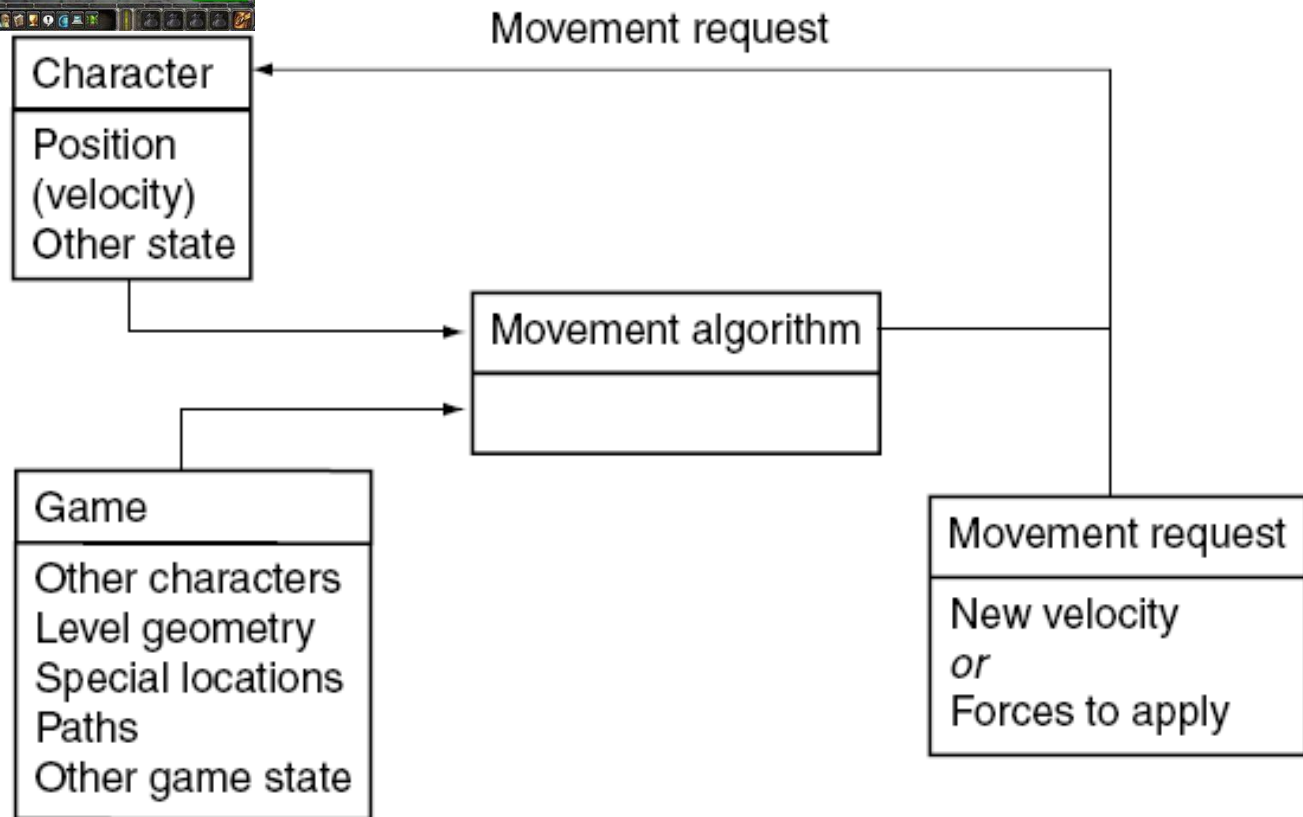


Movement: Basic Movement

Overall Movement Hierarchy



Overall Movement Hierarchy

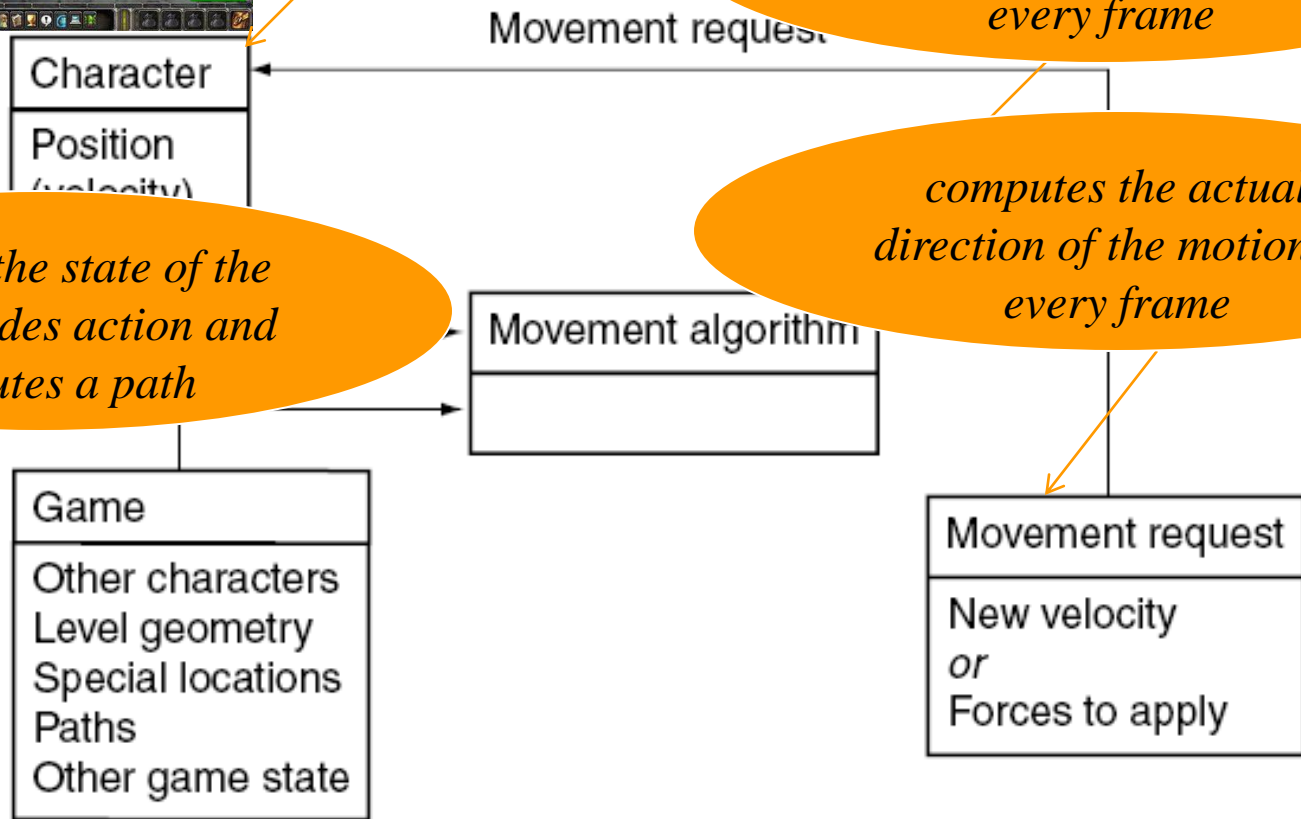


simulates the motion and updates the position/velocity of the character

computes the desired direction of the motion at every frame

computes the actual direction of the motion at every frame

based on the state of the game decides action and computes a path



from "Artificial Intelligence for Games" by I. Millington & J. y ge

Overall Movement Hierarchy

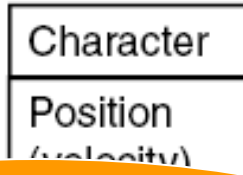


simulates the motion and updates the position/velocity of the character

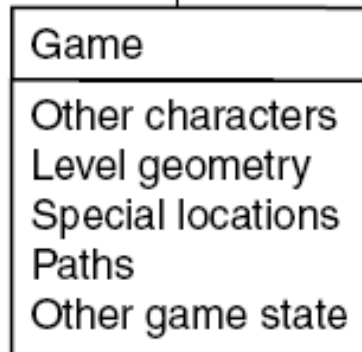
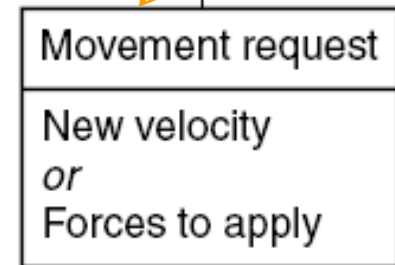
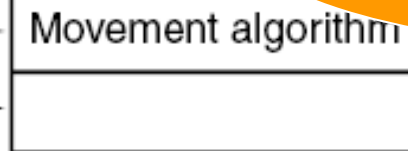
computes the desired direction of the motion at every frame

computes the actual direction of the motion at every frame

based on the state of the game decides action and computes a path

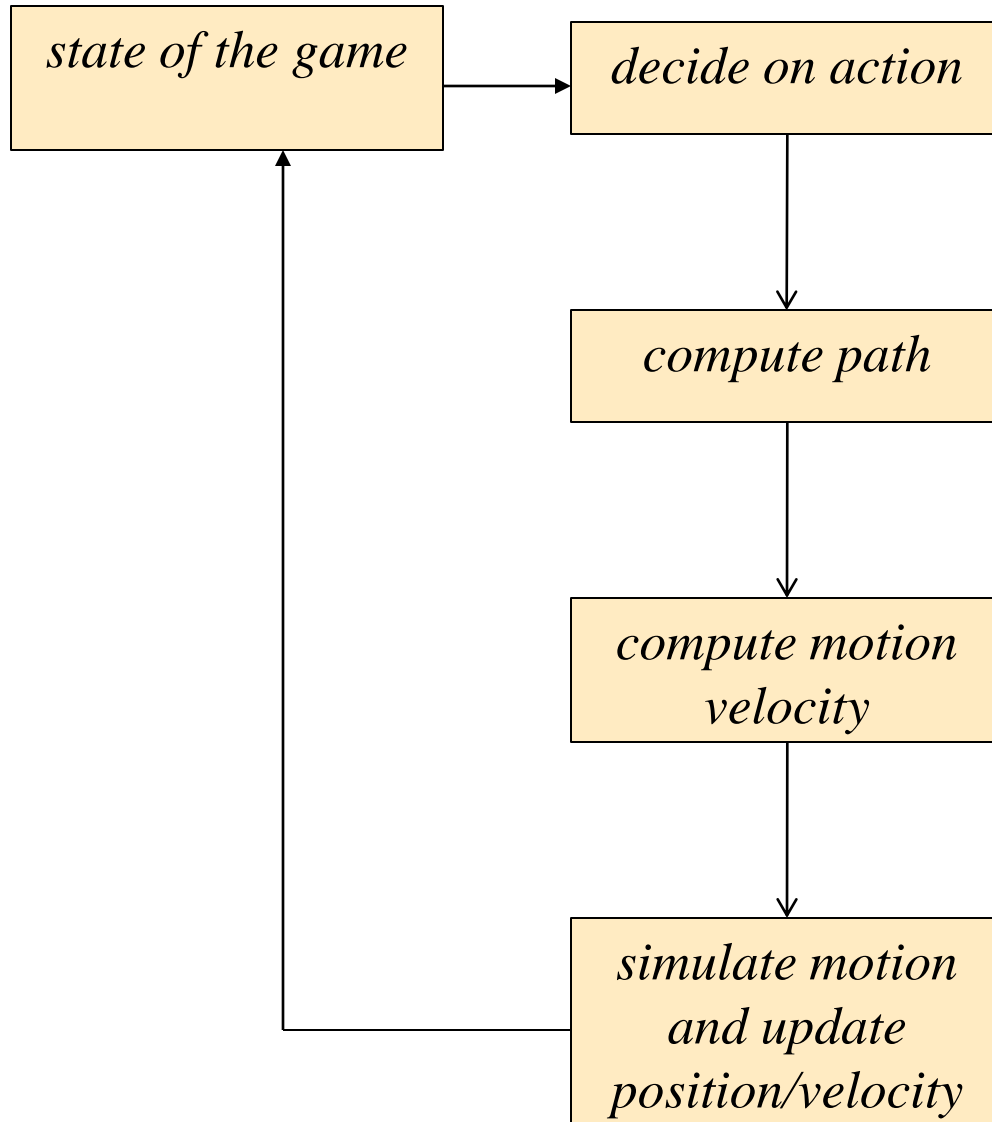


Movement request

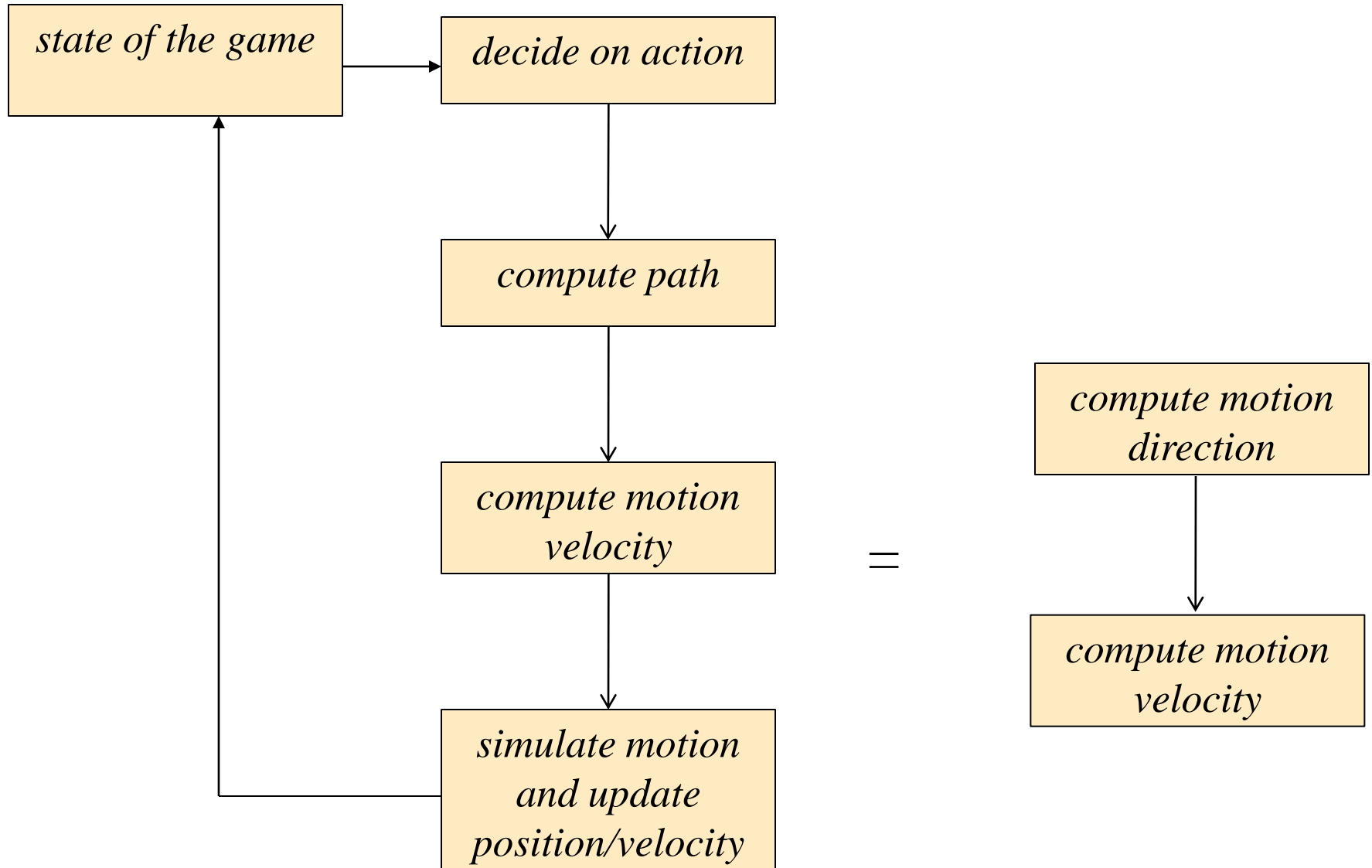


from "Artificial Intelligence for Games" by I. Millington & J. y ge

Overall Movement Hierarchy

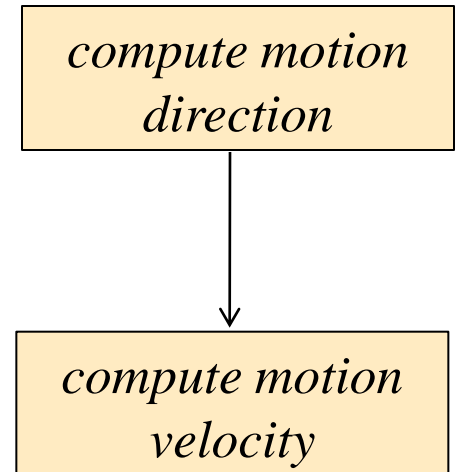
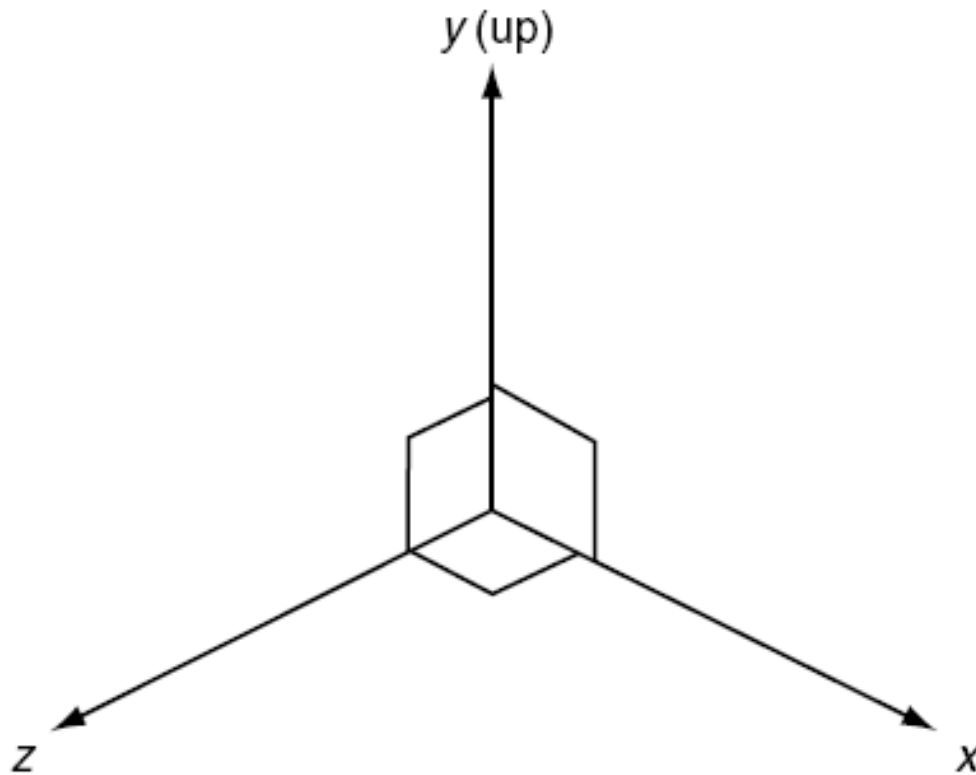


Overall Movement Hierarchy



Definition of the System

- Coordinate system for position $P=[x,z]$ or $P=[x,y,z]$

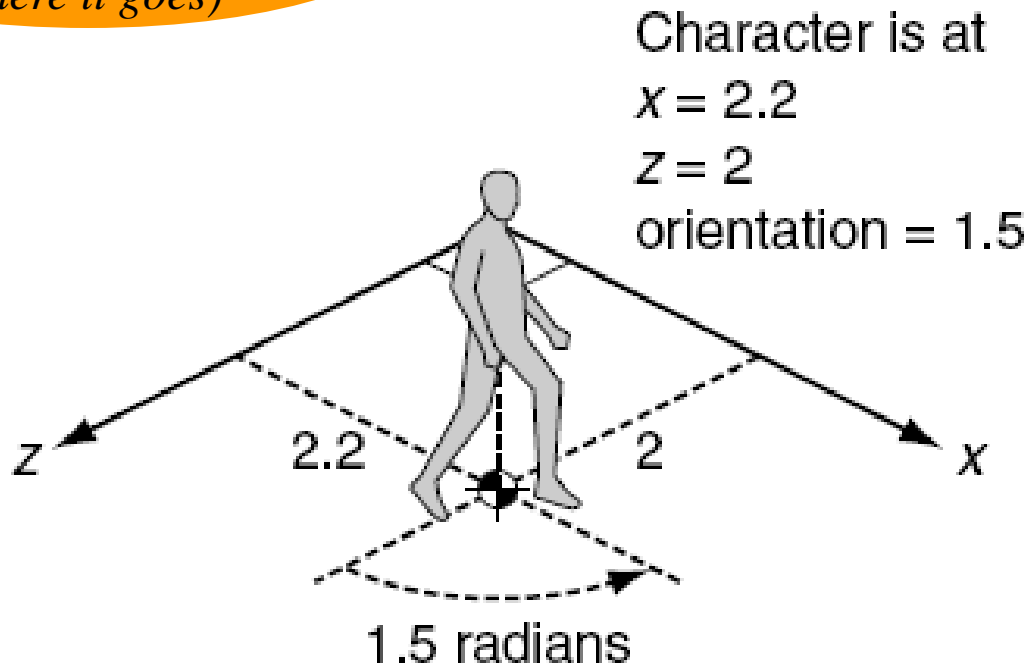


Definition of the System

- Coordinate system for orientation Ψ (*in rads*)

orientation is where it looks (not necessarily where it goes)

character is reduced to a point



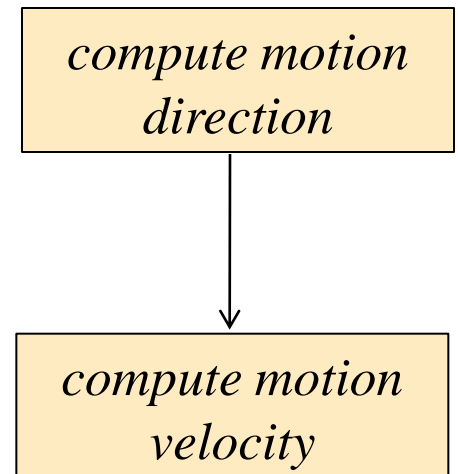
compute motion direction

compute motion velocity

Definition of the System

- Kinematic movement

State of system:
position $P = [x, z]$

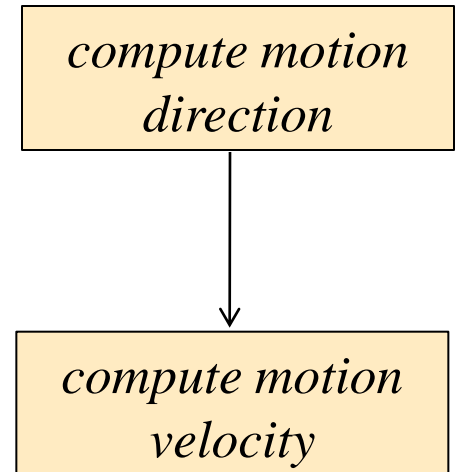


Definition of the System

- Kinematic movement

Output of system:

*velocity $V = [V_x, V_y] = [\text{magnitude } v, \text{direction } \theta]$,
orientation Ψ*



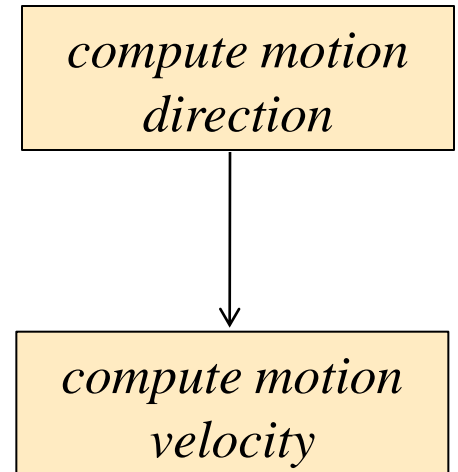
Definition of the System

- Kinematic movement

Output of system:

*velocity $V = [V_x, V_y] = [\text{magnitude } v, \text{direction } \theta]$,
orientation Ψ*

What Ψ should be set to?



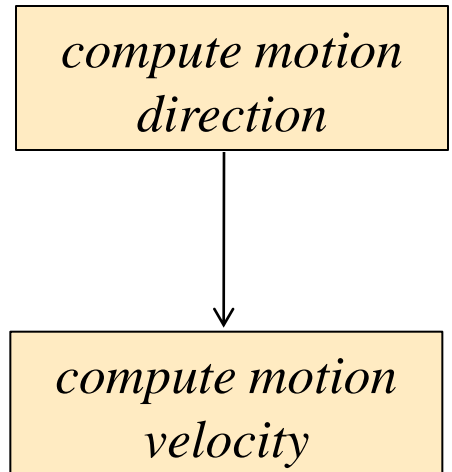
Definition of the System

- Kinematic movement

Output of system:

*velocity $V = [V_x, V_y] = [\text{magnitude } v, \text{direction } \theta]$,
orientation Ψ*

*Any problems with this
approach?*



Definition of the System

- Kinematic movement

Output of system:

*velocity $V = [V_x, V_y] = [\text{magnitude } v, \text{direction } \theta]$,
orientation Ψ*

Any solutions?

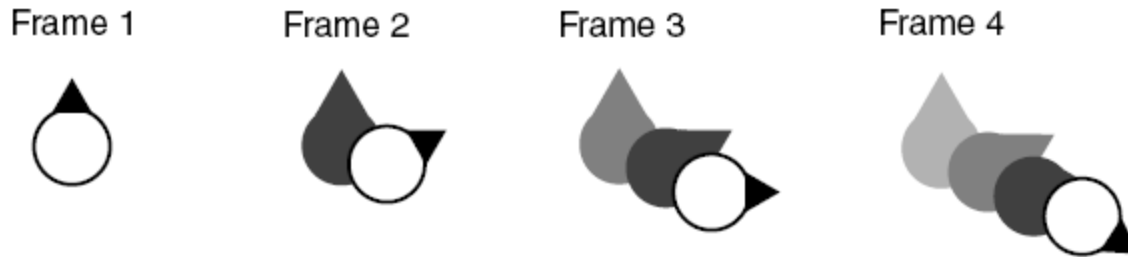
*compute motion
direction*



*compute motion
velocity*

Definition of the System

- Kinematic movement



from “Artificial Intelligence for Games” by I. Millington & J. nge

Output of system:

*velocity $V = [V_x, V_y] = [\text{magnitude } v, \text{direction } \theta]$,
orientation Ψ*

*instantaneous changes to
orientation & velocity can
be smoothed out here by
interpolation*

*compute motion
direction*



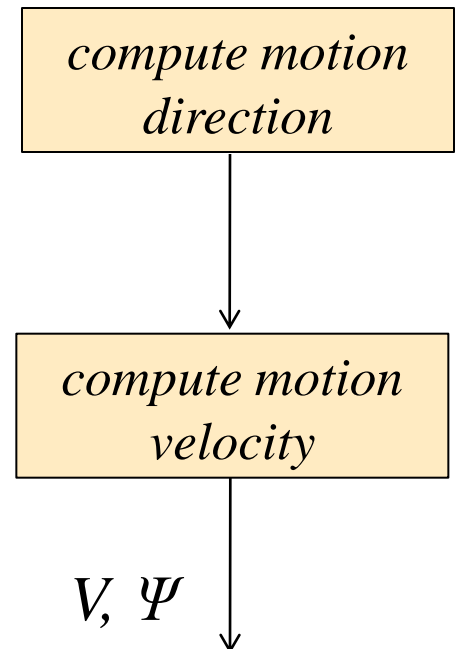
*compute motion
velocity*

Definition of the System

- Kinematic movement

Output of system:

*velocity $V = [V_x, V_y] = [\text{magnitude } v, \text{direction } \theta]$,
orientation Ψ*



Output of the overall system: V, Ψ

Definition of the System

- Dynamic movement

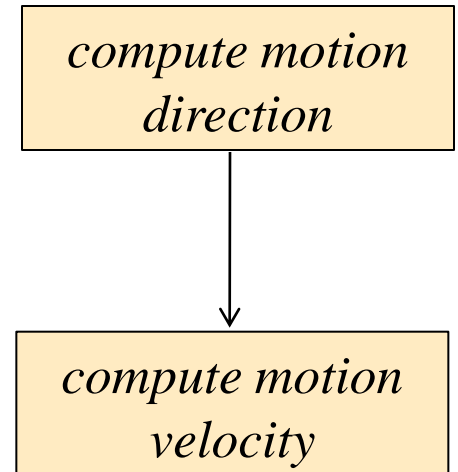
State of system:

position $P = [x, z]$,

velocity $V = [V_x, V_y] = [\text{magnitude } v, \text{direction } \theta]$,

orientation Ψ

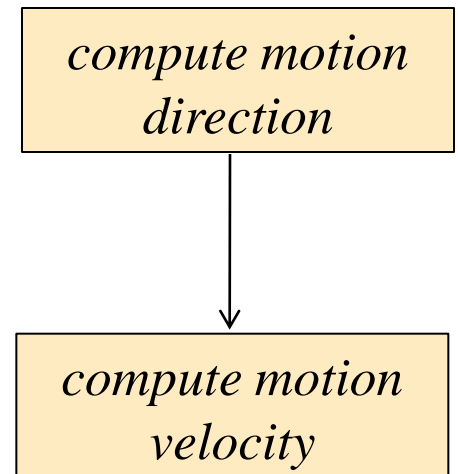
angular speed $d\Psi$



Definition of the System

- Dynamic movement

Output of system:
acceleration $A = [A_x, A_z]$,
angular acceleration $dd\Psi$



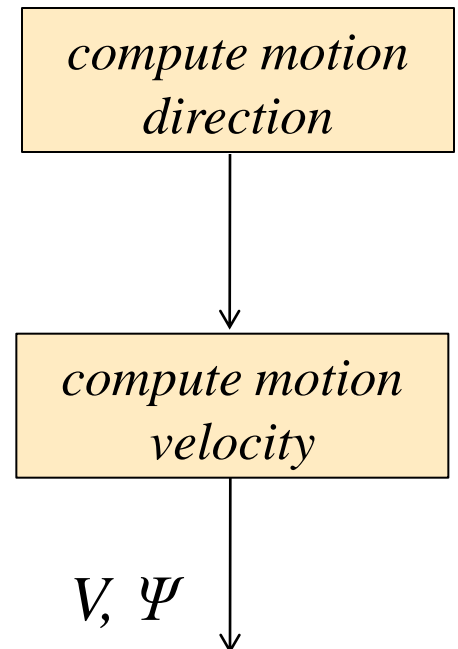
Definition of the System

- Dynamic movement

Output of system:
acceleration $A = [A_x, A_z]$,
angular acceleration $dd\Psi$

*Also limit V , $d\Psi$ to
their max values*

Output of the overall system: V, Ψ



Position Update According to Motion Equation

- Continuous formulation for constant acceleration:

$$a = \frac{dv}{dt}$$

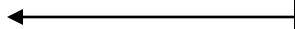
$$\int_0^t a dt = \int_0^t \frac{dv}{dt} dt$$

$$at = v(t) - v_0$$

$$v(t) = v_0 + at$$

*compute motion
velocity*

*simulate motion
and update
position/velocity*



$$v = \frac{dP}{dt}$$

$$\int_0^t v dt = \int_0^t \frac{dP}{dt} dt$$

$$\int_0^t (v_0 + at) dt = P(t) - P_0$$

$$v_0 t + \frac{1}{2} at^2 = P(t) - P_0$$

$$P(t) = P_0 + v_0 t + \frac{1}{2} at^2$$

Position Update According to Motion Equation

- Continuous formulation for constant acceleration:

$$a = \frac{dv}{dt}$$

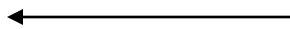
$$\int_0^t a dt = \int_0^t \frac{dv}{dt} dt$$

$$at = v(t) - v_0$$

$$v(t) = v_0 + at$$

*compute motion
velocity*

*simulate motion
and update
position/velocity*



$$v = \frac{dP}{dt}$$

*same derivation for
orientation Ψ and angular
speed $d\Psi$*

$$\int_0^t (v_0 + at) dt = P(t) - P_0$$

$$v_0 t + \frac{1}{2} at^2 = P(t) - P_0$$

$$P(t) = P_0 + v_0 t + \frac{1}{2} at^2$$

Position Update According to Motion Equation

- Discrete formulation:

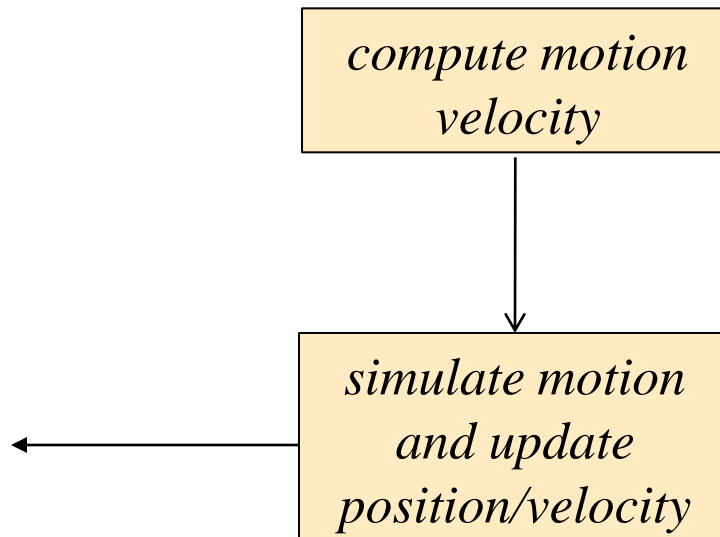
Units for Δt ?

$$V[t+1] = V[t] + A[t]\Delta t$$

$$P[t+1] = P[t] + V[t]\Delta t + 0.5A[t]\Delta t^2$$

$$d\Psi[t+1] = d\Psi[t] + dd\Psi[t]\Delta t$$

$$\Psi[t+1] = \Psi[t] + d\Psi[t]\Delta t + 0.5dd\Psi[t]\Delta t^2$$



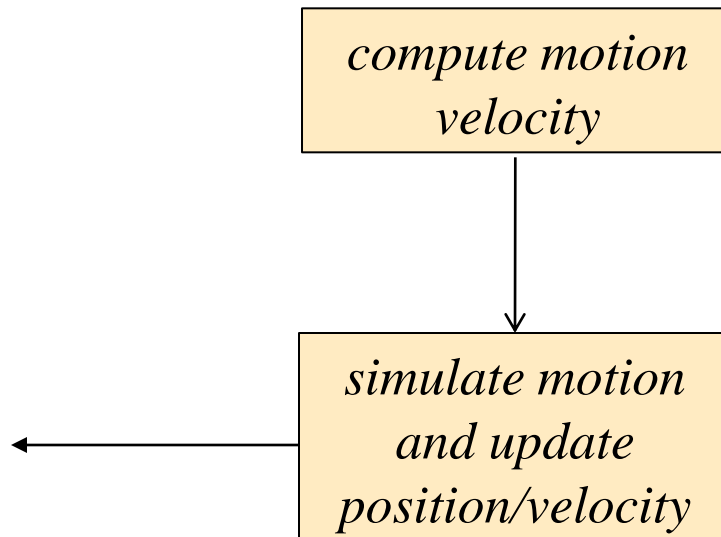
Position Update According to Motion Equation

- Discrete formulation simplified:

$$V[t+1] = V[t] + A[t]\Delta t$$
$$P[t+1] = P[t] + V[t]\Delta t$$

Why can we do it?

$$d\Psi[t+1] = d\Psi[t] + dd\Psi[t]\Delta t$$
$$\Psi[t+1] = \Psi[t] + d\Psi[t]\Delta t$$



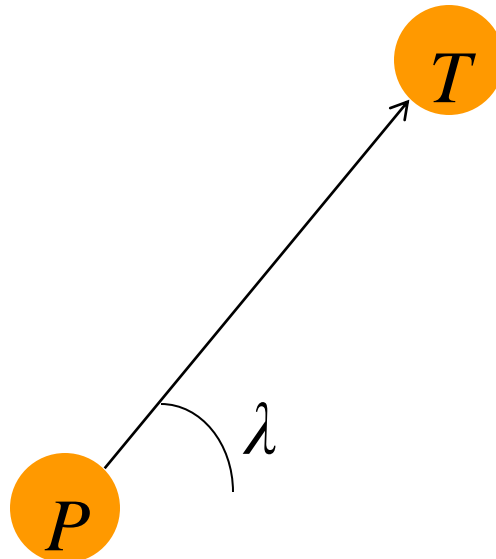
Kinematic Seek Behavior

- Move towards a target point T
 $V = [v, \theta] = [\text{max. speed}, \lambda]$
 $\Psi = \lambda$

*compute motion
direction*



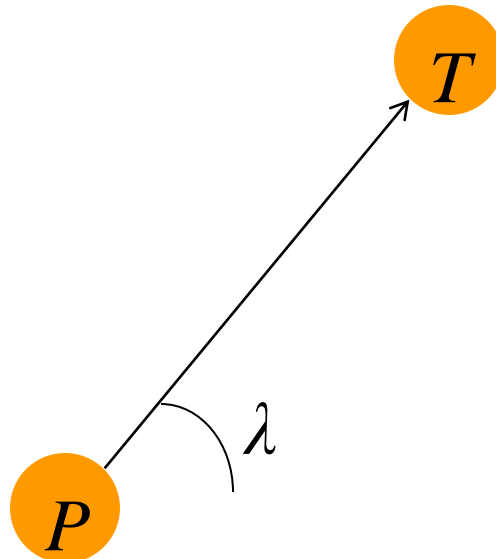
How do we do flee?



Kinematic Flee Behavior

- Move away from a target point T
 $V = [v, \theta] = [\text{max. speed}, \lambda + \pi]$
 $\Psi = \lambda + \pi$

*compute motion
direction*



Kinematic Seek Behavior

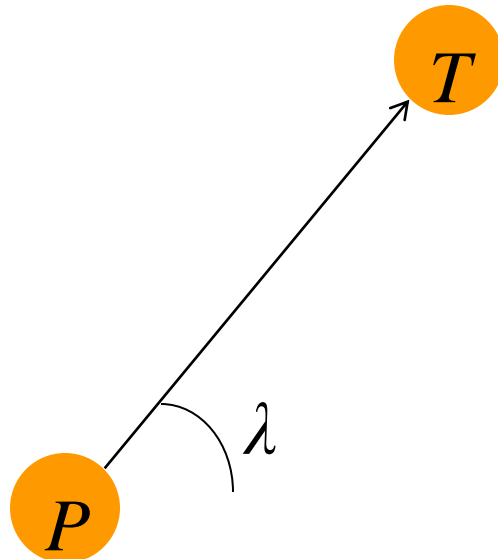
- Move towards a target point T
 $V = [v, \theta] = [\text{max. speed}, \lambda]$
 $\Psi = \lambda$

*compute motion
direction*



*Problems approaching a
moving target?*

Solutions?



Kinematic Arrival Behavior

- Approach a target point T

if $d < \text{arrival radius}$

$$V=[v, \theta]=[0, \lambda]$$

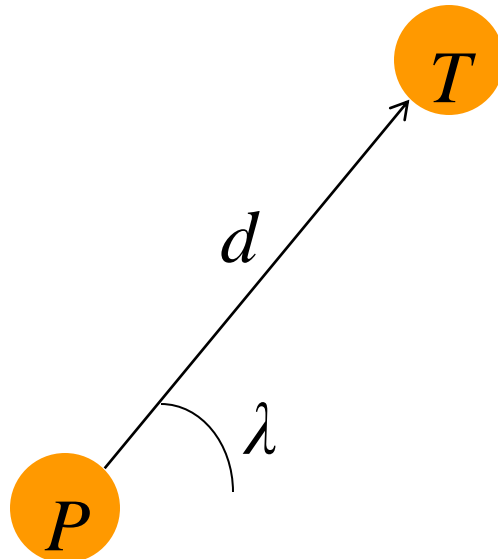
$$\Psi=\lambda$$

else

$$V=[v, \theta]=[K*d, \lambda] \text{ for some constant } K$$

$$\Psi=\lambda$$

*compute motion
direction*



Kinematic Wander Behavior

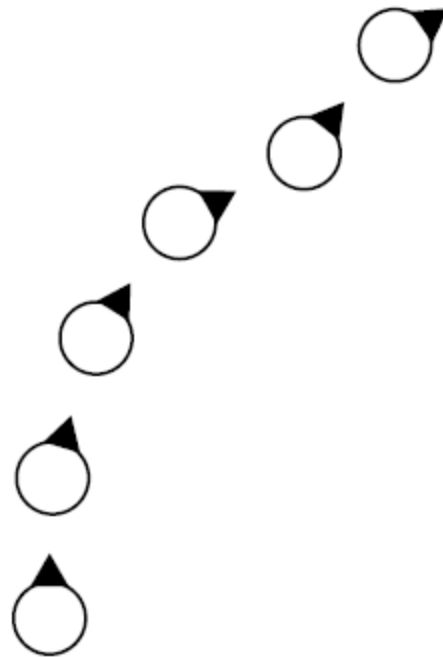
- Random wandering

$d\Psi = \text{random with bias towards } 0$

$\Psi = \Psi + d\Psi$

$V = [v, \theta] = [\text{max. speed}, \Psi]$

*compute motion
direction*



from “Artificial Intelligence for Games” by I. Millington & J. y ge

Dynamic Seek Behavior

- Move towards a target point T

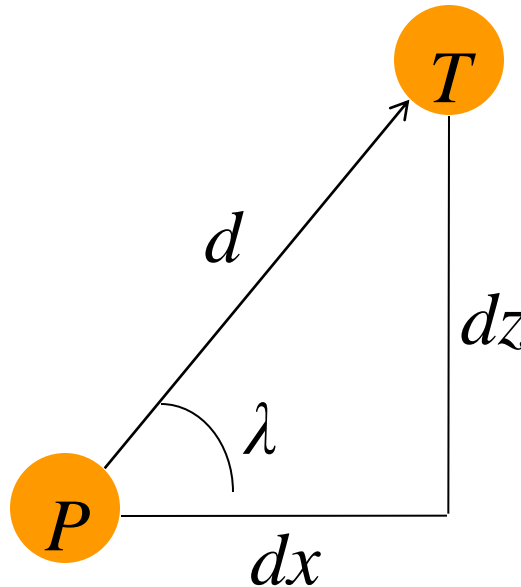
$$A = \text{max. accel} * \text{normalize}([dx, dz])$$

$$dd\Psi = K(\Psi - \lambda) \text{ limited by max. angular acceleration}$$

compute motion
direction



Take care for angle
wrapping



Dynamic Seek Behavior

- Move towards a target point T

$$A = \text{max. accel} * \text{normalize}([dx, dz])$$

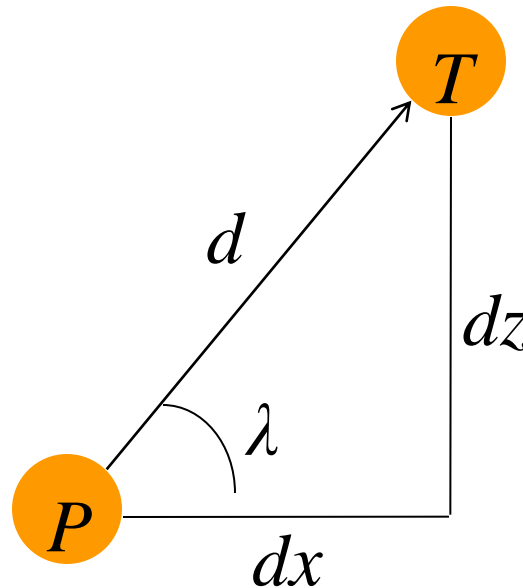
$$dd\Psi = K(\Psi - \lambda) \text{ limited by max. angular acceleration}$$

compute motion
direction



Take care for angle
wrapping

How do we do flee?



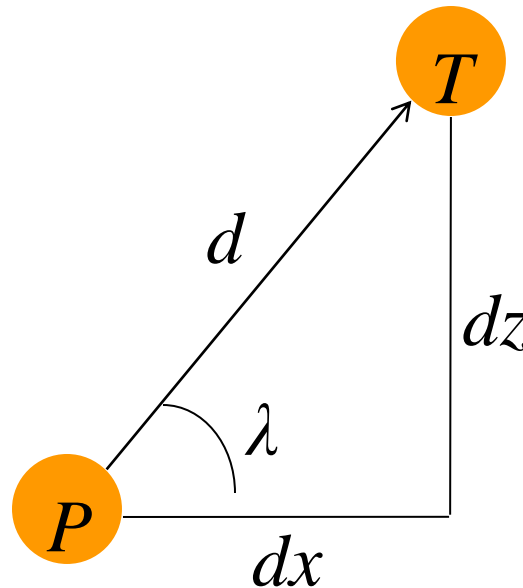
Dynamic Flee Behavior

- Move away from a target point T

$$A = -\text{max. accel} * \text{normalize}([dx, dz])$$

$$dd\Psi = K(\Psi - \lambda - \pi) \text{ limited by max. angular acceleration}$$

compute motion
direction



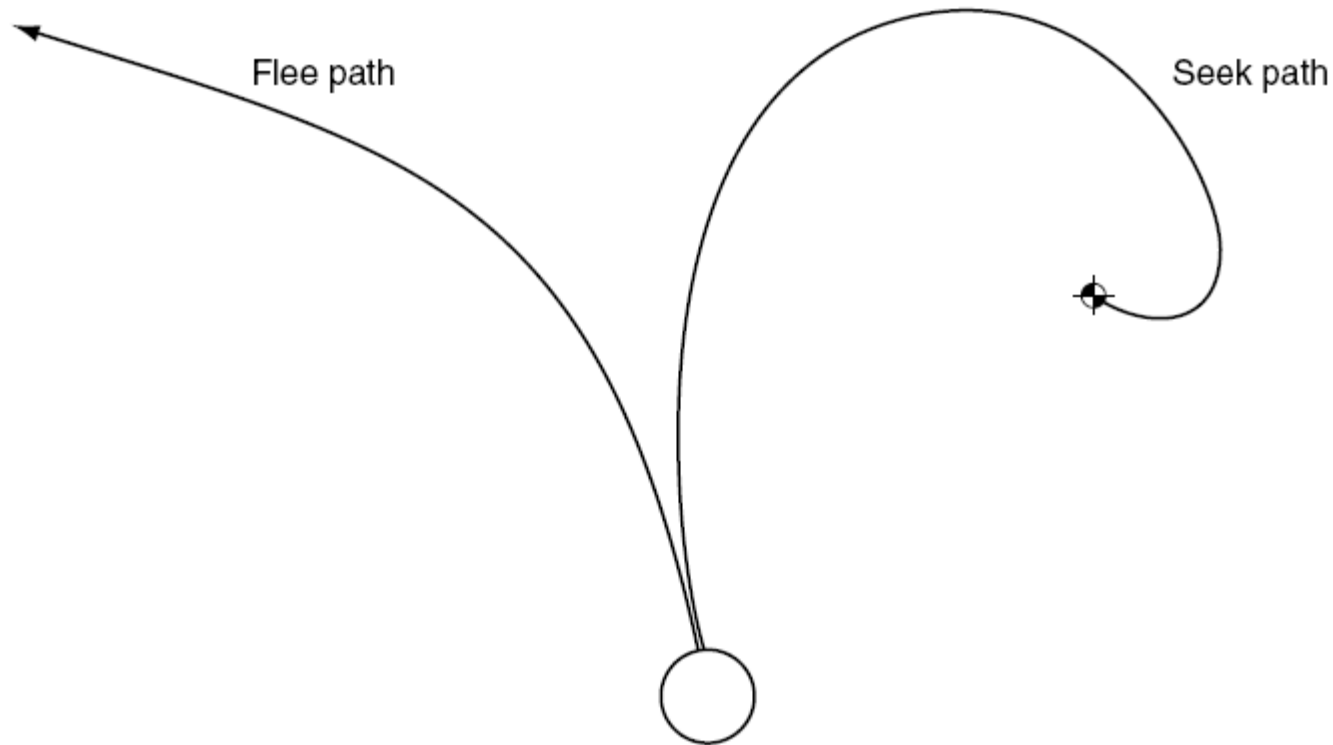
Dynamic Flee Behavior

- Move away from a target point T

$$A = -\text{max. accel} * \text{normalize}([dx, dz])$$

$$dd\Psi = K(\Psi - \lambda - \pi) \text{ limited by max. angular acceleration}$$

*compute motion
direction*



from "Artificial Intelligence for Games" by

I. Millington & J. y

ge

Dynamic Flee Behavior

- Move away from a target point T

$$A = -\text{max. accel} * \text{normalize}([dx, dz])$$

$$dd\Psi = K(\Psi - \lambda - \pi) \text{ limited by max. angular acceleration}$$

*compute motion
direction*



<http://www.red3d.com/cwr/steer/SeekFlee.html>

Dynamic Arrive Behavior

- Approach a target point T

if $d < \text{arrival radius}$ then $v_{des}=0$

*else $v_{des}=K*d$ for some constant K*

$A=K_1(v_{des}-v_{current})*\text{normalize}([dx,dz])$*

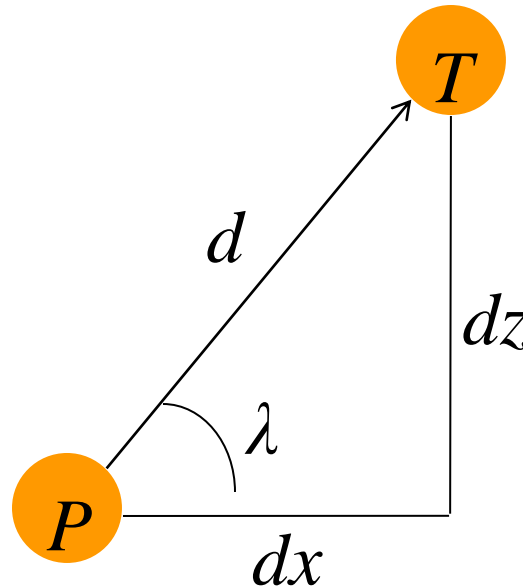
$dd\Psi=K(\Psi-\lambda-\pi)$ limited by max. angular acceleration

*compute motion
direction*



*K_1 can be set to $1/T$
(T is in secs)*

Meaning of T ?



Dynamic Arrive Behavior

- Approach a target point T

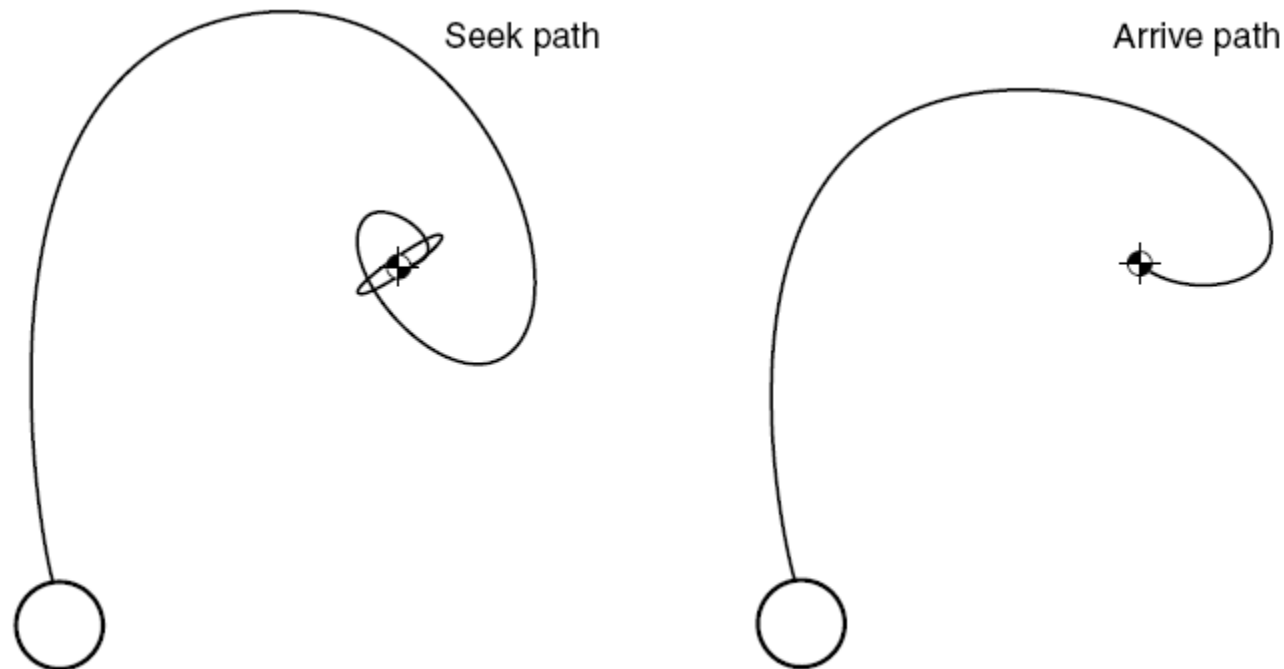
if $d < \text{arrival radius}$ then $v_{des}=0$

*else $v_{des}=K*d$ for some constant K*

$A=K_1(v_{des}-v_{current})*\text{normalize}([dx,dz])$*

$dd\Psi=K(\Psi-\lambda-\pi)$ limited by max. angular acceleration

*compute motion
direction*



from “Artificial Intelligence for Games” by I. Millington & J. y ge

Dynamic Arrive Behavior

- Approach a target point T

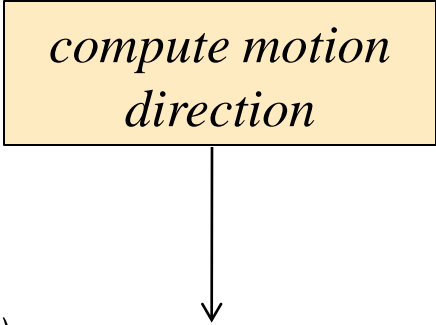
if $d < \text{arrival radius}$ then $v_{des}=0$

*else $v_{des}=K*d$ for some constant K*

$A=K_1(v_{des}-v_{current})*\text{normalize}([dx,dz])$*

$dd\Psi=K(\Psi-\lambda-\pi)$ limited by max. angular acceleration

*compute motion
direction*



<http://www.red3d.com/cwr/steer/Arrival.html>

Dynamic Arrive Behavior

- Approach a target point T

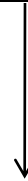
if $d < \text{arrival radius}$ then $v_{des}=0$

*else $v_{des}=K*d$ for some constant K*

$A=K_1(v_{des}-v_{current})*\text{normalize}([dx,dz])$*

$dd\Psi=K(\Psi-\lambda-\pi)$ limited by max. angular acceleration

compute motion
direction



How would you
implement
velocity matching
behavior?

Dynamic Pursue Behavior

- Pursue a moving target T that isn't close

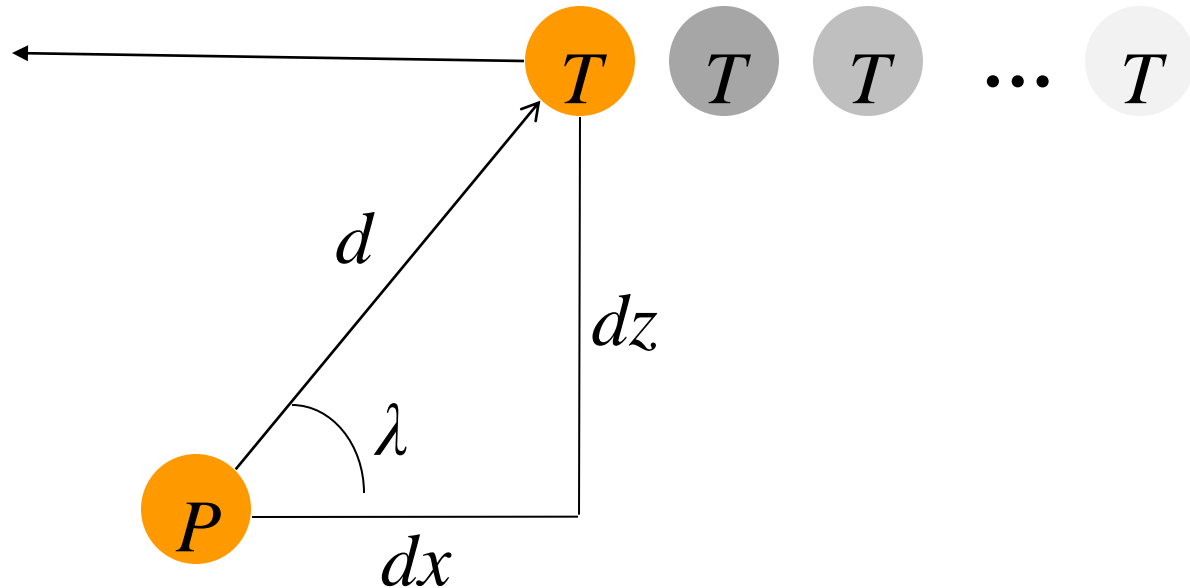
*compute motion
direction*



*Where will seek
direct the
character?*

*What's the
problem?*

Solutions?



Dynamic Pursue Behavior

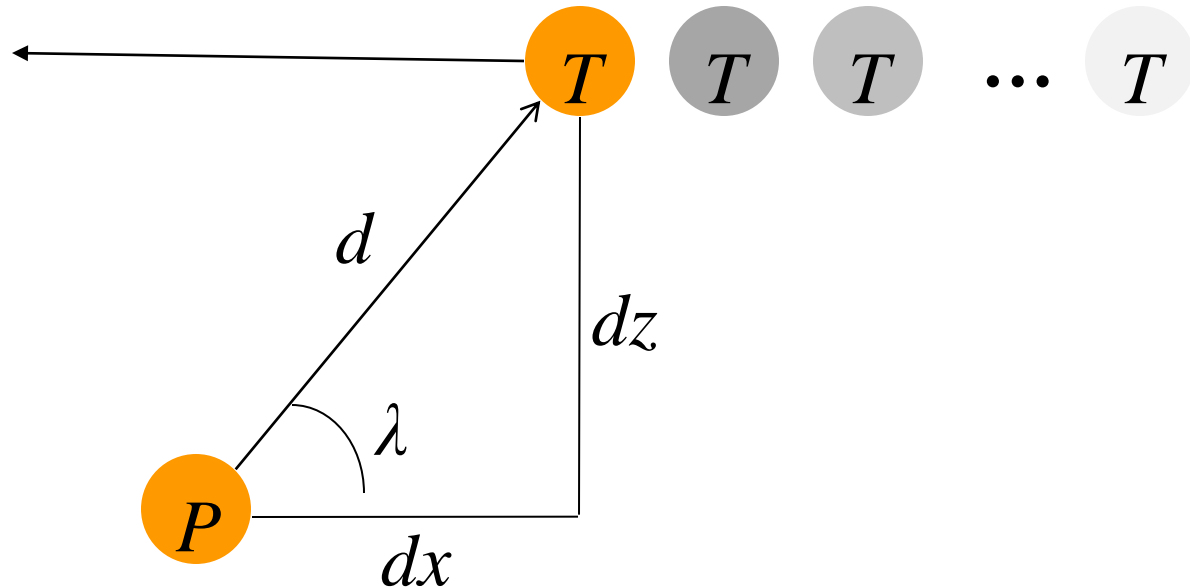
- Pursue a moving target T that isn't close
seek with target position at:

$$d/v_{current} * V_T$$

*compute motion
direction*



*Where will pursue
direct the
character?*

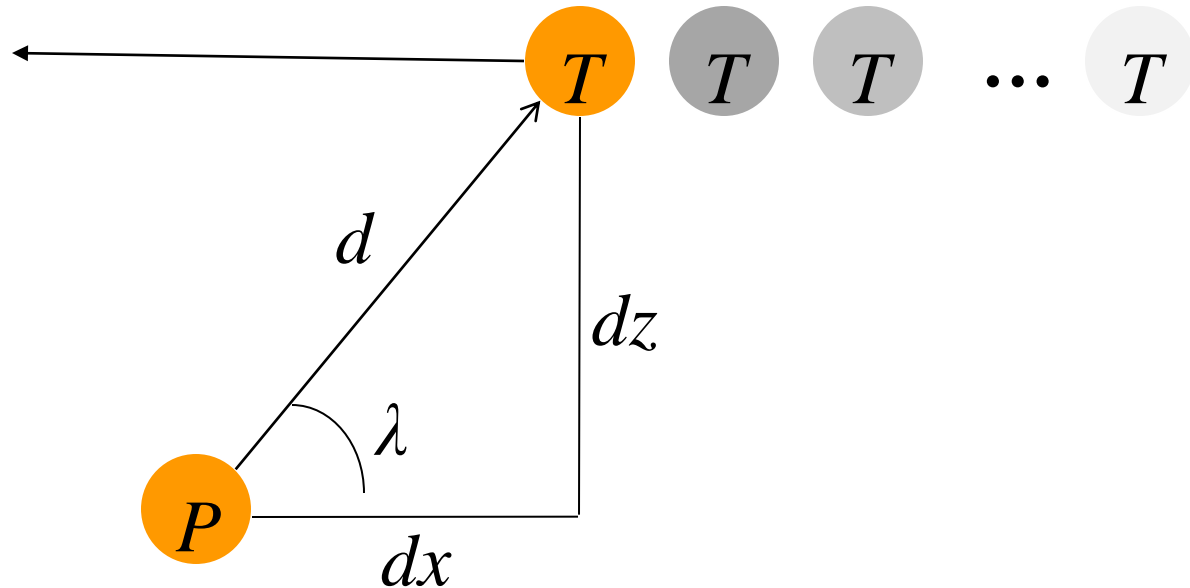


Dynamic Evade Behavior

- Evade a moving target T that isn't close
flee with target position at:

$$d/v_{current} * V_T$$

*compute motion
direction*

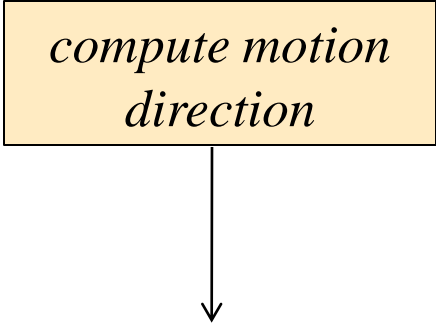


Dynamic Evade Behavior

- Evade a moving target T that isn't close
flee with target position at:

$$d/v_{current} * V_T$$

*compute motion
direction*



<http://www.red3d.com/cwr/steer/PursueEvade.html>