



Lecture 7-1: Ensemble Learning Overview

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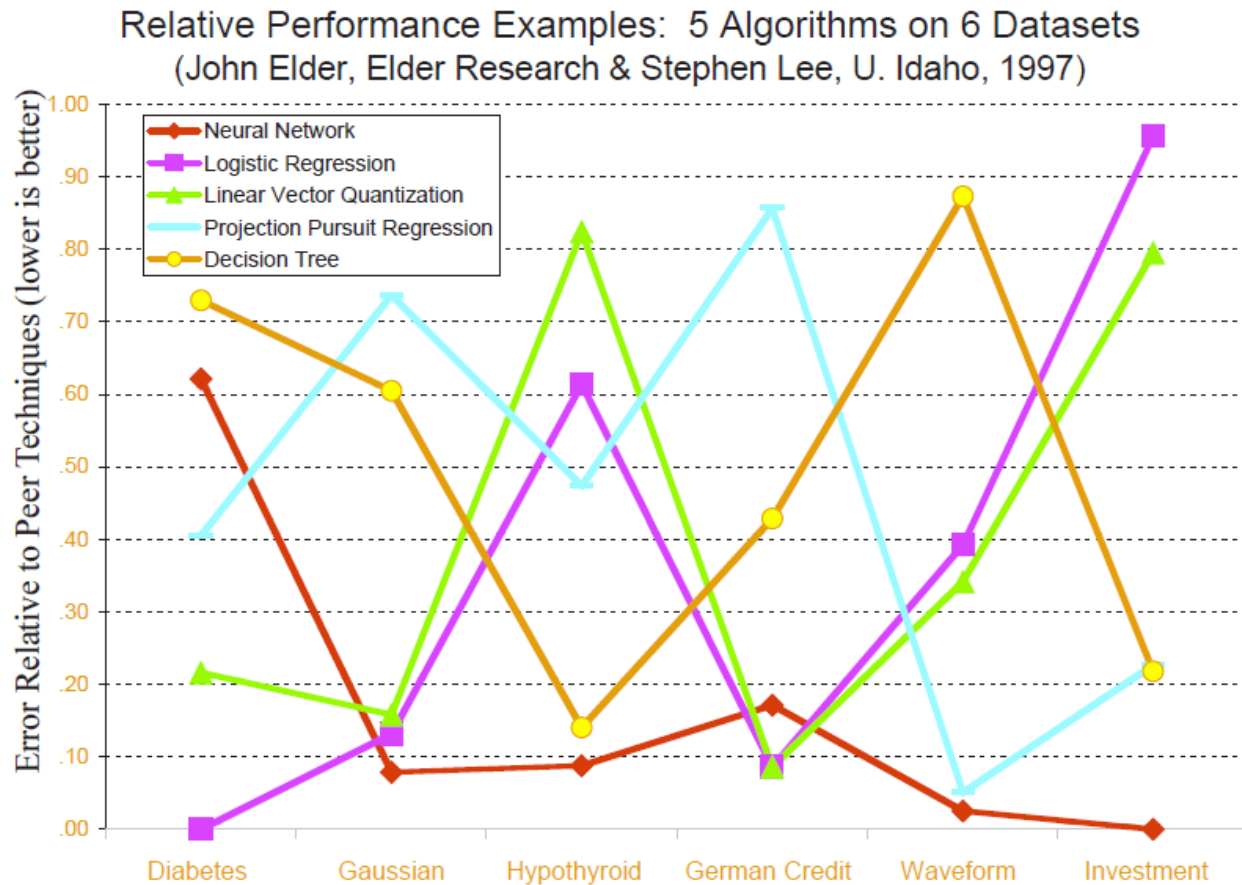
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Backgrounds

Seni and Elder (2010)

- Can we have a superior algorithm for all datasets?
 - ✓ Every algorithm scored best or next-to-best on at least two of the six data sets.



Backgrounds

- No Free Lunch Theorem

- ✓ Can we expect any classification method to be superior or inferior overall?

- ✓ No Free Lunch Theorem: No

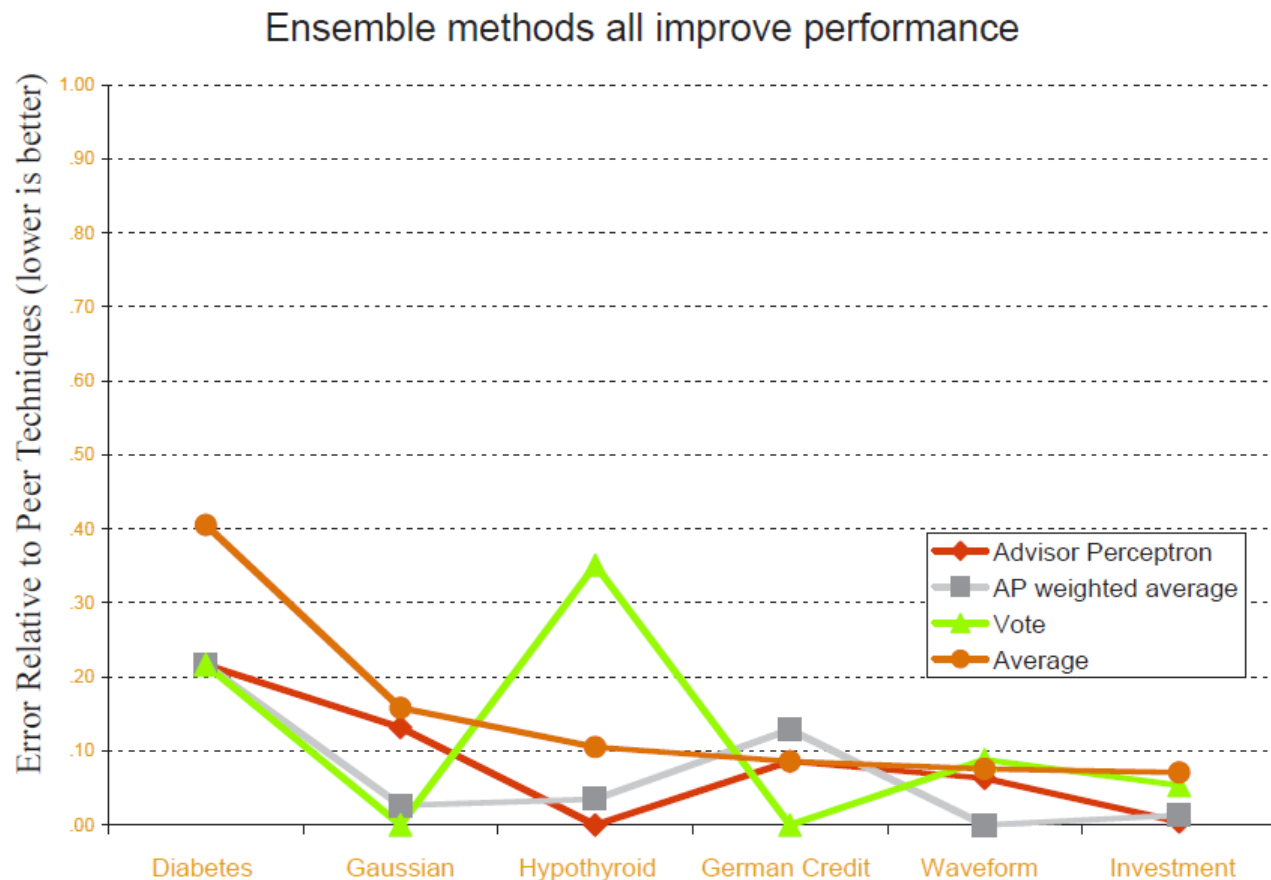
- ✓ If the goal is to obtain good generalization performance, there is no context-independent or usage-independent reasons to favor one algorithm over others

- ✓ If one algorithm seems to outperform another in a particular situation, it is a consequence of its fit to a particular pattern recognition problem

- ✓ In practice, experience with a broad range of techniques is the best insurance for solving arbitrary new classification problems

Motivation

- However, if they are properly combined...
 - ✓ Every ensemble method competes well against the best of the individual algorithms



Empirical Evidence

Opitz and Maclin (1999)

- Empirical study I: Single vs. Ensemble algorithms for 23 datasets

Data Set	Cases	Class	Features		Neural Network			
			Cont	Disc	Inputs	Outputs	Hiddens	Epochs
breast-cancer-w	699	2	9	-	9	1	5	20
credit-a	690	2	6	9	47	1	10	35
credit-g	1000	2	7	13	63	1	10	30
diabetes	768	2	9	-	8	1	5	30
glass	214	6	9	-	9	6	10	80
heart-cleveland	303	2	8	5	13	1	5	40
hepatitis	155	2	6	13	32	1	10	60
house-votes-84	435	2	-	16	16	1	5	40
hypo	3772	5	7	22	55	5	15	40
ionosphere	351	2	34	-	34	1	10	40
iris	159	3	4	-	4	3	5	80
kr-vs-kp	3196	2	-	36	74	1	15	20
labor	57	2	8	8	29	1	10	80
letter	20000	26	16	-	16	26	40	30
promoters-936	936	2	-	57	228	1	20	30
ribosome-bind	1877	2	-	49	196	1	20	35
satellite	6435	6	36	-	36	6	15	30
segmentation	2310	7	19	-	19	7	15	20
sick	3772	2	7	22	55	1	10	40
sonar	208	2	60	-	60	1	10	60
soybean	683	19	-	35	134	19	25	40
splice	3190	3	-	60	240	2	25	30
vehicle	846	4	18	-	18	4	10	40

Empirical Evidence

- Empirical study I: Single vs. Ensemble algorithms for 23 datasets
 - ✓ Error rate: the lower, the better

Data Set	Neural Network					C4.5			
	Stan	Simp	Bag	Boosting		Stan	Bag	Boosting	
breast-cancer-w	3.4	3.5	3.4	3.8	4.0	5.0	3.7	3.5	3.5
credit-a	14.8	13.7	13.8	15.8	15.7	14.9	13.4	14.0	13.7
credit-g	27.9	24.7	24.2	25.2	25.3	29.6	25.2	25.9	26.7
diabetes	23.9	23.0	22.8	24.4	23.3	27.8	24.4	26.0	25.7
glass	38.6	35.2	33.1	32.0	31.1	31.3	25.8	25.5	23.3
heart-cleveland	18.6	17.4	17.0	20.7	21.1	24.3	19.5	21.5	20.8
hepatitis	20.1	19.5	17.8	19.0	19.7	21.2	17.3	16.9	17.2
house-votes-84	4.9	4.8	4.1	5.1	5.3	3.6	3.6	5.0	4.8
hypo	6.4	6.2	6.2	6.2	6.2	0.5	0.4	0.4	0.4
ionosphere	9.7	7.5	9.2	7.6	8.3	8.1	6.4	6.0	6.1
iris	4.3	3.9	4.0	3.7	3.9	5.2	4.9	5.1	5.6
kr-vs-kp	2.3	0.8	0.8	0.4	0.3	0.6	0.6	0.3	0.4
labor	6.1	3.2	4.2	3.2	3.2	16.5	13.7	13.0	11.6
letter	18.0	12.8	10.5	5.7	4.6	14.0	7.0	4.1	3.9
promoters-936	5.3	4.8	4.0	4.5	4.6	12.8	10.6	6.8	6.4
ribosome-bind	9.3	8.5	8.4	8.1	8.2	11.2	10.2	9.3	9.6
satellite	13.0	10.9	10.6	9.9	10.0	13.8	9.9	8.6	8.4
segmentation	6.6	5.3	5.4	3.5	3.3	3.7	3.0	1.7	1.5
sick	5.9	5.7	5.7	4.7	4.5	1.3	1.2	1.1	1.0
sonar	16.6	15.9	16.8	12.9	13.0	29.7	25.3	21.5	21.7
soybean	9.2	6.7	6.9	6.7	6.3	8.0	7.9	7.2	6.7
splice	4.7	4.0	3.9	4.0	4.2	5.9	5.4	5.1	5.3
vehicle	24.9	21.2	20.7	19.1	19.7	29.4	27.1	22.5	22.9

Empirical Evidence

Caruana and Niculescu-Mizil (2006)

- Empirical study 2: 8 algorithms on 11 datasets

- ✓ Algorithms

- SVM, ANN, Logistic regression (LOGREG), Naïve Bayes (NB), KNN, Random Forests (RF), Decision Trees (DT), Bagged trees (BAG-DT), Boosted trees (BST-DT), Boosted stumps (BST-STMP)

- ✓ Data sets

PROBLEM	#ATTR	TRAIN SIZE	TEST SIZE	%POZ
ADULT	14/104	5000	35222	25%
BACT	11/170	5000	34262	69%
COD	15/60	5000	14000	50%
CALHOUS	9	5000	14640	52%
COV_TYPE	54	5000	25000	36%
HS	200	5000	4366	24%
LETTER.P1	16	5000	14000	3%
LETTER.P2	16	5000	14000	53%
MEDIS	63	5000	8199	11%
MG	124	5000	12807	17%
SLAC	59	5000	25000	50%

Empirical Evidence

- Empirical study 2: 8 algorithms on 11 datasets

✓ Normalized score by datasets

MODEL	CAL	COVT	ADULT	LTR.P1	LTR.P2	MEDIS	SLAC	HS	MG	CALHOUS	COD	BACT	MEAN
BST-DT	PLT	.938	.857	.959	.976	.700	.869	.933	.855	.974	.915	.878*	.896*
RF	PLT	.876	.930	.897	.941	.810	.907*	.884	.883	.937	.903*	.847	.892
BAG-DT	—	.878	.944*	.883	.911	.762	.898*	.856	.898	.948	.856	.926	.887*
BST-DT	ISO	.922*	.865	.901*	.969	.692*	.878	.927	.845	.965	.912*	.861	.885*
RF	—	.876	.946*	.883	.922	.785	.912*	.871	.891*	.941	.874	.824	.884
BAG-DT	PLT	.873	.931	.877	.920	.752	.885	.863	.884	.944	.865	.912*	.882
RF	ISO	.865	.934	.851	.935	.767*	.920	.877	.876	.933	.897*	.821	.880
BAG-DT	ISO	.867	.933	.840	.915	.749	.897	.856	.884	.940	.859	.907*	.877
SVM	PLT	.765	.886	.936	.962	.733	.866	.913*	.816	.897	.900*	.807	.862
ANN	—	.764	.884	.913	.901	.791*	.881	.932*	.859	.923	.667	.882	.854
SVM	ISO	.758	.882	.899	.954	.693*	.878	.907	.827	.897	.900*	.778	.852
ANN	PLT	.766	.872	.898	.894	.775	.871	.929*	.846	.919	.665	.871	.846
ANN	ISO	.767	.882	.821	.891	.785*	.895	.926*	.841	.915	.672	.862	.842
BST-DT	—	.874	.842	.875	.913	.523	.807	.860	.785	.933	.835	.858	.828
KNN	PLT	.819	.785	.920	.937	.626	.777	.803	.844	.827	.774	.855	.815
KNN	—	.807	.780	.912	.936	.598	.800	.801	.853	.827	.748	.852	.810
KNN	ISO	.814	.784	.879	.935	.633	.791	.794	.832	.824	.777	.833	.809
BST-STMP	PLT	.644	.949	.767	.688	.723	.806	.800	.862	.923	.622	.915*	.791
SVM	—	.696	.819	.731	.860	.600	.859	.788	.776	.833	.864	.763	.781
BST-STMP	ISO	.639	.941	.700	.681	.711	.807	.793	.862	.912	.632	.902*	.780
BST-STMP	—	.605	.865	.540	.615	.624	.779	.683	.799	.817	.581	.906*	.710
DT	ISO	.671	.869	.729	.760	.424	.777	.622	.815	.832	.415	.884	.709
DT	—	.652	.872	.723	.763	.449	.769	.609	.829	.831	.389	.899*	.708
DT	PLT	.661	.863	.734	.756	.416	.779	.607	.822	.826	.407	.890*	.706
LR	—	.625	.886	.195	.448	.777*	.852	.675	.849	.838	.647	.905*	.700
LR	ISO	.616	.881	.229	.440	.763*	.834	.659	.827	.833	.636	.889*	.692
LR	PLT	.610	.870	.185	.446	.738	.835	.667	.823	.832	.633	.895	.685
NB	ISO	.574	.904	.674	.557	.709	.724	.205	.687	.758	.633	.770	.654
NB	PLT	.572	.892	.648	.561	.694	.732	.213	.690	.755	.632	.756	.650
NB	—	.552	.843	.534	.556	.011	.714	-.654	.655	.759	.636	.688	.481

Empirical Evidence

- Empirical study 2: 8 algorithms on 11 datasets

✓ Normalized score by various metrics

MODEL	CAL	ACC	FSC	LFT	ROC	APR	BEP	RMS	MXE	MEAN	OPT-SEL
BST-DT	PLT	.843*	.779	.939	.963	.938	.929*	.880	.896	.896	.917
RF	PLT	.872*	.805	.934*	.957	.931	.930	.851	.858	.892	.898
BAG-DT	—	.846	.781	.938*	.962*	.937*	.918	.845	.872	.887*	.899
BST-DT	ISO	.826*	.860*	.929*	.952	.921	.925*	.854	.815	.885	.917*
RF	—	.872	.790	.934*	.957	.931	.930	.829	.830	.884	.890
BAG-DT	PLT	.841	.774	.938*	.962*	.937*	.918	.836	.852	.882	.895
RF	ISO	.861*	.861	.923	.946	.910	.925	.836	.776	.880	.895
BAG-DT	ISO	.826	.843*	.933*	.954	.921	.915	.832	.791	.877	.894
SVM	PLT	.824	.760	.895	.938	.898	.913	.831	.836	.862	.880
ANN	—	.803	.762	.910	.936	.892	.899	.811	.821	.854	.885
SVM	ISO	.813	.836*	.892	.925	.882	.911	.814	.744	.852	.882
ANN	PLT	.815	.748	.910	.936	.892	.899	.783	.785	.846	.875
ANN	ISO	.803	.836	.908	.924	.876	.891	.777	.718	.842	.884
BST-DT	—	.834*	.816	.939	.963	.938	.929*	.598	.605	.828	.851
KNN	PLT	.757	.707	.889	.918	.872	.872	.742	.764	.815	.837
KNN	—	.756	.728	.889	.918	.872	.872	.729	.718	.810	.830
KNN	ISO	.755	.758	.882	.907	.854	.869	.738	.706	.809	.844
BST-STMP	PLT	.724	.651	.876	.908	.853	.845	.716	.754	.791	.808
SVM	—	.817	.804	.895	.938	.899	.913	.514	.467	.781	.810
BST-STMP	ISO	.709	.744	.873	.899	.835	.840	.695	.646	.780	.810
BST-STMP	—	.741	.684	.876	.908	.853	.845	.394	.382	.710	.726
DT	ISO	.648	.654	.818	.838	.756	.778	.590	.589	.709	.774
DT	—	.647	.639	.824	.843	.762	.777	.562	.607	.708	.763
DT	PLT	.651	.618	.824	.843	.762	.777	.575	.594	.706	.761
LR	—	.636	.545	.823	.852	.743	.734	.620	.645	.700	.710
LR	ISO	.627	.567	.818	.847	.735	.742	.608	.589	.692	.703
LR	PLT	.630	.500	.823	.852	.743	.734	.593	.604	.685	.695
NB	ISO	.579	.468	.779	.820	.727	.733	.572	.555	.654	.661
NB	PLT	.576	.448	.780	.824	.738	.735	.537	.559	.650	.654
NB	—	.496	.562	.781	.825	.738	.735	.347	-.633	.481	.489

Empirical Evidence

Fernández-Delgado et al. (2014)

- Empirical study 3: 179 algorithms on 121 datasets

Data set	#pat.	#inp.	#cl.	%Maj.	Data set	#pat.	#inp.	#cl.	%Maj.	Data set	#pat.	#inp.	#cl.	%Maj.	Data set	#pat.	#inp.	#cl.	%Maj.
abalone	4177	8	3	34.6	energy-y1	768	8	3	46.9	monks-2	169	6	2	62.1	soybean	307	35	18	13.0
ac-inflam	120	6	2	50.8	energy-y2	768	8	3	49.9	monks-3	3190	6	2	50.8	spambase	4601	57	2	60.6
acute-nephritis	120	6	2	58.3	fertility	100	9	2	88.0	mushroom	8124	21	2	51.8	spect	80	22	2	67.1
adult	48842	14	2	75.9	flags	194	28	8	30.9	musk-1	476	166	2	56.5	spectf	80	44	2	50.0
annealing	798	38	6	76.2	glass	214	9	6	35.5	musk-2	6598	166	2	84.6	st-australian-credit	690	14	2	67.8
arrhythmia	452	262	13	54.2	haberman-survival	306	3	2	73.5	nursery	12960	8	5	33.3	st-german-credit	1000	24	2	70.0
audiology-std	226	59	18	26.3	hayes-roth	132	3	3	38.6	oocMerl2F	1022	25	3	67.0	st-heart	270	13	2	55.6
balance-scale	625	4	3	46.1	heart-cleveland	303	13	5	54.1	oocMerl4D	1022	41	2	68.7	st-image	2310	18	7	14.3
balloons	16	4	2	56.2	heart-hungarian	294	12	2	63.9	oocTris2F	912	25	2	57.8	st-landsat	4435	36	6	24.2
bank	45211	17	2	88.5	heart-switzerland	123	12	2	39.0	oocTris5B	912	32	3	57.6	st-shuttle	43500	9	7	78.4
blood	748	4	2	76.2	heart-va	200	12	5	28.0	optical	3823	62	10	10.2	st-vehicle	846	18	4	25.8
breast-cancer	286	9	2	70.3	hepatitis	155	19	2	79.3	ozone	2536	72	2	97.1	steel-plates	1941	27	7	34.7
bc-wisc	699	9	2	65.5	hill-valley	606	100	2	50.7	page-blocks	5473	10	5	89.8	synthetic-control	600	60	6	16.7
bc-wisc-diag	569	30	2	62.7	horse-colic	300	25	2	63.7	parkinsons	195	22	2	75.4	teaching	151	5	3	34.4
bc-wisc-prog	198	33	2	76.3	ilpd-indian-liver	583	9	2	71.4	pendigits	7494	16	10	10.4	thyroid	3772	21	3	92.5
breast-tissue	106	9	6	20.7	image-segmentation	210	19	7	14.3	pima	768	8	2	65.1	tic-tac-toe	958	9	2	65.3
car	1728	6	4	70.0	ionosphere	351	33	2	64.1	pb-MATERIAL	106	4	3	74.5	titanic	2201	3	2	67.7
ctg-10classes	2126	21	10	27.2	iris	150	4	3	33.3	pb-REL-L	103	4	3	51.5	trains	10	28	2	50.0
ctg-3classes	2126	21	3	77.8	led-display	1000	7	10	11.1	pb-SPAN	92	4	3	52.2	twonorm	7400	20	2	50.0
chess-krvk	28056	6	18	16.2	lenses	24	4	3	62.5	pb-T-OR-D	102	4	2	86.3	vc-2classes	310	6	2	67.7
chess-krvkv	3196	36	2	52.2	letter	20000	16	26	4.1	pb-TYPE	105	4	6	41.9	vc-3classes	310	6	3	48.4
congress-voting	435	16	2	61.4	libras	360	90	15	6.7	planning	182	12	2	71.4	wall-following	5456	24	4	40.4
conn-bench-sonar	208	60	2	53.4	low-res-spect	531	100	9	51.9	plant-margin	1600	64	100	1.0	waveform	5000	21	3	33.9
conn-bench-vowel	528	11	11	9.1	lung-cancer	32	56	3	40.6	plant-shape	1600	64	100	1.0	waveform-noise	5000	40	3	33.8
connect-4	67557	42	2	75.4	lymphography	148	18	4	54.7	plant-texture	1600	64	100	1.0	wine	179	13	3	39.9
contrac	1473	9	3	42.7	magic	19020	10	2	64.8	post-operative	90	8	3	71.1	wine-quality-red	1599	11	6	42.6
credit-approval	690	15	2	55.5	mammographic	961	5	2	53.7	primary-tumor	330	17	15	25.4	wine-quality-white	4898	11	7	44.9
cylinder-bands	512	35	2	60.9	miniboone	130064	50	2	71.9	ringnorm	7400	20	2	50.5	yeast	1484	8	10	31.2
dermatology	366	34	6	30.6	molec-biol-promoter	106	57	2	50.0	seeds	210	7	3	33.3	zoo	101	16	7	40.6
echocardiogram	131	10	2	67.2	molec-biol-splice	3190	60	3	51.9	semeion	1593	256	10	10.2					
ecoli	336	7	8	42.6	monks-1	124	6	2	50.0										

Empirical Evidence

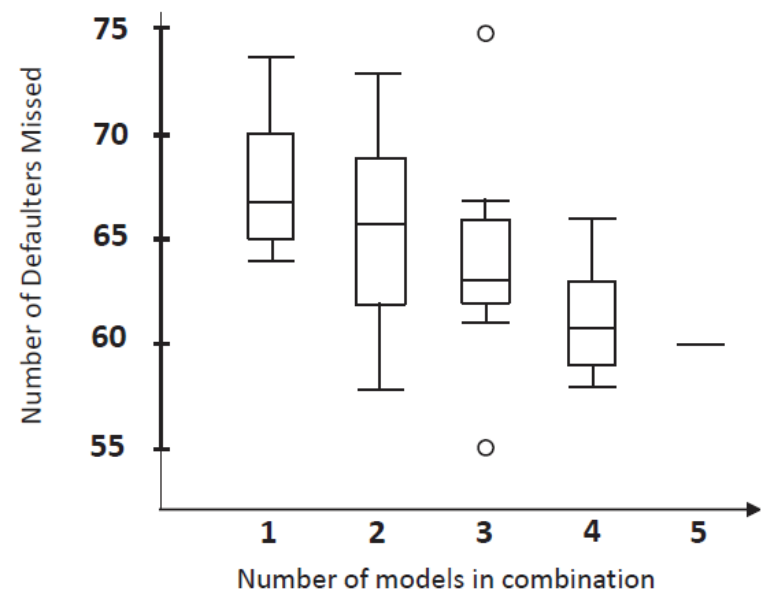
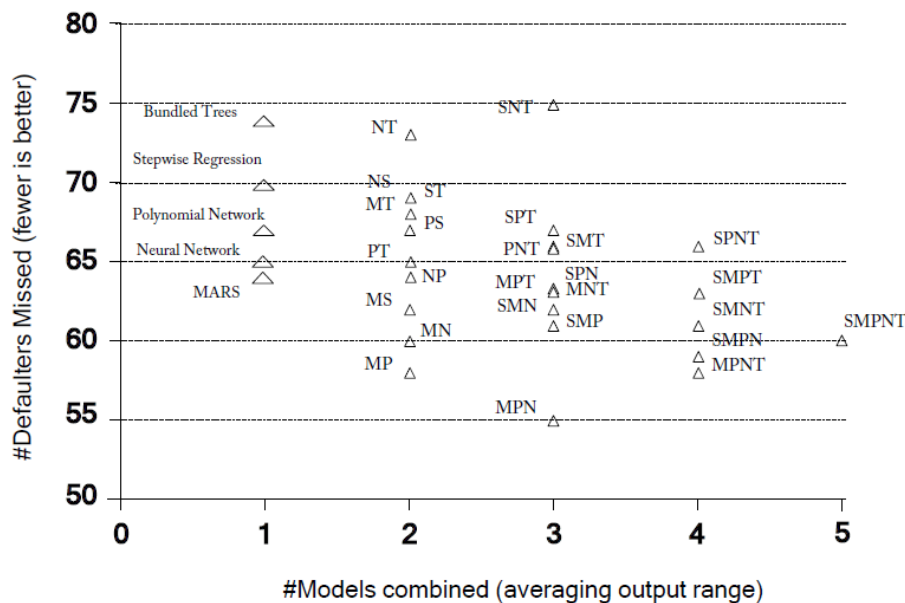
- Empirical study 3: 179 algorithms on 121 datasets

Rank	Acc.	κ	Classifier	Rank	Acc.	κ	Classifier
32.9	82.0	63.5	parRF.t (RF)	67.3	77.7	55.6	pda.t (DA)
33.1	82.3	63.6	rf.t (RF)	67.6	78.7	55.2	elm.m (NNET)
36.8	81.8	62.2	svm.C (SVM)	67.6	77.8	54.2	SimpleLogistic.w (LMR)
38.0	81.2	60.1	svmPoly.t (SVM)	69.2	78.3	57.4	MAB.J48.w (BST)
39.4	81.9	62.5	rforest.R (RF)	69.8	78.8	56.7	BG.REPTree.w (BAG)
39.6	82.0	62.0	elm.kerneLm (NNET)	69.8	78.1	55.4	SMO.w (SVM)
40.3	81.4	61.1	svmRadialCost.t (SVM)	70.6	78.3	58.0	MLP.w (NNET)
42.5	81.0	60.0	svmRadial.t (SVM)	71.0	78.8	58.23	BG.RandomTree.w (BAG)
42.9	80.6	61.0	C5.0.t (BST)	71.0	77.1	55.1	mlm.R (GLM)
44.1	79.4	60.5	avNNet.t (NNET)	71.0	77.8	56.2	BG.J48.w (BAG)
45.5	79.5	61.0	nnet.t (NNET)	72.0	75.7	52.6	rbf.t (NNET)
47.0	78.7	59.4	pcaNNet.t (NNET)	72.1	77.1	54.8	fda.R (DA)
47.1	80.8	53.0	BG.LibSVM.w (BAG)	72.4	77.0	54.7	lda.R (DA)
47.3	80.3	62.0	mlp.t (NNET)	72.4	79.1	55.6	svmlight.C (NNET)
47.6	80.6	60.0	RotationForest.w (RF)	72.6	78.4	57.9	AdaBoostM1.J48.w (BST)
50.1	80.9	61.6	RRF.t (RF)	72.7	78.4	56.2	BG.LBk.w (BAG)
51.6	80.7	61.4	RRFglobal.t (RF)	72.9	77.1	54.6	ldaBag.R (BAG)
52.5	80.6	58.0	MAB.LibSVM.w (BST)	73.2	78.3	56.2	BG.LWL.w (BAG)
52.6	79.9	56.9	LibSVM.w (SVM)	73.7	77.9	56.0	MAB.REPTree.w (BST)
57.6	79.1	59.3	adaboost.R (BST)	74.0	77.4	52.6	RandomSubSpace.w (DT)
58.5	79.7	57.2	pnn.m (NNET)	74.4	76.9	54.2	lda2.t (DA)
58.9	78.5	54.7	cforest.t (RF)	74.6	74.1	51.8	svmBag.R (BAG)
59.9	79.7	42.6	dkp.C (NNET)	74.6	77.5	55.2	LibLINEAR.w (SVM)
60.4	80.1	55.8	gaussprRadialR (OM)	75.9	77.2	55.6	rbfDDA.t (NNET)
60.5	80.0	57.4	RandomForest.w (RF)	76.5	76.9	53.8	sda.t (DA)
62.1	78.7	56.0	svmLinear.t (SVM)	76.6	78.1	56.5	END.w (OEN)
62.5	78.4	57.5	fda.t (DA)	76.6	77.3	54.8	LogitBoost.w (BST)
62.6	78.6	56.0	knn.t (NN)	76.6	78.2	57.3	MAB.RandomTree.w (BST)
62.8	78.5	58.1	mlp.C (NNET)	77.1	78.4	54.0	BG.RandomForest.w (BAG)
63.0	79.9	59.4	RandomCommittee.w (OEN)	78.5	76.5	53.7	Logistic.w (LMR)
63.4	78.7	58.4	Decorate.w (OEN)	78.7	76.6	50.5	ctreeBag.R (BAG)
63.6	76.9	56.0	mlpWeightDecay.t (NNET)	79.0	76.8	53.5	BG.Logistic.w (BAG)
63.8	78.7	56.7	rda.R (DA)	79.1	77.4	53.0	lvq.t (NNET)
64.0	79.0	58.6	MAB_MLP.w (BST)	79.1	74.4	50.7	pls.t (PLSR)
64.1	79.9	56.9	MAB.RandomForest.w (BST)	79.8	76.9	54.7	hdda.R (DA)
65.0	79.0	56.8	knn.R (NN)	80.6	75.9	53.3	MCC.w (OEN)
65.2	77.9	56.2	multinom.t (LMR)	80.9	76.9	54.5	mda.R (DA)
65.5	77.4	56.6	gcvEarth.t (MARS)	81.4	76.7	55.2	C5.0Rules.t (RL)
65.5	77.8	55.7	glmnet.R (GLM)	81.6	78.3	55.8	lssvmRadial.t (SVM)
65.6	78.6	58.4	MAB-PART.w (BST)	81.7	75.6	50.9	JRip.t (RL)
66.0	78.5	56.5	CVR.w (OM)	82.0	76.1	53.3	MAB.Logistic.w (BST)
66.4	79.2	58.9	treebag.t (BAG)	84.2	75.8	53.9	C5.0Tree.t (DT)
66.6	78.2	56.8	BG-PART.w (BAG)	84.6	75.7	50.8	BG.DecisionTable.w (BAG)
66.7	75.5	55.2	mda.t (DA)	84.9	76.5	53.4	NBTree.w (DT)

Real-world Examples

- Credit card scoring

- ✓ Mean error reduces with increasing degree of combination



- Netflix competition

- ✓ The final edge was obtained by **weighting contributions from the models of up to 30 competitors**

Real-world Examples

- The 10 main takeaways from MLConf SF (2016)

- ✓ It's (still) not all about Deep Learning
- ✓ Choose the right problem to solve, with the right metric
- ✓ Fine tuning your models is 5% of a project

✓ Ensembles almost always work better

- ✓ The trend towards personalization
- ✓ Manual curation of content is still used in practice
- ✓ Avoid the curse of complexity
- ✓ Learn the best practices from established players
- ✓ Everybody is using open source
- ✓ Make sure you have support from the executives



Real-world Examples

- Large Scale Visual Recognition Challenge
 - ✓ With given these images...

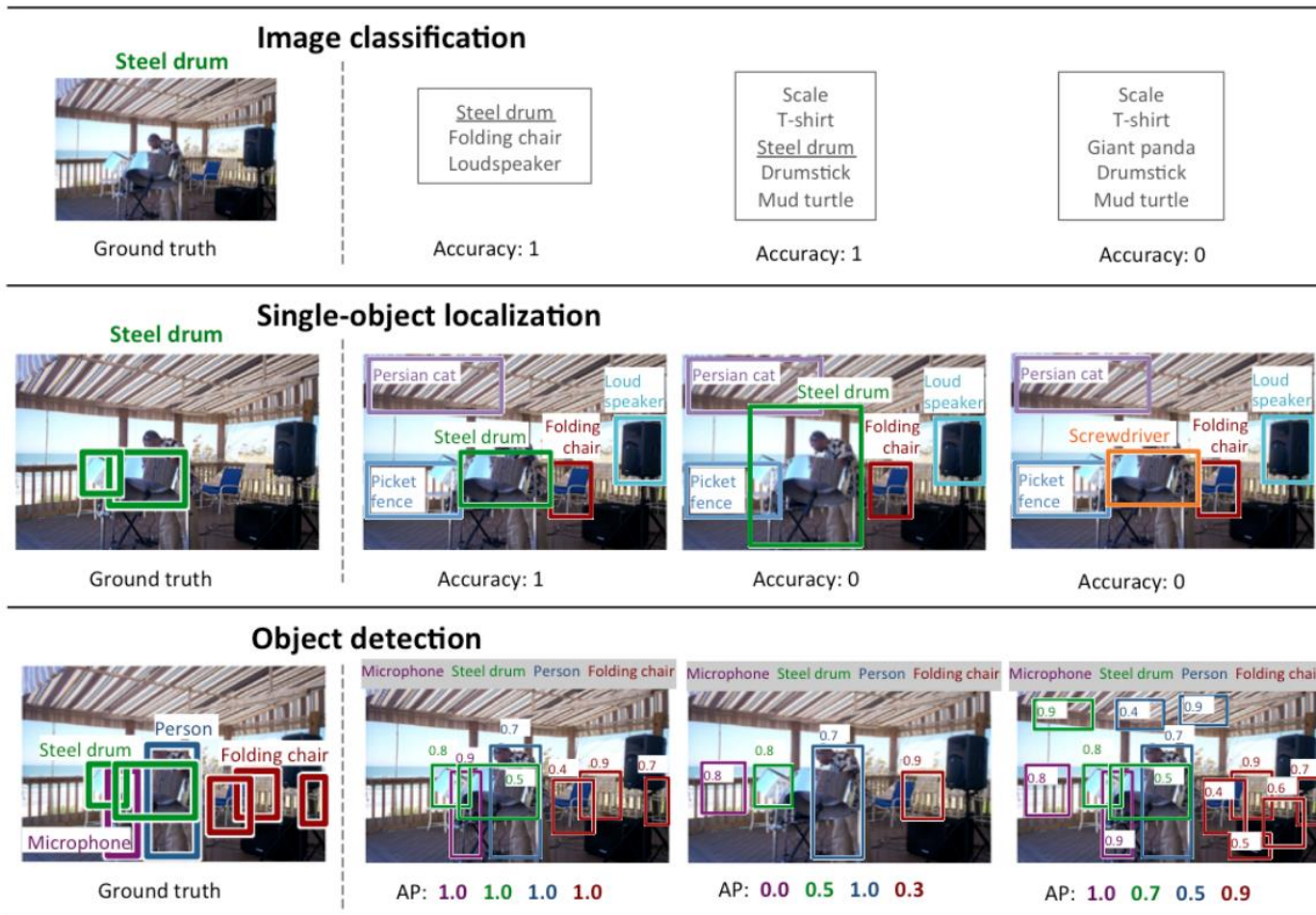


Real-world Examples

Russakovsky et al. (2015)

- Large Scale Visual Recognition Challenge

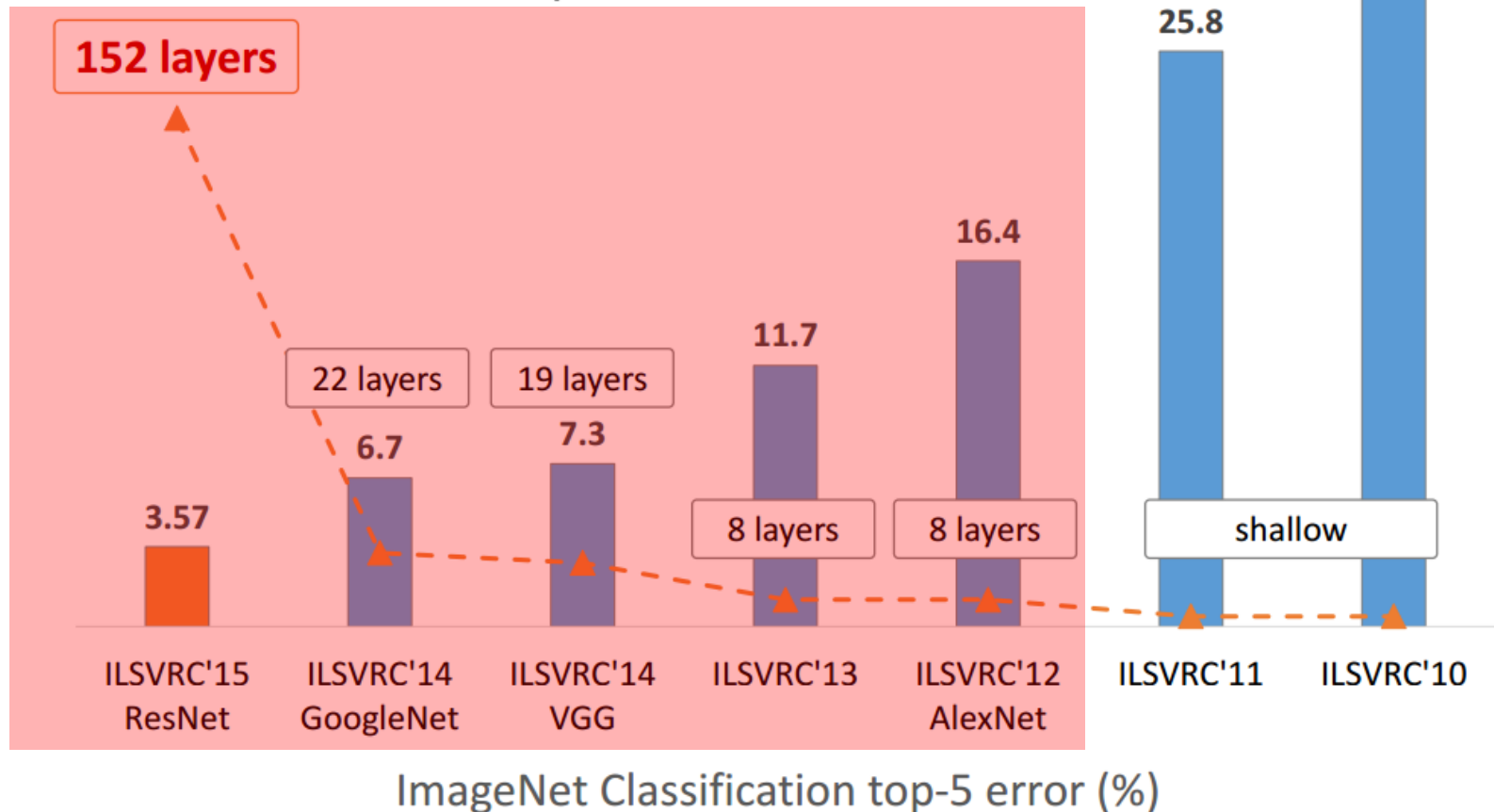
- ✓ Tasks



Real-world Examples

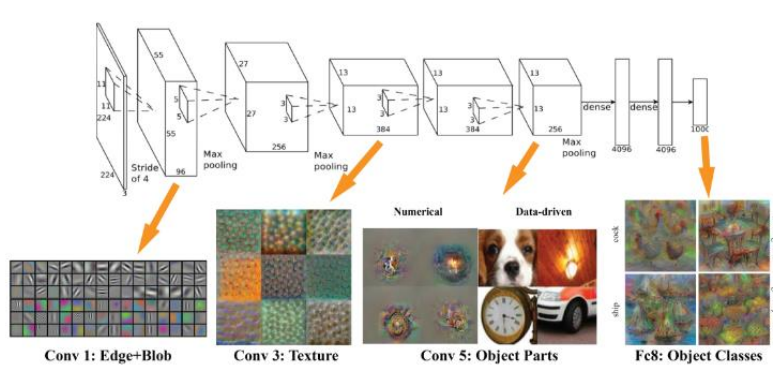
- Large Scale Visual Recognition Challenge (~ ILSVRC2015)

Revolution of Depth

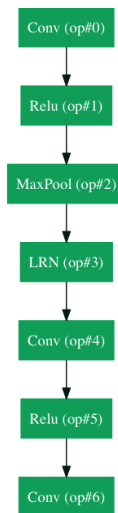


Real-world Examples

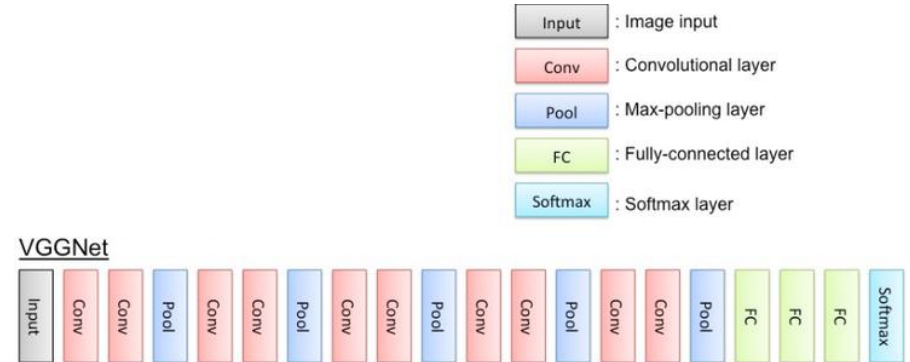
- Large Scale Visual Recognition Challenge (~ ILSVRC2015)



Alexnet



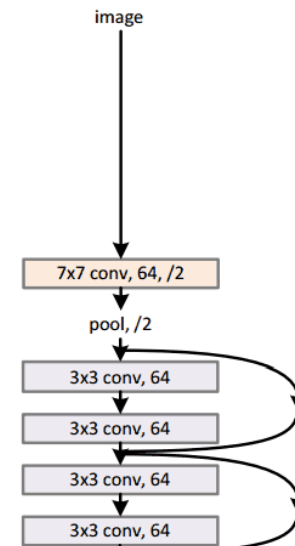
GoogLeNet



VGGNet

VGGNet

34-layer residual



ResNet

Real-world Examples

• Large Scale Visual Recognition Challenge (ILSVRC2016 ~)

✓ 2016

Object detection (DET)^[top]

Task 1a: Object detection with provided training data

Ordered by number of categories won

Team name	Entry description	Number of object categories won	mean AP
CUIImage	Ensemble of 6 models using provided data	109	0.662751
Hikvision	Ensemble A of 3 RPN and 6 FRCN models, mAP is 67 on val2	30	0.652704
Hikvision	Ensemble B of 3 RPN and 5 FRCN models, mean AP is 66.9, median AP is 69.3 on val2	18	0.652003

Object localization (LOC)^[top]

Task 2a: Classification+localization with provided training data

Ordered by localization error

Team name	Entry description	Localization error	Classification error
Trimps-Soushen	Ensemble 3	0.077087	0.02991
Trimps-Soushen	Ensemble 4	0.077429	0.02991
Trimps-Soushen	Ensemble 2	0.077668	0.02991
Trimps-Soushen	Ensemble 1	0.079068	0.03144

✓ 2017

Object detection (DET)^[top]

Task 1a: Object detection with provided training data

Ordered by number of categories won

Team name	Entry description	Number of object categories won	mean AP
BDAT	submission4	85	0.731392
BDAT	submission3	65	0.732227
BDAT	submission2	30	0.723712
DeepView(ETRI)	Ensemble_A	10	0.593084
NUS-Qihoo_DPNs (DET)	Ensemble of DPN models	9	0.656932
KAISTNIA_ETRI	Ensemble Model5	1	0.61022
KAISTNIA_ETRI	Ensemble Model4	0	0.609402
KAISTNIA_ETRI	Ensemble Model2	0	0.608299
KAISTNIA_ETRI	Ensemble Model1	0	0.608278
KAISTNIA_ETRI	Ensemble Model3	0	0.60631

Object localization (LOC)^[top]

Task 2a: Classification+localization with provided training data

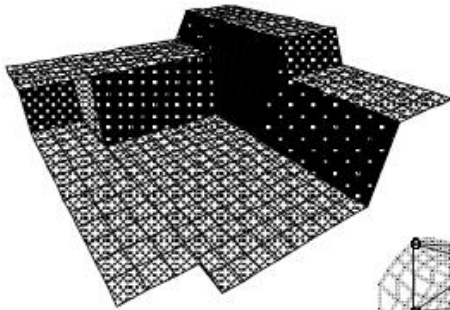
Ordered by localization error

Team name	Entry description	Localization error	Classification error
NUS-Qihoo_DPNs (CLS-LOC)	[E3] LOC:: Dual Path Networks + Basic Ensemble	0.062263	0.03413
Trimps-Soushen	Result-3	0.064991	0.02481
Trimps-Soushen	Result-2	0.06525	0.02481
Trimps-Soushen	Result-4	0.065261	0.02481
Trimps-Soushen	Result-5	0.065302	0.02481
Trimps-Soushen	Result-1	0.067698	0.02481

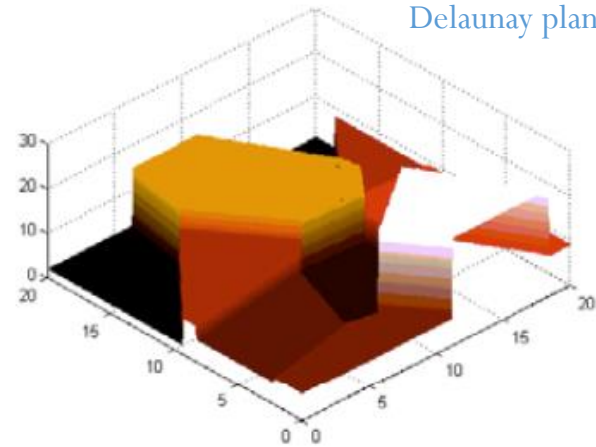
Theoretical Backgrounds: Model Space

- Different model produce different class boundaries or fitted functions

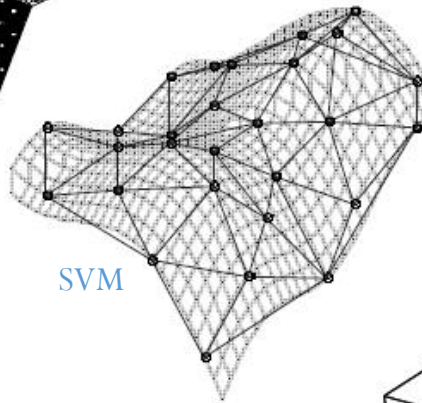
Decision Tree



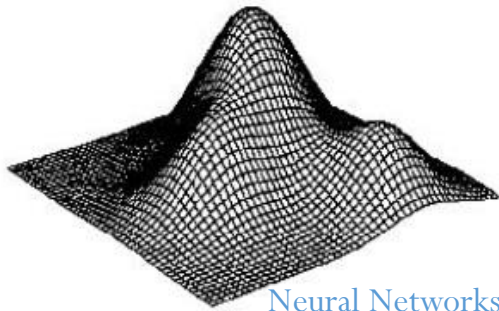
Delaunay planes



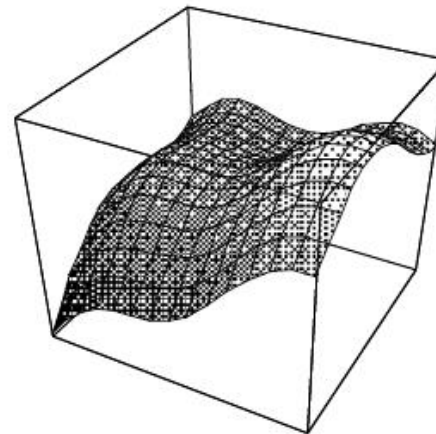
SVM



Neural Networks



k-NN



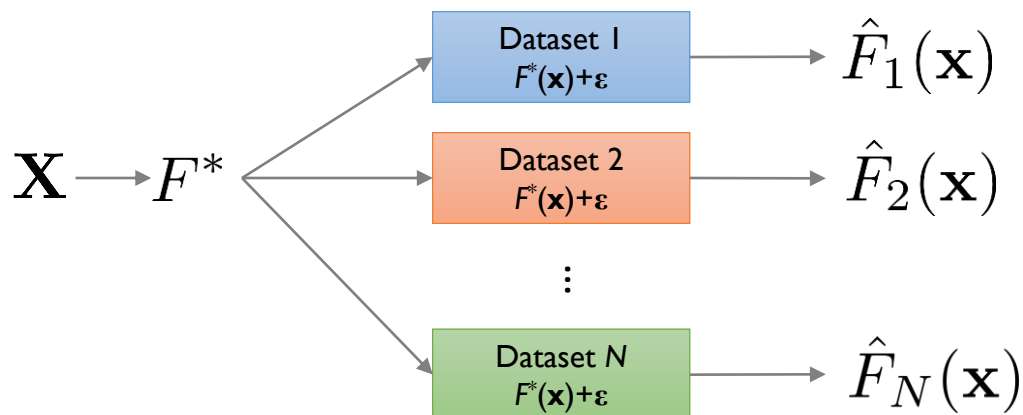
Theoretical Backgrounds: Bias-Variance Decomposition

- Suppose the data comes from the “additive error” model

$$y = F^*(\mathbf{x}) + \epsilon, \quad \epsilon \sim N(0, \sigma^2)$$

- ✓ $F^*(\mathbf{x})$ is the target function that we are trying to learn, but do not really know
- ✓ The errors are independent and identically distributed

- Consider the estimation process



- ✓ The average fit over all possible datasets:

$$\bar{F}(\mathbf{x}) = E[\hat{F}_D(\mathbf{x})]$$

Theoretical Backgrounds: Bias-Variance Decomposition

- The MSE for a particular data point

$$\begin{aligned} Err(\mathbf{x}_0) &= E \left[y - \hat{F}(\mathbf{x}) | \mathbf{x} = \mathbf{x}_0 \right]^2 && (y = F^*(\mathbf{x}) + \epsilon) \\ &= E \left[\hat{F}^*(\mathbf{x}_0) + \epsilon - \hat{F}(\mathbf{x}_0) \right]^2 \\ &= E \left[\hat{F}^*(\mathbf{x}_0) - \hat{F}(\mathbf{x}_0) \right]^2 + \sigma^2 \\ &= E \left[\hat{F}^*(\mathbf{x}_0) - \bar{F}(\mathbf{x}_0) + \bar{F}(\mathbf{x}_0) - \hat{F}(\mathbf{x}_0) \right]^2 + \sigma^2 \end{aligned}$$

Theoretical Backgrounds: Bias-Variance Decomposition

- The MSE for a particular data point

$$= E \left[\hat{F}^*(\mathbf{x}_0) - \bar{F}(\mathbf{x}_0) + \bar{F}(\mathbf{x}_0) - \hat{F}(\mathbf{x}_0) \right]^2 + \sigma^2$$

✓ By the properties of the expectation operator

$$= E \left[\hat{F}^*(\mathbf{x}_0) - \bar{F}(\mathbf{x}_0) \right]^2 + E \left[\bar{F}(\mathbf{x}_0) - \hat{F}(\mathbf{x}_0) \right]^2 + \sigma^2$$

$$= \left[\hat{F}^*(\mathbf{x}_0) - \bar{F}(\mathbf{x}_0) \right]^2 + E \left[\bar{F}(\mathbf{x}_0) - \hat{F}(\mathbf{x}_0) \right]^2 + \sigma^2$$

$$= \text{Bias}^2(\hat{F}(\mathbf{x}_0)) + \text{Var}(\hat{F}(\mathbf{x}_0)) + \sigma^2$$

Theoretical Backgrounds: Bias-Variance Decomposition

- Properties of Bias and Variance

- ✓ **Bias**²: the amount by which the average estimator differs from the truth

- Low bias: on average, we will accurately estimate the function from the dataset
 - High bias implies a **poor** match

- ✓ **Variance**: spread of the individual estimations around their mean

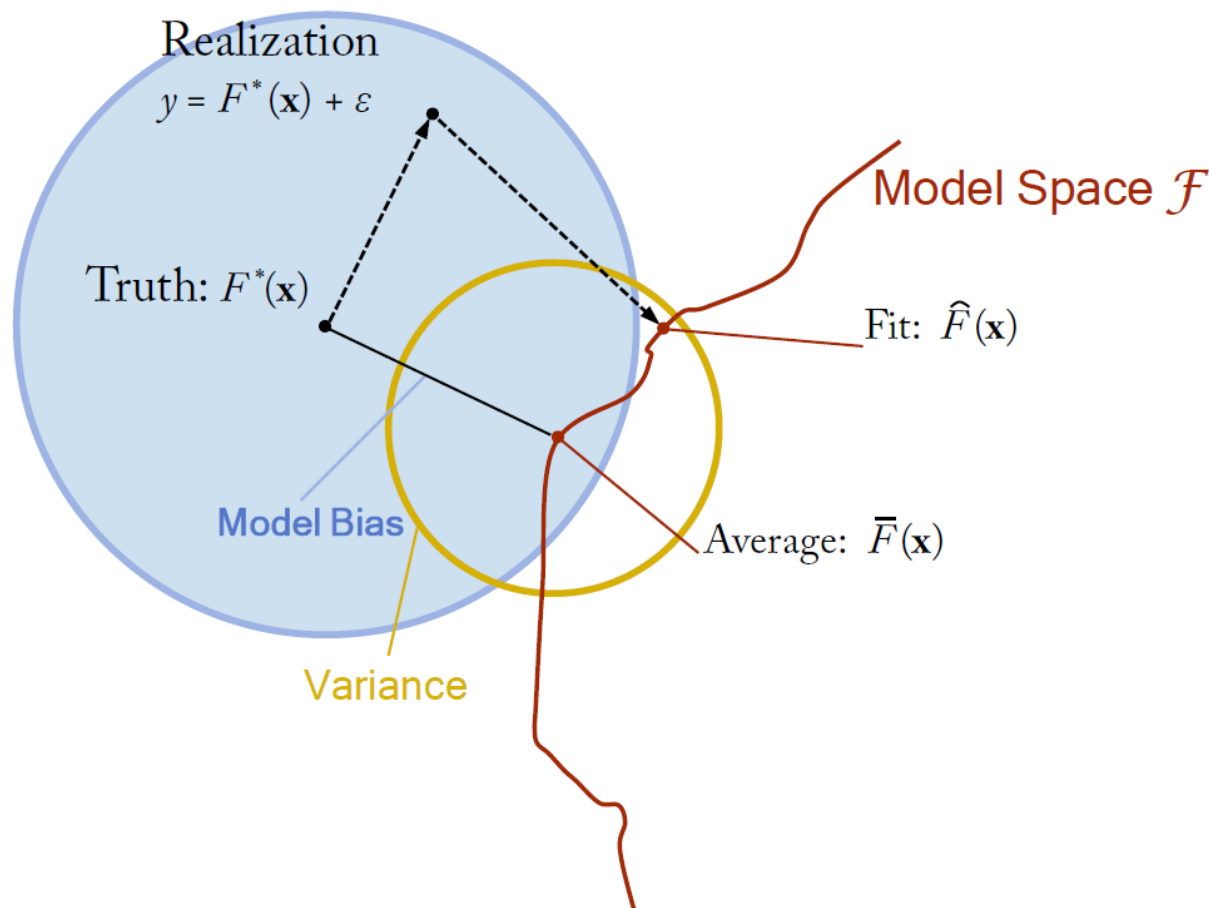
- Low variance: estimated function does not change much with different datasets
 - High variance implies a **weak** match

- ✓ Irreducible error: the error that was present in the original data

- ✓ Bias and variance are not independent of each other

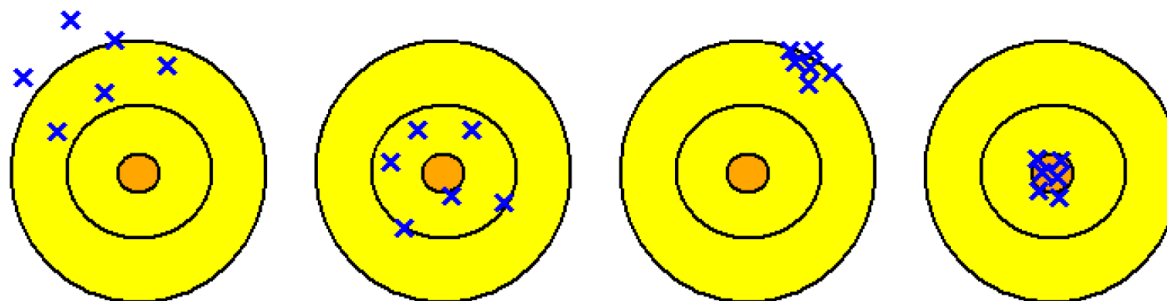
Theoretical Backgrounds: Bias-Variance Decomposition

- Graphical representation of Bias-Variance decomposition



Theoretical Backgrounds: Bias-Variance Decomposition

- Graphical representation of Bias-Variance decomposition



Bias	High	Low	High	Low
Variance	High	High	Low	Low

✓ Lower model complexity: high bias & low variance

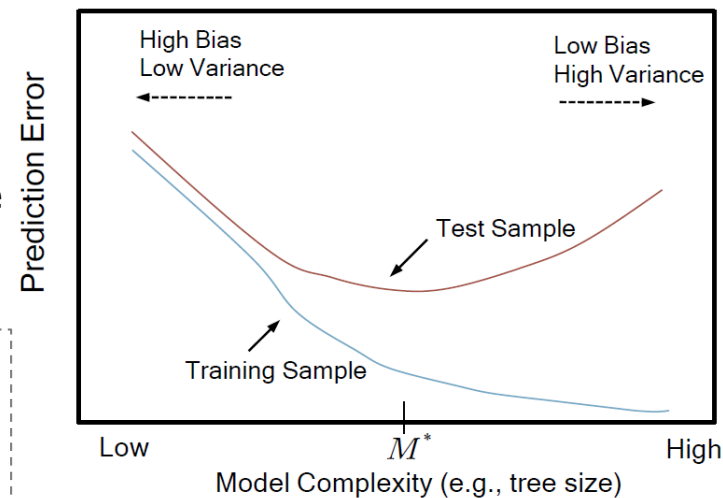
- Logistic regression, LDA, k-NN with large k, etc.

✓ Higher model complexity: low bias & high variance

- DT, ANN, SVM, k-NN with small k, etc.

Bias-Variance Dilemma

The more complex (flexible) we make the model,
the lower the bias but the higher the variance it is subjected to.

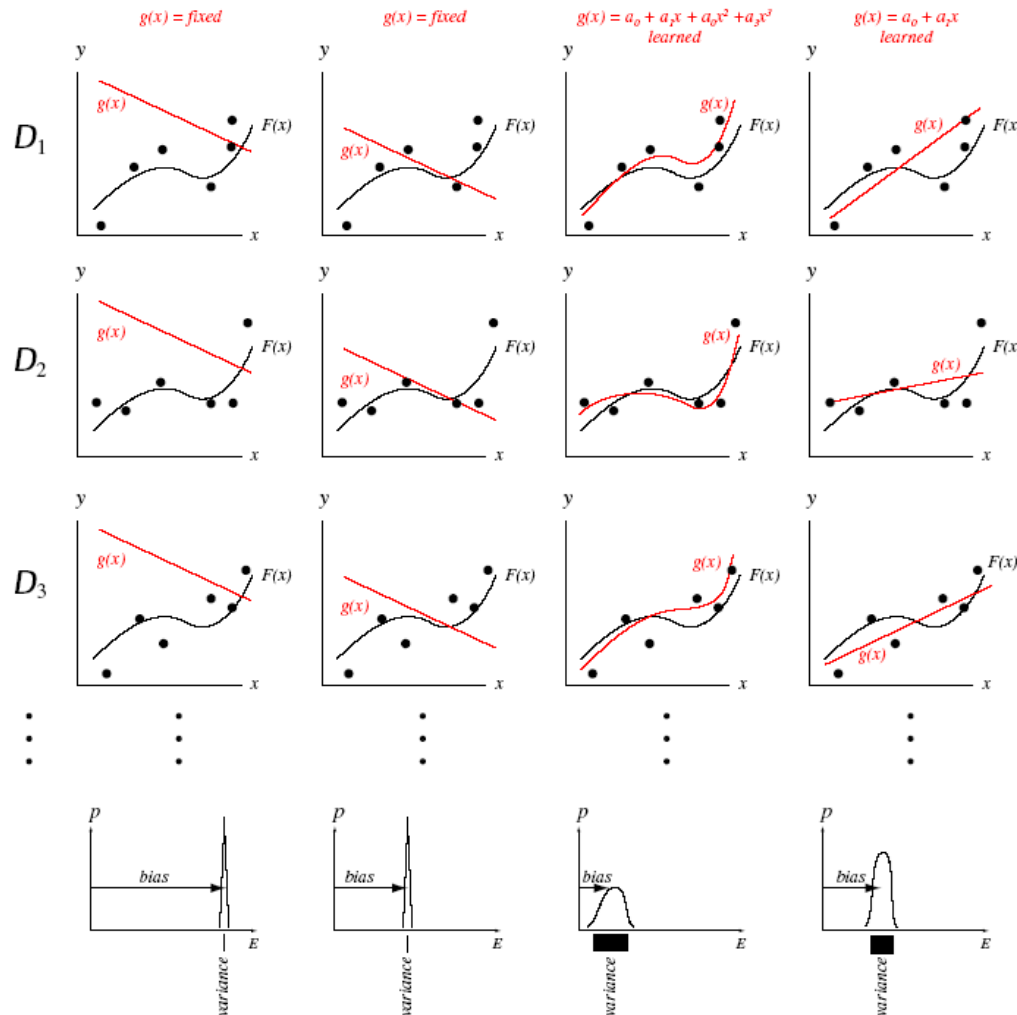


Theoretical Backgrounds: Bias-Variance Decomposition

- Bias-Variance example

Each column is a different model.

Each row is a different dataset of 6 points.



Histograms of mean-squared error of the fit.

Col 1:

Poor fixed linear model;
High bias, zero variance

Col 2:

Slightly better fixed linear model;
Lower (but high) bias,
zero variance.

Col 3:

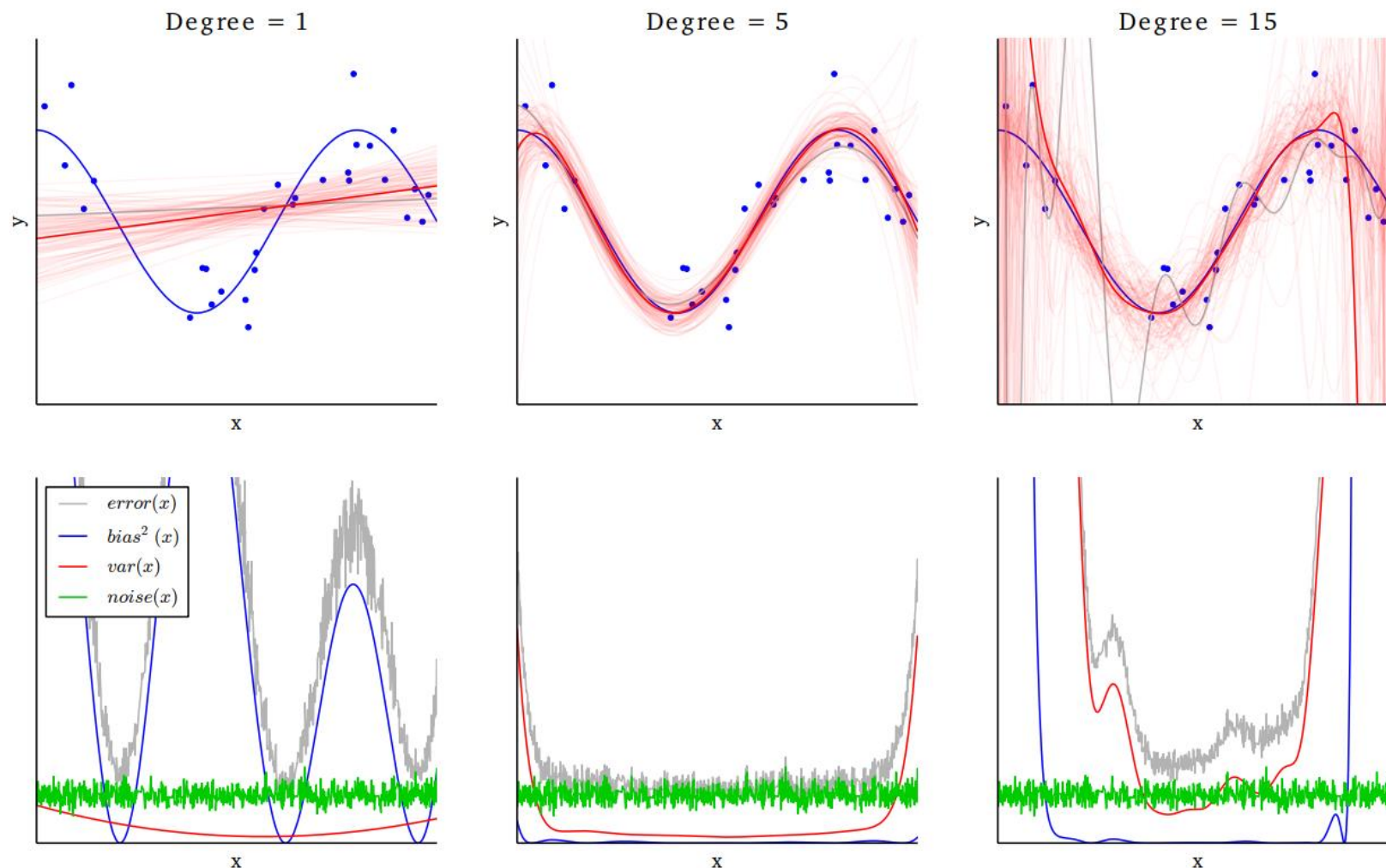
Learned cubic model;
Low bias, moderate variance.

Col 4:

Learned linear model;
Intermediate bias and variance.

Theoretical Backgrounds: Bias-Variance Decomposition

- Bias-Variance example



Purpose of Ensemble

- Goal: Reduce the error through constructing multiple learners to
 - ✓ Reduce the variance: Bagging, Random Forests
 - ✓ Reduce the bias: AdaBoost
 - ✓ Both: Mixture of experts
- Two key questions on the ensemble construction
 - ✓ Q1: How to generate individual components of the ensemble systems (base classifiers) to achieve sufficient degree of **diversity**?
 - ✓ Q2: How to **combine** the outputs of individual classifiers?

Ensemble Diversity

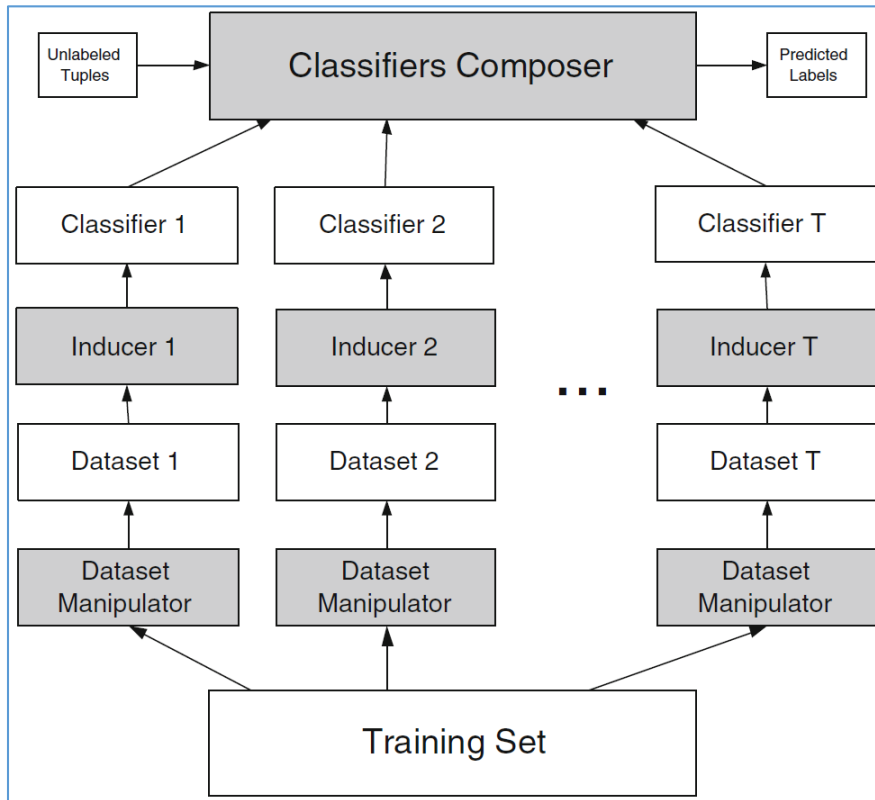
- Ensemble will have no gain from combining a set of identical models
 - ✓ Need base learners whose fitted functions are adequately different from those of others
 - ✓ Wish models to exhibit a **certain element of diversity** in their group behavior, though still **retaining good performance individually**.

Diversity	Implicit	Explicit
Description	Provide different random subset of the training data to each learner	Use some measurement ensuring it is substantially different from the other members
Ensemble Algorithms	Instance: Bagging Variables: Random Subspaces, Rotation Forests Both: Random Forests	Boosting, Negative Correlation Learning

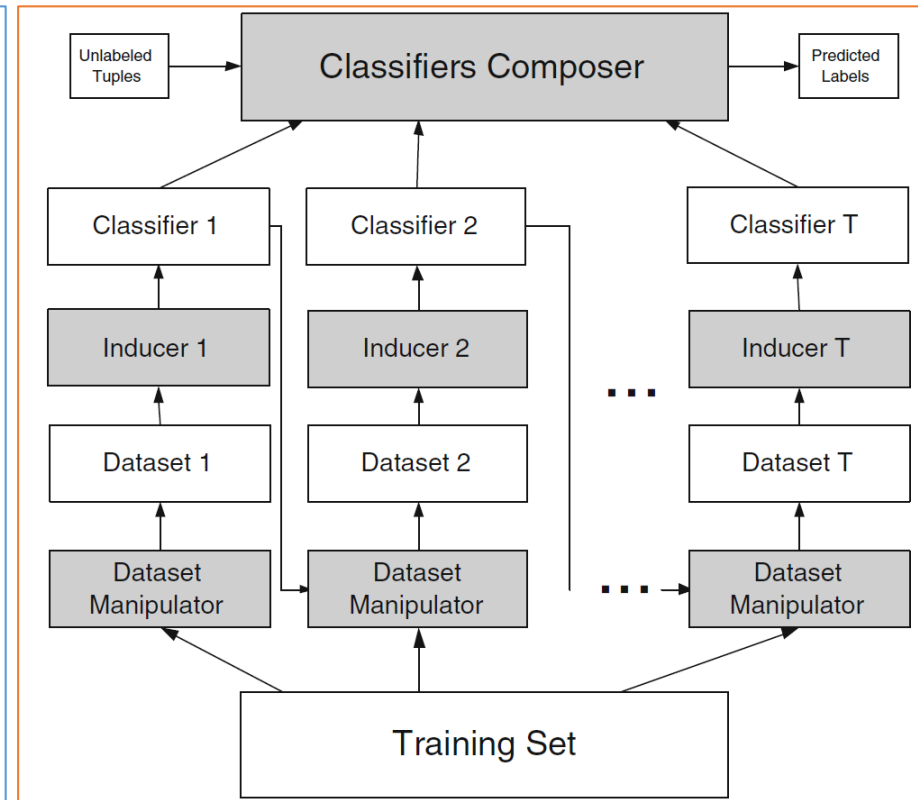
Ensemble Diversity

- Independent (implicit) vs. Model guided (explicit) instance selection

Independent instance selection



Model guided instance selection



Why Ensemble?

- Why Ensemble works?

- ✓ True functions, estimations, and the expected error

$$y_m(\mathbf{x}) = f(\mathbf{x}) + \epsilon_m(\mathbf{x}). \quad \mathbb{E}_{\mathbf{x}}[\{y_m(\mathbf{x}) - f(\mathbf{x})\}^2] = \mathbb{E}_{\mathbf{x}}[\epsilon_m(\mathbf{x})^2]$$

- ✓ The average error made by M individual models vs. Expected error of the ensemble

$$E_{Avg} = \frac{1}{M} \sum_{m=1}^M \mathbb{E}_{\mathbf{x}}[\epsilon_m(\mathbf{x})^2]$$

$$\begin{aligned} E_{Ensemble} &= \mathbb{E}_{\mathbf{x}} \left[\left\{ \frac{1}{M} \sum_{m=1}^M y_m(\mathbf{x}) - f(\mathbf{x}) \right\}^2 \right] \\ &= \mathbb{E}_{\mathbf{x}} \left[\left\{ \frac{1}{M} \sum_{m=1}^M \epsilon_m(\mathbf{x}) \right\}^2 \right] \end{aligned}$$

Why Ensemble?

- Why Ensemble works?

- ✓ Assume that the errors have **zero mean** and are **uncorrelated**,

$$\mathbb{E}_{\mathbf{x}}[\epsilon_m(\mathbf{x})] = 0, \quad \mathbb{E}_{\mathbf{x}}[\epsilon_m(\mathbf{x})\epsilon_l(\mathbf{x})] = 0 \quad (m \neq l)$$

- ✓ The average error made by **M individual models** vs. **Expected error of the ensemble**

$$E_{Ensemble} = \frac{1}{M} E_{Avg}$$

- ✓ In reality (errors are correlated), by the Cauchy's inequality

$$\left[\sum_{m=1}^M \epsilon_m(\mathbf{x}) \right]^2 \leq M \sum_{m=1}^M \epsilon_m(\mathbf{x})^2 \Rightarrow \left[\frac{1}{M} \sum_{m=1}^M \epsilon_m(\mathbf{x}) \right]^2 \leq \frac{1}{M} \sum_{m=1}^M \epsilon_m(\mathbf{x})^2$$

$$E_{Ensemble} \leq E_{Avg}$$

