## # Sandwich Variance Estimator of DR ATE Estimator #

: Renewal Version (9월 6일 Version)

$$\psi_{T}(\theta) = \begin{cases}
V_{I} - \frac{3}{2}E_{T}Y_{T} - (E_{I} - e_{T}) E[Y_{T}|E=I, X_{T}]}{e_{T}} & ---- (\psi_{V_{I}}) \\
V_{O} - \frac{3}{2}(I - E_{T}) Y_{T} - (E_{I} - e_{T}) E[Y_{T}|E=0, X_{T}]}{I - e_{T}} & ---- (\psi_{V_{O}}) \\
V_{O} - \frac{3}{2}(I - E_{T}) Y_{T} - (E_{I} - e_{T}) E[Y_{T}|E=0, X_{T}]}{I - e_{T}} & ---- (\psi_{O}) \\
V_{O} - \frac{3}{2}(I - E_{T}) Y_{T} - (E_{I} - e_{T}) E[Y_{T}|E=0, X_{T}]}{I - e_{T}} & ---- (\psi_{O}) \\
V_{O} - \frac{3}{2}(I - E_{T}) Y_{T} - (E_{I} - e_{T}) E[Y_{T}|E=0, X_{T}]}{I - e_{T}} & ---- (\psi_{O}) \\
V_{O} - \frac{3}{2}(I - E_{T}) Y_{T} - (E_{I} - e_{T}) E[Y_{T}|E=0, X_{T}]}{I - e_{T}} & ---- (\psi_{O}) \\
V_{O} - \frac{3}{2}(I - E_{T}) Y_{T} - (E_{I} - e_{T}) E[Y_{T}|E=0, X_{T}]}{I - e_{T}} & ---- (\psi_{O}) \\
V_{O} - \frac{3}{2}(I - E_{T}) Y_{T} - (E_{I} - e_{T}) E[Y_{T}|E=0, X_{T}]}{I - e_{T}} & ---- (\psi_{O}) \\
V_{O} - \frac{3}{2}(I - E_{T}) Y_{T} - (E_{I} - e_{T}) E[Y_{T}|E=0, X_{T}]}{I - e_{T}} & ---- (\psi_{O}) \\
V_{O} - \frac{3}{2}(I - E_{T}) Y_{T} - (E_{I} - e_{T}) E[Y_{T}|E=0, X_{T}]}{I - e_{T}} & ---- (\psi_{O}) \\
V_{O} - \frac{3}{2}(I - E_{T}) Y_{T} - (E_{I} - e_{T}) E[Y_{T}|E=0, X_{T}]}{I - e_{T}} & ---- (\psi_{O}) \\
V_{O} - \frac{3}{2}(I - E_{T}) Y_{T} - (E_{I} - e_{T}) E[Y_{T}|E=0, X_{T}]}{I - e_{T}} & ---- (\psi_{O}) \\
V_{O} - \frac{3}{2}(I - E_{T}) Y_{T} - (E_{I} - e_{T}) E[Y_{T}|E=0, X_{T}]}{I - e_{T}} & ---- (\psi_{O}) \\
V_{O} - \frac{3}{2}(I - E_{T}) Y_{T} - (E_{I} - e_{T}) E[Y_{T}|E=0, X_{T}]}{I - e_{T}} & ---- (\psi_{O}) \\
V_{O} - \frac{3}{2}(I - E_{T}) Y_{T} - (E_{I} - e_{T}) E[Y_{T}|E=0, X_{T}]}{I - e_{T}} & ---- (\psi_{O}) \\
V_{O} - \frac{3}{2}(I - E_{T}) Y_{T} - (E_{I} - e_{T}) E[Y_{T}|E=0, X_{T}]}{I - e_{T}} & ---- (\psi_{O}) \\
V_{O} - \frac{3}{2}(I - E_{T}) Y_{T} - (E_{I} - e_{T}) E[Y_{T}|E=0, X_{T}]}{I - e_{T}} & ---- (\psi_{O}) V_{O} - (\psi_{O}) Y_{O} \\
V_{O} - \frac{3}{2}(I - E_{T}) Y_{T} - (E_{I} - e_{T}) Y_{O} - (\psi_{O}) Y_{O} - (\psi_{O}) Y_{O} \\
V_{O} - (\psi_{O}) Y_{O} - (\psi_{$$

$$\frac{\partial}{\partial \theta'} \psi_{\overline{1}}(\hat{\theta}) = \begin{bmatrix}
\frac{\partial}{\partial \nu}, \psi_{\nu}, & \frac{\partial}{\partial \nu}, \psi_{\nu}, & \frac{\partial}{\partial \alpha}, \psi_{\nu}, & \frac{\partial}{\partial \beta}, \psi_{\nu}, & ---(1) \\
\frac{\partial}{\partial \nu}, \psi_{\nu}, & \frac{\partial}{\partial \nu}, \psi_{\nu}, & \frac{\partial}{\partial \alpha}, \psi_{\nu}, & \frac{\partial}{\partial \beta}, \psi_{\nu}, & ---(2) \\
\frac{\partial}{\partial \nu}, \psi_{\alpha}, & \frac{\partial}{\partial \nu}, \psi_{\alpha}, & \frac{\partial}{\partial \alpha}, \psi_{\alpha}, & \frac{\partial}{\partial \beta}, \psi_{\alpha}, & ---(3) \\
\frac{\partial}{\partial \nu}, \psi_{\beta}, & \frac{\partial}{\partial \nu}, \psi_{\beta}, & \frac{\partial}{\partial \alpha}, \psi_{\beta}, & \frac{\partial}{\partial \beta}, \psi_{\beta}, & ---(4)
\end{bmatrix}$$

$$| \psi_{V_{i}} = V_{i} - \frac{(1 + e^{\beta^{T}XT})^{\frac{1}{2}} \operatorname{Er} Y_{T} - (\operatorname{Er} - \frac{e^{\beta^{T}XT}}{1 + e^{\beta^{T}XT}}) \cdot (1, 1, X_{T}) \times q^{q}}{e^{\beta^{T}XT}}$$

$$= V_{i} - \frac{(1 + e^{\beta^{T}XT})^{\frac{1}{2}} \operatorname{Er} (1 + e^{\beta^{T}XT}) \cdot (1, 1, X_{T}) \times q^{q}}{e^{\beta^{T}XT}}$$

$$= e^{\beta^{T}XT}$$

$$= \mathcal{V}_{I} - \frac{\left(1 + e^{\beta^{T}XT}\right) E_{T}Y_{T}}{e^{\beta^{T}X_{T}}} + \frac{E_{T}\left(1 + e^{\beta^{T}X_{T}}\right)}{e^{\beta^{T}X_{T}}} \cdot \left(1, 1, X_{T}\right) \alpha - \left(1, 1, X_{T}\right) \alpha$$

$$\frac{\partial}{\partial v_1} \Psi v_1 = 1 / \frac{\partial}{\partial v_0} \Psi v_1 = 0$$

$$\frac{\partial}{\partial x} \psi_{2I} = \frac{\text{Er}\left(1 + e^{\beta^{T}XT}\right)}{e^{\beta^{T}XT}} \cdot (1, 1, X_{T}^{T}) - (1, 1, X_{T}^{T}) = \left(\frac{\text{Er}\left(1 + e^{\beta^{T}XT}\right)}{e^{\beta^{T}XT}} - 1\right) (1, 1, X_{T}^{T})$$

$$= \frac{\text{Er}\left(1 + e^{\beta^{T}XT}\right)}{e^{\beta^{T}XT}} \cdot (1, 1, X_{T}^{T}) - (1, 1, X_{T}^{T}) = \left(\frac{\text{Er}\left(1 + e^{\beta^{T}XT}\right)}{e^{\beta^{T}XT}} - 1\right) (1, 1, X_{T}^{T})$$

$$= \frac{\text{Scalar}}{\text{Scalar}} = \frac{\text{Scalar}}{\text{Scalar}} = \frac{\text{Coursel}}{\text{Scalar}} = \frac{\text{Coursel}}{\text{Sc$$

$$\begin{array}{lll} \mathring{,} \psi_{\mathcal{V}_{1}} \text{ orlist } & \beta \mathfrak{L} & \mathcal{L}_{\mathcal{C}}^{\mathsf{PT}XT} & \mathcal{L$$

$$\frac{\partial}{\partial v} \Psi v_0 = 0, \quad \frac{\partial}{\partial v_0} \Psi v_0 = 1, \quad \frac{\partial}{\partial x} \Psi v_0 = (1 + e^{\beta^T X \tau}) \cdot \text{E}_{\bar{\tau}} \cdot (1, 0, X_{\bar{\tau}}) - e^{\beta^T X \tau} (1, 0, X_{\bar{\tau}})$$

$$= \frac{\partial}{\partial v} (1 + e^{\beta^T X \tau}) \cdot \text{E}_{\bar{\tau}} - e^{\beta^T X \tau} \frac{\partial}{\partial v} (1, 0, X_{\bar{\tau}})$$

$$\frac{\partial}{\partial \beta} \Psi_{yo} = -e^{\theta^{T}XT} (1 - E_{\overline{1}}) Y_{\overline{1}} \cdot X_{\overline{1}} + e^{\theta^{T}XT} \cdot E_{\overline{1}} \cdot (1, 0, X_{\overline{1}}) d \cdot X_{\overline{1}} - e^{\theta^{T}XT} (1, 0, X_{\overline{1}}) d \cdot X_{\overline{1}}$$

$$= e^{\theta^{T}XT} \cdot X_{\overline{1}} \left( -(1 - E_{\overline{1}}) Y_{\overline{1}} + E_{\overline{1}} (1, 0, X_{\overline{1}}) d - (1, 0, X_{\overline{1}}) d \right)$$

$$= e^{\theta^{T}XT} \left( -(1 - E_{\overline{1}}) Y_{\overline{1}} - (1, 0, X_{\overline{1}}) d \cdot (1 - E_{\overline{1}}) \right) X_{\overline{1}} = -e^{\theta^{T}XT} \left( (1 - E_{\overline{1}}) (Y_{\overline{1}} + (1, 0, X_{\overline{1}}) d) \cdot X_{\overline{1}} \right)$$

$$\frac{\partial}{\partial v_{1}} \psi_{d} = 0$$
,  $\frac{\partial}{\partial v_{0}} \psi_{d} = 0$ ,  $\frac{\partial}{\partial \alpha} \psi_{d} = -\chi_{T} \chi_{T}^{T}$ ,  $\frac{\partial}{\partial \beta} \psi_{d} = Q \ (+ \Re t )$ 

4) 
$$\Psi_{\beta} = \frac{\chi_{T}}{1 + e^{\beta^{T}\chi_{T}}} \left( \chi_{T} + PS \text{ model } \text{model } \text{matrix} \Rightarrow (1, \chi) \right)$$

$$\frac{\partial}{\partial v_{i}} \psi_{\beta} = \frac{\partial}{\partial v_{o}} \psi_{\beta} = 0$$
,  $\frac{\partial}{\partial \alpha} \psi_{\beta} = 0$  ( $+ 2 \% \% \% \% \% \%$ )

$$\frac{\partial}{\partial \beta} \psi_{\beta} = \frac{-\chi_{T} \cdot e^{\beta^{T} \chi_{T}} \cdot \chi_{T}}{\left(1 + e^{\beta^{T} \chi_{T}}\right)^{2}} = \frac{-e^{\beta^{T} \chi_{T}} \cdot \chi_{T} \cdot \chi_{T}}{\left(1 + e^{\beta^{T} \chi_{T}}\right)^{2}} = \frac{-e^{\beta^{T} \chi_{T}} \cdot \chi_{T} \cdot \chi_{T}}{\left(1 + e^{\beta^{T} \chi_{T}}\right)^{2}} = \frac{-e^{\beta^{T} \chi_{T}} \cdot \chi_{T}}{\left(1 + e^{\beta^{T} \chi_{T}}\right)^{2}}$$