

# <New Simulation Scenario Result>

- 2월 20일 ~ 21일 Version

## <Preview>

: 새롭게 생성한 Simulation Scenario에 대하여,  $p=0.125$ 일 때 Simulation 결과 살펴봄.

## [Version 0]

①  $P(A=1 \mid B=b, C=c, D=d) = \text{expit}(-5.5 + 0.7B + 0.7C + 0.5D) \rightarrow p = 0.125$

②  $\mu = 1 + 2.5B + 2.5C + A + U$

For Scenario Version 4, ATT Performance Version 0						
Scenario (i)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	0.00823075561	0.080399423	0.949	0.999067603		
IPW	-0.00543264361	0.084441398	0.918	0.754513407	0.953	1.019217829
DR	0.00914683432	0.082134824	0.272	0.0296606278	0.955	1.076876684
Scenario (ii)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	1.397393736	2.088859905	0.036	1.584882157		
IPW	-0.00543264361	0.084441398	0.918	0.754513407	0.953	1.019217829
DR	-0.00606167914	0.084731758	0.347	0.051913523	0.953	1.104810623
Scenario (iii)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	0.00823075561	0.080399423	0.949	0.999067603		
IPW	1.395569397	2.083829891	0.006	0.507176493	0.038	0.994576588
DR	0.00811929842	0.080512604	0.263	0.0290941522	0.949	1.075486746
Scenario (iv)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	1.397393736	2.088859905	0.036	1.013840914		
IPW	1.395569397	2.083829891	0.006	0.507176493	0.038	0.994576588
DR	1.395569392	2.083829876	0	0.0572982065	0.046	1.280184245

: 분산 추정량의 Coverage와 SD Ratio는 GOOD

/ Scenario 별 추정량 간 bias가 동일한 현상이 나타나지 않음.

/ DR Estimator의 Bias가 예상과 다름. (Scenario가 mis-specified 되었을 때 bias가 더 낮음)

## [Version 1]

①  $P(A=1 \mid B=b, C=c, D=d) = \text{expit}(-5.4 + 0.7B + 0.5C + 0.5D) \rightarrow p = 0.125$

②  $\mu = 1 + 2.5B + 1.5C + A + U$

For Scenario Version 4, ATT Performance Version 1						
Scenario (i)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	0.00972862041	0.076766223	0.958	0.945588195		
IPW	-0.00151390088	0.080166145	0.915	0.681860175	0.957	0.964514753
DR	0.0108805514	0.078633623	0.292	0.0277543407	0.962	1.020682199
Scenario (ii)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	1.401653093	2.095919056	0.03	1.499921762		
IPW	-0.00151390088	0.080166145	0.915	0.681860175	0.957	0.964514753
DR	-0.00280168742	0.080516273	0.355	0.0484502522	0.965	1.04480528
Scenario (iii)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	0.00972862041	0.076766223	0.958	0.945588195		
IPW	1.400742154	2.093498101	0.006	0.451576005	0.029	0.936335905
DR	0.0096870198	0.076929826	0.284	0.027197232	0.965	1.01875336
Scenario (iv)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	1.401653093	2.095919056	0.03	0.95415514		
IPW	1.400742154	2.093498101	0.006	0.451576005	0.029	0.936335905
DR	1.400742153	2.093498096	0	0.0536592546	0.04	1.208102977

: Input Control 하는 Confounder “B”의 effect를 줄였음에도 Version 0과 동일한 결과가 나오고 있음.

$\therefore$  Random error라 간주하고, p 값 다양하게 바꾸어가며 결과 살펴보자.

[ $p = 0.5$ ]

①  $P(A=1 \mid B=b, C=c, D=d) = \text{expit}(-2.8 + 0.7B + 0.7C + 0.5D)$

②  $\mu = 1 + 2.5B + 2.5C + A + U$

For Scenario Version 4, ATT Performance Version 0 ( $p = 0.5$ )

Scenario (i)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	0.0028841906	0.039327509	0.95	1.003818749		
IPW	0.0032872935	0.049593818	0.976	1.339187649	0.954	1.001122625
DR	0.0016566883	0.043236989	0.699	0.270220437	0.957	1.02089948
Scenario (ii)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	1.157974732	1.405153099	0.008	1.554649834		
IPW	0.0032872935	0.049593818	0.976	1.339187649	0.954	1.001122625
DR	0.0028615676	0.049059448	0.834	0.567247894	0.956	1.160060347
Scenario (iii)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	0.0028841906	0.039327509	0.95	1.003818749		
IPW	1.15694812	1.404374816	0.011	1.055516929	0.008	0.996112142
DR	0.0024027246	0.040014804	0.691	0.257539824	0.953	1.025047382
Scenario (iv)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	1.157974732	1.405153099	0.008	0.998478048		
IPW	1.15694812	1.404374816	0.011	1.055516929	0.008	0.996112142
DR	1.156948119	1.404374814	0	0.294336547	0.011	1.068459982

[ $p = 0.25$ ]

①  $P(A=1 \mid B=b, C=c, D=d) = \text{expit}(-4.5 + 0.7B + 0.7C + 0.5D)$

②  $\mu = 1 + 2.5B + 2.5C + A + U$

For Simulation Scenario Version 4, ATT Performance Version 0 –  $p = 0.25$

Scenario (i)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	0.0110746815	0.054812802	0.943	1.000424934		
IPW	-0.00881398144	0.058594677	0.965	1.140475003	0.95	1.012846768
DR	0.0091945884	0.056328517	0.391	0.0766409487	0.954	1.05513604
Scenario (ii)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	1.264840368	1.685360455	0.004	1.562936267		
IPW	-0.00881398144	0.058594677	0.965	1.140475003	0.95	1.012846768
DR	-0.00904215482	0.058946739	0.521	0.148781451	0.955	1.111871296
Scenario (iii)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	0.0110746815	0.054812802	0.943	1.000424934		
IPW	1.262010796	1.678071469	0.003	0.795601046	0.005	0.989013239
DR	0.0106003596	0.054964231	0.377	0.0741227337	0.954	1.057919318
Scenario (iv)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	1.264840368	1.685360455	0.004	1.000067248		
IPW	1.262010796	1.678071469	0.003	0.795601046	0.005	0.989013239
DR	1.262010796	1.678071469	0	0.108280065	0.009	1.177263871

[ $p = 0.125$ ]

①  $P(A=1 \mid B=b, C=c, D=d) = \text{expit}(-5.5 + 0.7B + 0.7C + 0.5D)$

②  $\mu = 1 + 2.5B + 2.5C + A + U$

For Scenario Version 4, ATT Performance Version 0

Scenario (i)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	0.00823075561	0.080399423	0.949	0.999067603		
IPW	-0.00543264361	0.084441398	0.918	0.754513407	0.953	1.019217829
DR	0.00914683432	0.082134824	0.272	0.0296606278	0.955	1.076876684
Scenario (ii)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	1.397393736	2.088859905	0.036	1.584882157		
IPW	-0.00543264361	0.084441398	0.918	0.754513407	0.953	1.019217829
DR	-0.00606167914	0.084731758	0.347	0.051913523	0.953	1.104810623
Scenario (iii)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	0.00823075561	0.080399423	0.949	0.999067603		
IPW	1.395569397	2.083829891	0.006	0.507176493	0.038	0.994576588
DR	0.00811929842	0.080512604	0.263	0.0290941522	0.949	1.075486746
Scenario (iv)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	1.397393736	2.088859905	0.036	1.013840914		
IPW	1.395569397	2.083829891	0.006	0.507176493	0.038	0.994576588
DR	1.395569392	2.083829876	0	0.0572982065	0.046	1.280184245

[ $p = 0.065$ ]

①  $P(A=1 \mid B=b, C=c, D=d) = \text{expit}(-6.5 + 0.7B + 0.7C + 0.5D)$

②  $\mu = 1 + 2.5B + 2.5C + A + U$

For Simulation Scenario Version 4, ATT Performance Version 0 –  $p = 0.0625$

Scenario (i)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	-0.000184011744	0.16953389	0.941	1.012635211		
IPW	-0.00552950516	0.17631739	0.764	0.405170642	0.94	1.034540371
DR	0.00208804442	0.17205414	0.14	0.0109685337	0.953	1.104574273
Scenario (ii)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	1.528801181	2.61095665	0.163	1.638639646		
IPW	-0.00552950516	0.17631739	0.764	0.405170642	0.94	1.034540371
DR	-0.00660569391	0.17676508	0.171	0.0162163134	0.95	1.118138639
Scenario (iii)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	-0.000184011744	0.16953389	0.941	1.012635211		
IPW	1.527810354	2.6075284	0.031	0.261209274	0.152	0.996817
DR	-0.000430763826	0.16939005	0.139	0.0109149366	0.951	1.103729957
Scenario (iv)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	1.528801181	2.61095665	0.163	1.026210978		
IPW	1.527810354	2.6075284	0.031	0.261209274	0.152	0.996817
DR	1.527810347	2.60752838	0	0.0287014236	0.211	1.381897502

[ $p = 0.015$ ]

①  $P(A=1 \mid B=b, C=c, D=d) = \text{expit}(-8 + 0.7B + 0.7C + 0.5D)$

②  $\mu = 1 + 2.5B + 2.5C + A + U$

For Scenario Version4, ATT Performance Version 0 ( $p = 0.015$ )						
Scenario (i)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	-0.00150434493	0.54284485	0.958	1.025477602		
IPW	-0.000950405343	0.55042221	0.495	0.11204699	0.9246988	1.020269255
DR	0.00268710934	0.54922209	0.06	0.00291074059	0.964	1.12882388
Scenario (ii)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	1.670856819	3.72097981	0.587	1.695013823		
IPW	-0.000950405343	0.55042221	0.495	0.11204699	0.9246988	1.020269255
DR	-0.00255174337	0.55134379	0.071	0.00328732437	0.962	1.133777749
Scenario (iii)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	-0.00150434493	0.54284485	0.958	1.025477602		
IPW	1.670665767	3.72060519	0.099	0.0697029399	0.566	0.973815179
DR	-0.00164595374	0.54323854	0.066	0.00290227941	0.962	1.125868586
Scenario (iv)	Bias	rMSE	Naive_var_coverage	Naive_var_SD_Ratio	Sandwich_robust_var_coverage	Sandwich_var_SD_Ratio
Outcome_reg	1.670856819	3.72097981	0.587	1.039498509		
IPW	1.670665767	3.72060519	0.099	0.0697029399	0.566	0.973815179
DR	1.67066576	3.72060516	0.017	0.00872275964	0.78	1.499172522

(나의 생각)

- 1) model이 올바르게 적합 되었느냐의 여부에 상관없이 DR Estimator는 로버스트하다. Bias, rMSE, Sandwich robust variance의 Coverage probability에 큰 변화가 없음. - 단, Scenario (iv) 제외
- 2) model correctly specification 여부에 Outcome regression estimator, IPW estimator는 크게 영향 받는다.
  - Outcome regression estimator의 경우 bias가 1.66 정도 증가, 분산은 과대추정됨
  - IPW Estimator의 경우 bias가 1.669 정도 증가, 분산은 과소추정됨.
- 3) Naive variance estimator의 성능은 Exposure prevalence가 낮아질수록 나빠지는 반면(Coverage probability 확인), Sandwich robust variance estimator는 그런 경향이 보이지 않음. / 따라서, Sandwich variance estimator 사용하는 것을 추천한다.
- 4) Scenario (iv)에서 Exposure prevalence가 낮아질수록 Sandwich variance estimator의 Coverage probability가 높아진다.