegan' was built under R version 3.4.4
## Loading required package: permute
## Warning: package 'permute' was built under R version 3.4.4
## Loading required package: lattice
## This is vegan 2.4-6
```

```
data.D2<-vegdist(data[,-1], method="bray")
class(data.D2)
```

```
## [1] "dist"
```

Principal coordinate analysis. Save k=3 axes. Plot a graph of axes 1 and 2.

```
outBC=cmdscale(data.D2, 3, eig=TRUE)
plot(outBC$points[,1], outBC$points[,2], main="Bray-Curtis distance",asp=1, xlab="Axis 1", ylab="Axis 2",
names = rownames(data)
text(outBC$points[,1], outBC$points[,2], labels= names, pos=2, cex=0.5, offset=0.15)
```



Repeat the analysis after applying the Hellinger transformation (using function `decostand` of the `vegan` package) to the data. Hellinger transformation, followed by calculation of Euclidean distances.

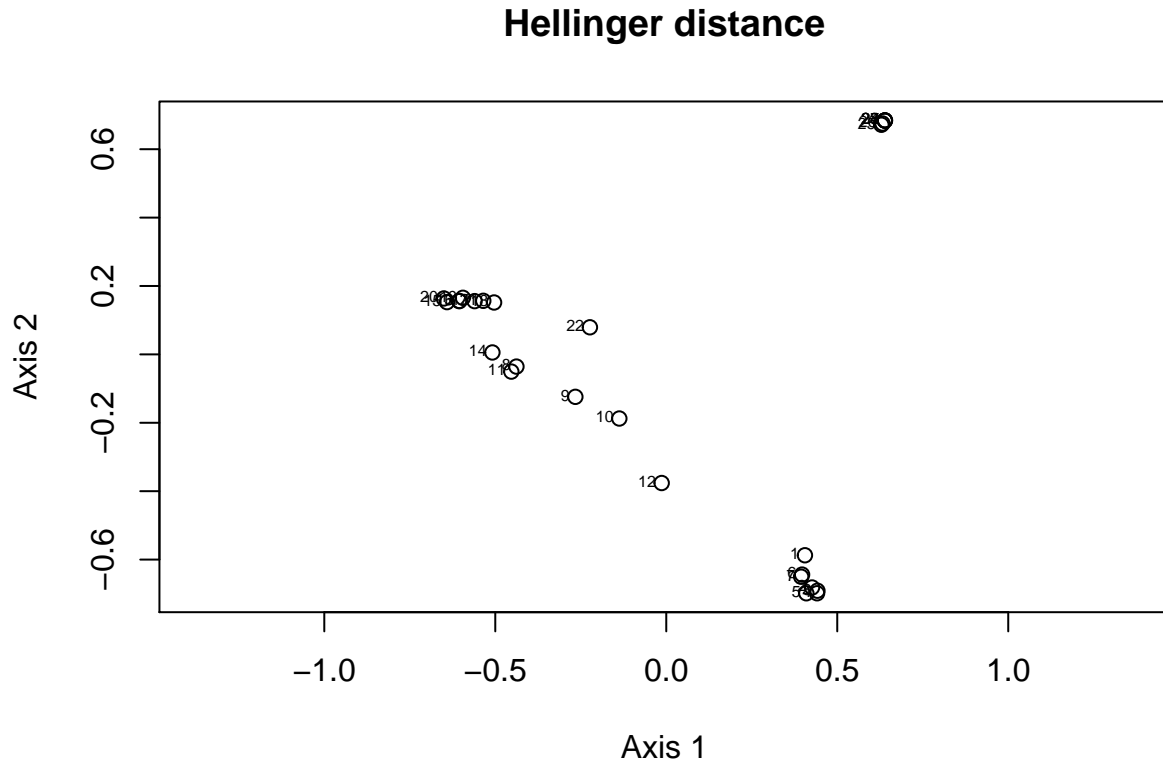
```
data.hel = decostand(data[,-1], "hel")
data.DHell = dist(data.hel)
```

Classical multidimensional scaling (MDS) of a data matrix. Also known as principal coordinates analysis

```

outDHell = cmdscale(data.DHell, 3, eig=TRUE)
plot(outDHell$points[,1], outDHell$points[,2], main="Hellinger distance",asp=1,
      xlab="Axis 1", ylab="Axis 2")
names = rownames(data)
text(outDHell$points[,1], outDHell$points[,2], labels= names, pos=2, cex=0.5, offset=0.15)

```



```

data.out = prcomp(data[, -1], scale=FALSE)

```

PCA

The values returned, by the function `prcomp()`

```

names(data.out)

```

```

## [1] "sdev"      "rotation" "center"   "scale"    "x"

```

The standard deviations of the principal components (the square roots of the eigenvalues)

```

data.out$sdev

```

```

## [1] 21.0738583 18.1325967 5.4141315 3.1737348 2.6736409 2.2126442
## [7] 1.0668062 0.7732629 0.6220504 0.5196187 0.3523081 0.2447178
## [13] 0.1532113

```

The matrix of variable loadings (columns are eigenvectors)

```

data.out$rotation

```

##	PC1	PC2	PC3	PC4	PC5
## Pat.file	-0.489926693	-0.806837465	-0.319464254	-0.02543856	0.003799339
## Tur.set	-0.126269799	-0.152783728	0.376319777	-0.09639962	0.247890408
## Ner.pli	0.038327483	-0.023116751	-0.001402709	-0.01314119	0.015564458
## Tec.gra	0.841006319	-0.531006033	0.037470986	0.06200510	-0.048032019
## Dru.ric	-0.185381440	-0.190721189	0.808957423	0.30258706	-0.309315885
## Mor.uva	-0.018033174	0.049212036	-0.195733807	0.88958026	0.271632278
## Mor.gra	-0.014752452	0.040411365	-0.157031168	0.27903635	-0.439297328
## Mit.lit	-0.016945543	0.046821665	-0.175760510	0.01186565	-0.727136406
## Con.ebr	-0.001115264	0.003232606	-0.011083720	-0.01573996	0.004589836
## Con.mil	-0.007364408	0.020487212	-0.069046836	-0.07133257	-0.203835033
## Con.spo	-0.001135945	0.003230676	-0.010847172	-0.01991969	-0.019562428
## Con.nan	-0.001889411	0.005422943	-0.019784991	-0.02794473	-0.035194023
## Con.ver	-0.003248274	0.008768235	-0.035301180	0.13643618	-0.040318496

##	PC6	PC7	PC8	PC9	PC10
## Pat.file	0.078410324	0.009769905	-0.0024812313	0.002484073	-0.0021785372
## Tur.set	-0.863042792	-0.053077104	0.0181069835	-0.014413992	0.0044302375
## Ner.pli	0.016632681	0.054593571	-0.0579047572	-0.992434448	0.0698441540
## Tec.gra	-0.032790150	-0.018488002	0.0071904799	0.041342981	0.0002640451
## Dru.ric	0.293495024	-0.033202576	0.0061803827	-0.008761684	0.0127101166
## Mor.uva	-0.098646491	-0.253505171	-0.1158471990	-0.017015186	-0.0179646748
## Mor.gra	-0.255313707	0.597091314	0.4390239180	0.009469781	0.1677332764
## Mit.lit	-0.288123281	-0.268040931	-0.5135388570	-0.011472542	-0.0866763151
## Con.ebr	0.010407987	-0.069668473	-0.0110094316	0.045017278	0.4653212457
## Con.mil	-0.027317143	-0.640871457	0.6742624338	-0.087486154	-0.2118626181
## Con.spo	0.002555158	-0.102113228	0.0001297512	0.014706871	0.1888235891
## Con.nan	-0.001505530	-0.254396076	0.0715315188	0.024434330	0.8072280696
## Con.ver	-0.052184281	0.096537294	0.2578188816	-0.045490666	-0.1014135311

##	PC11	PC12	PC13
## Pat.file	0.001475831	-0.0009347317	0.001556315
## Tur.set	-0.007240477	0.0047083620	-0.008004362
## Ner.pli	-0.024836821	0.0128989549	-0.019546218
## Tec.gra	-0.001494375	0.0010950223	-0.001932735
## Dru.ric	-0.006173145	0.0038644436	-0.006363865
## Mor.uva	-0.070266763	0.0288751594	-0.002024941
## Mor.gra	-0.209366373	0.1261861480	0.014852421
## Mit.lit	0.080798795	-0.0698149082	-0.011427318
## Con.ebr	-0.130262080	-0.3177082697	-0.811206659
## Con.mil	-0.160139376	0.0156620263	-0.059997684
## Con.spo	0.377584987	0.8562411757	-0.277610264
## Con.nan	0.106262118	-0.0934921163	0.505443423
## Con.ver	0.864588433	-0.3675459576	-0.070395049

PCA outputs:

```
summary(data.out)
```

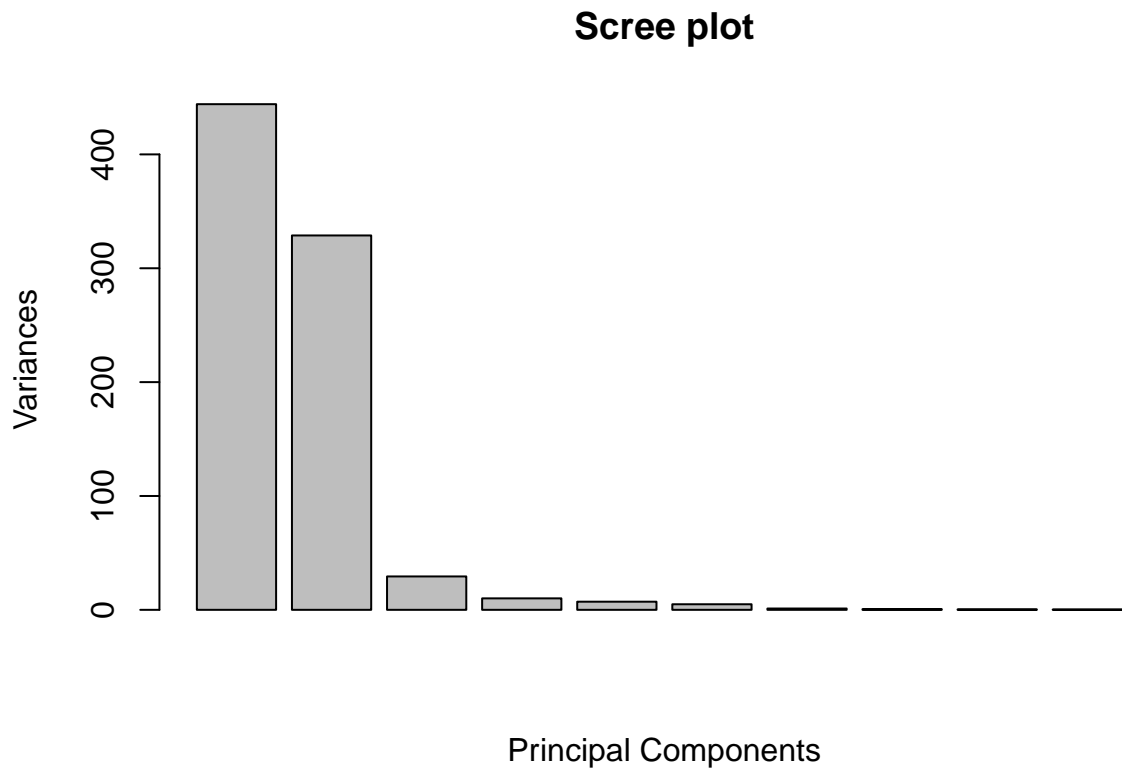
## Importance of components:	PC1	PC2	PC3	PC4	PC5	PC6
## Standard deviation	21.0739	18.1326	5.41413	3.17373	2.67364	2.21264
## Proportion of Variance	0.5371	0.3976	0.03545	0.01218	0.00864	0.00592
## Cumulative Proportion	0.5371	0.9347	0.97011	0.98229	0.99093	0.99686

##	PC7	PC8	PC9	PC10	PC11	PC12
## Standard deviation	1.06681	0.77326	0.62205	0.51962	0.35231	0.24472
## Proportion of Variance	0.00138	0.00072	0.00047	0.00033	0.00015	0.00007

```
## Cumulative Proportion  0.99823 0.99895 0.99942 0.99975 0.99990 0.99997
##                               PC13
## Standard deviation      0.15321
## Proportion of Variance 0.00003
## Cumulative Proportion  1.00000
```

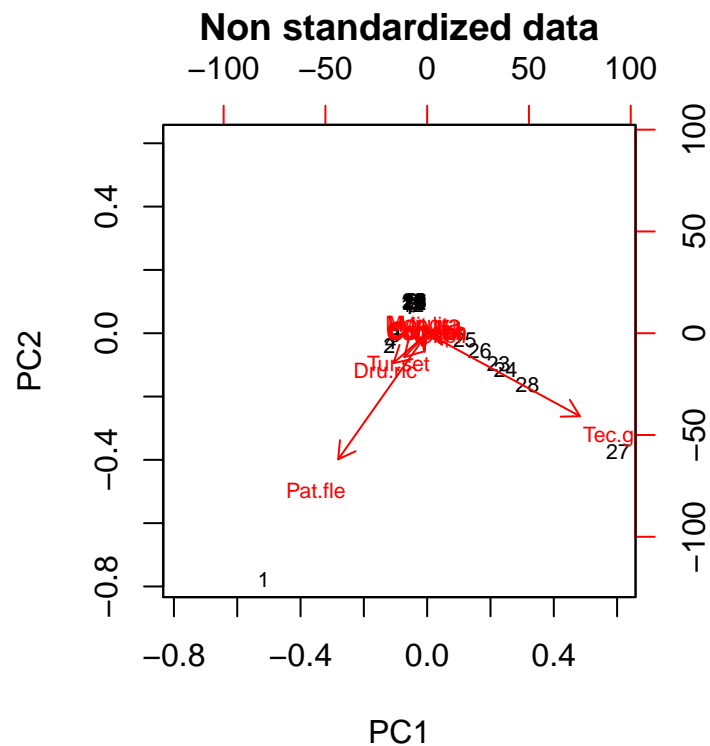
Shows a screeplot.

```
plot(data.out, main="Scree plot", xlab="Principal Components")
```



Shows coordinates of individuals on the principal components. Shows a biplot graph

```
biplot(data.out, main="Non standardized data", cex=0.7)
```



Repeat the analysis using the argument “scale=TRUE” means that the data is standardized and show a biplot graph.

```
data.out = prcomp(data[, -1], scale=TRUE)
biplot(data.out, main="Standardized data", cex=0.7)
```