Using Machine Learning to Predict the Correlation of Spectra Using SDSS Colour Magnitudes as an Improvement to the Locus Algorithm

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Abstract

The Locus Algorithm is a new technique to improve the quality of differential photometry by optimising the choices of reference stars. At the heart of this algorithm is a routine to assess how good each potential reference star is by comparing its sdss magnitude values to those of the target star. In this way, the difference in wavelength-dependent effects of the Earth's atmospheric scattering between target and reference can be minimised. This paper sets out a new way to calculate the quality of each reference star using machine learning. A random subset of stars from sdss with spectra was chosen. For each one, a suitable reference star, also with a spectrum, was chosen. The correlation between the two spectra was taken to be the gold-standard measure of how well they match up for differential photometry. The five sdss magnitude values for each of these stars were used as predictors. A number of supervised machine learning models were constructed on a training set of the stars and were each evaluated on a testing set. The model using Support Vector Regression had the best performance of these models. It was then tested of a final, hold-out, validation set of stars to get an unbiased measure of its performance. The dataset used, the model constructions, and performance evaluation are presented here.

1. Introduction

A wealth of astrophysics information is available through the study of the brightness of celestial objects as a function of time. For example, exoplanet detection by the transit method relies critically on measurements of intrinsic variability where such variability can be a small fraction of the total stellar brightness (Giltinan et al. (2011), Everett and Howell (2001)). Ground-based observations looking for such variability are complicated by the effects of the Earth's atmosphere which causes incoherent wavelength-dependent variations in the stellar flux detected. This can mask intrinsic variability and hamper the study of variable astrophysical phenomena (Smith et al. (2008)).

The technique of differential photometry has been developed in an attempt to mitigate the effects of the Earth's atmosphere on studies of stellar variability. Differential photometry uses references stars at small angular separations from the star of interest as comparators. Atmospheric effects should have similar effects on the measured flux from all of these stars causing them to vary in unison (Burdanov et al. (2014)). Because scattering in the Earth's atmosphere is wavelength dependent, the technique is especially successful if the target star and reference stars are spectrally similar (Milone and Pel (2011), Sterken et al. (2011)).

The Locus Algorithm (Creaner et al. (2022)) has been used to create catalogues of pointings suitable for differential photometry on astromonical targets based on a novel technique of choosing appropriate reference stars (Creaner et al. (2020) and Creaner EXO's). The algorithm no longer places the target in the centre of

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the field of view but, in general, repositions it so as to include the best set of reference stars. Assessment of each reference star is performed by referring to the sdss catalogue and the colour band magnitudes therein. These magnitudes can be used to infer the overall shape of the star's spectrum. Stars that have similar spectra will be effected by scattering from the Earth's atmosphere to a more comparable degree that stars with dissimilar spectra. The original Locus Algorithm used a rational, but ad-hoc, method to estimate the correlation of stellar spectra based on differences between their g, r, and i sdss colour magnitudes (?). This was necessary for computational efficiency. The work presented here presents a more rigorous technique to estimate the correlation of stellar spectra based on machine learning. The subset of stars in sdss that have their spectra measured are used. These stars are paired off such that each pair has similar colour magnitude differences and are thus potentially a good match for differential photometry. This corresponds to the pre-filtering step employed by ?. The correlation between each pair's spectra is calculated. This forms the basis of a goodness-of-fit between the two spectra. The sdss magnitudes (u, g, r, i, and z for both stars in the pair) are then used to train machine learning algorithms to predict this goodness-of-fit. The models produced are then applied to other pairs of stars, the test set, to evaluate their performance. The results show a significant improvement over the original ad-hoc Locus Algorithm routine, this model will be incorporated to future generations of the Locus Algorithm.

2. Data

This work uses 3556 stellar spectra from the SDSS SEGUE and BOSS observations and their physical parameters from the 13^{th} SDSS data release (Aguado et al. (2018)). The spectra are clipped to just the wavelengths contained in the sdss r band (between 550nm and 700nm). Stars are paired off based on their sdss colour magnitudes so that both stars in a pair are of similar colour. Specifically, both $(g_1 - r_1) - (g_2 - r_2)$ and $(r_1 - i_1) - (r_2 - i_2)$ will be between 0 and 0.3. 0.3 is thus called the *Colour Match Limit*. This ensures that these stars would be realistic matches for differential photometry. In addition, stars were chosen that had r colour magnitude values between 15 and 20. Care is taken to ensure that all 7112 stars in the 3556 pairs are unique. The SQL queries used to download physical parameters and the spectra are given in the supplementary materials for this paper. Correlations between spectra are calculated using the usual Pearson Correlation formula, equation (1).

$$r_{xy} = \frac{n \sum x_i y_i - \sum x_i \sum y_i}{\sqrt{n \sum x_i^2 - \left(\sum x_i\right)^2} \sqrt{n \sum y_i^2 - \left(\sum y_i\right)^2}}.$$
 (1)

where x_i refer to the flux from the first star at a given wavelength, i, in units of $erg/cm^2/s$ Å, y_i refer to the flux from the second star at the same wavelength. Figure 1 shows some pairs of stars along with their correlations. The first pair, A and B, are representative of the sample. The second pair, C and D, were chosen to have an unusually low correlation for this sample set.

Correlation is usually bounded by -1 and 1. And because these are spectra from stars and they have similar colour magnitudes, the correlations tend to be clustered near this higher end, see the histogram in figure 2A below. Machine learning algorithms work better with normally distributed values (need reference) and this is especially true when it comes to analysing model performance (another reference), so the correlation values were transformed. First of all by a logit transformation (2):

$$logit(x) = \ln\left(\frac{1+x}{1-x}\right) \tag{2}$$

And then by scaling and normalising the values to have a mean of 0 and a standard deviation of 1. The resulting transformed values are shown in figure 2B.

The data is split into test and training sets, with 70% of the data (2668 samples) in the training set and the remainder (888 samples) in the test set. Each set has a representative sample of correlation values, to do this the original sample of 3556 pairs is split into five groups based on percentiles of the correlation and both testing and training sets get a commensurate proportion of each group. In additional, completely independent set of 526 pairs of stars are used for final validation of the chosen model.

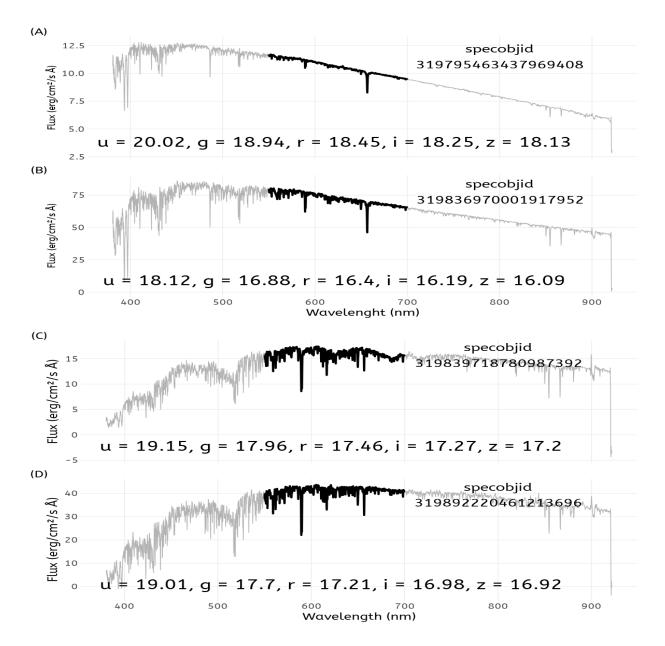


Figure 1: Two pairs of spectra downloaded from SDSS. The ugriz colour magnitudes for each star is given below its spectrum. The darkened area of the spectral line corresponds to the r-band wavelengths. The correlation between spectra A and C is 0.96. That between spectra B and D is 0.75.

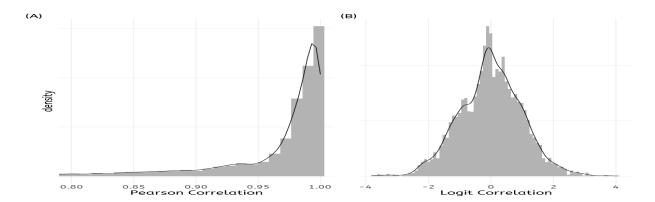


Figure 2: (A) Histogram of Pearson correlation values between r-band spectra between pairs of matched stars. (B) Values in (A) transformed by a logit function.

3. Models

Four types of machine learning algorithms were used: support vector regression (SVR), random forrest (RF), gradient boosting (GBM), and a linear model (LM). In each of the four cases, a model was built on the training set, using 10 predictors, namely the ugriz values for both stars in each pair. The target value was the logit(correlation) value. Cross validation, 20-fold repeated 10 times, was used to minimise model bias. Hyperparameters for each model were tuned. The results for RMSE, MAE, and \mathbb{R}^2 for all models are given in table 1.The details are given below:

- Support Vector Regression This used a radial basis kernal function (Karatzoglou2004). A grid search on the hyperparameters Cost (C) and sigma (σ) was undertaken for values 8 < C < 25 and $0.08 < \sigma < 0.20$. The model was optimised based on the RMSE of the training set. The best tune was obtained for C = 20 and $\sigma = 0.12$.
- Stochastic Gradient Boosting This used Friedman's gradient boosting algorithm (Boehmke and Greenwell (2019)). A grid search on the hyperparameters Number of Boosting Iterations (n.trees), Maximum Tree Depth (interaction.depth), Shrinkage (shrinkage), and Minimum Terminal Node Size (n.minobsinnode) was undertaken. The model was optimised based on the RMSE of the training set. The best tune was obtained for n.trees = 100, interaction.depth = 10, shrinkage = 0.1 and n.minobsinnode = 10.
- Random Forrest This used the ranger fast implementation of random forrests (Wright and Ziegler (2017)). The Minimum Node Size was set to be 5, the splitting rule was chosen to be variance. The number of variables to possibly split at each node (mtry) was tuned to be 6.
- Linear Model The final model was a linear model from the MASS R package (Venables and Ripley (2002)). There were no tunable parameters.

4. Model Evaluation

Table 1 gives the values for RMSE, MAE, and R^2 for each of the four values as they applied to the test set of 888 stellar pairs. To put these RMSE and MAE values in context, remember that the logit correlation values have been scaled to have a standard deviation of 1.

As can be seen from table 1, the best performing model was that produced by SVR. This is in line with expectations as our data set had few (10) predictors, they were all numeric as opposed to being a mix of numeric and categorical, and there were no missing values. These are all factors that favour SVR models.

Finally, the SVR model was applied to the validation set of 526 stellar pairs. The resulting predicted values has an RMSE of 0.564, an R^2 of 0.682, and an MAE of 0.399 when compared to the observed logit correlation values of the spectra.

Table 1: Results of applying the best tuned models on the test set. Root mean squared error (RMSE), R-squared value (R2), and mean average error (MAE) for each of the four model types. The models were built on the training set of 2668 stellar pairs. The values given below were obtained by applying each model to the test set of 888 stellar pairs

	RMSE	R^2	MAE
SVR	0.554	0.693	0.394
GBM	0.584	0.655	0.423
RF	0.590	0.648	0.427
LM	0.639	0.587	0.480

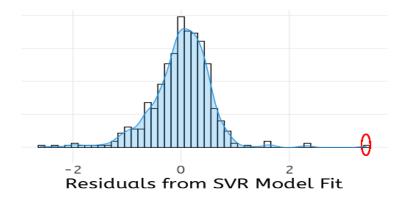


Figure 3: Residuals from the fit of the best performing SVR model on the validation dataset. Note one of the outlying values circled in red

The histogram of the residuals, the observations minus the predicted values, from this fit on the validation data is shown in figure 3. This histogram looks to be normally distributed with the addition of a significant number of outliers. Note the largest absolute residual with a value of 3.41 circled in red in figure 3. This particular value will be discussed below. Figure 4 shows the resulting values of observed logit correlation values against predicted logit correlation values. The points are coloured depending on the absolute value of the residual (how far they lie from the dashed line). The point at the bottom left corner is the one mentioned in the discussion of 3 above. Figure 5 shows the resulting values of the residuals against predicted logit correlation values. Figure 6 shows a quantile-quantile (QQ) plot of the residuals.

All of these plots point to the presence of outliers in the residuals. These were investigated. Looking at the histogram in figure 3. As stated earlier, there is a notable residual at 3.41, highlighted in red in the figure. The spectra of the pair of stars involved in this outlier were investigated and are shown in figure 7. Note that the top spectrum, from a star of spectral subclass CV located at $RA = 140.04^{\circ}$ and $Dec = 0.7125^{\circ}$, has emission lines rather than absorption lines more reminiscent of a galaxy rather than a star. This behaviour was noted for some, but not all, of the stellar pairs with high residuals. In all cases it involved a star with subclass CV.

Finally, the model presented here was compared with the model used in the original Locus Algorithm (?). That used a linear model of the differences in magnitudes in the g, r, and i SDSS bands between the two stars in each pair to calculate a rating for each pair. This is shown in equation 3.

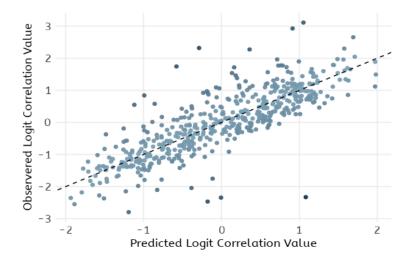


Figure 4: Observed versus predicted logit correlation values

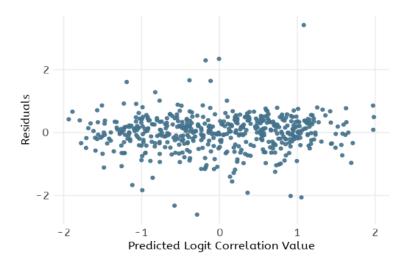


Figure 5: Residuals versus predicted logit correlation values

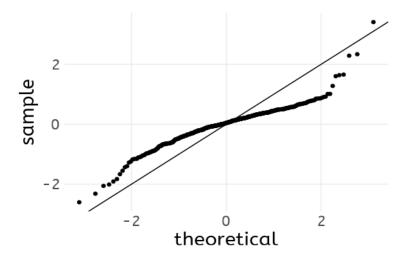


Figure 6: QQ Plot of the Residuals from the Fit of the SVR Model on the Validation Dataset

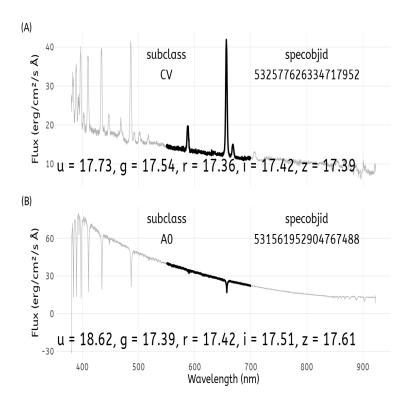


Figure 7: Spectra of the two stars involved in the outlier of the residuals histogram

$$rating = \left(1 - \left| \frac{\delta g - \delta r}{M} \right| \right) \times \left(1 - \left| \frac{\delta r - \delta i}{M} \right| \right) \tag{3}$$

Where δr stand for the difference between the r-band magnitudes for the two stars in each pair, and M is the Colour Match Limit of 0.3. Similarly for δg and δi .

When the ratings thus derived were compared with the logit correlation values derived from the spectra, an R^2 of 0.345 was obtained. This compares with the R^2 of 0.682 obtained by the SVR model here. There is a clear improvement in using the new machine learning approach to the Locus Algorithm.

5. Conclusions

The last numbered section should briefly summarise what has been done, and describe the final conclusions which the authors draw from their work.

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