

# The Locus Algorithm

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## Abstract

We describe the design, implementation and operation of a new algorithm, The Locus Algorithm; which enables optimised differential photometry. For a given target, The Locus Algorithm identifies the pointing for which the resultant FoV includes the target and the maximum number of similar reference stars available, thus enabling optimised differential photometry of the target. We describe the application of The Locus Algorithm to a target from the Sloan Digital Sky Survey to provide optimum differential photometry for that target. The algorithm was also used to generate catalogues of pointings to optimise Quasars variability studies and to generate catalogues of optimised pointings in the search for Exoplanets via the transit method.

## Introduction

Photometric variability studies involve identifying variations in brightness of a celestial point source over time. Such studies are hampered by the Earth's atmosphere, which causes first order and second order extinction Milone and Pel (2011) YOUNG et al. (1991). Differential Photometry mitigates the effect of the Earth's atmosphere by comparing the brightness of a target to reference stars in the same Field of View (FoV). Differential photometry can be optimised for the target by choosing a pointing whose Field of View (FoV) includes the target and the maximum number of reference stars of similar magnitude and colour. Milone and Pel (2011) YOUNG et al. (1991) Howell and B. (2000) Honeycutt (1992).

The Locus Algorithm enables optimised differential photometry by identifying the pointing for which the resultant FoV includes the target and the best set of similar reference stars available.

## Conceptual basis to The Locus Algorithm

A locus can be defined around any star such that a FoV centred on any point on the locus will include the star at the edge of the FoV. For fields containing stars close to one another, if one locus intersects with another, they produce Points of Intersection (PoIs) (Figure 1).

A FoV centred on any such PoI will include both stars associated with creating it. At Points of Intersection the set of stars that can be included in a FoV changes.

The Locus Algorithm considers candidate reference stars in what is termed a Candidate Zone (CZ) - the zone of sky centred on the target within which a FoV can be selected which includes both the reference star and the target. Within the Candidate Zone, all relevant Points of Intersection are identified. Each PoI is assigned a score derived from the number and similarity of reference stars included in it's resulting FoV. The PoI with the highest score becomes the pointing for the target.

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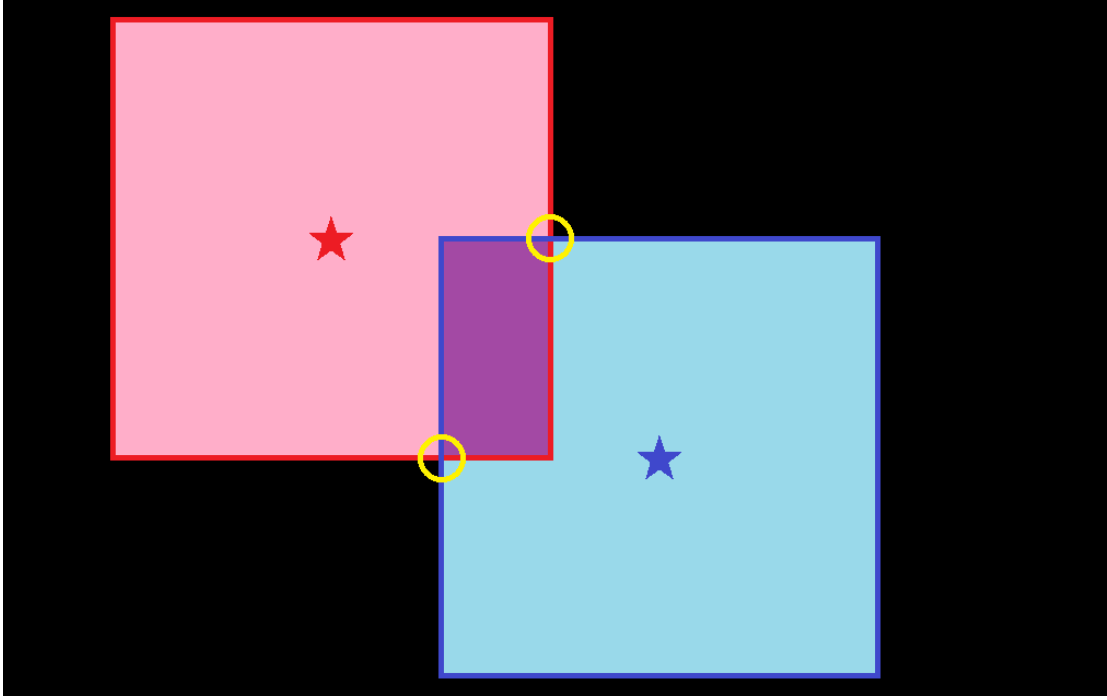


Figure 1: Figure 1. Diagrammatic representation of two stars with loci (red and blue perimeter lines), which intersect and produce two Points of Intersection (PoI's) circled in yellow.

## Locus Algorithm Design

### *Definition of Coordinate System and Locus*

For computational efficiency, The Locus Algorithm considers a Field of View to be a rectangular area on the sky orientated such that the edges are aligned with the primary x and y axes of the Cartesian coordinate system. Movement of the field is restricted to x or y translations.

However, the Celestial coordinate system is defined by the Equatorial coordinate system, with coordinates specified by Right Ascension (RA) and Declination (Dec). Because this is a spherical coordinate system, unit angle in RA is foreshortened, with the degree of foreshortening defined by:

$$angle \in RA = \frac{TrueAngle}{\cosine(Dec)} \quad (\text{Equation 1: Right Ascension foreshortening with Declination})$$

By using this conversion, it is possible to approximate to a high degree of accuracy a Cartesian coordinate system using RA and Dec; with a small FoV of horizontal size R and vertical size S about a star located at point  $RA_c$  and  $Dec_c$ , where

$$R' = \frac{R}{\cos(Dec_c)}$$

as:

$$RA_c - \frac{R'}{2} \leq RA \leq RA_c + \frac{R'}{2}$$

$$Dec_c - \frac{S}{2} \leq Dec \leq Dec_c + \frac{S}{2}$$

Equation 2. Definition of a FoV of size  $R \times S$  centred on a point  $(RA_c, Dec_c)$

This definition is accurate to approximately 1% for a FoV of area 15' square outside celestial polar regions; and does not consider RA “loop around” from 359.99° to 0.00°; resulting, for example, in the exclusion of 0.23% of the SDSS catalogue. Planned enhancements to The Locus Algorithm will resolve these shortcomings.

We can therefore define the locus about any star on the sky located at  $RA_c$  and  $Dec_c$  as the values of Right Ascension and Declination as defined in Equation 2.

#### *Candidate Zone*

A Candidate Zone is defined as a region centred on the target, equal to four times the area of any Field of View (Equation 3), within which any reference star can be included in a Field of View with the target and can therefore be considered as a candidate reference star in identifying the optimum pointing. Conversely, stars outside the candidate zone cannot be included in a Field of View with the target and cannot therefore be considered as candidates reference stars. Hence the Candidate Zone is the maximum region of sky centred on the target from which to choose candidate reference stars when identifying an optimum pointing for a given target. For a target positioned at coordinates  $RA_c$  and  $Dec_c$  the resulting Candidate Zone is defined by:

$$RA_c - R' \leq RA \leq RA_c + R'$$

$$Dec_c - S \leq Dec \leq Dec_c + S$$

Equation 3. Definition of a Candidate Zone of size  $2R \times 2S$  centred on a target with coordinates  $(RA_c, Dec_c)$

#### *Identification and Filtering of Reference Stars*

For each target, a list of candidate reference stars in its Candidate Zone is produced based on the following criteria:

- Position: the reference star must be in the Candidate Zone.
- Magnitude: the reference star must be within a user-defined limit of the target’s magnitude.
- Colour: the reference star must match the colour of the target to within a user-specified limit.
- Resolvability: the reference star must be resolvable, i.e. no other star that would impact a brightness measurements within a user-specified resolution limit.

All stars in the Candidate Zone which pass these initial filters become the list of candidate reference stars from which loci will be identified.

#### *Identifying the Effective Locus for each Candidate Reference Star*

The locus associated with each candidate reference star must be identified based on Equation 2. For the purposes of identifying Points of Intersection, only the side surrounding a given candidate reference star closest to the target need be considered. Hence, we can define the effective locus for such a candidate reference star as a single line of constant RA and a single line of constant Dec nearest the target star (Figure 3).

Specifically, the effective locus can be defined as a corner point of the locus and two lines: one of constant RA and the other of constant Dec emanating from the corner point. The direction of the lines is determined by the Right Ascension and Declination of the candidate reference star relative to the target; as follows:

- If the RA of the candidate is greater than the target, the line of constant Dec is drawn in the direction of increasing RA
- If the RA of the candidate is less than the target, the line of constant Dec is drawn in the direction of decreasing RA

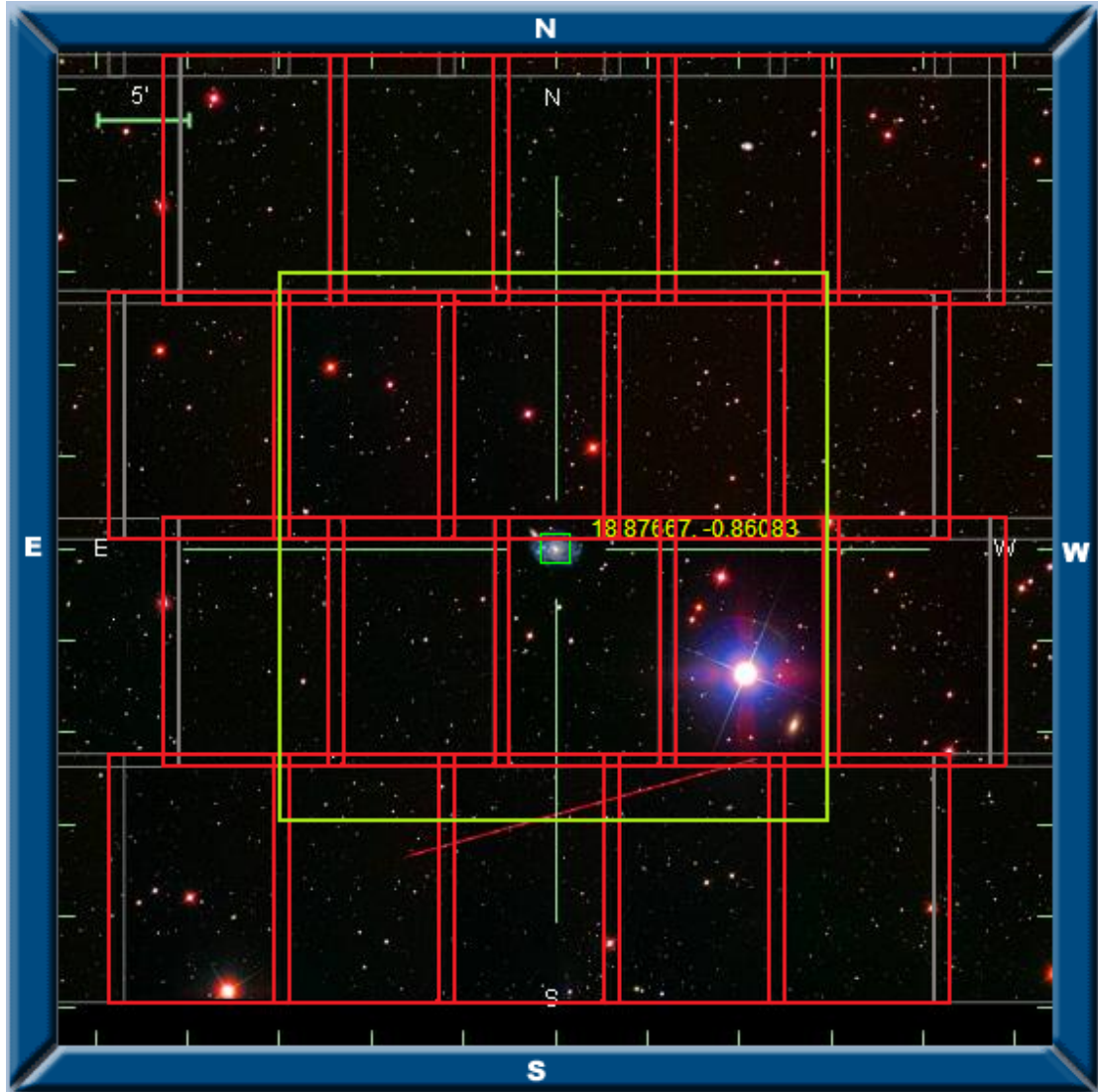


Figure 2: Figure 2. Modified image taken from the SDSS “Navigate” tool. The image showing fields (in red) needed to form a mosaic from which a Candidate Zone (green) centred on the target can be defined.

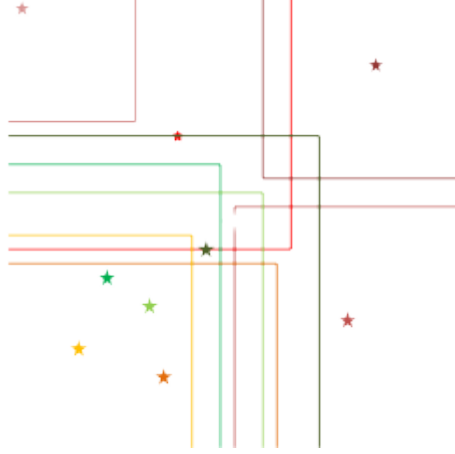


Figure 3: Figure 3: Each effective locus is defined by assigning a pair of RA and Dec coordinates for a corner point and a pair of lines North or South and East or West from the corner point. In this diagram, each candidate reference star is assigned a colour, and the effective locus that corresponds to it is drawn in the same colour.

- If the Dec of the candidate is greater than the target, the line of constant RA is drawn in the direction of increasing Dec
- If the Dec of the candidate is less than the target, the line of constant RA is drawn in the direction of decreasing Dec.

Using the Equatorial Coordinate System discussed in Section 3.1, with coordinates of the target specified by  $(RA_{target}, Dec_{target})$  and coordinates of the candidate reference star defined by  $(RA_{reference}, Dec_{reference})$  and a size of FoV of horizontal length R and vertical length S, the coordinates of the corner point  $(RA_{corner-point}, Dec_{corner-point})$  are defined as:

$$RA_{target} \leq RA_{reference} \Rightarrow RA_{corner-point} = RA_{reference} - R$$

$$RA_{target} > RA_{reference} \Rightarrow RA_{corner-point} = RA_{reference} + R$$

$$Dec_{target} \leq Dec_{reference} \Rightarrow Dec_{corner-point} = Dec_{reference} - \frac{S}{2}$$

$$Dec_{target} > Dec_{reference} \Rightarrow Dec_{corner-point} = Dec_{reference} + \frac{S}{2}$$

The direction of the lines of constant RA and Dec of the effective locus emanating from any such corner point are determined according to the criteria describe above.

#### *Identifying and Scoring Points of Intersection and identifying the pointing.*

The points where lines from any two loci are identified. This involves comparing the corner point RA and Dec and direction of lines for one locus with the corner point RA and Dec and direction of lines for a second locus. In total eight variable associated with each two loci are checked:

- For Locus 1:  $RA_1, Dec_1, DirRA_1, DirDec_1$
- For Locus 2:  $RA_2, Dec_2, DirRA_2, DirDec_2$

Using these parameters, a check as to whether an intersection between the two loci occurs is achieved as follows:

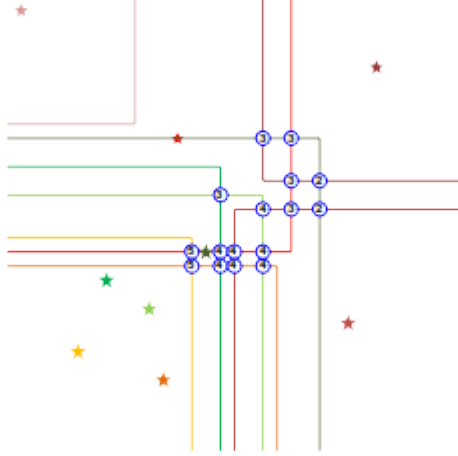


Figure 4: Figure 4. Points of Intersection (PoI), and their associated score. In this diagram each star has a rating of 1, hence the score associated with each PoI is equal to the number of reference stars within a FoV centred at that PoI.

- A line of constant Dec in the positive RA direction from the corner point of locus 1 will intersect with a line of constant RA in the positive Dec direction from the corner point of locus 2 if locus 1 has a lower RA than locus 2 and locus 1 has a higher Dec than locus 2.
- A line of constant RA in the positive Dec direction from the corner point of locus 1 will intersect with a line of constant Dec in the positive RA direction from the corner point of locus 2 if locus 1 has a lower Dec than locus 2 and locus 1 has a higher RA than locus 2.

... and so on. By checking all such possible combinations, all pairs of loci in the field which result in a Point of Intersection are identified and their RA and Dec noted.

Subsequent to identification, each Point of Intersection is then scored. This is achieved as follows:

- The number of reference stars in the Field of View centred on the Point of Intersection is counted.
- Each reference star is assigned a rating value between 0 and 1 based on its similarity in colour to the target.
- The ratings from all counted reference stars in the Field of View are combined into one overall score for the field (Figure 4).
- The Point of Intersection with the highest score becomes the pointing for the target (Figure 5).

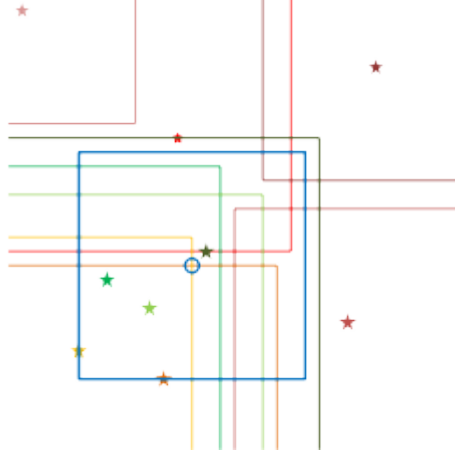


Figure 5: Figure 5: Locus Algorithm. Target: white star. Pointing & FoV: blue. Reference stars and their loci: Fully in the FoV: greens. On the edge of the FoV: yellows. Outside FoV: reds

Scenarios can arise which result in an inability to identify an optimum pointing for a given target for example if there are no, or a maximum of one reference stars in the candidate zone; and if no points of intersection arise – a scenario which can arise if two (or more) reference fall in one quadrant of the candidate zone resulting in concentric loci, or where reference stars are too far apart in different quadrants of the candidate zone in order for their loci to intersect. All four of these scenarios are considered in practical implementations of the locus algorithm aimed at identifying the optimum pointings for a set of targets in a catalogue or list of targets.

In summary, the Locus Algorithm successfully identifies the RA and Dec coordinates of the optimum pointing for a given target, where optimum means a field of view with the maximum number of reference stars which are similar in magnitude and colour to the target.

## Example Implementation of the Locus Algorithm

To illustrate the operations of the Locus Algorithm, a worked example is given here. The process described here in producing an optimal pointing for a given star follows the same sequence of steps described in the first part of this paper. The process is implemented in the R programming language and is geared for reproducible research. The code is available on [\*github\*](#). It can be trivially adapted for different target stars and telescope parameters.

### Target

The star with SDSS ID 1237680117417115655, henceforth called the target, (RA = 346.65 and DEC = -5.0393) is used as the example. This star, in the constellation Aquarius, has SDSS magnitudes as given in the table below.

Band	SDSS_Magnitude
u	17.20
g	15.38
r	14.65
i	14.40
z	14.28

The observational parameters are taken from the telescope at Blackrock Castle Observatory. This telescope has parameters given in the table below:

Parameters	Values
Field of View in degrees	0.1666667
Resolution Limit in degrees	0.0030000
Dynamic Range in magnitudes	2.0000000
Colour Match Limit	0.1000000

### Candidate Zone

The size of the FoV when corrected for shortening by declination is, by equation 1 above,

$$\begin{aligned}
 R' &= \frac{R}{\cos(Dec_c)} \\
 &= 0.1667 / \cos(-5.0393^\circ) \\
 &= 0.16731^\circ
 \end{aligned}$$

The locus of the target is, by equation 2 above,

$$\begin{aligned}
 346.5664 &\leq \text{RA} \leq 346.7337 \\
 -5.1226 &\leq \text{Dec} \leq -4.956
 \end{aligned}$$

The candidate zone as defined above is the area of sky within which reference stars can possibly be included in the same field of view as the target. This is four times the size of the FoV and is given by equation 3 above,

$$\begin{aligned}
 346.4827 &\leq \text{RA} \leq 346.8173 \\
 -5.206 &\leq \text{Dec} \leq -4.8726
 \end{aligned}$$



### Identification and Filtering of Reference Stars

The potential reference stars are selected as follows:

- Position: Within the Candidate Zone, SDSS records 1345 separate objects with clean photometry, (Aguado et al. (2018)).
- Magnitude: the reference star must be within the dynamic range, 2, of the target's magnitude of 14.648, e.g.  $12.648 \leq r \leq 16.648$ . This leaves 41 potential references.
- Colour: the reference star must match the colour of the target to within a user-specified limit. In this case this means  $g - r$  between 0.634 and 0.834 and  $r - i$  between 0.149 and 0.349 This leaves 15 potential references.
- Resolvability: the reference star must be resolvable, i.e. no other star that would impact a brightness measurements within a user-specified resolution limit, in this case 11 arc seconds, (0.18 arc minutes). Any object this close to a potential reference star and with an r-band magnitude which is 5 magnitudes greater than the potential reference or brighter will pollute the light from the potential reference star. This leaves 14 potential references.

These numbers are presented in the table below.

filters	numbers
Position, in Field of View	1345
Correct Magnitude	41
Correct Colour	15
Resolvable	14
In Final Field of View	7

The table below gives the 14 stars in the candidate zone along with the highlighted 7 stars in the final field of view.

ref.	objID	ra	dec	mag_u	mag_g	mag_r	mag_i	mag_z	ratings
1	1237680117417115701	346.743	-5.005	18.461	16.409	15.583	15.317	15.160	0.068
2	1237680065885306903	346.669	-4.915	17.716	15.654	14.897	14.691	14.450	0.429
3	1237680065885241371	346.560	-4.931	17.680	15.934	15.227	15.012	14.901	0.485
4	<b>1237680117417115762</b>	<b>346.676</b>	<b>-5.120</b>	<b>18.920</b>	<b>17.022</b>	<b>16.282</b>	<b>15.974</b>	<b>15.851</b>	<b>0.380</b>
5	1237680065885241391	346.483	-4.946	18.969	17.144	16.420	16.161	15.991	0.808
6	<b>1237680117417050133</b>	<b>346.594</b>	<b>-5.161</b>	<b>16.702</b>	<b>14.825</b>	<b>14.068</b>	<b>13.887</b>	<b>13.648</b>	<b>0.241</b>
7	1237680117417050117	346.538	-5.018	18.404	16.520	15.768	15.532	15.393	0.701
8	1237680117417181202	346.810	-4.975	17.461	15.616	14.852	14.579	14.443	0.535
9	<b>1237680117417050120</b>	<b>346.563</b>	<b>-5.153</b>	<b>18.460</b>	<b>16.498</b>	<b>15.771</b>	<b>15.533</b>	<b>15.397</b>	<b>0.830</b>
10	<b>1237680117417115683</b>	<b>346.713</b>	<b>-5.050</b>	<b>17.585</b>	<b>15.782</b>	<b>15.109</b>	<b>14.867</b>	<b>14.798</b>	<b>0.361</b>
12	1237680065348501526	346.804	-5.202	15.877	14.146	13.385	13.148	12.994	0.644
13	<b>1237680117417115692</b>	<b>346.724</b>	<b>-5.047</b>	<b>18.362</b>	<b>16.576</b>	<b>15.843</b>	<b>15.568</b>	<b>15.464</b>	<b>0.734</b>
14	<b>1237680065348435996</b>	<b>346.707</b>	<b>-5.199</b>	<b>16.704</b>	<b>14.699</b>	<b>13.905</b>	<b>13.676</b>	<b>13.515</b>	<b>0.322</b>
15	<b>1237680117417115655</b>	<b>346.650</b>	<b>-5.039</b>	<b>17.199</b>	<b>15.382</b>	<b>14.648</b>	<b>14.399</b>	<b>14.281</b>	<b>1.000</b>

The table above also includes ratings for each star. This gives a measure of how close, spectrally, each reference star is to the target. This rating hasn't been optimised and is the subject of further research by our group, but for the purpose of this work was calculated as follows:

$$rating = \left| \left( 1 - \frac{\delta g - \delta r}{M} \right) \right| \times \left| \left( 1 - \frac{\delta r - \delta i}{M} \right) \right|$$

Where  $\delta r$  stand for the difference between the r-band magnitude for the target and the reference star and M is the colour match limit.

For example, the star SDSS1237680117417050120 (Star 9 on figure N) has  $g_r = 16.498$ ,  $r_r = 15.771$ , and  $i_r = 15.533$ . This compares to the target magnitudes of  $g_t = 15.382$ ,  $r_t = 14.648$ , and  $i_t = 14.399$ .

This gives:  $\delta g = 16.498 - 15.382 = 1.116$ .  $\delta r = 15.771 - 14.648 = 1.122$ .  $\delta i = 15.533 - 14.399 = 1.134$ . Thus rating =  $(1 - (|1.116 - 1.122|/0.1)) \times (1 - (|1.122 - 1.134|/0.1)) = (0.93) \times (0.89) = 0.83$

From expression 8, the cornerpoints for a given reference can be calculated:

$$RA_r < RA_t \Rightarrow RA_c = RA_r + R'$$

$$Dec_r < Dec_t \Rightarrow Dec_c = Dec_r + S$$

For reference SDSS1237680117417050120 (Star 9 on figure N)

$$346.5626 < 346.65 \Rightarrow RA_c = 346.5626 + 0.0837 = 346.6463$$

$$-5.153 < -5.0393 \Rightarrow Dec_c = -5.153 + 0.0833 = -5.0697$$

From Expression 9:  $RA_r < RA_t \Rightarrow \text{DirRA} = +\text{ive}$   $Dec_r < Dec_t \Rightarrow \text{DirDec} = +\text{ive}$

For reference SDSS1237680117417050120 (Star 9 on figure N)

$$346.5626 < 346.65 \Rightarrow \text{DirDec} = +\text{ive},$$

$$-5.153 < -5.0393 \Rightarrow \text{DirRA} = +\text{ive}$$

Repeating this calculation for SDSS1237680117417115655 (Star 15 on figure N) gives  $RA_c = 346.7337$ ,  $Dec_c = -4.956$ ,

$$\text{DirRA} = +\text{ive}, \text{DirDec} = +\text{ive}.$$

We can compare these two effective loci to see if they intersect to form a valid PoI.

From Expression 10:  $\text{DirRA}_9 = +\text{ive}$ ,  $\text{DirDec}_{15} = +\text{ive}$   $RA_r9 > RA_r9$  AND  $Dec_r9 < Dec_r9$   
PoI exist at  $(RA_c9, Dec_c9) = (346.6463, -5.1226)$

From Expression 2, the FoV centred on the PoI (346.6463, -5.1226) can be calculated to be:

$$RA_c - \frac{R'}{2} \leq RA \leq RA_c + \frac{R'}{2}$$

$$Dec_c - \frac{S}{2} \leq Dec \leq Dec_c + \frac{S}{2}$$

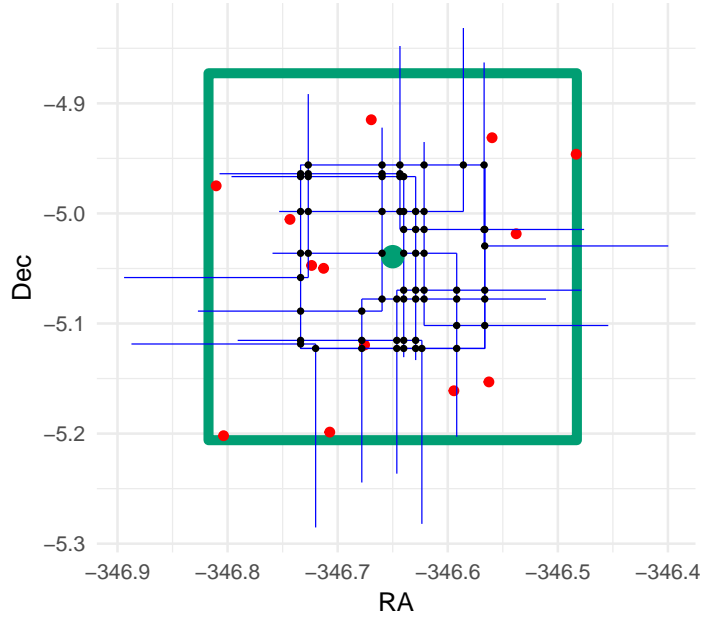
$$346.6463 - 0.1673134 \leq RA \leq 346.6463 + 0.1673134$$

$$-5.1226 - 0.1666667 \leq Dec \leq -5.1226 + 0.1666667$$

$$346.479 \leq RA \leq 346.8136$$

$$-5.2893 \leq Dec \leq -4.956$$

The locus associated with each of these 14 potential references is identified and the Points of Intersection associated with these loci are calculated. This leads to the situation shown in the diagram below



Plot Showing the Target (Green Circle),  
Potential Reference Stars (Red Circles),  
Associated Loci (Blue Squares),  
and Points of Intersection (Black Dots).  
The Candidate Zone is Shown by the Green Square

After checking different fields of view, a pointing with  $RA = 346.646$  and  $DEC = -5.123$  included both the target and 7 reference stars. This pointing is calculated to have a score of 3.87

The SQL query to download potential reference stars from SDSS is given below. This SQL query is run on the CAS database, release DR15, of SDSS. Note the flags to give clean photometry (Aguado et al. (2018))

```
SELECT objID, ra, dec, psfmag_u, psfmag_g, psfmag_r, psfmag_i, psfmag_z
FROM photoObj
WHERE (ra between (346.48270496969) AND (346.817331746246)
OR ra BETWEEN (706.48270496969) AND (706.817331746246)
OR ra BETWEEN (-13.5172950303096) AND (-13.1826682537544) ) AND dec BETWEEN
(-5.20597532982638) AND (-4.87264199649304)
AND psfmag_r BETWEEN 12.64849 AND 16.64849
AND (psfmag_g - psfmag_r) BETWEEN (0.633989999999999) AND (0.833989999999999)
AND (psfmag_r - psfmag_i) BETWEEN (0.149080000000001) AND (0.349080000000001)
AND clean = 1
AND (calibStatus_r & 1) != 0
```

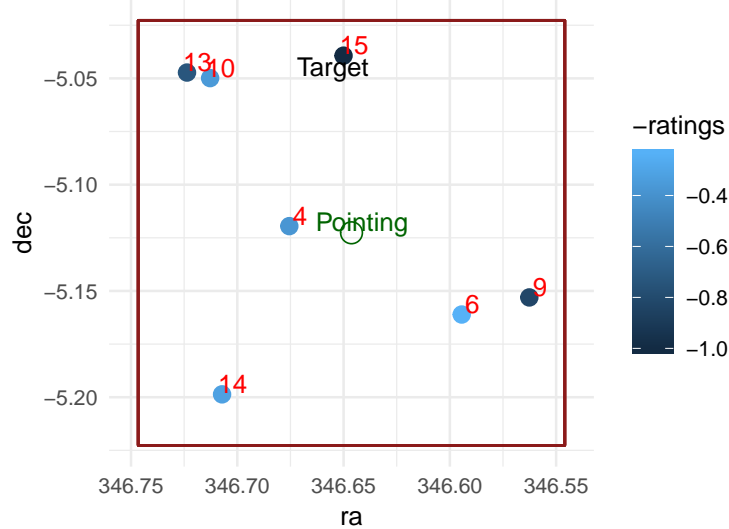
ref.	objID	ra	dec	mag_u	mag_g	mag_r	mag_i	mag_z	ratings
9	1237680117417050120	346.563	-5.153	18.460	16.498	15.771	15.533	15.397	0.830
6	1237680117417050133	346.594	-5.161	16.702	14.825	14.068	13.887	13.648	0.241
15	1237680117417115655	346.650	-5.039	17.199	15.382	14.648	14.399	14.281	1.000
4	1237680117417115762	346.676	-5.120	18.920	17.022	16.282	15.974	15.851	0.380
14	1237680065348435996	346.707	-5.199	16.704	14.699	13.905	13.676	13.515	0.322
10	1237680117417115683	346.713	-5.050	17.585	15.782	15.109	14.867	14.798	0.361
13	1237680117417115692	346.724	-5.047	18.362	16.576	15.843	15.568	15.464	0.734

The Field of View for SDSS1237680117417115655, showing the star its

the telescope pointing in green,

and the discovered reference stars graded by their ratings.

Note that the RA runs in the direction consistent with SDSS



### References

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