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Lightspeed, Groupvelocity max.:

$$
\begin{aligned}
c &= \frac{|\mathcal{E}|}{|\mathcal{B}|} = \frac{1}{\sqrt{\epsilon_0 \mu_0}} \left[\frac{F_\mathcal{B}}{F_\mathcal{E}} \right] = \frac{1}{\sqrt{\epsilon_0 \mu_0}} = \frac{\eta}{\sqrt{\varepsilon \mu}} = \frac{\eta}{\sqrt{\varepsilon_0 \varepsilon_r \mu_0 \mu_r}} = \\
\eta \cdot c_{ph} &= \sqrt{v_{phase} \cdot v_{matter}} = \\
\frac{\omega}{k} &= \frac{\lambda}{\mathcal{T}} = \nu\lambda = -\frac{d\lambda}{d\nu}\nu^2 = \lambda^2 \frac{\mathcal{J}_\lambda}{\mathcal{J}_\nu} = \frac{\langle|\mathcal{S}|\rangle}{\langle \mathrm{w}_{EM}\rangle} = v_{gr}^{max} \\
&\leq v_{ph} - \lambda\frac{d}{d\lambda}v_{ph} = \frac{d}{dk}\omega = v_{gr}
\end{aligned}
\tag{1}
$$

where:

$F_\mathcal{E} = q\mathcal{E} \equiv$ Coulomb-Force (Electric, charge presence, localization in space)

$F_\mathcal{B} = q(v \times \mathcal{B}) \equiv$ Lorentz-Force (Magnetic, charge movement, localization in time)

$\left[\frac{F_\mathcal{B}}{F_\mathcal{E}} \right] = 1$

$\mathcal{J} \equiv$ Flux Density

$\mathcal{S} \equiv$ Poynting-Vector, Intensity

$\mathrm{w}_{EM} \equiv$ Energy Density ElectroMagnetic

$\eta \equiv$ Refraction Index: Refraction for identifying matter (property of matter):

$$
\begin{aligned}
\eta &\stackrel{opt.}{=} \frac{sin(\alpha)}{\sin(\beta)} = \frac{\eta_\beta}{\eta_\alpha} \stackrel{prism}{=} \frac{\sin[\frac{1}{2}(\varpi + \varsigma_{min})]}{\sin[\frac{1}{2}\varpi]} \\
&\stackrel{phys.}{=} \sqrt{\epsilon_r \mu_r} = \frac{\lambda_\alpha}{\lambda_\beta} = \frac{v_{ph,\alpha}}{v_{ph,\beta}} = \frac{1}{2}\frac{\lambda}{d_r}\frac{n}{\cos(\beta)} = \sqrt{\left(\frac{n}{2}\frac{\lambda}{d_r}\right)^2 + \sin(\alpha)^2} \\
&\stackrel{dispersion}{=} \eta(\lambda) = \eta(\omega) \stackrel{anisotropy}{=} \eta(r)
\end{aligned}
\tag{2}
$$

$$
\text{Vacuum} \iff \eta = 1 \quad f = FocalLength \qquad D = RefractivePower(Dioptri)
$$

$n \equiv$ order ("Quantum"):

$$
n = \frac{\nu}{c}\Delta s = \frac{\Delta\varphi}{2\pi} = 2\eta\frac{d_r}{\lambda}\sqrt{\eta^2 - \sin(\alpha)^2} = 2\eta\frac{d_r}{\lambda}\cos(\beta) = \frac{q}{e_0} \quad \in \mathbb{N}
\tag{3}
$$

1

$$v^2 = \left(\frac{\nu\lambda}{\eta}\right)^2 = \left(\frac{\omega}{k\eta}\right)^2$$

$$\left(\frac{\eta}{c}\right)^2 = \epsilon\mu \qquad \epsilon = \epsilon_0\epsilon_r \qquad \mu = \mu_0\mu_r$$

where:

$d_r = r_{x+1} - r_x :=$ distance in space $\alpha :=$ irradiaton angle, incoming radiation direction, from source/sender (Einstrahlungswinkel zur Normalen auf Grenzfläche des Mediums)

$\beta :=$ refraction angle for bented transmitted radiation A_t orientation in matter (Durchstrahlungsswinkel zur Normalen aus Grenzfläche ins Medium)
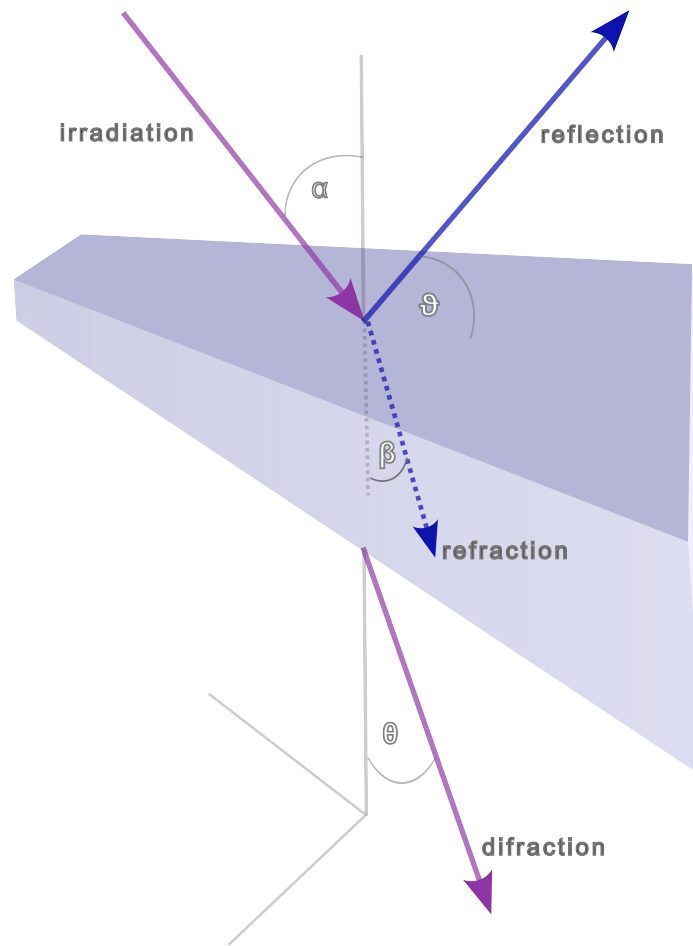
Orientation of Radiation:

Figure 1: Radiation

ϑ = reflection angle for redirected radiation $A_{r\parallel}$ parallel to α from matter [1]

θ = diffraction angle for redirected radiation $A_{r\perp}$ orthogonal to α from matter [2]

$\varpi = \beta_1 + \beta_2$ = angle of converging body surfaces (point tip of prismic medium), spread angle of prism

ς = deviation angle of redirected ray beam after refraction (transmission) and diffraction

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[1] Abstrahlwinkel zur Grenzfläche des Mediums

[2] Beugungswinkel durch Objekt ins Vakuum

3

u_g = aperture angle (acceptance) from sender source (at distance g)

w_b = inclination angle at observer receiver (at distance b)

ε = visual angle from observer/receiver (of eye)