

*Learning I:*  
*Learning to Adjust, Learning to Predict*

# Purpose/benefits of Learning

- More believable (less predictable) characters
- Less work to program decisions for all the possible situations



# Purpose/benefits of Learning

- More believable (less predictable) characters

*Challenges using  
learning in games?*

*Lack of control over  
learnt behaviors*

- Less work to program decisions for all possible situations

*Overfitting*



# Types of Learning

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- Offline

- between levels of games

- at the game development studio before the game is released

*Most common approach*

*Allows to test the learnt behaviors*

- Online

- during the game itself



# Types of Learning

- Adaptation of the behavior parameters (intra-behavior learning)
  - learning to target precisely
  - learning the best patrol routes on the current level
  - learning good set of cover points for the given room
  - ...



# Types of Learning

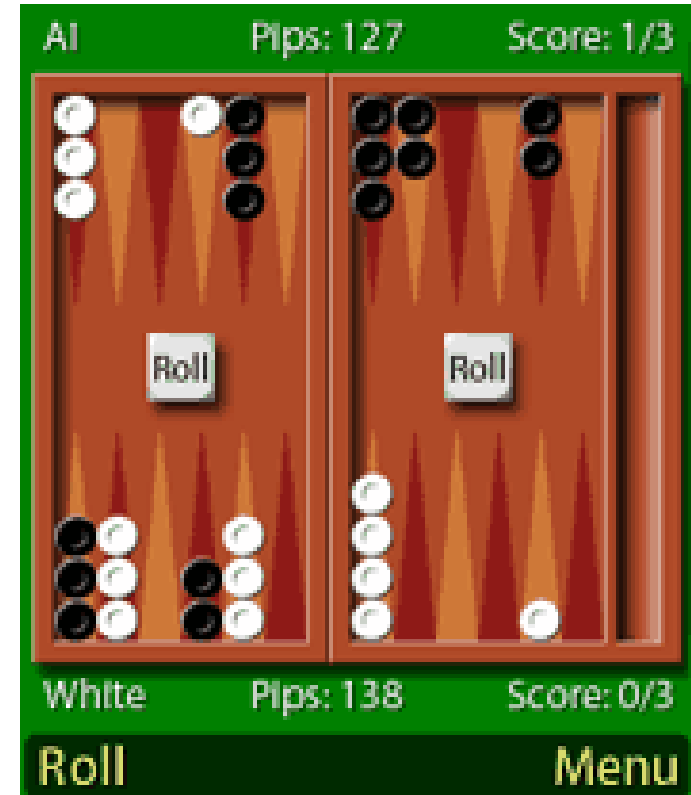
- Predicting the behavior of the enemy
  - predicting the next move in a fight based on the last few moves
  - predicting the attack based on the assembly of enemy troops
  - ...





# Types of Learning

- Reacting to the behavior of the enemy (inter-behavior learning)
  - making the most effective counter-move in a fight
  - making the most effective reallocation of the troops
  - making the best move in a board game based on all the pieces
  - ...



# Adaptation of the Parameters

- Hill Climbing

*The goal is to find the parameter vector that results in the most optimal value of the function:*

$$\Psi^* = \operatorname{argmax}_{\Psi} f(\Psi)$$

*Start with the best guess for the parameter vector  $\Psi$*

*Until no further improvement*

*try changing  $\Psi$  by small  $\Delta$  in all directions and pick the best:*

$$\Psi = \Psi + \operatorname{argmax}_{\Delta} f(\Psi + \Delta)$$



# Adaptation of the Parameters

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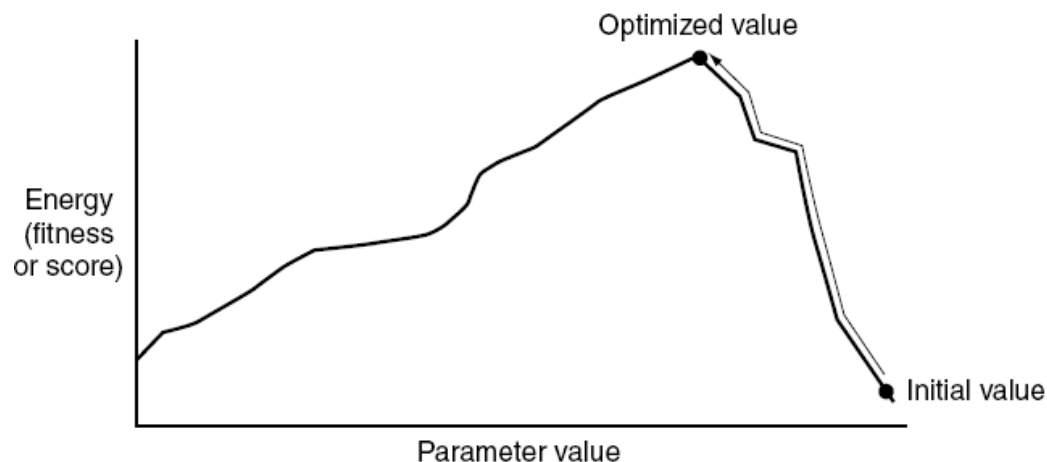
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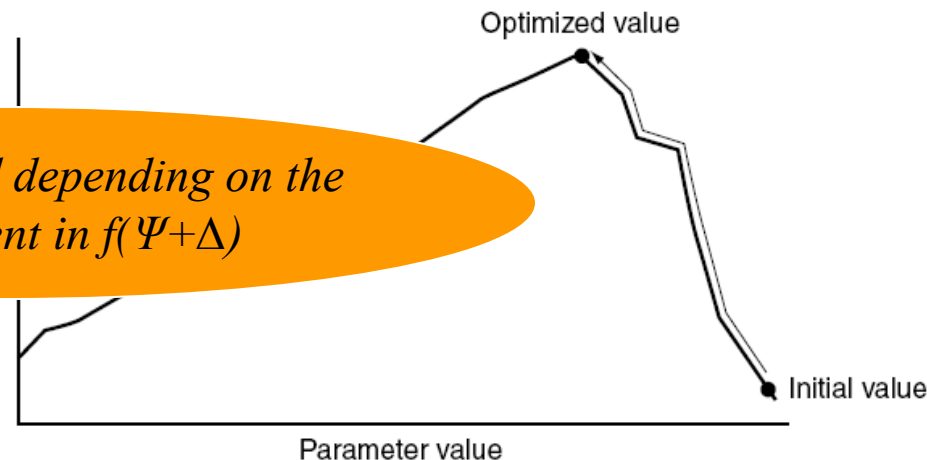
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*try changing  $\Psi$  by small  $\Delta$  in all directions and pick the best:*

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*$\Delta$  is often adapted depending on the rate of improvement in  $f(\Psi + \Delta)$*



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*Example:*

*finding the best shooting distance*

$\Psi = \text{distance (scalar variable)}$

$\Delta = +/-\text{distance increment}$

$f(\Psi) = \text{distance between enemy ship and where cannonball lands}$



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Equivalent formulation for differentiable functions (Steepest ascent):

*Start with the best guess for the parameter vector  $X$*

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$$X = X + \varepsilon f'(X)$$



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*try changing  $\Psi$  by small  $\Delta$  in all directions and pick the best:*

$$\Psi = \Psi + \operatorname{argmax}_{\Delta} f(\Psi + \Delta)$$

$$X = X + \operatorname{argmax}_{\Delta} f(X + \Delta) \quad \text{for small } |\Delta|,$$

$$X \approx X + \operatorname{argmax}_{\Delta} \{f(X) + f'(X)\Delta\}$$

$$X = X + \varepsilon f'(X) \quad \text{for small } \varepsilon > 0$$

Why?

Equivalent formulation for direction  $\Delta$  (gradient descent)  $\Delta = -\varepsilon f'(X)$ .

*Start with the best guess for the parameter vector  $X$*

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$$X = X + \varepsilon f'(X)$$

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Equivalent formulation for differentiable functions (Steepest ascent):

*Start with the best guess for the parameter vector  $X$*

*Until no further improvement*

$$X = X + \varepsilon \nabla f(X)$$

*For multi-dimensional vector  $X$ ,*

$$f'(X) \equiv \nabla f(X)$$

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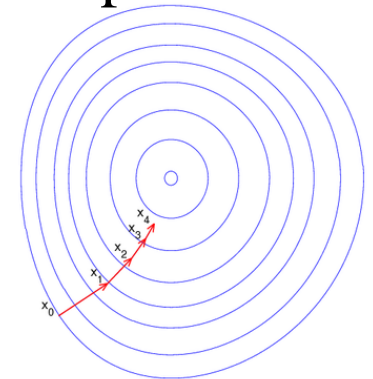
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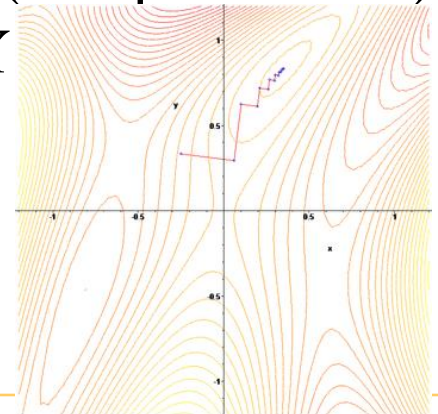
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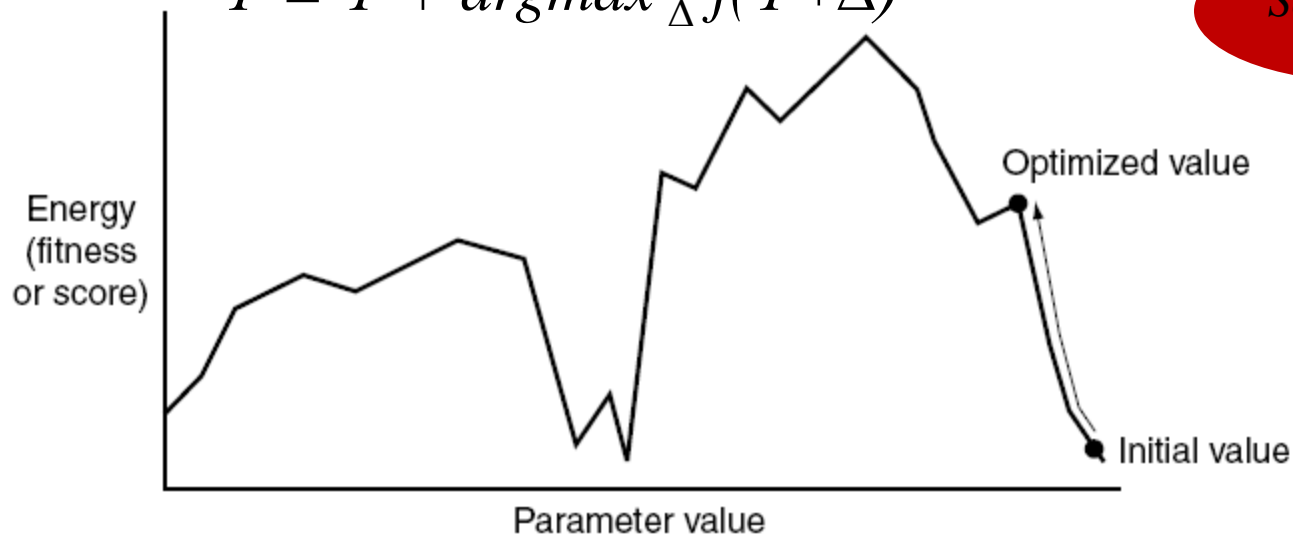
*Until no further improvement*

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*Typical problems?*

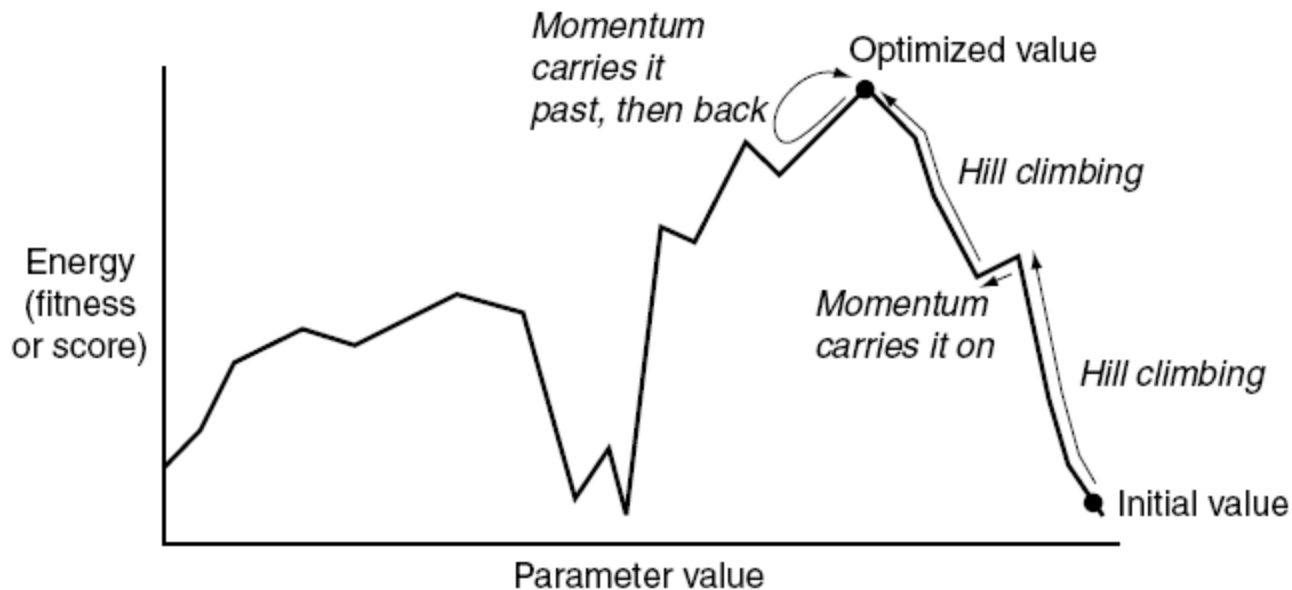
*Solutions?*



# Adaptation of the Parameters

- Extensions to Hill Climbing to overcome local minima problem
  - Momentum: persist in going in the same direction (*when picking the next  $\Delta$ , the previous direction  $\Delta$  gets an additional term proportional to the previous improvement*)

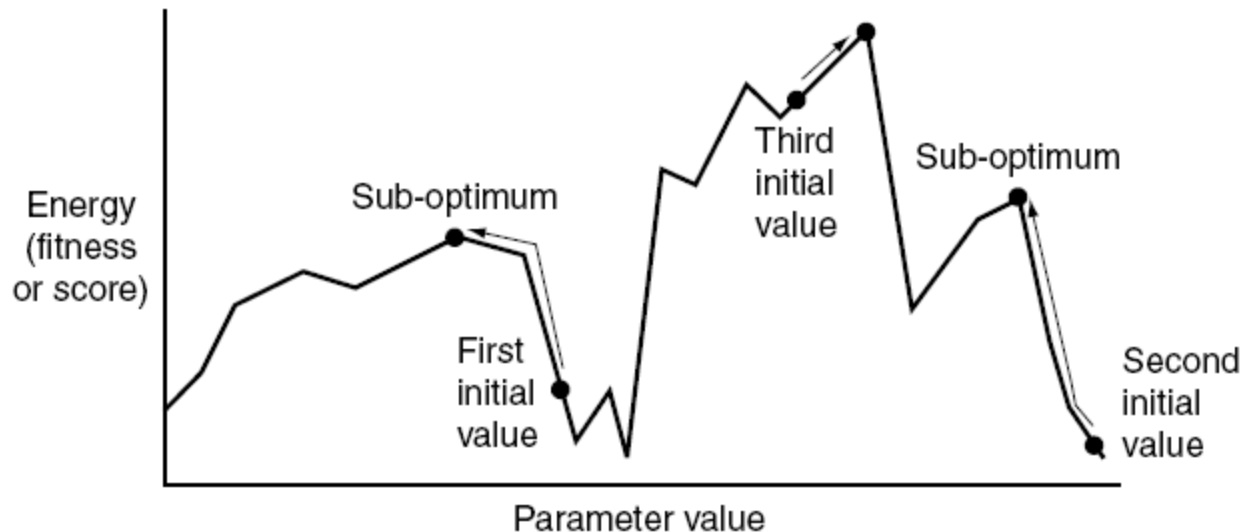
*Disadvantages?*



# Adaptation of the Parameters

- Extensions to Hill Climbing to overcome local minima problem
  - Multiple trials: try random initial locations

*Disadvantages, in particular in the context of games?*



# Adaptation of the Parameters

---

- Extensions to Hill Climbing to overcome local minima problem
  - Simulated Annealing: the selection of  $\Delta$  is done at random

*Start with the best guess for the parameter vector  $\Psi$*

*Until no further improvement*

*pick a random direction  $\Delta$*

*With probability  $P$ , set  $\Psi = \Psi + \Delta$ , where  $P$  is a function of the improvement  $(f(\Psi + \Delta) - f(\Psi))$  and temperature  $T$*



# Adaptation of the Parameters

- Extensions to Hill Climbing to overcome local minima problem
  - Simulated Annealing: the selection of  $\Delta$  is done at random

*Start with the best guess for the parameter vector  $\Psi$*

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*pick a random direction  $\Delta$*

*With probability  $P$ , set  $\Psi = \Psi + \Delta$ , where  $P$  is a function of the improvement ( $f(\Psi+\Delta)-f(\Psi)$ ) and temperature  $T$*

*$P$  is increasing as  $f(\Psi+\Delta)-f(\Psi)$  increases*

*$P$  is decreasing as  $T$  decreases*

*Temperature  $T$  is being decreased over time*

*Disadvantages?*

*As  $T$  gets closer to 0 ( $T$  “cools off”), the algorithm becomes greedy descent*

# Action Prediction

- Predict future action of the player based on past actions and anything else relevant

*Any ideas how to  
do it?*



# Action Prediction

- N-gram predictor
  - **Very** popular in all the combat (martial arts, boxing, swords, ...) games (e.g., predicting next move)
  - Often requires reduction in the power of AI to make it beatable
  - Extends to other predictions such as what weapons will be used or how the attacks will occur



# Action Prediction

- N-gram predictor
  - *Maintain the probabilities of future actions based on  $N-1$  preceding observations*
  - *For prediction, always return the most likely action based on last  $N-1$  observations*





# Action Prediction

- N-gram predictor
  - Maintain the probabilities of future actions based on  $N-1$  preceding observations
  - For prediction, always return the most likely action based on last  $N-1$  observations

*Example of applying 3-gram predictor:*

*training data (observed sequence of moves):* LRRLRLLLRLRLRR

*learnt prediction table:*

	<i>predicted actions</i>	
	..R	..L
LL	$\frac{1}{2}$	$\frac{1}{2}$
LR	$\frac{3}{5}$	$\frac{2}{5}$
RL	$\frac{3}{4}$	$\frac{1}{4}$
RR	$\frac{0}{2}$	$\frac{2}{2}$

*N-1 preceding observations* →

← *There were 5 LRs  
3 resulted in R  
2 resulted in L*

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*Mathematically, what are you learning?*

# Action Prediction

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*Mathematically, what are you learning?*

$P(A=L/LL),$   
 $P(A=L/LR),$

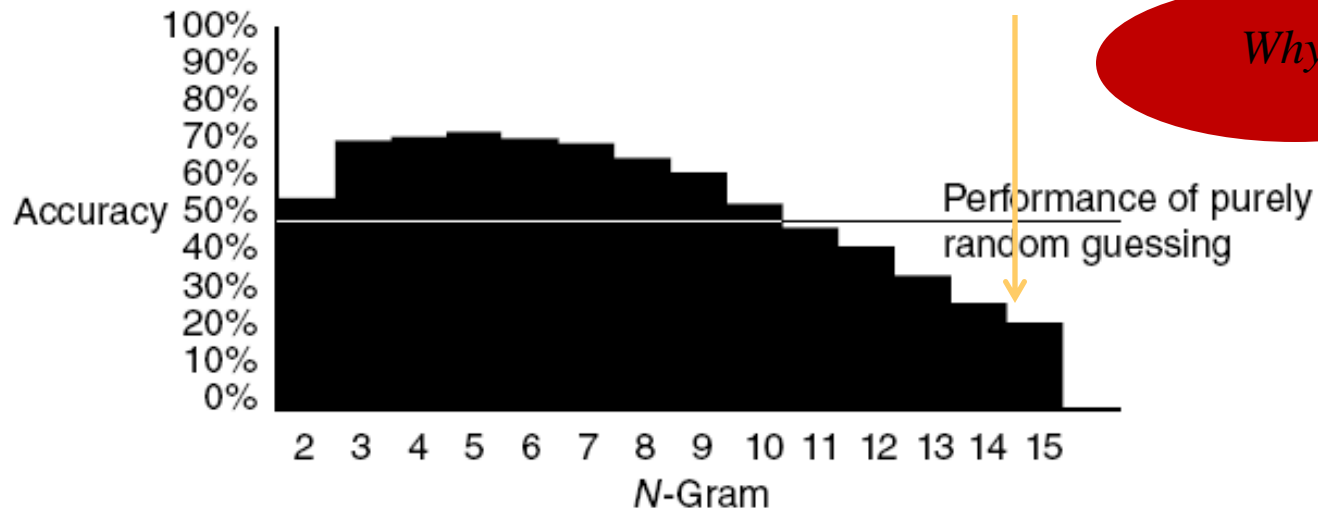
...

# Action Prediction

- N-gram predictor
  - *Maintain the probabilities of future actions based on  $N-1$  preceding observations*
  - *For prediction, always return the most likely action based on last  $N-1$  observations*

*Accuracy of prediction may reduce as  $N$  increases past some point*

*Why?*



# Action Prediction

- N-gram predictor
  - *Maintain the probabilities of future actions based on  $N-1$  preceding observations*
  - *For prediction, always return the most likely action based on last  $N-1$  observations*

*Game Performance in initial stages: what to do before the N-gram predictor is learnt?*





# Action Prediction

- Hierarchical N-gram predictor
  - *Learn 2-gram, 3-gram, ... predictors simultaneously*
  - *For prediction, pick N-gram predictor with largest N and sufficient number of training samples for the given input*

*Game Performance in initial stages: what to do before the N-gram predictor is learnt?*



# Action Prediction

---

- Hierarchical N-gram predictor
  - *Learn 1-gram, 2-gram, 3-gram, ... predictors simultaneously*
  - *For prediction, pick N-gram predictor with largest N and sufficient number of training samples for the given input*
  - *If none have sufficient samples, then output random prediction*

# Action Prediction

- Hierarchical N-gram predictor
  - *Learn 1-gram, 2-gram, 3-gram, ... predictors simultaneously*
  - *For prediction, pick N-gram predictor with largest N and sufficient number of training samples for the given input*
  - *If none have sufficient samples, then output random prediction*

*Example:*

*training data (observed sequence of moves):* LRRLRLLLRRRLRLRR

*1-gram:*

L	R	# of samples
7/15	8/15	15

*2-gram:*

Obs.	L	R	# of samples
L	2/7	5/7	7
R	4/7	3/7	7

*3-gram:*

Obs.	L	R	# of samples
LL	1/2	1/2	2
LR	2/5	3/5	5
RL	1/4	3/4	4
RR	1	0	2

# Action Prediction

- Hierarchical N-gram predictor
  - Learn 1-gram, 2-gram, 3-gram, ... predictors simultaneously
  - For prediction, pick N-gram predictor with at least N and sufficient number of training samples
  - If none have sufficient samples, pick the best 1-gram predictor

*Suppose we want to have at least 4 samples for prediction, what is the predicted next action for input=RRR?*

*Example:*

*training data (observed sequence of moves):* LRRLRLLLRRRLRLRR

*1-gram:*

L	R	# of samples
7/15	8/15	15

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Obs.	L	R	# of samples
LL	1/2	1/2	2
LR	2/5	3/5	5
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# Action Prediction

- Hierarchical N-gram predictor
  - Learn 1-gram, 2-gram, 3-gram, ... predictors simultaneously
  - For prediction, pick N-gram predictor with at least N and sufficient number of training samples
  - If none have sufficient samples, use 1-gram predictor

*Suppose we want to have at least 9 samples for prediction, what is the predicted next action for input=RRR?*

*Example:*

*training data (observed sequence of moves):* LRRLRLLLRRRLRLRR

*1-gram:*

L	R	# of samples
7/15	8/15	15

*2-gram:*

Obs.	L	R	# of samples
L	2/7	5/7	7
R	4/7	3/7	7

*3-gram:*

Obs.	L	R	# of samples
LL	1/2	1/2	2
LR	2/5	3/5	5
RL	1/4	3/4	4
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# Action Prediction

- Hierarchical N-gram predictor
  - Learn 1-gram, 2-gram, 3-gram, ... predictors simultaneously
  - For prediction, pick N-gram predictor with largest N and sufficient number of training samples  $f$
  - If none have sufficient samples, then

*N-gram based prediction is still hard to scale with large # of possibly relevant observations*

*Example:*

*training data (observed sequence of moves):* LRRLRLLLRRRLRLRR

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L	R	# of samples
7/15	8/15	15

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Obs.	L	R	# of samples
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# Action Prediction

---

- Naïve Bayes Classifiers
  - Scale much better to large # of input variables
  - Very popular (and powerful) for machine learning problems

# Action Prediction

---

- Naïve Bayes Classifiers
  - predicts action  $A^{predict} = \operatorname{argmax}_a P(A=a) \prod_i P(X_i=u_i / A=a)$

# Action Prediction

- Naïve Bayes Classifiers

- predicts action  $A^{predict} = \operatorname{argmax}_a P(A=a) \prod_i P(X_i=u_i / A=a)$

*Derivations of the above formula:*

$$A^{predict} = \operatorname{argmax}_a P(A=a / X_1=u_1 \dots X_k=u_k)$$

$$A^{predict} = \operatorname{argmax}_a P(A=a \ X_1=u_1 \dots X_k=u_k) / P(X_1=u_1 \dots X_k=u_k)$$

$$A^{predict} = \operatorname{argmax}_a P(X_1=u_1 \dots X_k=u_k / A=a) P(A=a) / P(X_1=u_1 \dots X_k=u_k)$$

$$A^{predict} = \operatorname{argmax}_a P(X_1=u_1 \dots X_k=u_k / A=a) P(A=a)$$

*Why?*

*Assuming conditional independence of input variables given predicted output:*

$$A^{predict} = \operatorname{argmax}_a P(A=a) \prod_i P(X_i=u_i / A=a)$$

# Action Prediction

- Naïve Bayes Classifiers

- predicts action  $A^{predict} = \operatorname{argmax}_a P(A=a) \prod_i P(X_i=u_i / A=a)$

*Example: Predicts whether the player will slow down (break) based on the distance to obstacle corner and the speed of the car*

*training data (previously collected): Suppose our current input is:*

brake?	distance	speed
Y	near	slow
Y	near	fast
N	far	fast
Y	far	fast
N	near	slow
Y	far	slow
Y	near	fast

*Distance = far, Speed = slow*

*Will character break?*

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*Distance = far, Speed = slow*

*Will character break?*

$P(\text{break}) = 5/7;$

$P(\text{Dist}=\text{far}/\text{break})=2/5; P(\text{Speed}=\text{slow}/\text{break}) = 2/5;$

$P(A=a) \prod_i P(X_i=u_i / A=a) = 5/7*2/5*2/5=4/35;$

$P(\text{not break}) = 2/7;$

$P(\text{Dist}=\text{far}/\text{not break})=1/2; P(\text{Speed}=\text{slow}/\text{not break}) = 1/2;$

$P(A=a) \prod_i P(X_i=u_i / A=a) = 2/7*1/2*1/2=1/14;$



# Action Prediction

- Naïve Bayes Classifiers

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*Example: Predicts whether the player will slow down (break) based on the distance to obstacle corner*

*The character is more likely to break ( $4/35 > 1/14$ )*

*training data (previously collected): Suppose our current input is:*

*Distance = far, Speed = slow*

brake?	distance	speed
Y	near	slow
Y	near	fast
N	far	fast
Y	far	fast
N	near	slow
Y	far	slow
Y	near	fast

*Will character break?*

$P(\text{break}) = 5/7;$

$P(\text{Dist}=\text{far}/\text{break})=2/5; P(\text{Speed}=\text{slow}/\text{break}) = 2/5;$

$P(A=a) \prod_i P(X_i=u_i / A=a) = 5/7*2/5*2/5=4/35;$

$P(\text{not break}) = 2/7;$

$P(\text{Dist}=\text{far}/\text{not break})=1/2; P(\text{Speed}=\text{slow}/\text{not break}) = 1/2;$

$P(A=a) \prod_i P(X_i=u_i / A=a) = 2/7*1/2*1/2=1/14;$