Deep Learning in Insurance Risk Quantification: A Comparative Study

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I. Definition

Project Overview

Balancing losses and premiums is the crux of managing a successful insurance business. This balancing act consists of being able to quantify and understand these financial losses (risk) that will be incurred in order to set premiums at rates that are both profitable and attractive to consumers. Here I focus on methods for quantifying risk. Insurers invest heavily on teams of analysts, domain experts and actuaries to perform this task. Countless studies are also regularly published exploring machine learning approaches to solve this problem and evaluate commercial solutions (see comparative analysis of risk models in healthcare by the Society of Actuaries from 2016)¹. In short, risk prediction is and always has been one of the biggest challenges in insurance.

With the advent of machine learning and big data in commercial insurance, companies are eagerly seeking new ways to apply novel techniques to improve their business, but are often challenged with the complexities that come with supporting these technologies. Traditional methods used in practice include actuarial sciences and mostly linear models. More robust techniques like ensembling are recently being utilized. However, the industry is still behind in terms of state of the art methods like deep learning and the technologies to support them.

The goal of this project is to [1] determine the feasibility of deep learning in this task and [2] to do a proof of concept to make a case for insurers to invest in deep learning technologies. Allstate ran a Kaggle competition in 2016 and provided an anonymized dataset well-suited for this task².

Problem Statement

Can deep neural networks provide a viable solution for risk modeling in insurance claims?

Predictive models for assessing future risk are commercially available across nearly all insurance domains from automobile to healthcare. For example, Equifax offers its Insight Score³ product while companies like Verscend sells its DxCG⁴ product for healthcare insurance. In general, these solutions do not utilize deep learning for predicting future risk. The upfront investments needed simply do not justify the marginal increase in performance deep learning often provides. Additionally, many domains have a strong preference for model interpretability, which is often why linear models are so well received

I attempt to make a case for deep learning through this proof of concept. Three models were trained and evaluated.

- 1. Benchmark Model: A benchmark ensemble model was trained as a proxy for a competitive market solution that a deep learning model needed to beat.
- 2. Deep Learning Model (CPU): A deep neural network was trained to compare against the benchmark model. This model was also used to benchmark the cost-benefits of technologies optimal for deep learning (namely GPU's).
- 3. Deep Learning Model (GPU): The same deep neural network architecture was trained on a GPU cluster for comparison against the CPU trained model.

A successful deep learning model had to [1] beat the benchmark model in validation or cross-validation performance, [2] be comparible to the solutions provided via Kaggle submissions for Allstate's competition, and [3] be more computationally efficient on a GPU cluster. I prototyped a functional machine learning platform that can integrate with an organization's database technology stack to further simulate a business setting.

Inputs

The inputs to solve the problem will be data provided by Allstate via Kaggle for the Claims Severity competition. Data include a train.csv file and a test.csv file without labels. The data is discussed in more detail within the *Analaysis* section.

Learning to be Done

The learning will consist of the three models outlined above. For each model, the training data will be split into a training and validation partition. Models will be validated on the validation set during training. The provided test.csv file will serve as the hold-out test set to be scored through the Kaggle submission API.

$Target\ Outputs$

The models are predicting the label provided by Allstate called loss. Each observation in the data is a unique insurance claim. The target variable is simply the cost of a claim. Basically, the goal is to predict the cost of a future claim based on all relevant features of the claim. Features are anonymized, but claim features typically include demographics like age/gender, date, and information encoding the details surrounding the event for which the claim is being made.

Metrics

The problem statement is broken into three comparisons as outlined above. Each comparison will be based on a different set of metrics specific to the goals at hand.

Deep Learning vs Benchmark

One of the most common metrics to compare solutions and models is the humble coefficient of determination (\mathbb{R}^2). If a suitable benchmark cannot be beaten, then there is no point in continuing with deep learning. The \mathbb{R}^2 was computed on validation partitions.

	R-Squared		MAE		95th Percentile of Error	
1,000 10,0		10,000	1,000	10,000	1,000	10,000
	Diagnosis-Only Models					
ACG System	12.1%	16.0%	9.4%	2.9%	22.5%	7.2%
CDPS	7.8%	9.6%	9.2%	3.1%	22.5%	7.3%
DxCG	14.5%	18.8%	9.2%	2.9%	21.9%	7.2%
Impact Pro	13.1%	18.1%	9.2%	2.9%	22.2%	6.9%
MARA	15.2%	19.8%	9.2%	2.9%	21.7%	7.1%
Truven	16.6%	20.7%	9.1%	2.8%	21.3%	7.3%
Wakely	13.8%	17.4%	9.2%	2.9%	21.8%	7.2%
Pharmacy-Only Models						
ACG System	10.6%	14.0%	9.4%	3.0%	22.2%	7.1%
DxCG	13.8%	14.4%	9.2%	3.0%	22.0%	7.2%
Impact Pro	13.8%	13.8%	9.2%	3.0%	21.9%	7.3%
MARA	14.0%	15.3%	9.2%	2.9%	22.1%	7.1%
MedicaidRx	8.8%	8.4%	9.5%	3.1%	22.6%	7.3%
Wakely	10.3%	9.7%	9.4%	3.0%	22.9%	7.5%
	D	iagnosis-and	l-Pharmacy I	Models		
ACG System	13.9%	18.5%	9.4%	2.9%	22.3%	7.1%
CDPS+MRX	9.7%	10.7%	9.5%	3.1%	22.6%	7.2%
CRG	11.8%	12.1%	9.3%	3.0%	22.2%	7.4%
Impact Pro	15.8%	20.6%	9.1%	2.9%	22.0%	6.8%
MARA	18.5%	21.6%	8.9%	2.8%	21.7%	7.0%
Wakely	16.0%	18.5%	9.1%	2.9%	21.4%	7.1%
Prior Cost Models						
ACG System	14.5%	20.0%	9.2%	2.9%	21.9%	6.9%
DxCG	22.1%	24.3%	8.8%	2.8%	23.0%	7.1%
MARA	22.4%	24.9%	8.7%	2.8%	21.9%	6.8%
SCIO	14.3%	15.8%	9.2%	2.9%	22.1%	7.2%

Figure 1: 2016 Risk model comparisons by Society of Actuaries

Figure 1 shows a great example of how different models are compared taken from a Society of Actuaries report¹. I compared a deep learning model to the ensemble benchmark using the r2_score implementation from scikit-learn.

$$Eq 1. R^2$$

$$R^{2}(y,\hat{y}) = 1 - \frac{\sum_{i=0}^{n_{samples}-1} (y_{i} - \hat{y}_{i})^{2}}{\sum_{i=0}^{n_{samples}-1} (y_{i} - \bar{y}_{i})^{2}}$$

Deep Learning vs Kaggle

If a simple deep learning model beats the ensemble, it will be compared to other solutions provided through the 2016 Kaggle competition. The competition uses mean absolute error (MAE) on the provided test data to rate submissions. Again, I used scikit-learn's implementation during model training on validation partitions. The final MAE was computed via Kaggle submission and is a measure of how viable deep learning is as a risk assessment tool. I tried to beat the median submission MAE of 1,125, but fell short during the time I had for this project. I plan to continue modifying my network to beat this score.

Eq 2. Mean Absolute Error

$$MAE(y, \hat{y}) = \frac{\sum_{i=0}^{n_{samples}-1} |y_i - \hat{y}_i|}{n_{samples}}$$

Return on Investment

Lastly, I gathered metrics for computation performance, financial costs and opportunity costs to make a case for the return on investment on a full deep learning solution (including the technology stack). More specifically:

- Cost per R² gain
- Training and scoring times
- Storage and computational overhead

Justification

I am using R² to evaluate my models as that is a common metric used in insurance to compare models. It is easily understood by even those without deep statistical knowledge as the values always ranges between 0 and 1. The idea here is to simulate an actual business scenario and report metrics meaningful even to those in executive leadership. MAE is the metric that Allstate judges submissions on in the Kaggle competition. In order to see how my model compares to other solutions directly, MAE is required. Lastly, the supplemental metrics such as costs and run times are primarily to understand the investments needed for a deep learning solution.

II. Analysis

Data Exploration and Visualizations

Data Description

The data was provided in a fully anonymized state from Allstate via Kaggle. A training and test dataset were given.

Table 1: Counts from data provided by Allstate

partition	rows	columns	count_rows_na	count_rows_dupe_id
train	188318	133	0	0
test	125546	131	0	0

The training data had about 188k rows. There are 130 continuous and categorical features and 1 label "loss". I created an additional column called "log_loss" which is just the natural log of the label column provided. Each row represents a single claim. The data were scrubbed and cleaned by Allstate so minimal data processing was needed for this project. There were no duplications or nulls. This is actually how a machine learning application may work in practice. The application will only see data that is in some canonical format provided by the organization's data engineering processes.

There were 14 continuous features prefixed with "cont", 116 categorical features prefixed with "cat", and a claim identifier.

Target Variable

75000 - 25000 - 0 40000 80000 120000

Figure 2: Histogram of the loss variable

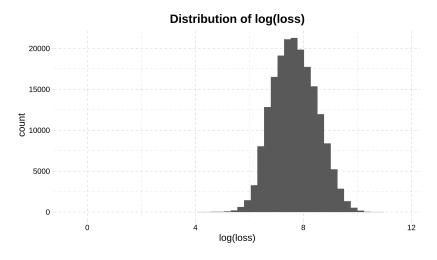


Figure 3: Histogram of the loss variable log transformed

Figures 2 and 3 show the distribution of the provided target variable before and after \log transformation to improve the distribution for machine learning.

Continuous Features

The 14 continuous variables provided appear to have been normalized to a mean of 0.5 and standard deviation of 0.2 by Allstate.

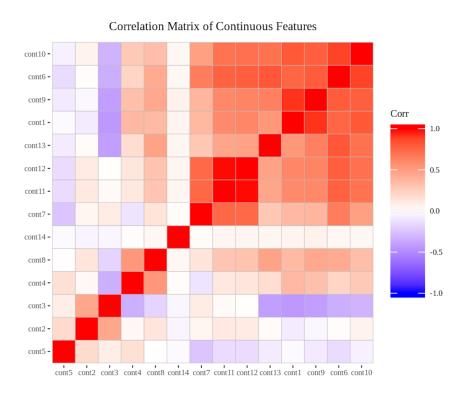


Figure 4: Correlation heatmap of the continuous features

Several features are highly correlated with each other such as cont6 and cont10. Those at the bottom left of the correlation heatmap in Figure 4 have much less collinearity and ended up being good predictors.

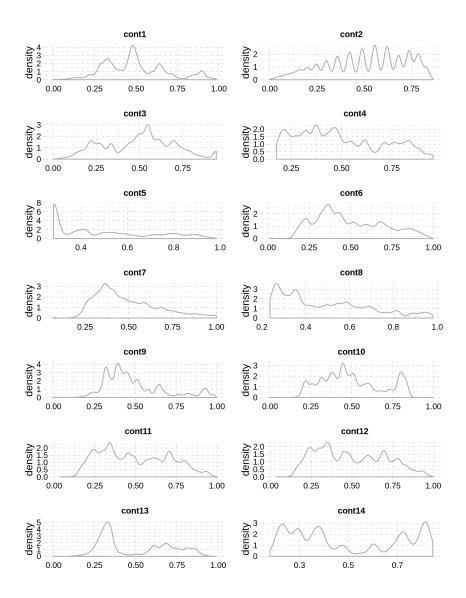


Figure 5: Density plots of the continuous features

The density plots show that not all continuous variables appear to be truly continuous. In particular cont2, looks like it could have been a discretized numeric variable given its density patterns.

Categorical Features

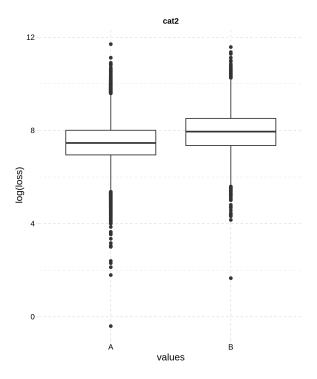


Figure 6: Box plot of cat2

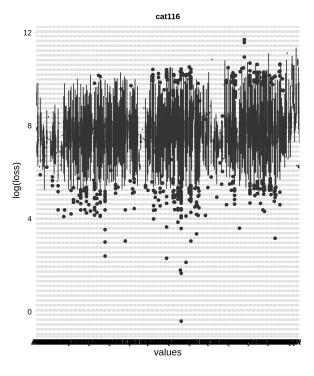


Figure 7: Box plot of cat116

Figure 6 shows an example of how most categorical variables were distributed. They had a cardinality of two with some outliers. There were 17 categorical variables with a cardinality greater than ten with cat116 (Figure 7) having the highest cardinality of 326.

Note: I did not apply any logic for dealing with high cardinality as my goal was not winning Kaggle, but rather to prove a case for deep learning. Also, this kept things simple enough for this project to remain tractable given the limited time provided.

Algorithms and Techniques

Feature Selection

The only pre-processing step on the feature space was to one-hot encode all of the categorical variables. This gave me 1,153 features in total. A decision tree regressor was fit to this processed dataset and feature importances extracted. Over many iterations, I found that a threshold of $1.05 \times mean(all feature importances)$ gave me reasonably performant models. In other words, I selected variables with a feature importance score greater than this threshold value, netting me 152 input features.

Benchmark Ensemble Model

I tried multiple regressor classes available in scikit-learn's library and settled on simpler algorithms for the three sub-models that I ensembled. Two were simple linear models and one was a decision tree. I started with more complex algorithms, but found them to be too slow to iterate on and decided to use very simple models that are easy to tune and scale well.

- 1. **Decision tree** Decision trees
- 2. Ordinary least squares OLS
- 3. Stochastic Gradient Descent regressor

The final ensembler was an ordinary least square linear regression model to stack the results of the three sub-models. Grid search and 10-fold cross-validation were used to explore a wide hyperparameter space.

Deep Neural Network Model

For the purposes of this exercise, I designed a simple Multilayer Perceptron that can train relatively quickly, allowing me to iterate and test my development in the shortest amount of time possible. Again, the goal was not to build the most accurate model. The details of the model is discussed in the Methodology section of this document.

Network architecture:

Layer (type)	Output	Shape	Param #
dense_1 (Dense)	(None,	1024)	156672
dense_2 (Dense)	(None,	512)	524800
dropout_1 (Dropout)	(None,	512)	0
dense_3 (Dense)	(None,	256)	131328
dropout_2 (Dropout)	(None,	256)	0
dense_4 (Dense)	(None,	64)	16448
dropout_3 (Dropout)	(None,	64)	0
dense_5 (Dense)	(None,	32)	2080
dense_6 (Dense)	(None,	16)	528
dense_7 (Dense)	(None,	1)	17
Total narama, 021 072			

Total params: 831,873 Trainable params: 831,873 Non-trainable params: 0

Benchmark Results

The benchmark model was trained and validated on the training data with a 15% validation split. The best parameters were chosen using grid search with 10 fold cross validation and determined by generalizability on the validation set.

- Sub-model 1: Decision Tree Regressor
 - max_depth: 10
 - max_features: 10
 - min_samples_leaf: 0.05
 - min_samples_split: 0.15
- Sub-model 2: SGD Regressor
 - learning_rate: optimal
 - max_iter: 7000
 - penalty: l2

- tol: 0.001
- Sub-model 3: Linear Regression
 - No parameters searched

Figures 8 and 9 show the R^2 and MAE results, respectively. We can see that that model is not overfit with relatively decent performance scores indicating that it is a suitable benchmark for the deep learning comparison.

Benchmark R–Squared 0.507 0.506 0.4 0.3 0.2 0.1 0.0 Train Validation

Figure 8: R-Squared results of the benchmark ensemble model

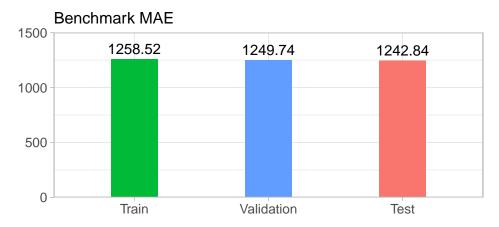


Figure 9: MAE results of the benchmark ensemble model

III. Methodology

Data Preprocessing

As mentioned earlier, categorical variables were one-hot encoded, the target variable was log-transformed, and a decision tree was used to select relevant predictors. To allow more time on the deep learning portion and prototyping a machine learning platform, I decided to forego any further improvements to the feature space as I found reasonable comparisons can be made with just these

few. Also, the data were anonymized so my ability to engineer better features was greatly limited. The only other pre-processing step was to shuffle the training data to remove bias from ordering.

Implementation

Technology Stack

This project was developed on a personal computer with the following specifications:

- Software (Open Source)
 - Ubuntu 18.04 Linux Distribution
 - Anaconda 4.5.10 with Python 3.6.5
 - numpy = 1.14.3
 - pandas = = 0.23.0
 - scikit-learn==0.19.1
 - scipy = = 1.1.0
 - tensorflow==1.10.0
 - Keras = 2.2.2
 - seaborn==0.8.1
 - matplotlib==2.2.2
- Hardware (\$1,100)
 - Processor: AMD Ryzen 3 4-Core 3.4GHz
 - Storage: 2TB Hybrid SSD+HD
 Memory: 16gb DDR4 RAM
 GPU: 2x GeForce GTX 1070

Machine Learning

Classes

In order to simulate/prototype a functional application, I created classes that wrap the benchmark ensemble learning and deep learning pipelines into self contained modules. All data, predictions, model objects and diagnostics are written to standard output directories. The user only needs to pass configurations to corresponding run scripts to invoke learning.

Methods

Each class contains 3 methods: [1] buildModel to run feature selection and train the model, [2] makePredictions to make predictions on canonical data, and [3] getDrivers to get feature rankings based on the feature selection algorithm. These classes also store all metrics of interest such as training scores, validation scores, and training run times as attributes.

The ensemble learner's buildModel method contains a pipeline for the algorithms. The user passes a parameter grid as a dictionary, fraction of data to partition for validation, and an argument for a feature selection cutoff threshold to control learning and model complexity.

With the deep learner, the user can define the network architecture as a function, a learning rate decay function, epochs, feature selection cutoff, batch size, number of epochs and the fraction of data to partition for validation. Early stopping of 10 epochs without improvement was applied.

Complications

The most challenging part of the implementation was combining grid search with scikit-learn's Pipeline API. Firstly, a helper class was needed to provide an estimator with a fit_transform() method for each sub-model so that these models can output predictions within a FeatureUnion. The sub-model predictions are then passed to a final ensemble algorithm to stack the sub-models in order

to create a single output. Being able to pass parameters to these nested methods is where the bulk of trial and error occured.

Docstrings were included with examples of how to configure each of these components.

Helper Functions

Three helper functions were created for preparing data for the learner classes. The first simply reads in data from a standard location and outputs Pandas dataframes. The next method shuffles, one-hot encodes and separates the input features from the label column. It also stores down an ordered list of the features. The final helper function reconciles new data to the same layout as the training data using that ordered list. If columns are missing from the new data, they get added in the correct position and filled in with zeroes.

Outputs

Important outputs include:

- 1. Pipeline model object as *.pkl (benchmark) or Keras best model checkpoint as *.hdf5 (deep learner).
- 2. Feature selection pipeline object as a *.pkl file.
- 3. Reports:
 - Feature importances and rankings spreadsheet
 - Training reports: training and validation scores, run times, best model parameters, helpful charts for diagnostics

Refinement

I started with building out the benchmark model first with fairly complex algorithms as my sub-models such as the Extra Trees Regressor. I found that the computational costs of running this would be a serious impediment to completing this project. So I decided to take the approach of treating this as a proof of concept and greatly simplify the algorithm space with simpler more efficient algorithms optimal for this data.

After finding a set of sub-models that trained reasonably fast, I next worked on fine-tuning the feature selection pipeline. I started going down the route of an ensembling technique for feature selection, which I also found to be far too computationally expensive and ended up with a single model (decision tree). I did leave the feature selector as a pipeline to work on this at a later point since I believe an ensemble approach could be powerful in providing better data for learning.

Once these two components were brought to a state to allow quicker development, the remaining effort was focused on building out the classes and methods to build out the prototype. I relied mostly on built-in methods provided by the Python libraries to simplify the task, continuously testing on a small sample of the Allstate data to ensure things worked correctly before iterating the actual model training on the full dataset.

With the deep learning model, I started with a single layer neural network as my test case. From here I started adding layers until I found a model that was able to beat the benchmark model and with limited overfitting.

Iterations Summary

Below is a summary outlining the iterations I made with the deep learning model.

Table 2: Deep learning model training iterations

Model_Changes	$Feature_Selection_Threshold$	Result
Single Layer Neural Network Add two hidden layers; Learning Rate Decay; Early Stopping Swap out ADAM for SGD optimizer Add 3 more layers; Dropouts; Increase Nodes Lowered batch size to 16	Mean Mean Mean Mean 0.5*Mean	Model learned nothing; R2 scores were near 0 and MAE was about 2500 Model predictions was just predicting the mean and not learning; Found issue to be adam optimizer but unclear as to why Model learning and predictions improved dramatically reaching R2 scores of around 0.40-0.45 Significant improvement in R2 and MAE; reaching 0.5 (R2) and about 1400 MAE Model was overtrained due to wider feature space
Increased batch size 100 Lowered batch size to 64 Lowered batch size to 32 Kept the network	1.5*Mean 0.75*Mean 1.25*Mean 1.05*Mean	Model performance dropped back down to the $0.4~(R2)$ range Model was overtrained but not as much as 0.5^* Mean in feature selection Model fit was back to around the $0.45~(R2)$ range Model performance increased to $0.55~(R2)$ range and wasn't too overfit

IV. Results

Model Evaluation and Validation

The final network architecture for the deep learning model is a Multi-Layer Perceptron with 5 hidden layers. It's architecture is outlined earlier in the *Algorithms and Techniques* section. I built up from a simple single layer model until I found an architecture and parameters that were able to beat the benchmark.

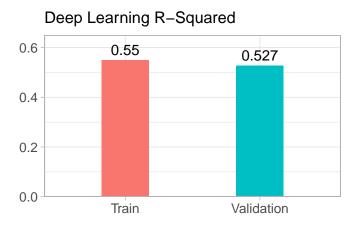


Figure 10: R-Squared results of the deep learning model

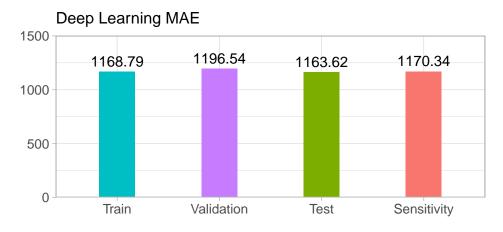


Figure 11: MAE results of the deep learning model

Figure 10 shows that I was able to achieve better fitted models than our benchmark in both training and validation. It is important to note that the computation and complexity in implementing the benchmark model was far greater than the deep learning solution, which I found interesting.

Figure 11 shows how the deep learning model performed in terms of MAE. Again, it did much better than the benchmark across the board. The Test MAE was extracted from Kaggle (as labels are hidden in the test data provided). Although, this simple model was not able to beat the median score of 1,125, it still performs reasonably well given the simplicity of the network. I also did a sensitivity test on the model's robustness against noise by converting one of the strongest predictors (cont14) to random noise. Although the error increased in the test data, it is still reasonably close to the training MAE.

GPU vs CPU

In the final comparison, I looked at metrics for understanding the costs both financially and computationally for a deep learning solution.

- Cost per R² gained over benchmark
 - 2 Nvidia GeForce GTX 1070's cost about in \$800 market value
 - Assuming that the only investment is GPU's, and with about a 2.1 point increase in validation R², the cost equates to approximately \$380.95 per point increase in R²
- Training and scoring times
 - Training
 - * CPU: 1,434.7 seconds (total) | \sim 42 seconds (per epoch)
 - * GPU: 548.9 seconds (total) | ~20 seconds (per epoch)
 - Scoring New Data (time includes feature selection transformation and writing results on 125k records)
 - * CPU: 8.5 seconds
 - * GPU: 4.7 seconds
- Storage costs of each model
 - Benchmark: 16KB
 - Deep Learning: 6,700KB

Justification

As showcased above, the deep learning solution performed significantly better than the benchmark in both R^2 and MAE. The benchmark itself is a fairly decent model that generalizes well making it a good comparison. The deep learning model also outperformed the benchmark in train, validation, and test iterations by a significant amount. I believe that this clearly demonstrates that deep learning can be a viable solution for building competitive models for predicting financial risk.

Recall the SOA comparison of healthcare models in Figure 1. In terms of performance across solution offerings, it is common to see R^2 values be really close. Vendors are fighting over small improvements over each other. At face value, a 2.1 point improvement in validation R^2 for the deep learning solution may not seem like much. However, given this context, we can imagine that even a marginal improvement in accuracy can be a highly valuable result. According to a 2015 study by the US Department of Transportation⁶, automobile accidents cost about \$241 billion in the US in 2010. When putting dollars like that into perspective, the opportunities provided by even a seemingly marginal increase can lead to significant outcomes for both insurers and consumers alike.

Lastly, a \$400 per R² investment for a fully production grade system in-house consisting of hundreds of GPU's is high. Factoring in the other costs like time and systemic infrastructure improvements required, then it stands to reason large organizations may be hesitant to invest in a solution with no

guarantee. However, these technologies are becoming more affordable and better. The market is seeing more competition with Google's TPU and AMD making strides in deep learning. It is only a matter of time before the question is no longer whether it is worth investing in.

To summarize, deep learning is certainly a viable solution for financial risk prediction in insurance. As of now, such incremental gains in performance is still difficult to justify investing in the labor and infrastructure required for an optimal system. However, as with all other technologies, the marketplace will soon offer affordable and better solutions to help make deep learning a norm in this industry.

V. Conclusion

Free-Form Visualization

Here I want to highlight that the deep learning networks converge very quickly. I believe this could be due to either the network architecture itself or perhaps the learning rate was too aggressive. Regardless, this is an area I am continuing to research as I further develop my expertise in this problem.

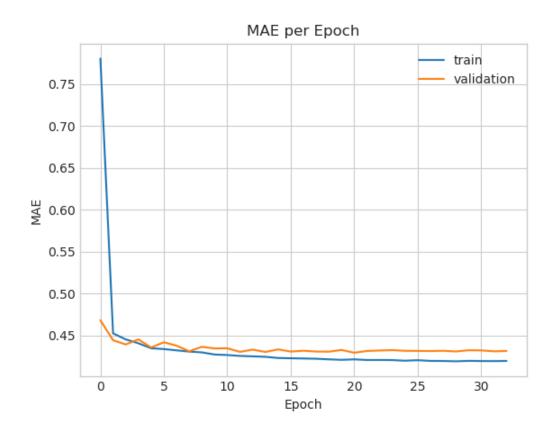


Figure 12: MAE per epoch for CPU run

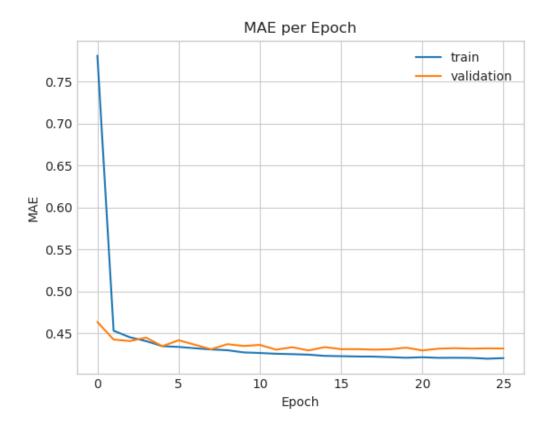


Figure 13: MAE per epoch for GPU run

Reflection

This project can be summarize in the following steps:

- 1. The problem domain was researched for a better understanding of what I can solve with this data.
- 2. The data were downloaded and explored in R (my preferred ad-hoc analysis tool) with relevant visualizations created.
- 3. Determined the approach to take. I decided to build learner classes and a prototype over an interactive approach via notebooks to have a reusable tool.
- 4. Build benchmark learner and train many iterations until a reasonable set of hyperparameters was found.
- 5. Build a deep neural network learner and try different networks until I beat the benchmark model without overfitting.
- 6. Run the same model through GPUs for performance comparisons.
- 7. Send all predictions to Kaggle for one true test evaluation.

The most difficult part was building working learner classes for this exercise for a problem that is relatively complex. I had to make several concessions along the way to build a simpler solution. One of my main reasons for going with this Kaggle competition was that the data were already cleaned and anonymized so I could focus less on the time consuming part of data preparation and focus more

on the machine learning aspects. There is still quite a bit of work needed to make my classes more generalizable to new problem sets, but I believe the core functionality is laid out.

Improvement

In order to have a more generalizable solution, I plan to look at the following in the near-term:

- 1. Decouple the prediction functionality from the model learner classes to have a more modular solution.
- 2. Implement methods optimized for GPU processing of neural networks (e.g. multi_gpu_model() in Keras)
- 3. Currently, the classes are only tested on regression problems. I plan to create classifiers as well.
- 4. To build a production grade system, there is a balancing act between how much flexibility to give the user and how automated the tool needs to be to iterate quickly. I think one test case is certainly not enough to find this balance. More problems to solve will help find it.
- 5. Test various network architectures like RNN's to see if they work.
- 6. Minor improvements to pathing and file naming.

Sources

Supplemental Information

All code and additional documentation and visualizations can be retrieved from my github repository. git clone $https://github.com/eugenekwak/Allstate_DL.git$

¹ https://www.soa.org/research-reports/2016/2016-accuracy-claims-based-risk-scoring-models/

² https://www.kaggle.com/c/allstate-claims-severity

³ https://www.equifax.com/business/insight-score-insurance/

⁴ https://www.verscend.com/solutions/performance-analytics/dxcg-intelligence

⁵ Exploratory Data Analysis guided by Kaggle Kernel submissions (https://www.kaggle.com/c/allstate-claims-severity/kernels)

 $^{^6~\}rm https://crashstats.nhtsa.dot.gov/Api/Public/ViewPublication/812013$