**ModEvo: The Science**

**Our Program**

We have developed a code base, ModEvo, that implements a novel mathematical framework derived by Rice [8] for predicting the evolution of phenotypic traits that share at least some underlying developmental factors. Our updated models rely on a well-defined phenotype landscape to specify trait values as a function of underlying developmental factors [11]. Additionally, the object-oriented code base is generalized to allow users to easily develop custom models for studying the evolution of traits of an organism.

With our program, users can develop custom simulations for analyzing the evolution of multiple phenotypic traits by allowing non-additive developmental interactions between specific traits. Simulations of evolutionary processes using our updated framework may aid in the study of phenotypic evolution, multilevel selection, and social evolution for the fields of evolutionary developmental biology, quantitative genetics, and ecology [11, 8]. The simulations produced by ModEvo may be used to analyze the strength of selection on the co-variances of traits, as well as the constancy of the G-matrix by comparative analysis to traditional, G-matrix based models.

**Significance**

A primary goal of evolutionary biology is to predict the effect of selection on the evolution of traits. The multivariate evolutionary response of a population depends upon patterns of inheritance as well as the strength and direction of selection. The additive genetic variance-covariance matrix (G-matrix), which summarizes the distribution of genetic variance among multiple traits, is a central concept in evolutionary theory and quantitative genetics [1, 8, 7]. The geometry of the G-matrix quantifies genetic constraints that can hinder, facilitate, or bias evolution towards “genetic lines of least resistance,” the direction in which most genetic variation exists [14]. However, the predictive power of G-matrix based models depends upon the stability of the matrix, which is not clearly understood [2, 1, 14].

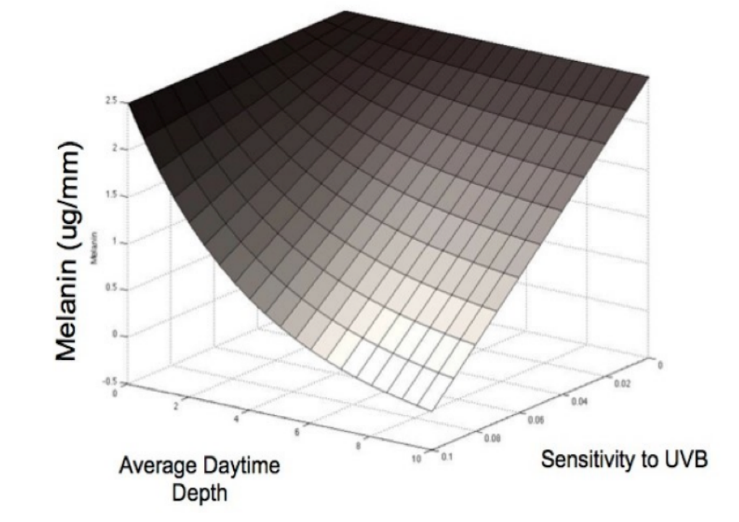
Shared developmental processes represent a principal contributor to the geometry of the G-matrix [15]. In fact, the G-matrix is generally assumed to efficiently and satisfactorily capture the developmental association between traits for the purposes of predicting evolutionary trajectories. To predict evolution in response to selection, the G-matrix is generally assumed to remain either constant or change proportionally to the original matrices [2, 1, 12]. However, nonadditive developmental interactions can dramatically alter genetic variances and co-variances of traits [3, 13], rendering approaches based on a constant G-matrix questionable [4, 5].

**Background**

A revolutionary mathematical and conceptual framework derived by Sean Rice [10, 9, 8, 16] explicitly incorporates the effect of non-additive developmental interactions on the evolution of traits. This framework encompasses quantitative genetics as a special case but is far more flexible, allowing for the exploration of the effects of different types of selection, under essentially any form of genetic and developmental architecture.

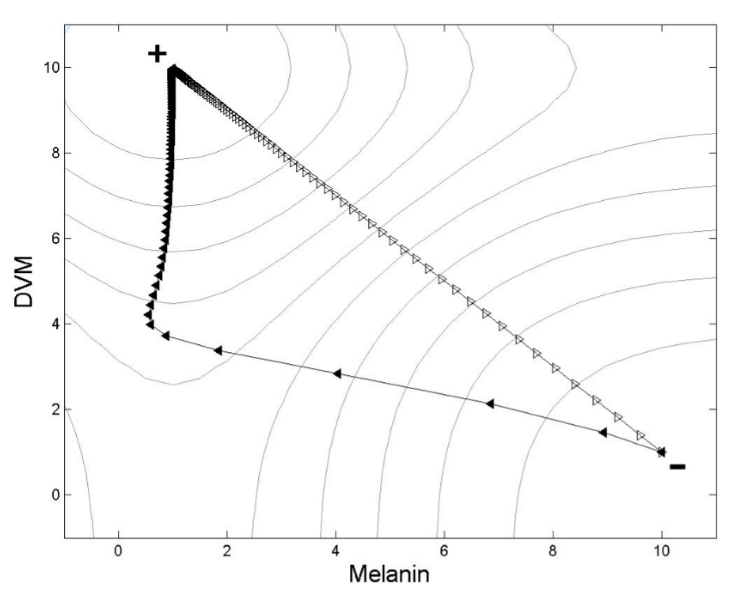
A central concept of the framework is the phenotypic landscape, which is constructed by plotting the value of a phenotype against the values of the underlying genetic and environmental factors that interact in its development [10].

The phenotypic landscape in Figure 1 shows the melanic pigmentation in *Daphnia melanica*, a species of freshwater zooplankton, as a function of average daytime depth (diel vertical migration, DVM) and sensitivity to induction via UVB radiation. The strength and direction of selection is captured by the individual fitness surface, which describes the expected reproductive success of an individual as a function of its trait values.

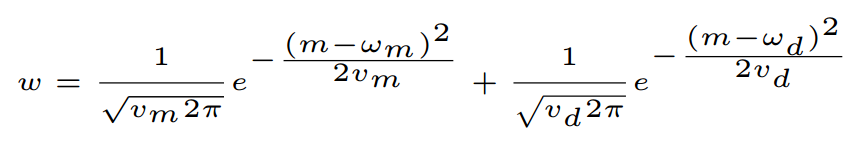


*Figure 1*

The fitness surface in Figure 2, given by the equation in Figure 3, depicts the expected fitness of *Daphnia melanica* in the presence of fish predators, based on its melanin pigmentation and tendency to move downward in the water column (DVM). As represented in Figure 2, there exists a value of those two traits such that a maximum fitness is attained, depicted by the peak (plus sign).



*Figure 2*



*Figure 3*

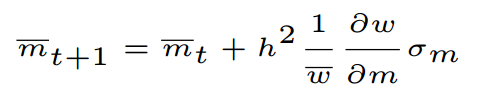
**Program Development**

We have developed an object-oriented code infrastructure that implements the mathematical framework of Sean Rice, allowing a user to test hypotheses regarding the evolutionary consequences of non-linear developmental interactions. As a case study, we have designed three models of increasing developmental complexity for predicting evolutionary trajectories specific to high-alpine populations of *Daphnia melanica*. ModEvo, can be extended to produce custom models for analyzing the evolution of trait means and co-variances for a given species of organisms and specific set of underlying genetic or environmental factors [10].

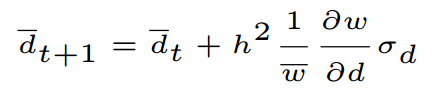
As a first step, we have developed in the Java programming language a traditional, G-matrix based model (Model One: Classic) for predicting the evolution of melanin (Figure 4) and DVM (Figure 5) over time, based on the current genetic co-variance of these traits and the natural selection imposed by the introduction of a novel fish predator. The variables and initial values used for testing Model One are given in Table 1.

|  |  |
| --- | --- |
| **Parameter** | **Initial Value** |
| Mean Melanin (ug/mm) | 2.5 |
| Mean DVM (meters) | 1 |
| Mean Population Fitness | N/A, Figure 3 |
| Phenotypic Variance of Melanin | 0.04 |
| Phenotypic Variance of DVM | 0.2 |
| Optimum Value of Melanin | 0.4 |
| Optimum Value of DVM | 12 |
| Variance of Gaussian Function Relating Melanin to Fitness | 100 |
| Variance of Gaussian Function Relating DVM to Fitness | 500 |
| Heritability | 0.5 |

*Table 1*



*Figure 4*

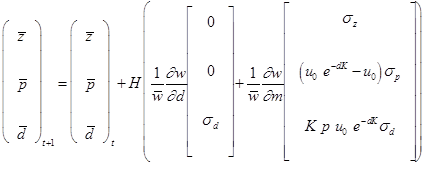


*Figure 5*

Next, we incorporated the updated mathematical and conceptual framework derived by Rice into two increasingly advanced models to account for “developmental entanglement” DVM (Figure 6) and melanin (Figure 7). In the second model (Model Two: Tanning), developmental entanglement arises from the fact that DVM influences exposure to UV radiation, which decays exponentially with depth in the water, and UV radiation stimulates production of melanin. The variables and initial values used for testing Model Two are given in Table 2.

|  |  |
| --- | --- |
| **Parameter** | **Initial Value** |
| Mean Melanin (ug/mm) | 2.5 |
| Mean DVM (meters) | 1 |
| Mean Population Fitness | N/A, Figure 3 |
| Mean Slope of Reaction Norm of Melanin with Respect to UVB | 0 |
| Mean Intercept of Reaction Norm of Melanin with Respect to UVB | 2.5 |
| Phenotypic Variance of Melanin | 0.04 |
| Phenotypic Variance of DVM | 0.2 |
| Optimum Value of Melanin | 0.4 |
| Optimum Value of DVM | 12 |
| Variance of Gaussian Function Relating Melanin to Fitness | 100 |
| Variance of Gaussian Function Relating DVM to Fitness | 500 |
| Heritability | 0.5 |
| Attenuation Coefficient | 0.26 |
| UVB Dose at Water Surface | 27.9 W-h/m2 |

*Table 2*



*Figure 6*

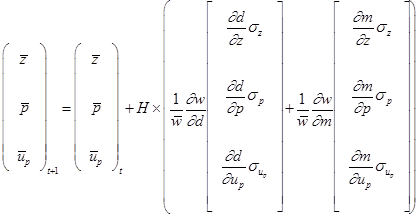
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*Figure 7*

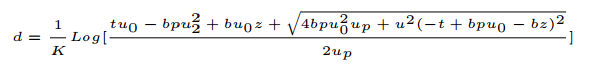
The third model (Model Three: Tolerance) extends this entanglement (Figure 8) by allowing DVM (Figure 9) to be determined by behavioral avoidance of UV penetration, which is itself partially determined by melanin (Figure 10). The variables and initial values used for testing Model Three are given in Table 3.

|  |  |
| --- | --- |
| **Parameter** | **Initial Value** |
| Mean Melanin (ug/mm) | N/A, Figure 10 |
| Mean DVM (meters) | N/A, Figure 9 |
| Mean Population Fitness | N/A, Figure 3 |
| Mean Slope of Reaction Norm of Melanin with Respect to UVB | 0 |
| Mean Intercept of Reaction Norm of Melanin with Respect to UVB | 2.5 |
| Mean Preference for UV Penetration of the Carapace | 10 W-h/m2 |
| Phenotypic Variance of Intercept | 0.2 |
| Phenotypic Variance of Slope | 0.04 |
| Phenotypic Variance of Preference for UV Penetration | 0.5 |
| Optimum Value of Melanin | 0.4 |
| Optimum Value of DVM | 12 |
| Variance of Gaussian Function Relating Melanin to Fitness | 100 |
| Variance of Gaussian Function Relating DVM to Fitness | 500 |
| Heritability | 0.5 |
| Attenuation Coefficient | 0.26 |
| UVB Dose at Water Surface | 27.9 W-h/m2 |
| Transmittance of Non-Melanized Daphnia | 0.8 |
| Slope Relating Concentration of Melanin to Change in UVB Transmittance | -0.16 |

*Table 3*



*Figure 8*



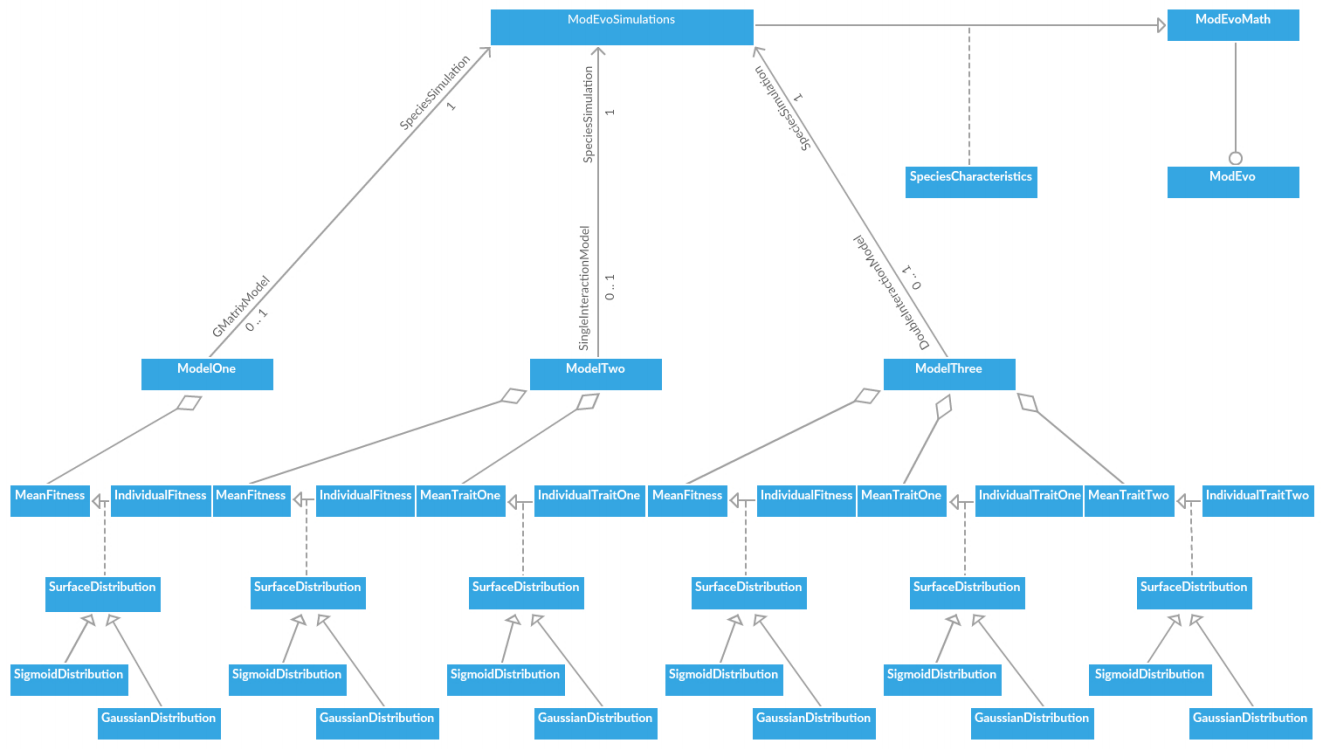
*Figure 9*

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*Figure 10*

Models Two and Three incorporate underlying developmental factors to project changes from generation *t* to generation *t*+1 due to directional selection. Evolutionary dynamics depend upon the partial derivatives of the phenotypic landscape, which is constructed by plotting trait values as a function of underlying developmental factors, and partial derivatives of the fitness landscape, which is constructed by plotting the fitness values as a function of the two traits under investigation.

All three models are deterministic. However, mean population values and derivatives of the phenotypic landscape for Model Three are estimated via simulation, due to the complexity of the set of biologically relevant roots used for the system of equations describing these traits. These mean trait values are then passed to the functions that calculate the new mean values in the next generation; this iterative process is used to predict the evolutionary response of both traits and is shown in the class structure diagram for ModEvo (Figure 11).



*Figure 11*

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