Sandwich Variance Estimator of DR ATE Estimator

: Reupdate Version (9월 20일 Version)

: Estimating equation 잘못 작성한 부분 수정

$$\psi_{T}(\theta) = \begin{bmatrix}
v_{1} - \frac{3}{4}E_{T}Y_{T} - (E_{i} - e_{T}) E[Y_{T}|E=1, X_{T}]^{\frac{3}{4}} \\
e_{T} \\
v_{0} - \frac{3}{4}(1-E_{T}) Y_{T} + (E_{i} - e_{T}) E[Y_{T}|E=0, X_{T}]^{\frac{3}{4}} \\
1 - e_{T} \\
V_{0} - e_{T}$$

$$\frac{\partial}{\partial 0} \Psi_{\overline{1}}(\hat{0}) = \begin{bmatrix} \frac{\partial}{\partial \nu_{1}} \Psi_{\nu_{1}}, & \frac{\partial}{\partial \nu_{0}} \Psi_{\nu_{1}}, & \frac{\partial}{\partial \alpha} \Psi_{\nu_{1}}, & \frac{\partial}{\partial \beta} \Psi_{\nu_{1}} & ---(1) \\ \frac{\partial}{\partial \nu_{1}} \Psi_{\nu_{0}}, & \frac{\partial}{\partial \nu_{0}} \Psi_{\nu_{0}}, & \frac{\partial}{\partial \alpha} \Psi_{\nu_{0}}, & \frac{\partial}{\partial \beta} \Psi_{\nu_{0}} & ---(2) \\ \frac{\partial}{\partial \nu_{1}} \Psi_{\alpha}, & \frac{\partial}{\partial \nu_{0}} \Psi_{\alpha}, & \frac{\partial}{\partial \alpha} \Psi_{\alpha}, & \frac{\partial}{\partial \beta} \Psi_{\alpha} & ----(3) \\ \frac{\partial}{\partial \nu_{1}} \Psi_{\beta}, & \frac{\partial}{\partial \nu_{0}} \Psi_{\beta}, & \frac{\partial}{\partial \alpha} \Psi_{\beta}, & \frac{\partial}{\partial \beta} \Psi_{\beta} & ----(4) \end{bmatrix}$$

$$| \psi_{V_{1}} = V_{1} - \frac{(1+e^{\beta^{T}XT})^{\frac{1}{2}} E_{1} Y_{1} - (E_{1} - \frac{e^{\beta^{T}XT}}{1+e^{\beta^{T}XT}}) \cdot (1,1,X_{1}) \alpha^{q}}{e^{\beta^{T}XT}}$$

$$= V_{1} - \frac{(1+e^{\beta^{T}XT})^{\frac{1}{2}} (E_{1} Y_{1}) - E_{1} (1+e^{\beta^{T}XT}) \cdot (1,1,X_{1}) \alpha^{q}}{e^{\beta^{T}XT}}$$

$$= e^{\beta^{T}XT}$$

$$= V_{1} - \frac{(1+e^{\beta^{T}XT})^{\frac{1}{2}} (E_{1} Y_{1}) - E_{1} (1+e^{\beta^{T}XT})}{e^{\beta^{T}XT}}$$

$$= \mathcal{V}_{I} - \frac{(1+e^{\beta^{T}XT}) \operatorname{Ei}Y_{T}}{e^{\beta^{T}X_{T}}} + \frac{\operatorname{Et}(1+e^{\beta^{T}X_{T}})}{e^{\beta^{T}X_{T}}} \cdot (1,1,X_{T}) \alpha - (1,1,X_{T}) \alpha$$

$$\frac{\partial}{\partial v_1} \psi v_1 = 1 / \frac{\partial}{\partial v_0} \psi v_1 = 0$$

$$\frac{\partial}{\partial v_{1}} \psi_{a} = 0$$
, $\frac{\partial}{\partial v_{0}} \psi_{a} = 0$, $\frac{\partial}{\partial \alpha} \psi_{a} = -X_{T} X_{T}^{T}$, $\frac{\partial}{\partial \beta} \psi_{a} = Q \ (+ \Re t)$

$$\frac{\partial}{\partial u} V_{\beta} = \frac{\partial}{\partial v_{0}} V_{\beta} = 0$$
, $\frac{\partial}{\partial \alpha} V_{\beta} = 0$ ($+ 2t^{\alpha} 7t^{\beta} + \sqrt{2} 2t^{\alpha} 7t^{\beta}$)

$$\frac{\partial}{\partial \beta} \psi_{\beta} = \frac{-e^{X\tau^T \beta}}{1 + e^{X\tau^T \beta}} \cdot X_T \cdot X_T^T$$