

## Problem 60-1

David Gieseeman

November 2020

**1**    $3n^2 + 2n + 1 = O(n^2)$

When we apply the first definition of  $O$  we get  $\lim_{x \rightarrow \infty} \frac{3n^2 + 2n + 1}{n^2}$ . You do L'Hospital's rule twice and you find that it converges to 3.

**2**    $O(f + g) = O(\max(f, g))$

$h = O(f+g)$  so  $h$

**3**    $O(f * g) = O(f) * O(g)$

**4**   **If  $f = O(g)$  and  $g = O(h)$  then  $f = O(h)$**

For some constant  $k$ ,  $f(n) < c * g(n) < k * h(n)$  therefore  $f(n) < k * h(n)$  and  $f = O(h)$ .