

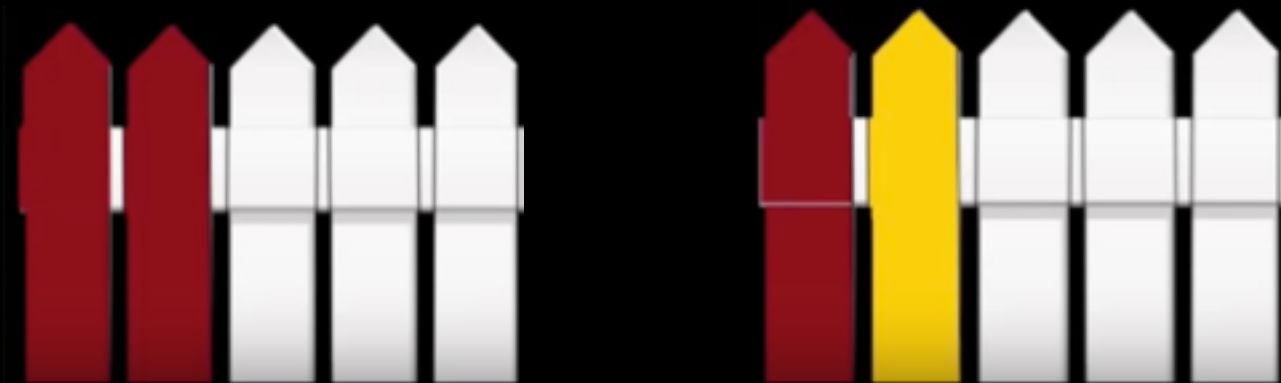
PAINTING FENCE ALGORITHM

<https://www.geeksforgeeks.org/painting-fence-algorithm/>

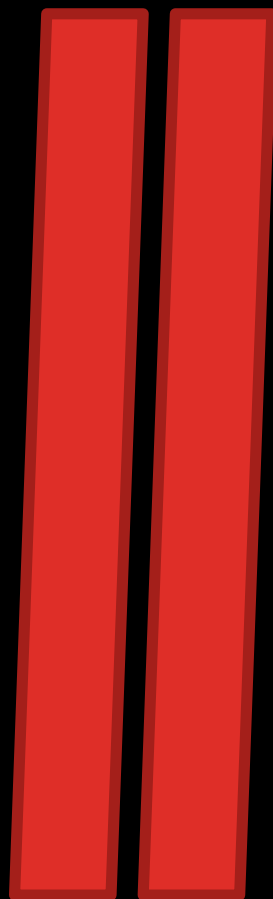
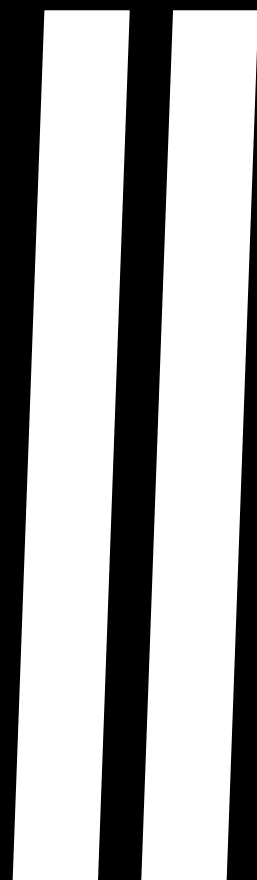
2018.07.08 원은지

어떤 문제인가?

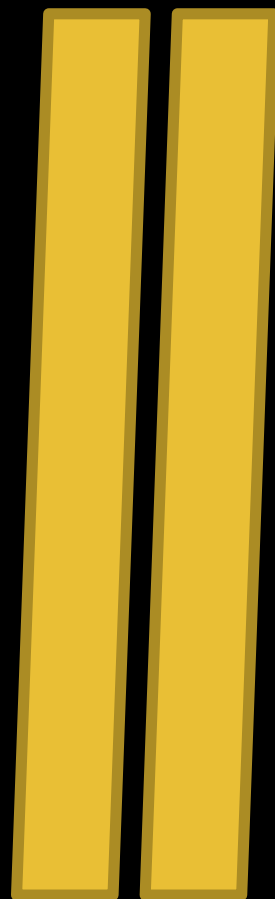
- n 개의 개수의 울타리를 k 개의 색깔을 가지고 칠하려고 한다.
- 2개 이상 같은 색으로 칠할 수 없다.
- 울타리를 칠할 수 있는 모든 경우의 수를 구해라.



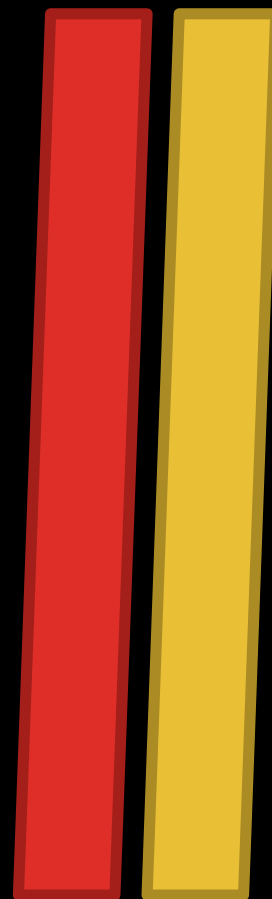
$n = 2 / k = 2$



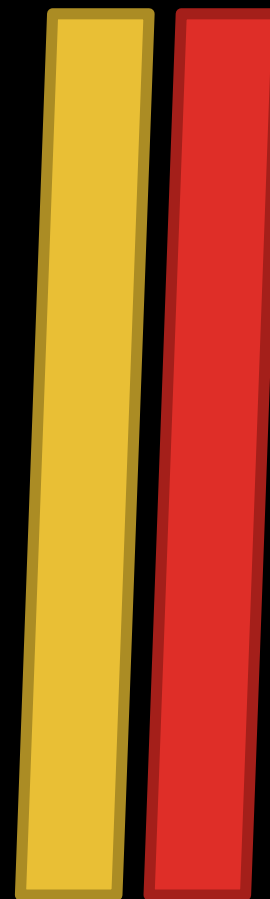
same



same



diff



diff

총 4가지 경우

어떻게 풀 것인가?

- 동적 프로그래밍 이용

Consider these two terms

Same



No of ways when color of last two posts is same

Diff



No of ways when color of last two posts is different

$n=1$

$\text{diff} = k, \text{same} = 0$

$\text{total} = k$



For one post we just have k choices

$n=2$

$\text{diff} = k * (k-1)$

$\text{same} = k$



k choices for common color of two posts

$\text{Total} = k + k * (k-1)$

$n = 3$

$$\text{diff} = [k + k * (k-1)] * (k-1)$$

2- different = $k * (k-1)$ choices

1 - same = k choices



3 -different = $k-1$ choices

$n = 3$

$$\text{diff} = [k + k * (k-1)] * (k-1)$$

$$\text{same} = k * (k-1)$$

$K - 1$ choices for these two



K choices for this

Summary for these cases

for $n = 1$

diff = k , same = 0

total = k

for $n = 3$

diff = $[k + k * (k-1)] * (k-1)$

same = $k * (k-1)$

for $n = 2$

diff = $k * (k-1)$

same = k

total = $k + k * (k-1)$

total = $[k + k * (k-1)] * (k-1) + k * (k-1)$

Hence we deduce that

$$\text{total}[i] = \text{same}[i] + \text{diff}[i]$$

$$\text{same}[i] = \text{diff}[i-1]$$

$$\text{diff}[i] = (\text{diff}[i-1] + \text{diff}[i-2]) * (k-1)$$

$$= \text{total}[i-1] * (k-1)$$

복잡도

- 시간 복잡도 : $O(n)$
- 공간 복잡도 : $O(n)$