# The amsmath package

Frank Mittelbach Rainer Schöpf Michael Downes David M. Jones

Version 2.13, 2000/07/18

### 1 Introduction

A LATEX package named amstex was created in 1988–1989 by adapting amstex.tex for use within LATEX. The amsmath package is the successor of the amstex package. It was substantially overhauled to integrate it with LATEX2e, which arrived on the scene in 1994. It provides more or less the same features, but there are quite a few organizational differences as well as some new features and bug fixes. For example, the amstex package automatically loaded the amsfonts package, but the amsmath package does not. At the present time (November 1999) user-level documentation of the commands provided here is found in the AMSmath Users' Guide, amsldoc.tex.

Standard file identification.

- 1 \NeedsTeXFormat{LaTeX2e}% LaTeX 2.09 can't be used (nor non-LaTeX)
- 2 [1994/12/01]% LaTeX date must be December 1994 or later
- 3 \ProvidesPackage{amsmath}[2000/07/18 v2.13 AMS math features]

### 2 Catcode defenses

Some packages change the catcode of characters that are essential in low-level TEX syntax. Any package that does so does not qualify as a PWWO package ("Plays Well With Others") because it can cause other packages to fail if they are loaded later. LATEX is partly to blame for this because it fails to provide adequate built-in safeguards in the package loading mechanisms. In the absence of such safeguards, we will provide them here.

```
4 \edef\@temp{\catcode 96=\number\catcode 96 }
5 \catcode\string '\'=12
6 \def\do#1{\catcode\number'#1=\number\catcode'#1}
7 \edef\@temp{%
    \noexpand\AtEndOfPackage{%
      \do''\do''\do'(\do')\do'*\do'+\do',\do'-\do'.%
10
      \do /\do =\do >\do (\do )^\do /\relax
11
12
    }%
13 }
14 \@temp
15 \def\do#1{\catcode\number'#1=12 }
16 \do''\do''\do''\do''\do'+\do',\do'-\do'.
17 \do\/\do\=\do\>\do\[\do\]
18 \catcode'\^=7 \catcode'\_=8
```

## 3 Declare some options

Handling of limits on integrals, sums, operatornames.

- 20 \DeclareOption{nointlimits}{\let\ilimits@\nolimits}

```
21 \DeclareOption{sumlimits}{\let\slimits@\displaylimits}
22 \DeclareOption{nosumlimits}{\let\slimits@\nolimits}
23 \DeclareOption{namelimits}{\PassOptionsToPackage{namelimits}{\mathbf{Amsopn}}}
24 \DeclareOption{nonamelimits}{\mathbf{M}}
25 \PassOptionsToPackage{nonamelimits}{\mathbf{amsopn}}}
```

The following two switches might have been defined already by the document class, but it doesn't hurt to re-execute the \newif's.

```
26 \newif\ifctagsplit@
27 \newif\iftagsleft@
```

Right or left placement of equation numbers.

```
28 \DeclareOption{leqno}{\tagsleft@true}
29 \DeclareOption{reqno}{\tagsleft@false}
30 \DeclareOption{centertags}{\ctagsplit@true}
31 \DeclareOption{tbtags}{\ctagsplit@false}
```

The cmex10 option is an escape hatch for people who don't happen to have sizes 7–9 of the cmex fonts available to them yet. (Strictly speaking they are considered part of a minimum LATEX distribution now, i.e., all LATEX  $2_{\varepsilon}$  users should have them, without needing to get the AMSFonts distrib.)

```
32 \DeclareOption{cmex10}{%
33 \ifnum\cmex@opt=\@ne \def\cmex@opt{0}}%
34 \else \def\cmex@opt{10}\fi
35 }
```

To help things work out better with various package loading orders of amsmath and amsfonts, we establish a variable to communicate the status of the cmex font definition. If the amsfonts package was loaded first this variable might be already defined, in which case we want to preserve its value.

 $36 \verb|\defined{cmex@opt}{\def\cmex@opt{7}}{} \\$ 

# 4 Flush-left equations [DMJ]

The left margin of math environments is controlled by \@mathmargin. This can be set to \@centering to implement the default behaviour, i.e., centered equations, and to something else to implement the flushleft style.

In theory, all that's needed to activate the flushleft mode in the AMS document classes is something like this:

```
\DeclareOption{fleqn}{%
  \AtBeginDocument{\@mathmargin30pt\relax}%
}
```

(In fact, unless the document class wants to specify the \@mathmargin, it doesn't need to do anything with the fleqn option.)

```
37 \newif\if@fleqn
38 %
39 \newskip\@mathmargin
40 \@mathmargin\@centering
41 %
42 \DeclareOption{fleqn}{%
43
       \@fleqntrue
       \mbox{Qmathmargin} = -1sp
44
       \let\mathindent=\@mathmargin
45
       \AtBeginDocument{%
47
           \ifdim\@mathmargin= -1sp
48
                \@mathmargin\leftmargini minus\leftmargini
49
           \fi
      }%
50
```

51 }

DMJ: This ensures that \@mathmargin is given some sort of sensible default if the class doesn't specify one, while still allowing a user to override the default value in their document preamble. (Incidentally, I'm initializing \@mathmargin to \leftmargini for compatibility with fleqn.clo, but I'm not at all convinced that's the right thing to do.)

The next question is what happens when amsmath is used with one of the standard classes. Unfortunately, IATEX implements fleqn somewhat clumsily; instead of paramaterizing the definitions of the math structures (as I've attempted to do here), fleqn.clo declares a dimen \mathindent that is much like my \@mathmargin and then redefines \[ [, \] , \equation, and \equarray. This means that things could get rather messy in 2.09 compatibility mode, since fleqn.clo might be loaded after amsmath.sty, which could cause a real mess.

[mjd,1999/07/07]: Let \mathindent = \@mathmargin as envisioned by DMJ. Compatibility-mode documents will all use the amstex package, not amsmath. There is a remote chance of a problem if someone makes an assignment to \mathindent in a way that implicitly assumes it is a dimen register (inasmuch as it has now become a skip register), and the string "plus" follows in the input stream, but if someone's document croaks in that way, I think they will just have to bite the bullet and fix it. The alternative is to penalize a lot of other users with a known handicap.

- 52 \DeclareOption{?}{}
- 53 \ExecuteOptions{nointlimits, sumlimits, namelimits, centertags}

The \par after \ProcessOptions is to ensure the correct line number on screen if an error occurs during option processing; otherwise the lookahead for a \* option would result in TeX showing the following line instead.

```
54 \ProcessOptions\par
```

```
55 \@ifpackagewith{amsmath}{?}{%
56 \typeout{^^J%
57 Documentation for the amsmath package is found in amsldoc.dvi^^J%
58 \text{ (or .pdf or .tex).}^{58}
59 ^^J%
60 See also http://www.ams.org/tex/amslatex.html.^^J%
62 Note: Using the first edition of The LaTeX Companion (1994) without \^J\%
63 errata as a guide for amsmath use is not recommended.^^J%
64
    }%
65 }{%
    \typeout{%
66
67 For additional information on amsmath, use the \lq ?\rq\space option.%
68
69 }
```

Processing to handle the cmex10 option is a little tricky because of different possible loading orders for amsmath and amsfonts. The package amsmath sets the \cmex0opt flag to 7 or 10, and the package amsfonts sets the flag to 1 or 0.

Force reloading of the OMX/cmex font definition file.

```
78 \begingroup
79 \fontencoding{OMX}\fontfamily{cmex}%
80 \expandafter\let\csname OMX+cmex\endcsname\relax
81 \try@load@fontshape
82 \endgroup
```

The cmex10 font gets special preload handling in the building of the LATEX format file, need an extra bit here to work around that.

```
83 \expandafter\let\csname OMX/cmex/m/n/10\endcsname\relax
84 \def\cmex@opt{10}%
85 \fi
86 \fi
```

## 5 Call some other packages

The amstext package provides the \text command. The amsbsy package provides \boldsymbol and \pmb. (Since 1997 it is usually better to use the bm package instead; but I think we have to keep amsbsy here for backward compatibility [mjd,1999/11/19].) The amsopn package provides \DeclareMathOperator.

```
87 \RequirePackage{amstext}[1995/01/25]
88 \RequirePackage{amsbsy}[1995/01/20]
89 \RequirePackage{amsopn}[1995/01/20]
```

### 6 Miscellaneous

\@amsmath@err

Defining this error function saves main mem.

90 \def\@amsmath@err{\PackageError{amsmath}}

\AmS The \AmS prefix can be used to construct the combination \AmS-\LaTeX.

```
91 \providecommand{\AmS}{{\protect\AmSfont 92 A\kern-.1667em\lower.5ex\hbox{M}\kern-.125emS}}
```

In \AmSfont we call cmsy directly in lieu of trying to access it through the math fonts setup (e.g. \the\textfont2) because math fonts can't be relied on to be properly set up if we are not inside a math formula. This means that if this command is used in a document where CM fonts are not wanted, then a font substitution will need to be declared, e.g.:

where xxx is some alternate font family. Taking the first letter of \f@series will produce b or m for the most common values (b,bx,m). It may produce nonsense for more unusual values of \f@series, so for safety's sake we have an additional \if test. We want to avoid setting the series to bx because in a standard LATEX installation the combination cmsy/bx/n does not have a font definition, and the user would get a font substitution warning on screen.

```
93 \newcommand{\AmSfont}{%
94 \usefont{OMS}{cmsy}{\if\@xp\@car\f@series\@nil bb\else m\fi}{n}}
```

 $\0$ mathmeasure

The function \@mathmeasure takes three arguments; the third arg is typeset as a math formula in an hbox, using arg #2 as the mathstyle, and the result is left in the box named by the first arg. It is assumed that we are already in math mode, so we can turn off \everymath (in particular, \check@mathfonts).

```
95 \end{2} \end{2} $95 \end{2} \end{
```

6. MISCELLANEOUS 5

The \inf@bad constant is for testing overfull boxes.

```
97 \@ifundefined{inf@bad}{%

98 \newcount\inf@bad \inf@bad=1000000 \relax

99 }{}
```

### 6.1 Math spacing commands

Here we fill in some gaps in the set of spacing commands, and make them all work equally well in or out of math. We want all these commands to be robust but declaring them all with \DeclareRobustCommand uses up an control sequence name per command; to avoid this, we define a common command \tmspace (text-or-math space) which carries the robustness burden for all of them. The standard \relax before the \iffmode is not necessary because of the \protect added by \DeclareRobustCommand.

```
100 \DeclareRobustCommand{\tmspace}[3]{%
101 \ifnmode\mskip#1#2\else\kern#1#3\fi\relax}
102 \renewcommand{\,}{\tmspace+\thinmuskip{.1667em}}
103 \let\thinspace\,
104 \renewcommand{\!}{\tmspace-\thinmuskip{.1667em}}
105 \let\negthinspace\!
106 \renewcommand{\:}{\tmspace+\medmuskip{.2222em}}
107 \let\medspace\:
108 \newcommand{\negmedspace}{\tmspace-\medmuskip{.2222em}}
109 \renewcommand{\;}{\tmspace+\thickmuskip{.2777em}}
110 \let\thickspace\;
111 \newcommand{\negthickspace}{\tmspace-\thickmuskip{.2777em}}
```

And while we're at it, why don't we provide an equivalent of hspace for math mode use. This allows use of mu units in (for example) constructing compound math symbols.

112  $\med{\mspace}[1]{\mskip#1\relax}$ 

### 6.2 Vertical bar symbols

Add left/right specific versions of \vert, \Vert. Don't assume the delimiter codes are the CM defaults.

```
113 \def\@tempa#1#2\@nil{%
114 \ifx\delimiter#1\@tempcnta#2\relax\else\@tempcnta\z@\fi
115 }
116 \@xp\@tempa\vert\@empty\@nil
117 \ifnum\@tempcnta>\z@
    \advance\@tempcnta "4000000
118
     \xdef\lvert{\delimiter\number\@tempcnta\space }
119
     \advance\@tempcnta "1000000
120
121 \xdef\rvert{\delimiter\number\@tempcnta\space }
122 \else
     \ifx\@@undefined\lvert
123
       % Fall back to cmex encoding since we don't know what else to do.
124
       \DeclareMathDelimiter{\lvert}
         {\mathopen}{symbols}{"6A}{largesymbols}{"0C}
126
       \DeclareMathDelimiter{\rvert}
127
         {\mathclose}{symbols}{"6A}{largesymbols}{"0C}
128
    \fi
129
130 \fi
131 \@xp\@tempa\Vert\@empty\@nil
132 \ifnum\@tempcnta>\z@
133
    \advance\@tempcnta "4000000
     \xdef\lVert{\delimiter\number\@tempcnta\space }
    \advance\@tempcnta "1000000
```

#### 6.3 Fractions

Bury the generalized fraction primitives \over, \atop, etc., because of their bizarre syntax, which is decidedly out of place in a LATEX document.

```
145 \@saveprimitive\over\@@over
146 \@saveprimitive\atop\@@atop
147 \@saveprimitive\above\@@above
148 \@saveprimitive\overwithdelims\@@overwithdelims
149 \@saveprimitive\atopwithdelims\@@atopwithdelims
150 \@saveprimitive\abovewithdelims\@@abovewithdelims
```

If someone insists on using **\over**, give a warning the first time and then resurrect the old definition. Laissez-faire policy.

```
151 \DeclareRobustCommand{\primfrac}[1]{%
     \PackageWarning{amsmath}{%
153 Foreign command \@backslashchar#1;\MessageBreak
154 \protect\frac\space or \protect\genfrac\space should be used instead%
155 \MessageBreak
156 }
     \global\@xp\let\csname#1\@xp\endcsname\csname @@#1\endcsname
157
     \csname#1\endcsname
158
159 }
160 \renewcommand{\over}{\primfrac{over}}
161 \renewcommand{\atop}{\primfrac{atop}}
162 \renewcommand{\above}{\primfrac{above}}
163 \renewcommand{\overwithdelims}{\primfrac{overwithdelims}}
164 \enskip {\tt primfrac\{atopwithdelims\}} \\
165 \renewcommand{\abovewithdelims}{\primfrac{abovewithdelims}}
```

\frac calls \@@over directly instead of via \genfrac, for better speed because it is so common. \tfrac and \dfrac are abbreviations for some commonly needed mathstyle overrides. To conserve csnames we avoid making \dfrac and \tfrac robust (\genfrac is itself robust).

The \binom command for binomial notation works like \frac and has similar variants. Note that we do not use \z@ in \dbinom and \tbinom because they are not top-level robust like \binom, and so the \z@ with the potentially problematic @ character would become visible when writing one of those commands to a .toc file.

```
169 \DeclareRobustCommand{\binom}{\genfrac()\z0{}} 170 \newcommand{\dbinom}{\genfrac(){0pt}0} 171 \newcommand{\tbinom}{\genfrac(){0pt}1}
```

\genfrac

This command provides access to TEX's generalized fraction primitives. Args: #1 left delim, #2 right delim, #3 line thickness, #4 mathstyle override, #5 numerator, #6 denominator. But we only read the first four args at first, in order to give us a moment to select the proper generalized fraction primitive. Any

6. MISCELLANEOUS 7

of those four args could be empty, and when empty the obvious defaults are selected (no delimiters, default line thickness (normally .4pt), and no mathstyle override).

```
172 \DeclareRobustCommand{\genfrac}[4]{%
173 \def\0tempa{#1#2}%
174 \edef\0tempb{\0nx\0genfrac\0mathstyle{#4}%
175 \csname 00\ifx 0#30over\else above\fi
176 \ifx\0tempa\0empty \else withdelims\fi\endcsname}
177 \0tempb{#1#2#3}}
```

**\@genfrac** takes the preceding arguments and reads the numerator and denominator. Note that there's no convenient way to make the numerator and denominator *contents* displaystyle, through this interface.

Args: #1 mathstyle, #2 fraction primitive, #3 delimiters and rule thickness, #4 numerator, #5 denominator.

```
178 \end{figure} 178
```

Empty mathstyle arg: no change; 0 = displaystyle, 1 = textstyle, 2 = script-style, 3 = scriptscriptstyle.

```
179 \def\@mathstyle#1{%

180 \ifx\@empty#1\@empty\relax

181 \else\ifcase#1\displaystyle % case 0

182 \or\textstyle\or\scriptstyle\else\scriptscriptstyle\fi\fi}
```

### 6.4 Sums and Integrals

Default value for sum limits is \displaylimits, see option 'nosumlimits'.

We redefine all the cumulative operator symbols to use \slimits@ so that switching between \displaylimits and \nolimits can be controlled by package options. Also add \DOTSB for the benefit of the dots lookahead. But we'd better make sure \coprod and the others are simple mathchars; if not, the attempted changes will probably fail miserably.

```
183 \begingroup
184 \edef\@tempa{\string\mathchar"}
185 \def\@tempb#1"#2\@ni1{#1"}
186 \edef\@tempc{\expandafter\@tempb\meaning\coprod "\@nil}
187 \ifx\@tempa\@tempc
     \global\let\coprod@\coprod
188
     \gdef\coprod{\DOTSB\coprod@\slimits@}
189
     \global\let\bigvee@\bigvee
190
     \gdef\bigvee{\DOTSB\bigvee@\slimits@}
191
     \global\let\bigwedge@\bigwedge
192
     \gdef\bigwedge{\DOTSB\bigwedge@\slimits@}
193
194
     \global\let\biguplus@\biguplus
     \gdef\biguplus{\DOTSB\biguplus@\slimits@}
195
     \global\let\bigcap@\bigcap
196
     \gdef\bigcap{\DOTSB\bigcap@\slimits@}
197
     \global\let\bigcup@\bigcup
198
     \gdef\bigcup{\DOTSB\bigcup@\slimits@}
199
200
     \global\let\prod@\prod
     \gdef\prod{\DOTSB\prod@\slimits@}
201
     \global\let\sum@\sum
202
     \gdef\sum{\DOTSB\sum@\slimits@}
203
     \global\let\bigotimes@\bigotimes
204
     \gdef\bigotimes{\DOTSB\bigotimes@\slimits@}
205
     \global\let\bigoplus@\bigoplus
206
     \gdef\bigoplus{\DOTSB\bigoplus@\slimits@}
207
     \global\let\bigodot@\bigodot
208
     \gdef\bigodot{\DOTSB\bigodot@\slimits@}
209
```

```
210 \global\let\bigsqcup@\bigsqcup
211 \gdef\bigsqcup{\DOTSB\bigsqcup@\slimits@}
212 \fi
213 \endgroup
```

#### 6.5 Roots and radicals

This root stuff needs syntax work and implementation work. Surely something more compact can be done?? [mjd, 1994/09/05]

```
215 \newcommand{\uproot}{\@amsmath@err{\Invalid@@\uproot}\@eha}
216 \newcount\uproot@
217 \newcount\leftroot@
218 \renewcommand{\root}{\relaxnext@
    \DN@{\ifx\@let@token\uproot\let\next@\nextii@\else
     \ifx\@let@token\leftroot\let\next@\nextiii@\else
221
      \let\next@\plainroot@\fi\fi\next@}%
222
     \def\nextii@\uproot##1{\uproot@##1\relax\FN@\nextiv@}%
     \def\nextiv@{\ifx\@let@token\@sptoken\DN@. {\FN@\nextv@}\else
     \DN0.{\FN0\nextv0}\fi\next0.}%
224
225
    \def\nextv@{\ifx\@let@token\leftroot\let\next@\nextvi@\else
226
     \let\next@\plainroot@\fi\next@}%
    \def\nextvi@\leftroot##1{\leftroot@##1\relax\plainroot@}%
227
     \def\nextiii@\leftroot##1{\leftroot@##1\relax\FN@\nextvii@}%
228
    \def\nextvii@{\ifx\@let@token\@sptoken
229
     \DN@. {\FN@\nextviii@}\else
230
     \DN@.{\FN@\nextviii@}\fi\next@.}%
231
    \def\nextviii@{\ifx\@let@token\uproot\let\next@\nextix@\else
     \let\next@\plainroot@\fi\next@}%
234
    \def\nextix@\uproot##1{\uproot@##1\relax\plainroot@}%
    \bgroup\uproot@\z@\leftroot@\z@\FN@\next@}
236 \def\plainroot@#1\of#2{\setbox\rootbox\hbox{%
237 $\m@th\scriptscriptstyle{#1}$}%
238 \mathchoice{\r@@t\displaystyle{#2}}{\r@@t\textstyle{#2}}
239 {\r@@t\scriptstyle{#2}}{\r@@t\scriptscriptstyle{#2}}\egroup}
```

Name change from \@@sqrt to \sqrtsign happened in the 1995/12/01 release of IATEX. If we were to assume that \sqrtsign is defined then someone with the 1995/06/01 release of IATEX would have trouble using this package.

```
240 \@ifundefined{sqrtsign}{\let\sqrtsign\@@sqrt}{}
241 \def\r@@t#1#2{\setboxz@h{$\m@th#1\sqrtsign{#2}$}%
242 \dimen@\ht\z@\advance\dimen@-\dp\z@
243 \setbox\@ne\hbox{$\m@th#1\mskip\uproot@ mu$}%
244 \advance\dimen@ by1.667\wd\@ne
245 \mkern-\leftroot@ mu\mkern5mu\raise.6\dimen@\copy\rootbox
246 \mkern-10mu\mkern\leftroot@ mu\boxz@}
```

#### 6.6 Et cetera

Specific names for the variant italic cap Greek letters are not defined by LATEX. If no preceding package defined these, we will define them now.

```
247 \@ifundefined{\varGamma}{\%
248 \DeclareMathSymbol{\varGamma}{\mathord}{letters}{"00}\
249 \DeclareMathSymbol{\varDelta}{\mathord}{letters}{"01}\
250 \DeclareMathSymbol{\varTheta}{\mathord}{letters}{"02}\
251 \DeclareMathSymbol{\varLambda}{\mathord}{letters}{"03}\
252 \DeclareMathSymbol{\varXi}{\mathord}{letters}{"04}\
253 \DeclareMathSymbol{\varPi}{\mathord}{letters}{"05}\
254 \DeclareMathSymbol{\varSigma}{\mathord}{letters}{"06}\
255 \DeclareMathSymbol{\varUpsilon}{\mathord}{letters}{"07}\
256 \DeclareMathSymbol{\varPhi}{\mathord}{letters}{"08}\
257 \DeclareMathSymbol{\varPhi}{\mathord}{letters}{"08}\
258 \DeclareMathSymbol{\varPhi}{\mathord}{letters}{"08}\
259 \DeclareMathSymbol{\varPhi}{\mathord}{letters}{"08}\
250 \DeclareMathSymbol{\varPhi}{\mathord}{letters}{"08}\
250 \DeclareMathSymbol{\varPhi}{\mathord}{letters}{"08}\
251 \DeclareMathSymbol{\varPhi}{\mathord}{letters}{"08}\
252 \DeclareMathSymbol{\varPhi}{\mathord}{letters}{"08}\
253 \DeclareMathSymbol{\varPhi}{\mathord}{letters}{"08}\
254 \DeclareMathSymbol{\varPhi}{\mathord}{letters}{"08}\
255 \DeclareMathSymbol{\varPhi}{\mathord}{letters}{"08}\
256 \DeclareMathSymbol{\varPhi}{\mathord}{letters}{"08}\
```

7. ELLIPSIS DOTS 9

```
257 \DeclareMathSymbol{\varPsi}{\mathord}{letters}{"09}  
258 \DeclareMathSymbol{\varOmega}{\mathord}{letters}{"0A}  
259 }{}
```

 $\mathcal{A}_{\mathcal{M}}\mathcal{S}$ -TEX redefines **\overline** as shown here, for reasons that are probably less important in LATEX: Make it read its argument as a macro argument rather than a "math field" (*The TeXbook*, Chapter 26), to avoid problems when something that is apparently a single symbol is actually a non-simple macro (e.g., \dag) and is given as a single-token argument without enclosing braces.

```
260 \@saveprimitive\overline \@@overline 261 \DeclareRobustCommand{\overline}[1]{\@@overline{#1}}
```

The \boxed command is specifically intended to put a box around an equation or piece of an equation. (Not including the equation number.) This isn't trivial for end-users to do it properly with \fbox so we provide a command for them.

```
262 \newcommand{\boxed}[1]{\fbox{\m@th$\displaystyle#1$}}
263 \newcommand{\implies}{\DOTSB\;\Longrightarrow\;}
264 \newcommand{\impliedby}{\DOTSB\;\Longleftarrow\;}
265 \def\And{\DOTSB\;\mathchar"3026 \;}
```

The command \nobreakdash is designed only for use before a hyphen or dash (-, --, or ---). Setting the hyphen in a box and then unboxing it means that the normal penalty will not be added after it—and if the penalty is not there a break will not be taken (unless an explicit penalty or glue follows, thus the final \nobreak).

```
266 \newcommand{\nobreakdash}{\leavevmode
267 \toks@\@emptytoks \def\@tempa##1{\toks@\@xp{\the\toks@-}\FN@\next@}%
268 \DN@{\ifx\@let@token-\@xp\@tempa
269 \else\setboxz@h{\the\toks@\nobreak}\unhbox\z@\fi}%
270 \FN@\next@
271 }
```

\colon is for a colon in math that resembles a text colon: small space on the left, larger space on the right. The : character by itself is treated as a \mathrel i.e. large, equal spacing on both sides.

```
272 \renewcommand{\colon}{\nobreak\mskip2mu\mathpunct{}\nonscript 273 \mkern-\thinmuskip{:}\mskip6muplus1mu\relax}
```

# 7 Ellipsis dots

We can't use \newif for \ifgtest@ because we want to include \global in the definitions of \gtest@true and \gtest@false.

```
274 \left| \text{ifgtest@\iffalse} \right|
                                                         % initial value
275 \def\gtest@true{\global\let\ifgtest@\iftrue}
276 \def\gtest@false{\global\let\ifgtest@\iffalse}
277 \let\DOTSI\relax
278 \let\DOTSB\relax
279 \let\DOTSX\relax
280 {\uccode'7='\\ \uccode'8='m \uccode'9='a \uccode'0='t \uccode'!='h
281 \uppercase{%
     \gdef\math@#1#2#3#4#5#6\math@{\gtest@false\ifx 7#1\ifx 8#2%
282
     \ifx 9#3\ifx 0#4\ifx !#5\xdef\meaning0{#6}\gtest@true
     \fi\fi\fi\fi\fi\}}
285 {\uccode'7='c \uccode'8='h \uccode'9='\"
286 \uppercase{\gdef\mathch@#1#2#3#4#5#6\mathch@{\gtest@false
    \ifx 7#1\ifx 8#2\ifx 9#5\gtest@true\xdef\meaning@{9#6}\fi\fi\fi\}}
288 \newcount\classnum@
```

10 THE AMSMATH PACKAGE

```
289 \def\getmathch0#1.#2\getmathch0{\classnum0#1 \divide\classnum04096}
 290 \ifcase\number\classnum@\or\or\gdef\thedots@{\dotsb@}\or
 291 \gdef\thedots0{\dotsb0}\fi}
 292 {\uccode'4='b \uccode'5='i \uccode'6='n
 293 \uppercase{\gdef\mathbin@#1#2#3{\relaxnext@
        \def\nextii@##1\mathbin@{\ifx\@sptoken\@let@token\gtest@true\fi}%
 295 \gtest@false\DN@##1\mathbin@{}%
 296 \ifx 4#1\ifx 5#2\ifx 6#3\DN@{\FN@\nextii@}\fi\fi\fi\next@}}
 297 {\uccode'4='r \uccode'5='e \uccode'6='1
 298 \uppercase{\gdef\mathrel@#1#2#3{\relaxnext@
         \def\nextii@##1\mathrel@{\ifx\@sptoken\@let@token\gtest@true\fi}%
 300 \gtest@false\DN@##1\mathrel@{}%
 301 \ifx 4#1\ifx 5#2\ifx 6#3\DN@{\FN@\nextii@}\fi\fi\fi\next@}}}
 302 {\uccode'5='m \uccode'6='a \uccode'7='c
 303 \uppercase{\gdef\macro@#1#2#3#4\macro@{\gtest@false
         \ifx 5#1\ifx 6#2\ifx 7#3\gtest@true
          305
 306 \ensuremath{\model{1-}}\#2\model{2}
 307 \newcount\DOTSCASE@
 308 {\uccode'6='\\ \uccode'7='D \uccode'8='0 \uccode'9='T \uccode'0='S
 309 \uppercase{\gdef\DOTS0#1#2#3#4#5{\gtest0false\DN0##1\DOTS0{}%}
        \ifx 6#1\ifx 7#2\ifx 8#3\ifx 9#4\ifx 0#5\let\next@\DOTS@@
 311 \fi\fi\fi\fi
 312 \next@}}}
 313 {\uccode'3='B \uccode'4='I \uccode'5='X
 314 \uppercase{\gdef\DOTS@@#1{\relaxnext@
 \label{lem:condition} $$15 \ \end{condition} $$ \end{condition} $$15 \ \end{condition} $$ \end{condition} $$15 \ \end{condition} $$ \end{conditi
 316
         \DN@{\FN@\nextii@}%
 317 \ifx 3#1\global\DOTSCASE@\z@\else
         \ifx 4#1\global\DOTSCASE@\@ne\else
 318
         \ifx 5#1\global\DOTSCASE@\tw@\else\DN@##1\DOTS@{}%
 319
         \fi\fi\fi\next@}}}
 321 {\uccode'5='\\ \uccode'6='n \uccode'7='o \uccode'8='t
 322 \uppercase{\gdef\not@#1#2#3#4{\relaxnext@
         \def\nextii@##1\not@{\ifx\@sptoken\@let@token\gtest@true\fi}%
 324 \ \text{gtest@false\DNQ##1\not@{}}\%
325 \ifx 5#1\ifx 6#2\ifx 7#3\ifx 8#4\DN@{\FN@\nextii@}\fi\fi\fi
326 \left\{ i\left( x \right) \right\}
327 \def\keybin@{\gtest@true
328 \ifx\@let@token+\else\ifx\@let@token=\else
329 \ifx\@let@token<\else\ifx\@let@token>\else
330 \ifx\@let@token-\else\ifx\@let@token*\else\ifx\@let@token:\else
            \gtest@false\fi\fi\fi\fi\fi\fi\fi\}
Patch to ensure \@ldots is defined. (Name changed to \mathellipsis in Dec
94 release of LATEX.)
332 \@ifundefined{@ldots}{\def\@ldots{\mathellipsis}}{}
Reiterate the standard definition of \ldots to keep it from being clobbered by
the redefinition of \dots.
 333 \DeclareRobustCommand{\ldots}{%
 334
         \ifmmode \mathellipsis \else \textellipsis \fi
 336 \DeclareRobustCommand{\dots}{%
 337
         \ifmmode \@xp\mdots@\else \@xp\textellipsis \fi
 338 }
 339 \def\tdots@{\leavevmode\unskip\relaxnext@
 340 \DNQ{\$\m@th\@ldots\}
           \ifx\@let@token,\,$\else\ifx\@let@token.\,$\else
 341
 342
           \ifx\@let@token;\,$\else\ifx\@let@token:\,$\else
```

7. ELLIPSIS DOTS 11

```
\ifx\@let@token?\,$\else\ifx\@let@token!\,$\else
        $ \fi\fi\fi\fi\fi\fi\}%
344
346 \def\mdots@{\FN@\mdots@0}
347 \ensuremath{$\dots@{\dotso@}\%}
348 \ \fraken\boldsymbol \gdef\thedots@\boldsymbol{\boldsymboldots@}\%
349 \le ifx,\end{0.0} \
350 \else\ifx\not\ellet\token \gdef\thedots\ellet\token\
351 \else\keybin@
352 \left( \frac{\dotsb@}{\dotsb@} \right)
353 \else\xdef\meaning@{\meaning\@let@token.....}%
354
      \xdef\meaning@@{\meaning@}%
355
     \@xp\math@\meaning@\math@
356
     \ifgtest@
      \@xp\mathch@\meaning@\mathch@
357
      \ifgtest@\@xp\getmathch@\meaning@\getmathch@\fi
358
     \else\@xp\macro@\meaning@@\macro@
359
     \ifgtest@
360
      361
     \else\@xp\DOTS@\meaning@\DOTS@
362
363
     \ifgtest@
      \ifcase\number\DOTSCASE@\gdef\thedots@{\dotsb@}%
364
       \or\gdef\thedots@{\dotsi}\else\fi
365
     \else\@xp\math@\meaning@\math@
     \ifgtest@\@xp\mathbin@\meaning@\mathbin@
367
368
     \ifgtest@\gdef\thedots@{\dotsb@}%
369
     \else\@xp\mathrel@\meaning@\mathrel@
     \ifgtest@\gdef\thedots@{\dotsb@}%
370
     \fi\fi\fi\fi\fi\fi\fi\fi
371
372 \thedots@}
   The = character is necessary in the two \let assignments in \boldsymboldots@,
because the symbol we are making bold might be an = sign.
373 \def\boldsymboldots@#1{%
     \bold@true\let\@let@token=#1\let\delayed@=#1\mdots@@
     \boldsymbol#1\bold@false}
   The definition of \@cdots is merely the plain.tex definition of \cdots.
376 \def\@cdots{\mathinner{\cdotp\cdotp\cdotp}}
377 \newcommand{\dotsi}{\!\@cdots}
378 \let\dotsb@\@cdots
   If any new right delimiters are defined, they would need to be added to the
definition of \rightdelim@ in order for \dots to work properly in all cases.
379 \def\rightdelim@{\gtest@true
380 \ifx\@let@token)\else
381 \ifx\@let@token]\else
382 \ifx\@let@token\rbrack\else
383 \ifx\@let@token\}\else
384 \ifx\@let@token\rbrace\else
385 \ifx\@let@token\rangle\else
386 \ifx\@let@token\rceil\else
387 \ifx\@let@token\rfloor\else
388 \ifx\@let@token\rgroup\else
389 \ifx\@let@token\rmoustache\else
390 \ifx\@let@token\right\else
391 \ifx\@let@token\bigr\else
392 \ifx\@let@token\biggr\else
```

393 \ifx\@let@token\Bigr\else

394 \ifx\@let@token\Biggr\else\gtest@false

12 THE AMSMATH PACKAGE

```
396 \def\extra@{%
397 \rightdelim@\ifgtest@
398 \else\ifx\@let@token$\gtest@true
399 \else\xdef\meaning@{\meaning\@let@token.....}%
400 \@xp\macro@\meaning@\macro@\ifgtest@
401 \ \ensuremath{\texttt{Qxp\DOTS@\mathbb{N}}}\
402 \ifgtest@
403 \ifnum\DOTSCASE@=\tw@\gtest@true\else\gtest@false
404 \fi\fi\fi\fi\
405 \newif\ifbold@
406 \def\dotso@{\relaxnext@}
407 \ifbold@
     \let\@let@token\delayed@
     \def\nextii@{\extra@\@ldots\ifgtest@\,\fi}%
409
410 \else
    \def\nextii@{\DN@{\extra@\@ldots\ifgtest@\,\fi}\FN@\next@}%
411
412 \fi
413 \nextii@}
Why not save some tokens? (space vs. time).
414 \def\extrap@#1{%
415 \DN@{#1\,}%
416 \ifx\@let@token,\else
417 \ifx\@let@token;\else
418 \ifx\@let@token.\else\extra@
419 \ifgtest@\else
420 \let\next@#1\fi\fi\fi\next@}
   The \cdots command.
421 \end{\cdots}{\DNO{\entrope}(\cdots)\FNO\nextO)}
422 \left| dotsb \right|
423 \left| dotsm \right|
424 \DeclareRobustCommand{\dotso}{\relax
425 \ifmmode \DN@{\extrap@\@ldots}%
426 \else \let\next@\tdots@\fi
427 \ \FN@\next0
428 \DeclareRobustCommand{\dotsc}{\%}
429 \DN@{\ifx\@let@token;\@ldots\,%
          \else \ifx\@let@token.\@ldots\,%
430
          \else \extra@\@ldots \ifgtest@\,\fi
431
          fi\fi}%
432
433 \FN@\next@}
434 \renewcommand{\longrightarrow}{%
435 \DOTSB\protect\relbar\protect\joinrel\rightarrow}
436 \renewcommand{\Longrightarrow}{%
437 \DOTSB\protect\Relbar\protect\joinrel\Rightarrow}
438 \renewcommand{\longleftarrow}{%
439 \DOTSB\leftarrow\protect\joinrel\protect\relbar}
440 \renewcommand{\Longleftarrow}{%
441 \DOTSB\Leftarrow\protect\joinrel\protect\Relbar}
442 \renewcommand{\longleftrightarrow}{\DOTSB\leftarrow\joinrel\rightarrow}
443 \renewcommand{\Longleftrightarrow}{\DOTSB\Leftarrow\joinrel\Rightarrow}
444 \renewcommand{\mapsto}{\DOTSB\mapstochar\rightarrow}
445 \renewcommand{\longmapsto}{\DOTSB\mapstochar\longrightarrow}
446 \renewcommand{\hookrightarrow}{\DOTSB\lhook\joinrel\rightarrow}
447 \renewcommand{\hookleftarrow}{\DOTSB\leftarrow\joinrel\rhook}
448 \renewcommand{\iff}{\DOTSB\;\Longleftrightarrow\;}
```

8. INTEGRAL SIGNS 13

The \doteq command formerly used \buildrel; we avoid that because it requires '\over' as part of its syntax. Use 0pt instead of \z@ for robustitude.

```
449 \renewcommand{\doteq}{%
450 \DOTSB\mathrel{\mathop{\kernOpt =}\limits^{\textstyle.}}}
```

## 8 Integral signs

The straightforward \ifinner test to see if the current math context is non-display, fails if, for instance, we are typesetting a multiline display within an \halign, with the pieces going into constructions like

```
$\displaystyle...$
```

So we need a better test to find out if we are 'in a display'. We therefore create \if@display.

Default value for integral limits is **\nolimits**, see the definition of the 'nointlimits' option.

```
453 \renewcommand{\int}{\DOTSI\intop\ilimits@}
454 \renewcommand{\oint}{\DOTSI\ointop\ilimits@}
455 \def\intkern@{\mkern-6mu\mathchoice{\mkern-3mu}{}{}}
456 \def\intdots@{\mathchoice{\@cdots}%
457 {{\cdotp}\mkern1.5mu{\cdotp}\mkern1.5mu{\cdotp}}%
458 {{\cdotp}\mkern1mu{\cdotp}}%
459 {{\cdotp}\mkern1mu{\cdotp}}}
460 %
461 \newcommand{\iint}{\DOTSI\protect\MultiIntegral{2}}
462 \newcommand{\iiint}{\DOTSI\protect\MultiIntegral{4}}
464 \newcommand{\iiotsint}{\DOTSI\protect\MultiIntegral{4}}
```

If the \limits option is applied, use \mathop and fudge the left-hand space a bit to make the subscript visually centered.

**#1** is the multiplicity.

```
465 \newcommand{\MultiIntegral}[1]{%
     \edef\ints@c{\noexpand\intop
       \ifnum#1=\z@\noexpand\intdots@\else\noexpand\intkern@\fi
467
468
       \ifnum#1>\tw@\noexpand\intop\noexpand\intkern@\fi
469
       \ifnum#1>\thr@@\noexpand\intop\noexpand\intkern@\fi
       \noexpand\intop
470
       \noexpand\ilimits@
471
472
     }%
473
     \futurelet\@let@token\ints@a
474 }
475 \def\ints@a{%
     \ifx\limits\@let@token \ints@b
476
     \else \ifx\displaylimits\@let@token \ints@b
477
     \else\ifx\ilimits@\displaylimits \ints@b
478
     \fi\fi\fi
479
     \ints@c
480
481 }
482 \left\ \frac{82 \right.}{
     \mbox{mkern-7mu}\mbox{mthchoice}\mbox{mkern-2mu}{}{}%
483
484
     \mathop\bgroup
       \mbox{\mbox{$\mbox{mkern2mu}}{}}{}
       \let\ilimits@\egroup
486
487 }%
```

## 9 Size dependent definitions

We now define all stuff which has to change whenever a new math size is to be activated. LATEX provides a hook called \every@math@size to support such a need. All assignments in the \every@math@size hook that need to take outside effect should be global.

#### 9.1 Struts for math

The various kinds of struts could use some analysis and perhaps consolidation. For example perhaps the **\bBigg** delimiters could use

```
1.2\ht\strutbox (1.8, 2.4, 3.0)
```

instead of

```
1.0\big@size (1.5, 2.0, 2.5)
```

since \strut is reset with every size change [mjd, 1994/10/07]. But this change would introduce the possibility of changed line and page breaks in existing documents, so would need to be handled with care.

\Mathstrut@

Here comes the code for Spivak's \Mathstrut@.

\Mathstrutbox@ \resetMathstrut@

```
here comes the code for spivax's mathstruc
```

489 \setbox\Mathstrutbox@=\hbox{}

488 \newbox\Mathstrutbox@

490 \def\Mathstrut@{\copy\Mathstrutbox@}

The setting of the height and depth of the \Mathstrutbox@ is done in the \every@math@size hook since it depends on the height of a paren. As \every@math@size is triggered by \$ after a font size change, we want to avoid using another math formula \$...\$ to measure the math paren height; instead we go through the mathcode of the ( character. We assume that the mathcode has a leading hex digit 4 indicating 'open delimiter'; this allows us to make a relatively simple function to get the correct font and character position.

```
491 \def\resetMathstrut@{%
492 \setbox\z@\hbox{%
493 \mathchardef\@tempa\mathcode'\(\relax
494 \def\@tempb##1"##2##3{\the\textfont"##3\char"}%
495 \expandafter\@tempb\meaning\@tempa \relax
496 }%

These height and depth assignments are implicitly global.
497 \ht\Mathstrutbox@\ht\z@ \dp\Mathstrutbox@\dp\z@
498 }
```

499 \addto@hook\every@math@size{\resetMathstrut@}

\strut@

Next follows a special internal strut which is supposed to match the height and the depth of a normal \strut minus \normallineskiplimit according to M. Spivak.

This should really go into the definition of \sizeQupdate, and then the box reset could be local; but \sizeQupdate doesn't have any hook and is handled in such a way that it cannot even be changed except by changing \setQfontsize. So instead we put \resetQstrutboxQ into \everyQmathQsize and make it global. Then because of some complications in the way \glbQsettings and \checkQmathfonts work, we have to re-invoke it at the beginning of every environment that might use \strutQ. Fortunately this can be achieved (more or less) through the \spreadQequation hook. [mjd,2000/03/10]

```
500 \newbox\strutbox@
501 \def\strut@{\copy\strutbox@}
```

502 \def\reset@strutbox@{%

10. MATH ACCENTS 15

```
503 \global\setbox\strutbox@\hbox{%
504 \lower.5\normallineskiplimit
505 \vbox{\kern-\normallineskiplimit\copy\strutbox}}}
506 \addto@hook\every@math@size{\reset@strutbox@}
507 \AtBeginDocument{\reset@strutbox@}
```

### 9.2 Big delimiters

We are now going to redefine the plain TEX commands \big, \big1, etc., to produce different results in different sizes. Actually we only have to define \big, \Big, etc., since they are used to construct the directional versions \big1, \bigr, and the rest.

\big \Big \bigg \Bigg To save token space we put everything into the common macro \bBigg@. The macros are now simply a call to \bBigg@ with a factor to determine the correct height of the delimiter as an argument. This code should better go into a future version of the LATEX kernel; the macro \n@space is then superfluous (since it is only used once) and should be removed to avoid wasting hash table space unnecessarily.

```
508 \renewcommand{\big}{\bBigg@\@ne}
509 \renewcommand{\Big}{\bBigg@\1.5}}
510 \renewcommand{\bigg}{\bBigg@\tw@}
511 \renewcommand{\Bigg}{\bBigg@\2.5}}
```

\bBigg@ Now we tackle the macro which has to do the real work. It actually has two arguments, the factor and the wanted delimiter.

```
512 \def\bBigg@#1#2{%
```

We start with an extra set of braces because we want constructions like \def\bigl{\mathopen\big} to work without the overhead of extra arguments.

```
513 {\@mathmeasure\z@{\nulldelimiterspace\z@}%
514 {\left#2\vcenter to#1\big@size{}\right.}%
515 \box\z@}}
```

\big@size

\big@size needs to be set to 1.2 times the height of a math paren. This height is already recorded in \Mathstrutbox@.

```
516 \addto@hook\every@math@size{%
517 \global\big@size 1.2\ht\Mathstrutbox@
518 \global\advance\big@size 1.2\dp\Mathstrutbox@ }
519 \newdimen\big@size
```

#### 10 Math accents

We want to change the leading digit of math accents to be **\accentclass@** so that it can vary according to certain internal purposes.

```
520 \def\accentclass@{7}
521 \def\noaccents@{\def\accentclass@{0}}
```

There are a few  $\langle math\ alphabet \rangle$ s in the standard fonts where we have to change the extra macros because the standard definitions don't account for these accent problems. The first is for the \mathit command.

```
522 \label{lem:coding_OML} $$ 122 \end{cont} $
```

The next one corrects the \cal alphabet.

```
523 \DeclareFontEncoding{OMS}{}{\noaccents@}
```

Triple and quadruple dot accents.

The following code deals with support for compound accents. By redefining \set@mathaccent we ensure that \DeclareMathAccent will define accent commands to run our \mathaccentV function instead of the primitive \mathaccent.

```
530 \def\set@mathaccent#1#2#3#4{%

531 \xdef#2{\@nx\protect\@nx\mathaccentV

532 {\@xp\@gobble\string#2}\hexnumber@#1#4}%

533 }
```

We redefine the standard math accent commands to call \mathaccentV, using the mathgroup/encoding-number information embedded in their previous definitions. If the definition of an accent command does not have the expected form, we leave the accent command alone, but give a warning. For widehat and widetilde, we need to avoid clobbering the definitions done by the amsfonts package. Arbitrating the contention between amsmath and amsfonts to allow doubling a widetilde accent looks tricky, so for the time being [mjd,1999/07/19] we just leave \widehat and \widetilde alone. As a result, if the amsmath package is loaded on top of a vanilla LATEX documentclass, everything runs through with no warnings. If a Lucida Math or other math fonts package is loaded in addition to amsmath, there are greater difficulties, but those are addressed elsewhere.

```
534 \ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{
535 \def\@tempb#1>#2#3 #4\@nil#5{%
                    \@xp\ifx\csname#3\endcsname\mathaccent
                             \@tempc#4?"7777\@ni1#5%
537
                     \else
538
539
                             \PackageWarningNoLine{amsmath}{%
540
                                     Unable to redefine math accent \string#5}%
541
542 }
543 \ensuremath{ \frac{43}{4}} 44546\ensuremath{ \frac{117}{\%}}
                    \chardef\@tempd="#3\relax\set@mathaccent\@tempd{#7}{#2}{#4#5}}
545 \ensuremak{\hat}
546 \@tempa{\check}
547 \@tempa{\tilde}
548 \@tempa{\acute}
549 \@tempa{\grave}
550 \@tempa{\dot}
551 \@tempa{\ddot}
552 \@tempa{\breve}
553 \@tempa{\bar}
554 \@tempa{\vec}
555 \@ifundefined{mathring}{%
                     \DeclareMathAccent{\mathring}{\mathalpha}{operators}{"17}
556
557 }{%
558
                    \@tempa{\mathring}
559 }
560 %%\@tempa\widetilde
561 %%\@tempa\widehat
```

Regression testing of amsmath 2.0 showed that in some documents there occurred fragments of the form

```
\hat\mathcal{G}
```

This is not at all correct syntax for the argument of a LATEX command but it produced the intended result anyway because of the internal syntax of the

10. MATH ACCENTS 17

\mathaccent primitive. With \mathaccentV, it will yield an error message. We therefore do a special check for such syntax problems in order to make the error message more informative.

```
562 \newcommand{\acc@check}{} $ 563 \newcommand{\acc@error}{} $ 564 \def\acc@check{\difnextchar\empty\relax\acc@error}
```

We put most of the tokens in a separate macro so they do not get scanned unless they are actually needed.

```
565 \def\acc@error{%
566     \@amsmath@err{%
567      Improper argument for math accent:\MessageBreak
568      Extra braces must be added to prevent wrong output%
569     }\@ehc
570 }
```

For \mathaccentV part of the processing is dependent on the depth of nesting of math accent commands. We introduce a dedicated counter for this instead of using chardef because we want to increment/decrement it during processing, and incrementing a chardef integer is more work.

#### 571 \newcount\macc@depth

Provide this function in case it is not already available.

```
572 \long\def\@gobblethree#1#2#3{}
```

The \mathaccentV function first counts the number of nested math accents by setting the argument in a throw-away box. (This is not as risky as such an operation would normally be because the argument is generally either a simple math symbol or a nested math accent call with a simple math symbol at the bottom of the nesting.)

There are two benefits from counting the nesting levels first before doing anything else: (1) we can fall back to a simple \mathaccent call if the nesting depth is 1, and (2) if the nesting depth is greater than 1, we would like to be able to tell when we have reached the lowest level, because at that point we want to save the argument for later use and place an accent on top of a phantom copy.

When we have multiple accents, they will be placed on top of the invisible box, followed by some suitable kerns, then a visible copy of the nucleus. To see why, let us look at what goes wrong with a double application of the \mathaccent primitive. The standard definition of \hat is \mathaccent"705E, so \hat{\hat{F}} expands to

```
\mbox{\mbox{$\mathaccent''}705E{\mathbb{F}}}
```

```
The result of this operation is 
\vbox(12.11111+0.0)x7.81946
.\hbox(6.94444+0.0)x0.0, shifted 1.40973
.\OT1/cmr/m/n/10 ^
.\kern-4.30554
.\vbox(9.47221+0.0)x7.81946
.\hbox(6.94444+0.0)x0.0, shifted 2.24309
...\OT1/cmr/m/n/10 ^
..\kern-4.30554
..\hbox(6.83331+0.0)x7.81946
...\OML/cmm/m/it/10 F
```

TEX starts by constructing a vbox with the hat character on top of the F. Then it puts another hat character on top of the vbox; but without skew information, because that is only applied by \mathaccent when the base object is a simple symbol. So the first accent is skewed to the correct position but all later accents are not. By the way, the actual width of the F in the above example is less

18 THE AMSMATH PACKAGE

than 7.81946; the box in which it is packed was automatically lengthened by the width of the F's italic correction (without actually putting in a kern for it).

To get the second accent shifted farther to the right we artificially increase the width of the innermost box and add a compensating kern afterward. Furthermore, to get proper placement of a following subscript or superscript, we take the base symbol out, leaving a phantom in its place, and print it by itself following the kern. We then need to increase the kern amount to move the base character backward under the accents again. Here is what the results look like:

```
\vbox(12.11111+0.0)x9.48618
.\hbox(6.94444+0.0)x0.0, shifted 2.24309
.\OT1/cmr/m/n/10 ^
.\kern-4.30554
.\vbox(9.47221+0.0)x9.48618
..\hbox(6.94444+0.0)x0.0, shifted 2.24309
..\OT1/cmr/m/n/10 ^
..\kern-4.30554
..\hbox(6.83331+0.0)x9.48618
..\hbox(6.83331+0.0)x7.81946
...\kern 1.66672
\kern -9.48618
\OML/cmm/m/it/10 F
```

Much of this implementation is based on code from the accents package of Javier Bezos. I added the test to revert to a simple \mathaccent when accents are not nested, and some other refinements to reduce the number of kerns used (to conserve box memory) and the number of cycles through \mathchoice (to make things run a little faster). It was all rather difficult and my first two attempts had serious bugs but I hope and believe that this version will do better. [mjd,2000/03/15]

The "V" in \mathaccentV is just an indication that it takes five arguments. It is important that the name includes mathaccent, otherwise \DeclareMathAccent will balk at redefining one of our accent commands, for example when an alternative math font package is loaded.

```
573 \def\mathaccentV#1#2#3#4#5{%
     \ifmmode
574
575
       \gdef\macc@tmp{\macc@depth\@ne}%
       \setbox\z@\hbox{%
576
         \let\mathaccentV\macc@test
577
         \let\use@mathgroup\@gobbletwo \let\select@group\@gobblethree
578
579
         \frozen@everymath{}$#5$%
580
       }%
       \macc@tmp
581
582
       \ifnum\macc@depth=\@ne
         \global\let\macc@nucleus\@empty
583
         \mathaccent"\accentclass@
584
       \else
585
         \@xp\macc@nested
586
587
       \fi
       #2#3#4{#5}%
       \macc@nucleus
589
590
591
       \@xp\nonmatherr@\csname#1\endcsname
592
593 }
594 \def\macc@test#1#2#3#4{\xdef\macc@tmp\advance\macc@depth\@ne}}
595 \def\macc@group{-1}
596 \def\macc@nested#1#2#3#4{%
```

10. MATH ACCENTS 19

```
597 \begingroup
598 \let\math@bgroup\@empty \let\math@egroup\macc@set@skewchar
599 \mathsurround\z@ \frozen@everymath{\mathgroup\macc@group\relax}%
600 \macc@set@skewchar\relax
601 \let\mathaccentV\macc@nested@a
602 \macc@nested@a\relax#1#2#3{#4}%
603 \endgroup
604 }
605 \let\macc@palette\mathpalette
606 \def\macc@nested@a#1#2#3#4#5{%
```

This test saves some work that would otherwise be always repeated fourfold thanks to \mathchoice.

```
607 \ifnum\macc@group=\mathgroup
608 \else \macc@set@skewchar\relax \edef\macc@group{\the\mathgroup}%
609 \fi
610 \mathchardef\macc@code "\accentclass@ #2#3#4\relax
611 \macc@palette\macc@a{#5}%
612 }
```

The reason that \macc@set@skewchar takes an argument is so that it can serve as a direct substitute for \math@egroup, in addition to being used separately.

Setting a skewchar with this method works for symbols of variable mathgroup (class 7, letters and numbers) but not necessarily for special symbols like \partial or \xi whose mathgroup doesn't change; fortunately the most commonly used ones come from mathgroup one, which is the fall-back mathgroup for skewchar.

```
613 \def\macc@set@skewchar#1{%
614
     \begingroup
     \ifnum\mathgroup=\m@ne \let\@tempa\@ne
615
616
       \ifnum\skewchar\textfont\mathgroup=\m@ne \let\@tempa\@ne
617
       \else \let\@tempa\mathgroup
618
619
       \fi
620
     \count@=\skewchar\textfont\@tempa
     \advance\count@"7100
     \edef\@tempa{\endgroup
623
       \mathchardef\noexpand\macc@skewchar=\number\count@\relax}%
624
     \@tempa
625
626
     #1%
```

Arg1 is math-style, arg2 is accent base object. We assume that math style doesn't change within the nested group of accents; this means we can set \macc@style only once and redefine \macc@palette to use it, in order to run \mathchoice only once instead of multiplying the calls exponentially as the nesting level increases.

```
628 \def\macc@a#1#2{%
629 \begingroup
630 \let\macc@style#1\relax
631 \def\macc@palette##1{##1\macc@style}%
632 \advance\macc@depth\m@ne
633 \ifnum\macc@depth=\z@
634 \gdef\macc@nucleus{#2}%
```

Extra  $\ensuremath{\texttt{Qempty}}$  tokens are to prevent low-level  $T_EX$  errors from the potential syntactic error that  $\ensuremath{\texttt{Acc@check}}$  checks for.

20 THE AMSMATH PACKAGE

```
\setbox\z@\hbox{$#1#2\@empty{}\macc@skewchar$}%
635
        \setbox\tw@\hbox{$#1#2\@empty\macc@skewchar$}%
636
        637
        \xdef\macc@kerna{\the\dimen@\relax}%
638
639
        \setbox4\hbox{$#1#2\acc@check\@empty$}%
        \global\setbox\@ne\hbox to\wd4{}%
640
        \  \ht\ \dp\dp4
641
        \xdef\macc@kernb{\the\wd4\relax}%
642
        \mathaccent\macc@code{\box\@ne\kern\macc@kerna}%
643
644
645
        \mathaccent\macc@code{\let\macc@adjust\@empty #1#2\@empty}%
646
        \macc@adjust
647
648
     \endgroup
649 }
650 \def\macc@adjust{%
     \dimen@\macc@kerna\advance\dimen@\macc@kernb
652
     \kern-\dimen@
653 }
   The commands \Hat, \Tilde, ..., are supported as synonyms of \hat,
\tilde, ..., for backward compatibility.
654 \left\{ \frac{1}{hat} \right\}
655 \def\Check{\check}
656 \def\Tilde{\tilde}
657 \def\Acute{\acute}
658 \def\Grave{\grave}
659 \def\Dot{\dot}
660 \def\Ddot{\ddot}
661 \def\Breve{\breve}
662 \def\Bar{\bar}
663 \def\Vec{\vec}
   This error message about math mode is used several times so we make an
```

### 11 Mods, continued fractions, etc.

664 \def\nonmatherr@#1{\@amsmath@err{\protect 665 #1 allowed only in math mode}\@ehd}

The commands \bmod, \pmod, \pod, \mod aren't currently robust. [mjd, 1994/09/05]

```
666 \renewcommand{\bmod}{\nonscript\mskip-\medmuskip\mkern5mu\mathbin
667 {\operator@font mod}\penalty900
668 \mkern5mu\nonscript\mskip-\medmuskip}
669 \newcommand{\pod}[1]{\allowbreak
670 \if@display\mkern18mu\else\mkern8mu\fi(#1)}
671 \renewcommand{\pmod}[1]{\operator@font mod}\mkern6mu#1}}
672 \newcommand{\mod}[1]{\allowbreak\if@display\mkern18mu
673 \else\mkern12mu\fi{\operator@font mod}\,\,#1}
```

Continued fractions. The optional arg l or r controls horizontal placement of the numerators. The \kern-\nulldelimiterspace is needed in the definition if we want the right-hand sides of the fraction rules to line up. The \strut keeps the numerator of a subsidiary cfrac from coming too close to the fraction rule above it.

```
674 \newcommand{\cfrac}[3][c]{{\displaystyle\frac{%}
675 \strut\ifx r#1\hfill\fi#2\ifx l#1\hfill\fi}{#3}}%
676 \kern-\nulldelimiterspace}
```

\overset and \underset put symbols above, respectively below, a symbol that is not a \mathop and therefore does not naturally accept limits. \binrel@@ uses information collected by \binrel@ to make the resulting construction be of type mathrel or mathbin if the base symbol is either of those types.

```
677 \newcommand{\overset}[2]{\binrel@{#2}%
678 \binrel@@{\mathop{\kern\z@#2}\limits^{#1}}}
679 \newcommand{\underset}[2]{\binrel@{#2}%
680 \binrel@@{\mathop{\kern\z@#2}\limits_{#1}}}
```

\sideset allows placing 'adscript' symbols at the four corners of a \mathop, in addition to limits. Left-side adscripts go into arg #1, in the form \_{...}^{...}, and right-side adscripts go into arg #2.

As currently written [mjd, 1995/01/21] this is pretty haphazard. In order to really make it work properly in full generality we'd have to read and measure the top and bottom limits and use mathchoice to always get the right mathstyle for each piece, etc., etc.

```
681 \newcommand{\sideset}[3]{%
682 \@mathmeasure\z@\displaystyle{#3}%
```

Use a global box assignment here since the depth override is implicitly global. Then move the constructed box to a local box register (2) to ensure it won't get destroyed during the next two mathemasure statements. This precaution may be more extreme than necessary in practice.

```
683 \global\setbox\@ne\vbox to\ht\z@{}\dp\@ne\dp\z@
684 \setbox\tw@\box\@ne
685 \@mathmeasure4\displaystyle{\copy\tw@#1}%
686 \@mathmeasure6\displaystyle{#3\nolimits#2}%
687 \dimen@-\wd6 \advance\dimen@\wd4 \advance\dimen@\wd\z@
688 \hbox to\dimen@{}\mathop{\kern-\dimen@\box4\box6}%
689 }
```

\smash We add to the \smash command an optional argument denoting the part of the formula to be smashed.

```
690 \renewcommand{\smash}[1][tb]{%
691 \def\mb@t{\ht}\def\mb@b{\dp}\def\mb@tb{\ht\z@\z@\dp}%
692 \edef\finsm@sh{\csname mb@#1\endcsname\z@\z@ \box\z@}%
693 \ifmmode \@xp\mathpalette\@xp\mathsm@sh
694 \else \@xp\makesm@sh
695 \fi
696 }
```

### 12 Extensible arrows

The minus sign used in constructing these arrow fills is smashed so that superscripts above the arrows won't be too high. This primarily affects the \xleftarrow and \xrightarrow arrows.

```
698 \mathchardef\std@equal\mathcode'\=\relax
In case some alternative math fonts are loaded later:
699 \AtBeginDocument{%
700 \mathchardef\std@minus\mathcode'\-\relax
701 \mathchardef\std@equal\mathcode'\=\relax
702 }
```

697 \mathchardef\std@minus\mathcode'\-\relax

```
703 \def\relbar{\mathbf{\mathbb{C}}\hspace{200}} \\ 704 \def\Relbar{\mathbf{\mathbb{C}}\hspace{200}} \\
```

```
705 \def\arrowfill@#1#2#3#4{%
           \mbox{\mbox{$\mbox{$\mbox{$}}\mbox{$\mbox{$}}\mbox{\mbox{$}}\mbox{\mbox{$}}\mbox{\mbox{$}}\mbox{\mbox{$}\mbox{$}}\mbox{\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox
             \relax#4#1\mkern-7mu%
 708
             \cleaders\hbox{$\#4\mkern-2mu$}\hfill
             mkern-7mu#3$%
 709
 710 }
 711 \def\leftarrowfill@{\arrowfill@\leftarrow\relbar\relbar}
 712 \def\rightarrowfill@{\arrowfill@\relbar\relbar\rightarrow}
 713 \def\leftrightarrowfill@{\arrowfill@\leftarrow\relbar\rightarrow}
 714 \def\Leftarrowfill@{\arrowfill@\Leftarrow\Relbar\Relbar}
 715 \def\Rightarrowfill@{\arrowfill@\Relbar\Relbar\Rightarrow}
 716 \def\Leftrightarrowfill@{\arrowfill@\Leftarrow\Relbar\Rightarrow}
 717 \def\overarrow@#1#2#3{\vbox{\ialign{##\crcr#1#2\crcr
 718 \noalign{\nointerlineskip}$\m@th\hfil#2#3\hfil$\crcr}}}
 719 \renewcommand{\overrightarrow}{%
 720 \mathpalette{\overarrow@\rightarrowfill@}}
 721 \renewcommand{\overleftarrow}{%
 722 \mathpalette{\overarrow@\leftarrowfill@}}
 723 \newcommand{\overleftrightarrow}{%
          \mathpalette{\overarrow@\leftrightarrowfill@}}
 725 \def\underarrow@#1#2#3{%
 726 \vtop{\ialign{##\crcr$\m@th\hfil#2#3\hfil$\crcr
 727 \noalign{\nointerlineskip\kern1.3\ex0}#1#2\crcr}}
 728 \newcommand{\underrightarrow}{%
          \mathpalette{\underarrow@\rightarrowfill@}}
 730 \newcommand{\underleftarrow}{%
         \mathpalette{\underarrow@\leftarrowfill@}}
 732 \newcommand{\underleftrightarrow}{%
         \mathpalette{\underarrow@\leftrightarrowfill@}}
 734 %\newcommand{\xrightarrow}[2][]{\ext@arrow 0359\rightarrowfill@{#1}{#2}}
 735 \def\ext@arrow#1#2#3#4#5#6#7{%
 736 \mathrel{\mathop{%
Measure the superscript and subscript.
               \setbox\z@\hbox{#5\displaystyle}%
 737
               \setbox\tw@\vbox{\m@th
 738
 739
                   \hbox{$\scriptstyle\mkern#3mu{#6}\mkern#4mu$}%
 740
                   \hbox{$\scriptstyle\mkern#3mu{#7}\mkern#4mu$}%
 741
                   \copy\z@
               }%
 742
               \hbox to\wd\tw@{\unhbox\z@}}%
We don't want to place an empty subscript since that will produce too much
blank space below the arrow.
 744
           \limits
 745
               \@ifnotempty{#7}{^{\if0#1\else\mkern#1mu\fi
 746
                                                    #7\if0#2\else\mkern#2mu\fi}}%
 747
               \@ifnotempty{#6}{_{\if0#1\else\mkern#1mu\fi
                                                    #6\if0#2\else\mkern#2mu\fi}}%
 748
 749 }
     Some extensible arrows to serve as mathrels and taking sub/superscripts.
These commands are robust because they take an optional argument.
```

750 \newcommand{\xrightarrow}[2][]{\ext@arrow 0359\rightarrowfill@ $\{#1\}$ {#2}} 751 \newcommand{\xleftarrow}[2][]{\ext@arrow 3095\leftarrowfill@ $\{#1\}$ {#2}}

#### 13 Array-related environments

#### 13.1 Remarks

Because these environments can be nested within the equation structures that allow \tag, there is some cross-influence in the internal workings of the \\ command.

#### 13.2The \substack command

The \substack command can be used to set subscripts and superscripts that consist of several lines. Usage:

```
X_{\substack{a=1\b=2}}
```

subarrav

The subarray environment makes a small-size array suitable for use in a subscript or superscript. At the moment the supported arguments are not the full possibilities of array but only c or 1 for centered or left-aligned. And only one

```
752 \newenvironment{subarray}[1]{%
```

Note: The predecessors of subarray (Sb and Sp, inherited from  $A_MS$ -T<sub>F</sub>X) used \vbox instead of \vcenter. But when a multiline subscript is placed in \limits position \vcenter is no worse than \vbox, and when it is placed in the \nolimits position (e.g., for an integral), \vcenter provides clearly better positioning than \vbox.

```
\vcenter\bgroup
```

Use \Let@ to set the proper meaning of the \\ and \\\* commands. And restore the meaning of \math@cr@@@ to \cr (see above) in case subarray is used inside one of the more complicated alignment macros where the meaning of \math@cr@@@ is different. Similarly, call \default@tag to ensure that a line break here doesn't get an equation number!

```
\Let@ \restore@math@cr \default@tag
```

Set the line spacing to be the same as \atop (when \atop occurs in \textstyle or smaller), cf The T<sub>E</sub>Xbook, Appendix G.

```
\baselineskip\fontdimen10 \scriptfont\tw@
755
```

\advance\baselineskip\fontdimen12 \scriptfont\tw0 756

757 \lineskip\thr@@\fontdimen8 \scriptfont\thr@@

\lineskiplimit\lineskip

Start the \vbox \halign structure that encloses the contents. Notice that we never get \scriptscriptstyle. That would require a \mathchoice (ugh).

```
\ialign\bgroup\ifx c#1\hfil\fi
759
       $\m@th\scriptstyle##$\hfil\crcr
760
761 }{%
762
     \crcr\egroup\egroup
```

\substack The \substack command is just an abbreviation for the most common use of subarray.

764 \newcommand{\substack}[1]{\subarray{c}#1\endsubarray}

#### 13.3 Matrices

smallmatrix

smallmatrix is again an alignment, this time in a centered box. The opening incantations are basically the same as those in \multilimits@, followed by the alignment itself. A remark: the baselineskip (9\ex0) used in  $A_MS$ -T<sub>F</sub>X is too large for use in text with the usual baselineskip of 12 or 13 points; we change it here to 6\ex@ and also adjust the \lineskip and \lineskiplimit slightly to compensate. (MJD)

```
765 \newenvironment{smallmatrix}{\null\,\vcenter\bgroup
     \Let@\restore@math@cr\default@tag
     \baselineskip6\ex@ \lineskip1.5\ex@ \lineskiplimit\lineskip
767
     \ialign\bgroup\hfil\m0th\scriptstyle##\hfil&&\thickspace\hfil
769
     $\m@th\scriptstyle##$\hfil\crcr
770 }{%
771 \crcr\egroup\egroup\,%
772 }
```

The matrix environment is just an array that provides up to ten centered columns, so that users don't have to give the col-spec argument explicitly unless they want some of the columns noncentered, that is. The maximum number of columns is actually not fixed at ten but given by the counter MatrixCols, and can therefore be increased by changing that counter.

The extra space of \arraycolsep that array adds on each side is a waste so we remove it here (perhaps we should instead remove it from array in general, but that's a harder task).

TODO: Think about re-implementing \matrix to get rid of the \c@MatrixCols limit and have hard-wired preamble that doesn't have to be rebuilt each time.

We must use \renewenvironment for matrix and pmatrix because LATEX doesn't kill the definitions found in plain.tex, even though it probably should because of their foreign syntax.

```
773 \renewenvironment{matrix}{%
     \matrix@check\matrix\env@matrix
775 }{%
776
     \endarray \hskip -\arraycolsep
777 }
```

\env@matrix

```
778 \def\env@matrix{\hskip -\arraycolsep
    \let\@ifnextchar\new@ifnextchar
     \array{*\c@MaxMatrixCols c}}
780
```

\c@MaxMatrixCols

781 \newcount\c@MaxMatrixCols \c@MaxMatrixCols=10

\matrix@check For various reasons, authors sometimes use the Plain TFX form of \matrix or \pmatrix in LATEX documents. If they later add an invocation of the amsmath package to their document, the Plain TFX syntax would lead to rather unintelligible error messages. The \matrix@check function does some checking to forestall that problem.

```
782 \def\matrix@check#1{%
     \@xp\ifx\csname\@currenvir\endcsname#1%
784
     \else\matrix@error#1%
```

This error recovery is not that good but is better than the infinite loop that can result from calling \array without a matching \endarray. (The array setup leaves \par empty.)

```
785
        \@xp\@gobble
786
     \fi
787 }
```

\matrix@error

```
788 \def\matrix@error#1{%
```

```
789 \@amsmath@err{%
790 Old form '\string#1' should be \string\begin{\@xp\@gobble\string#1}%
792 '\string#1{...}' is old Plain-TeX syntax whose use is
793 ill-advised in LaTeX.%
794 }%
795 }
796 \renewenvironment{pmatrix}{%
797 \left(%
     \matrix@check\pmatrix\env@matrix
799 }{
800
     \endmatrix\right)%
802 \newenvironment{bmatrix}{\left[\env@matrix}{\endmatrix\right]}
803 \newenvironment{Bmatrix}{%
804 \left\lbrace\env@matrix
805 }{%
806
     \endmatrix\right\rbrace
807 }
808 \newenvironment{vmatrix}{\left\lvert\env@matrix}{\endmatrix\right\rvert}
809 \newenvironment{Vmatrix}{\left\lVert\env@matrix}{\endmatrix\right\rVert}
810 \let\hdots\@ldots
811 \newcommand{\hdotsfor}[1]{%
12 \int f(x)^{\frac{41}{\exp}} \left( \frac{41}{fi} \right)
813 \newmuskip\dotsspace@
814 \def\shdots@for#1] {\hdots@for{#1}}
815 \def\hdots@for#1#2{\multicolumn{#2}c%
816 {\m@th\dotsspace@1.5mu\mkern-#1\dotsspace@
       \xleaders\hbox{$\m@th\mkern#1\dotsspace@.\mkern#1\dotsspace@$}%
818
               \hfill
       \mkern-#1\dotsspace@}%
819
The easiest way to produce the cases environment is to base it on the array
environment. We must use \renewenvironment to override the definition of
\cases that LATEX (unwisely) leaves in place from plain.tex.
821 \renewenvironment{cases}{%
822 \matrix@check\cases\env@cases
823 }{%
824 \endarray\right.%
825 }
826 \def\env@cases{%
827 \let\@ifnextchar\new@ifnextchar
828 \left\lbrace
     \def\arraystretch{1.2}%
```

## 14 Equation sub-numbering

\array{0{}10{\quad}10{}}%

831 }

 $832 \mbox{\ensuremath{\mbox{\sc Newcounter}}\xspace}\xspace^{\mbox{\sc Newcounter}}\xspace^{\mbox{\sc Newcounter}\xspace}\xspace^{\mbox{\sc Newc$ 

We can't assume \ignorespacesafterend is defined since it was not there in the earliest releases of LATEX 2e. And we need to include the \global for the same reason.

```
833 \@ifundefined{ignorespacesafterend}{%
834 \def\ignorespacesafterend{\global\@ignoretrue}%
835 }{}
```

836 \newenvironment{subequations}{%

Before sending down the 'equation' counter to the subordinate level, add 1 using standard \refstepcounter.

```
837 \refstepcounter{equation}%
```

Define \theparentequation equivalent to current \theequation. \edef is necessary to expand the current value of the equation counter. This might in rare cases cause something to blow up, in which case the user needs to add \protect.

- \$38 \protected@edef\theparentequation{\theequation}\%
- 339 \setcounter{parentequation}{\value{equation}}%

And set the equation counter to 0, so that the normal incrementing processes in the various equation environments will produce the desired results.

```
840 \setcounter{equation}{0}%

841 \def\theequation{\theparentequation\alph{equation}}%

842 \ignorespaces

843 }{%

844 \setcounter{equation}{\value{parentequation}}%

845 \ignorespacesafterend

846 }
```

## 15 Equation numbering

In the multiline equation environments provided here, the task of equation numbering is linked to the task of line breaking in the sense that it is the \\ command that marks where an equation number for the current line will be processed and added to the page.

Provide a convenient way to specify that equations should be numbered within sections.

```
847 \newcommand{\numberwithin}[3] [\arabic]{\%
848 \@ifundefined{c@#2}{\@nocounterr{#2}}{\%
849 \@ifundefined{c@#3}{\@nocnterr{#3}}{\%
850 \@addtoreset{#2}{#3}\%
851 \@xp\xdef\csname the#2\endcsname{\%
852 \@xp\@nx\csname the#3\endcsname .\@nx#1{#2}}}\%
853 }
```

To make references to equation numbers easier, we provide \eqref. We almost don't need \textup, except that \tagform@ doesn't supply the italic correction.

 $854 \ensuremath{\eqref}[1]{\textup{\tagform@{\ref{#1}}}}$ 

#### 15.1 Preliminary macros

The following macros implement the LATEX syntax for the \\ command, i.e. the possibility to add an asterisk to inhibit a page break, or an optional argument to denote additional vertical space. They are modelled more or less after the corresponding macros for LATEX's equarray and array environments.

[We can perhaps use the equarray mechanism if we change it so that it also uses \openup.]

\dspbrk@lvl

We begin by defining the  $\del{dspbrk@lvl}$  counter. This counter records the desirability of a break after the current row, as a number between 0 and 4. Its default value is -1 meaning that no explicit  $\del{displaybreak}$  command was given, and the default  $\del{displaylinepenalty}$  is to be used.

```
855 \newcount\dspbrk@lvl
856 \dspbrk@lvl=-1
```

\interdisplaylinepenalty We set the \interdisplaylinepenalty to 10000.

```
857 \interdisplaylinepenalty\@M
```

\allowdisplaybreaks

The \allowdisplaybreaks command. Since this is intended for use outside displayed formulas (typically in the preamble), it does not need to use \new@ifnextchar.

```
858 \newcommand{\allowdisplaybreaks}[1][4]{%
859 \interdisplaylinepenalty\getdsp@pen{#1}\relax
860 }
```

\getdsp@pen

Modelled after IAT<sub>E</sub>X's \@getpen. We use higher numbers than would normally be provided by \@lowpenalty, \@medpenalty, and \@highpenalty, since display breaks are almost always less desirable.

\displaybreak

nogood@displaybreak

\dspbrk@ 864 \newcommand{\displaybreak}{\new@ifnextchar[\dspbrk@{\dspbrk@[4]}}\dspbrk@context 865 \chardef\dspbrk@context=\sixt@@n

For breaks in a certain row of a alignment.

```
865 \chardef\dspbrk@context=\sixt@@n
866 \ensuremath{\mbox{\sc k0[\#1]}} \
     \ifmeasuring@
867
868
     \else
       \ifcase\dspbrk@context % case 0 --- OK
869
870
          \global\dspbrk@lvl #1\relax
871
                                 % case 1 --- inside a box
          \nogood@displaybreak
                                 % other cases --- outside of a display
          \@amsmath@err{\Invalid@@\displaybreak}\@eha
874
875
       \fi
876
     \fi
```

This is the value of \displaybreak when it occurs inside some structure where it will not work.

```
878 \def\nogood@displaybreak{%

879 \@amsmath@err{\protect

880 \displaybreak\space cannot be applied here}%

881 {One of the enclosing environments creates an

882 unbreakable box\MessageBreak

883 (e.g., split, aligned, gathered, ...).}%

884 }
```

\math@cr

877 }

The macro \math@cr ends a row inside one of the equation environments, i.e., this is the internal name of the \\ commands in these environments. As usual for this kind of macro inside of alignments we insert a special brace into  $T_EX$ 's input stream. The initial \relax is needed to trigger entry into the u template of the current column if the author ended the current row with an empty column (i.e., the mather was immediately preceded by an ampersand).

```
885 \def\math@cr{\relax\iffalse{\fi\ifnum0='}\fi}
```

The first step is now to check whether an asterisk follows. \@eqpen is used to hold the penalty value to be put on the vertical list. Then we call up \math@cr@ which performs the next step. If an asterisk is read page breaking is inhibited.

```
886 \@ifstar{\global\@eqpen\@M\math@cr@}%
```

Otherwise we have to check the \dspbrk@lvl value.

```
887 {\global\@eqpen
888 \ifnum\dspbrk@lvl <\z@ \interdisplaylinepenalty
889 \else -\@getpen\dspbrk@lvl \fi
890 \math@cr@}}</pre>
```

\math@cr@

The purpose of \math@cr@ is to check whether an optional argument follows. If not it provides \z@ as default value.

\math@cr@@

\math@cr@@ closes the special brace opened in \math@cr, and calls \math@cr@@@ which is supposed the 'real' row ending command. The meaning of this macro depends on the environment in which it is used.

```
892 \def\math@cr@@[#1]{\ifnumO='{\fi \iffalse}\fi\math@cr@@@
```

Finally we put the additional space onto the vertical list.

```
893 \noalign{\vskip#1\relax}}
```

\Let@ \Let@ is called by all environments where \\ ends a row of an alignment.

```
894 \def\Let@{\let\\\math@cr}
```

\restore@math@cr

We mentioned already that the exact meaning of \math@cr@@@ depends on the current environment. Since it is often a simple \cr we provide \restore@math@cr to reset it.

```
895 \def\restore@math@cr{\def\math@cr@@@{\cr}}
```

This is also the default case.

```
896 \restore@math@cr
```

\intertext

The \intertext command is used for inserting text between the rows of an alignment. It might better be done as an environment, but the \begingroup from \begin would cause the \noalign to fail.

```
897 \newcommand{\intertext}{\@amsmath@err{\Invalid@@\intertext}\@eha}
```

\intertext@ is called by all environments that allow the use of the \intertext command.

```
898 \def\intertext@{%
899 \def\intertext##1{%
```

If current mode is not vmode, the most likely reason is that the writer forgot the \\ that is supposed to precede \intertext. All right, then, let's try adding it our ownself. But, to be slightly careful: \\ does a futurelet, and it's slightly dangerous to allow a letted token to barge around loose in our internal code when it has been let to a conditional token like \fi. So let's interpose something in front of the \fi for the futurelet to take instead. (And careful again: it has to be something evanescent, not (e.g.) \relax which would cause the next halign cell to fire up and keep \noalign from working.)

```
900 \ifvmode\else\\@empty\fi

901 \noalign{%

902 \penalty\postdisplaypenalty\vskip\belowdisplayskip

903 \vbox{\normalbaselines
```

We need to do something extra if the outside environment is a list environment. I don't see offhand an elegant way to test "are we inside any list environment" that is both easy and reliable (for example, checking for zero \@totalleftmargin wouldn't catch the case where \@totalleftmargin is zero but \linewidth is less than \columnwidth), so it seems to me checking \linewidth is the best practical solution.

```
904 \ifdim\linewidth=\columnwidth
905 \else \parshape\@ne \@totalleftmargin \linewidth
906 \fi
907 \noindent##1\par}%
908 \penalty\predisplaypenalty\vskip\abovedisplayskip%
909 }%
910 }}
```

#### 15.2Implementing tags and labels

In this section we describe some of the macros needed to make the \tag command work in various places. We start by defining a help text to be used when a \tag command is used somewhere it should not appear.

\tag@help This is the default error help text provided when \tag generates an error message. Note that \newhelp generates a control sequence name from the string given as its argument so that a leading backslash is provided automatically.

- 911 \newhelp\tag@help
- {tag cannot be used at this point.\space
- If you don't understand why^^Jyou should consult 913
- the documentation.^^JBut don't worry: just continue, and I'll 914
- 915 forget what happened.}

\gobble@tag

This macro is to be used when \tag should silently skip its argument. It is made to handle the \*-form of \tag as well.

916 \def\gobble@tag{\@ifstar\@gobble\@gobble}

\invalid@tag

\invalid@tag is a macro that should be used whenever \tag appears in an illegal place. It sets up \tag@help (as defined above) as help message, prints its argument as error message, and skips \tag's argument.

917 \def\invalid@tag#1{\@amsmath@err{#1}{\the\tag@help}\gobble@tag}

\dft@tag \default@tag

\dft@tag provides a convenient way to disallow the use of \tag at certain points. One simply has to write

\let\tag\dft@tag

and the \tag command will produce an error message, with a suitable error help text, and discard its argument.

918 \def\dft@tag{\invalid@tag{\string\tag\space not allowed here}}

Since this is used several times we provide an abbreviation for it.

919 \def\default@tag{\let\tag\dft@tag}

Since this is also the default, i.e. the \tag command should not be used except in special places, we issue a \default@tag command.

920 \default@tag

Now that we have taken care of the case that \tag is not allowed we will provide some macros to process tags appropriately. As the user documentation states, a \tag command (without the asterisk typesets its argument according to the document styles' conventions, whereas a \tag\* command typesets its argument exactly as given. We define therefore the following interface:

\maketag@@ \maketag@@@ \tagform@ \tag is supposed to call \maketag@@ which checks whether an asterisk follows. If this is the case it calls up \maketag@@@ which sets its argument 'as is'. Otherwise \tagform@ is called to do the job. (This macro is to be defined appropriately by the document style.)

921 \def\maketag@@{\@ifstar\maketag@@@\tagform@}

We define \maketag@@@ to use the normal font of the document text (since this is the usual practice for numbering of document elements) and to put a box around the tag. Furthermore we use \moth for exceptional cases where the tag involves a superscript or some such math. (Probably from an explicit use of \tag\* rather than from the automatic numbering.)

922 \def\maketag@@@#1{\hbox{\m@th\normalfont#1}}

We use the following default definition for \tagform@ that puts only parentheses around the tag.

```
923 \def\tagform@#1{\maketag@@@{(\ignorespaces#1\unskip\@@italiccorr)}}
```

We need to insinuate \tagform@ into \@eqnnum in case eqnarray is used (probably in a document that was originally written without use of the amsmath package).

```
924 \iftagsleft@
925 \def\@eqnnum{\hbox to1sp{}\rlap{\normalfont\normalcolor
926 \hskip -\displaywidth\tagform@\theequation}}
927 \else
928 \def\@eqnnum{{\normalfont\normalcolor \tagform@\theequation}}
929 \fi
```

\thetag

Sometimes one needs to set a literal tag according to the rules of the document style. To achieve this we provide the \thetag command. It typesets its argument by calling \tagform@ on it.

```
930 \newcommand{\thetag}{\leavevmode\tagform@}
```

\df@tag \make@df@tag \make@df@tag@@ \make@df@tag@@@ Sometimes it is necessary for a \tag command to store a tag in a safe place and to process it later, e.g., for a tag in a row of an alignment where the tag can only be typeset when the \\\ at the end of the row was seen. Such a tag is stored in the macro \df@tag (for 'deferred tag'). For this purpose we provide the \make@df@tag macro. It is built very similar to the \maketag@@ macro above.

```
931 \let\df@tag\@empty 932 \def\make@df@tag{\@ifstar\make@df@tag@@\make@df@tag@@@}
```

\make@df@tag sets \@currentlabel and defines \df@tag appropriately.

To simplify the task of tracking \tag and \label commands inside math display environments, we defer \label commands until the tag is typeset, similar to the way that \tags themselves are deferred. This allows arbitrary placement of \label and \tag commands and also means we only increment the \equation counter when we really need to, thus avoiding the \setb@ck nonsense that used to be required.

```
933 \def\make@df@tag@@#1{%

934 \gdef\df@tag{\maketag@@@{#1}\def\@currentlabel{#1}}}

Autogenerated number:

935 \def\make@df@tag@@@#1{\gdef\df@tag{\tagform@{#1}%

936 \toks@\@xp{\p@equation{#1}}\edef\@currentlabel{\the\toks@}}}
```

\ltx@label \label@in@display \df@label Next, we store the default definition of \label in \ltx@label and then define a new version of \label for use in math display environments. \label@in@display merely issues a warning message if there is already a pending label (which will be discarded) and then stores the label in \df@label.

```
937 \let\ltx@label\label
938 %
939 \def\label@in@display{%
940 \ifx\df@label\@empty\else
941 \@amsmath@err{Multiple \string\label's:
942 \label '\df@label' will be lost}\@eha
943 \fi
944 \gdef\df@label
945 }
```

In case there is an enumerate inside a minipage inside an equation, we need to reset \label to its normal value:

```
946 \toks@\@xrp{\@arrayparboxrestore \let\label\ltx@label}% 947 \edef\@arrayboxrestore{\the\toks@} 948 \let\df@label\@empty
```

\make@display@tag

Now we define a macro to process \tag and \label commands in various display environments. If the @eqnsw switch is set, then we should supply an equation number; otherwise, if the @tag switch is set, we should use the tag stored in \df@tag. Finally, we process any pending \labels.

TODO: Arguably, \make@display@tag should issue a warning message if there is a \label but neither a tag nor an equation number. Also, it would probably be worthwhile to explore whether \iftag@ could be done away with and replaced by checks to see if \df@tag is empty or not.

```
949 \def\make@display@tag{%

950 \if@eqnsw \incr@eqnum \print@eqnum

951 \else \iftag@ \df@tag \global\let\df@tag\@empty \fi

952 \fi
```

Need to check the \ifmeasuring@ flag otherwise the \write node from \label might be discarded in a temp box and clearing \df@label will keep it from being reiterated on the real typesetting pass.

```
953 \ifmeasuring@
954 \else
955 \ifx\df@label\@empty
956 \else
957 \@xp\ltx@label\@xp{\df@label}%
958 \global\let\df@label\@empty
959 \fi
960 \fi
961 }
```

Now we define the special versions of \tag used within the align environments.

\tag@in@align

The \tag command may only appear once in a row of an alignment. Therefore we first check the switch tag@ that is set to false at the begin of every row. If this switch is true a \tag was already given in this row and we define \next@ to expand to a call to \invalid@tag.

```
962 \def\tag@in@align{%
963 \relax
964 \iftag@
965 \DN@{\invalid@tag{Multiple \string\tag}}%
966 \else
```

Otherwise we set the tag@ switch. But there is more to be done: we must also prevent the automatic generation of a tag. Therefore we also reset the @eqnsw.

```
967 \global\tag@true
```

Changed to  $\mbox{nonumber}$ , since that seems to be all that's required.—dmj, 1994/12/21

```
968 \nonumber
```

Within a row of an align environment the \tag command must not typeset the tag immediately since its position can be determined only later. Therefore we use the \make@df@tag macro defined earlier. Finally we call \next@ to process the argument that follows.

```
969 \let\next@\make@df@tag
```

```
970 \fi
971 \next@
972 }
```

\raisetag

This will modify the vertical placement of the tag of the current equation by  $\langle dimen \rangle$ . Note that according to the current uses of \raiseQtag in e.g., \placeQtagQgather, no adjustment occurs if the tag falls in its normal position; i.e., \raisetag has no effect unless the tag has already been shifted off-line.

```
973 \newcommand{\raisetag}[1]{\skip@#1\relax 974 \xdef\raise0tag{\vskip\iftagsleft0\else-\fi\the\skip0\relax}% 975}
```

\raise@tag will be reemptied at the beginning of each equation, which might occur at a \begin{xxx} or \\.

```
976 \let\raise@tag\@empty
```

\notag

For consistency we provide \notag, equivalent to \nonumber. The alternative would have been to rename \tag as \number to go along with \nonumber, but of course \number is a TeX primitive that should not be redefined.

```
977 \newcommand{\notag}{\nonumber}
```

\nonumber

Need to add some additional code to \nonumber to deal with some complications related to nested environments.

```
978 \renewcommand{\nonumber}{%
979 \if@eqnsw
980 \ifx\incr@eqnum\@empty \addtocounter{equation}\m@ne \fi
981 \fi
982 \let\print@eqnum\@empty \let\incr@eqnum\@empty
983 \global\@eqnswfalse
984 }
985 \def\print@eqnum{\tagform@\theequation}
986 \def\incr@eqnum{\refstepcounter{equation}\let\incr@eqnum\@empty}
```

# 16 Multiline equation environments

### 16.1 Remarks

In late 1994 David M. Jones did a thorough overhaul of these environments so that the number placement and a few other aspects are substantially improved over the original versions that were ported essentially unchanged from amstex.tex in 1989. Most of the commentary in this section is DMJ's, and comments of any significance that I added are marked by my initials and date [mjd, 1995/01/11].

### 16.2 Preliminaries

\ifinalign@ \ifingather@ We define two switches that are set to true in certain alignments: inalign@ and ingather@ inside of the align and gather environments. These switches are needed to control certain actions that depend on the surrounding conditions, more specifically: on the setting already done by the surrounding environments.

```
987 \newif\ifinalign@
988 \newif\ifingather@
```

Historical Note: Removed the \iffinany@ test [mjd,1999/06/28] since it was mainly used for the purpose now handled by \spread@equation.

```
@arrayparboxrestore Here we must reset a few additional parameters.
                      989 \@xp\def\@xp\@arrayparboxrestore\@xp{\@arrayparboxrestore
                            \ingather@false\inalign@false \default@tag
                      990
                            \let\spread@equation\@spread@equation
                      991
                      992
                            \let\reset@equation\@empty
                      993
                            \def\print@eqnum{\tagform@\theequation}%
                            \def\incr@eqnum{\refstepcounter{equation}\let\incr@eqnum\@empty}%
                      994
                      995 }
                     The switch tag@ is set to false at the beginning of every row and set to true by
            \iftag@
                     a \tag command. This allows us to check whether there is more than one tag
                     on a row.
                      996 \neq \sqrt{\frac{9}{1000}}
         \ifst@rred The switch st@rred is set to true by all starred environments and set to false
                     by the unstarred versions.
                      997 \newif\ifst@rred
                     All display environments get typeset twice—once during a "measuring" phase
      \ifmeasuring@
                     and then again during a "production" phase; \ifmeasuring@ will be used to
                     determine which case we're in, so we can take appropriate action.
                      998 \newif\ifmeasuring@
                     \ifshifttag@ is used by gather to communicate between \calc@shift@gather
       \ifshifttag@
                     and \place@tag@gather whether an equation tag should be shifted to a sepa-
                     rate line. It's also used by multline.
                      999 \newif\ifshifttag@
              \row@
                      1000 \newcount\row@
           \column@ The counter \column@ is used by the alignment macros to keep track of the
                     current column.
                     1001 \newcount\column@
       \column@plus \column@plus is a useful abbreviation.
                     1002 \def\column@plus{%
                     1003
                              \global\advance\column@\@ne
                     1004 }
        \maxfields@
                      1005 \newcount\maxfields@
           \add@amp
          \add@amps
                     1006 \end{add@amp} 1{\inf m#1&\end{add@amp}fi}
                     1007 \def\add@amps#1{%
                     1008
                              \begingroup
                     1009
                              \count@#1\advance\count@-\column@
                      1010
                              \edef\@tempa{\endgroup
                                \@xp\add@amp\romannumeral\number\count@ 000q}%
                      1011
                     1012
                              \@tempa
                     1013 }
```

```
The help text stored in \andhelp@ is used for errors generated by too many &
                 characters in a row.
                  1014 \newhelp\andhelp@
                  1015 {An extra & here is so disastrous that you should probably exit^^J
                  1016 and fix things up.}
                 \eqnshift@ is used by align and gather as the indentation of the lines of the
     \eqnshift@
                 environment from the left margin.
                  1017 \newdimen\eqnshift@
     \alignsep@
                  1018 \newdimen\alignsep@
     \tagshift@
                  1019 \newdimen\tagshift@
                 \mintagsep is the minimum allowable separation between an equation and its
     \mintagsep
                  tag. We set it to half a quad in \textfont2, which is TFX's built-in value.
                  1020 \mbox{\command{\mintagsep}{.5\fontdimen6\textfont\tw0}}
                 This should probably be a skip register [mjd,1999/06/18]
   \minalignsep
                  1021 \newcommand{\minalignsep}{10pt}
     \tagwidth@
                  1022 \newdimen\tagwidth@
     \totwidth@
                  1023 \newdimen\totwidth@
       \lineht@
                 The dimen register \lineht@ is used to keep track of the height (or depth, if
                  tags are on the right) of a row in an alignment.
                  1024 \newdimen\lineht@
     \tag@width
\savetaglength@
                 1025 \left\ \frac{1}{25} \right.
     \shift@tag
                          \ifcase\@xp#1\tag@lengths\fi
                 1026
                 1027 }
    \tag@shifts
                 1028
                 1029 \def\savetaglength@{%
                          \begingroup
                 1030
                 1031
                              \let\or\relax
                              \\del{tag0lengths} \
                 1032
                  1033
                          \endgroup
                  1034 }
                 1035
                 1036 \def\shift@tag#1{%
                          \ifcase\@xp#1\tag@shifts\fi\relax
                 1037
                 1038 }
                  1040 \let\tag@shifts\@empty
    \saveshift@
                 1041 \def\saveshift@#1{%
                 1042
                          \begingroup
                 1043
                              \let\or\relax
                 1044
                              \xdef\tag@shifts{\or#1\tag@shifts}%
                          \endgroup
                  1045
                  1046 }
```

\spread@equation

This does the line-spacing adjustment that is normally wanted for displayed equations. We also call \reset@strutbox@ here because otherwise a preceding font size change might leave \strutbox@ with wrong contents. This is a less-than-ideal solution but probably good enough for now, until the situation can be overhauled.

```
1047 \end{0} $1048 \end{0} in {\end{0} equation $$ 1048 \end{0} equation $$ 1049 \end{0} equat
```

\displ@y \displ@y@ \@display@init \displ@y is from plain.tex, with \interdisplaylinepenalty changed to \@eqpen. Also we transplanted most of its internal organs to \@display@init to support \displ@y@ and other possibilities. Don't try to make sense of these naming conventions! They are a narrowly calculated mishmash of Knuth/Spivak/Lamport/Mittelbach precedents. The reason for not cleaning them up and forcing all names to a consistent scheme is that then in principle we'd have to do it everywhere else too. And we programmers are paranoid about the side effects of name changes.

```
1050 \def\displ@y{\@display@init{}}
1051 \def\@display@init#1{%
        \global\dt@ptrue \spread@equation
1052
        \everycr{%
1053
             \noalign{%
1054
                 #1%
1055
                 \ifdt@p
1056
                      \global\dt@pfalse
1057
                      \vskip-\lineskiplimit
1058
                      \vskip\normallineskiplimit
1059
                 \else
1060
                      \penalty\@eqpen \global\dspbrk@lvl\m@ne
1061
                 \fi
1062
1063
             }%
1064
        }%
1065 }
```

\displ@y@ is nearly the same; it additionally sets the tag@ switch and the \column@ and \dspbrk@lvl counters to their default values. The argument is normally a bit of code to empty out \raise@tag, but in multline we don't want that to happen in \everycr.

```
\label{local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_loc
```

\black@

This macro is made to produce an overfull box message and possibly (depending on the value of **\overfullrule**) a rule in the margin if the total width of an alignment is larger than the value of **\displaywidth**.

```
1070 \def\black@#1{%
        \noalign{%
1071
             \ifdim#1>\displaywidth
1072
1073
                 \dimen@\prevdepth
1074
                 \nointerlineskip
1075
                 \vskip-\ht\strutbox@
                 \vskip-\dp\strutbox@
1076
                 \vbox{\noindent\hbox to#1{\strut@\hfill}}%
1077
                 \prevdepth\dimen@
1078
             \fi
1079
1080
        }%
1081
```

\restorecounters@

\savecounters@ These are used during the measuring phase of the various display math environments to save and restore the values of all LATEX counters. We make these local to a group, so nested environments works.

> Changed \stepcounter to \csname c@...\endcsname to avoid overhead of ifundefined test [mjd, 1995/01/20].

```
1082 \def\savecounters@{%
        \begingroup
1084
             \def\@elt##1{%
               \global\csname c@##1\endcsname\the\csname c@##1\endcsname}%
1085
             \xdef\@gtempa{%
1086
                 \cl@@ckpt
1087
                 \let\@nx\restorecounters@\@nx\@empty
1088
            }%
1089
        \endgroup
1090
1091
        \let\restorecounters@\@gtempa
1092 }
1093 %
1094 \let\restorecounters@\@empty
```

\savealignstate@ \restorealignstate@

These are used to save the values of various parameters that are shared by align and gather when the former is used inside the latter.

```
1095 \def\savealignstate@{%
1096
        \begingroup
1097
             \let\or\relax
1098
             \xdef\@gtempa{%
1099
                 \global\totwidth@\the\totwidth@
                 \global\row@\the\row@
1100
                 \gdef\@nx\tag@lengths{\tag@lengths}%
1101
                 \let\@nx\restorealignstate@\@nx\@empty
1102
1103
            }%
1104
        \endgroup
        \let\restorealignstate@\@gtempa
1105
1106 }
1107
1108 \let\restorealignstate@\@empty
```

\savecolumn@

\restorecolumn@

```
1109 \def\savecolumn@{%
      \edef\restorecolumn@{%
1110
        \global\column@\number\column@
1111
1112
        \let\@nx\restorecolumn@\@nx\@empty
1113
1114 }
1115 \let\restorecolumn@\@empty
```

#### Scanning the environment's body 16.3

Several of the math alignment macros must scan their body twice: once to determine how wide the columns are and then to actually typeset them. This means that we must collect all text in this body before calling the environment macros.

\@envbody We start by defining a token register to contain the body.

1116 \newtoks\@envbody

\addto@envbody

Then we define a macro to add something (i.e. its argument) to the token register \@envbody.

```
1117 \end{add} to @envbody #1{\global\envbody \envbody \envbody $$1}}
```

\collect@body

The macro \collect@body starts the scan for the \end{...} command of the current environment. It takes a macro name as argument. This macro is supposed to take the whole body of the environment as its argument. For example, \begin{align} would call \collect@body\@align if @align#1{...} is the macro that sets the alignment with body #1.

```
1118 \def\collect@body#1{%
1119 \@envbody{\@xp#1\@xp{\the\@envbody}}%
1120 \edef\process@envbody{\the\@envbody\@nx\end{\@currenvir}}%
1121 \@envbody\@emptytoks \def\begin@stack{b}%
```

If we simply called **\collect@body** directly, the error message for a **\par** token (usually from a blank line) would be

! Paragraph ended before \collect@@body was complete.

But we use a little finesse to get a more intelligible error message:

! Paragraph ended before \multline\* was complete.

In order to avoid using up csnames unnecessarily we use the actual environment name as the name of the temporary function that is \let to \collect@body; but then in order to preserve the theoretical possibility of nesting for environments that use \collect@body (not currently required by any amsmath environment [mjd,1999/06/23]), we do the \let inside a group.

```
1122 \begingroup
1123 \@xp\let\csname\@currenvir\endcsname\collect@@body
This small twist eliminates the need for \expandafter's in \collect@@body.
1124 \edef\process@envbody{\@xp\@nx\csname\@currenvir\endcsname}%
1125 \process@envbody
1126 }
```

\push@begins

When adding a piece of the current environment's contents to \@envbody, we scan it to check for additional \begin tokens, and add a 'b' to the stack for any that we find.

```
1127 \def\push@begins#1\begin#2{%
1128 \ifx\end#2\else b\@xp\push@begins\fi
1129 }
```

\collect@@bodv

\collect@body takes two arguments: the first will consist of all text up to the next \end command, the second will be the \end command's argument. If there are any extra \begin commands in the body text, a marker is pushed onto a stack by the \push@begins function. Empty state for this stack means that we have reached the \end that matches our original \begin. Otherwise we need to include the \end and its argument in the material that we are adding to our environment body accumulator.

**Historical Note:** In a former implementation, the error messages resulting from a typo in the environment name were unsatisfactory, because it was matching of the environment name that was used to determine the end of our environment body, instead of counting begin-end pairs. Thanks to Lars Hellström for a suggestion that led to this improvement. [mjd,1999/06/23]

```
1130 \def\collect@@body#1\end#2{%

1131 \edef\begin@stack{\push@begins#1\begin\end \@xp\@gobble\begin@stack}%

1132 \ifx\@empty\begin@stack

1133 \endgroup
```

```
1134 \@checkend{#2}%
1135 \addto@envbody{#1}%
1136 \else
1137 \addto@envbody{#1\end{#2}}%
1138 \fi
1139 \process@envbody % A little tricky! Note the grouping
1140 }
```

## 16.4 Simple aligning environments

\math@cr@@@aligned

From tabskip we get an extra space of minalignsep after every second column; but when this falls at the right edge of the whole aligned structure, we need to cancel that space.

```
1141 \def\math@cr@@@aligned{%

1142 \ifodd\column@ \let\next@\@empty

1143 \else \def\next@{&\kern-\alignsep@}%

1144 \fi

1145 \next@ \cr

1146 }
```

\start@aligned

The aligned and alignedat environments are identical except that the latter takes a mandatory argument to specify the number of align structures, while the former allows any number of align structures automatically (the use of alignedat is deprecated). So, they will be defined in terms of  $\slash$  which will take two arguments. The first argument specifies the placement of the environments; it is either c, t, or b. The second is the number of align structures; a value of -1 means that an arbitrary number are allowed.

```
1147 \newcommand{\start@aligned}[2]{%
1148 \RIfM@\else
1149 \nonmatherr@{\begin{\@currenvir}}%
1150 \fi
1151 \savecolumn@ % Assumption: called inside a group
```

The \null here is to keep the \, glue from causing the invocation of the clause in TeX's built-in tag placement algorithm that can cause an equation to be shifted all the way over to the margin.

```
1152 \null\,%
1153 \if #1t\vtop \else \if#1b \vbox \else \vcenter \fi \fi \bgroup
1154 \maxfields@#2\relax
1155 \ifnum\maxfields@>\m@ne
1156 \multiply\maxfields@\tw@
```

Introduced new  $\mbox{math@cr@@@}$  so we can provide standard error message for too many &'s in alignedat.

Reset the meaning of  $\setminus \setminus$ .

1163 \Let@ \chardef\dspbrk@context\@ne

Restore the default definition of \tag (error message), in case aligned is used inside, e.g., a gather environment that accepts \tag.

```
1164 \default@tag
1165 \spread@equation % no-op if already called
```

Finally we start the alignment itself. For aligned we add \minalignsep after every second column to mimic the behavior of align. For alignedat the user has to specify interalign space explicitly.

```
1166
             \global\column@\z@
1167
             \ialign\bgroup
                &\column@plus
1168
                 \hfil
1169
                 \strut@
1170
                 $\m@th\displaystyle{##}$%
1171
                 \tabskip\z@skip
1172
                &\column@plus
1173
                 $\m@th\displaystyle{{}##}$%
1174
1175
                 \hfil
                 \tabskip\alignsep@
1176
1177
                 \crcr
1178 }
```

\math@cr@@@aligned

\math@cr@@@aligned checks to make sure the user hasn't put in too many &s in alignedat. Since alignedat doesn't use \displ@y@, we also reset \column@ here. Note than in aligned, \column@ will increase without bound, since it never gets reset, but this is harmless.

```
1179 \def\math@cr@@@alignedat{%
        \ifnum\column@>\maxfields@
1180
1181
             \begingroup
               \measuring@false
1182
               \@amsmath@err{Extra & on this line}%
1183
                 {\the\andhelp@}% "An extra & here is disastrous"
1184
1185
             \endgroup
        \fi
1186
        \global\column@\z@
1187
1188
        \cr
1189 }
```

\alignsafe@testopt

Testing for an optional argument can be really, really tricky in certain complicated contexts. This we discovered by getting some bug reports for uses of aligned. So here is a safer form of LATEX's \@testopt function.

```
1190 \def\alignsafe@testopt#1#2{%
1191 \relax\iffalse{\fi\ifnum'}=0\fi
1192 \@ifnextchar[%
1193 {\let\@let@token\relax \ifnum'{=\z@\fi\iffalse}\fi#1}%
1194 {\let\@let@token\relax \ifnum'{=\z@\fi\iffalse}\fi#1[#2]}%
1195 }
```

aligned The aligned environment takes an optional argument that indicates its vertical position in relation to surrounding material: t, c, or b for top, center, or bottom.

```
1196 \newenvironment{aligned}{%
1197  \let\@testopt\alignsafe@testopt
1198  \aligned@a
1199 }{%
1200  \crcr\egroup
1201  \restorecolumn@
1202  \egroup
1203 }
1204 \newcommand{\aligned@a}[1][c]{\start@aligned{#1}\m@ne}
```

alignedat

To get a top or bottom positioned alignedat structure, you would write something like

```
\begin{alignedat}[t]{3}
               1205 \newenvironment{alignedat}{%
               1206 \let\@testopt\alignsafe@testopt
               1207
                    \alignedat@a
               1208 }{%
               1209
                     \endaligned
               1210 }
               1211 \newcommand{\alignedat@a}[1][c]{\start@aligned{#1}}
     gathered The gathered environment is for several lines that are centered independently.
               1212 \newenvironment{gathered}[1][c]{%
                       \RIfM@\else
               1213
               1214
                           \nonmatherr@{\begin{gathered}}%
                       \fi
               1215
                       \null\,%
               1216
                       \if #1t\vtop \else \if#1b\vbox \else \vcenter \fi\fi \bgroup
               1217
                           \Let@ \chardef\dspbrk@context\@ne \restore@math@cr
               1218
                           \spread@equation
               1219
               1220
                           \ialign\bgroup
               1221
                               \hfil\strut@$\m@th\displaystyle##$\hfil
               1222
               1223 }{%
               1224
                     \endaligned
               1225 }
                       The gather environment
               16.5
\start@gather
               1226 \def\start@gather#1{%
                       \RIfM@
               1227
                           \nomath@env
               1229
                           \DN@{\@namedef{end\@currenvir}{}\@gobble}%
               1230
                    \else
               1231
                           $$%
               1232
                           #1%
               1233
                           \ifst@rred \else \global\@eqnswtrue \fi
               1234
                           \let\next@\gather@
                       \fi
               1235
               1236
                       \collect@body\next@
               1237 }
       gather
      gather*
               1238 \newenvironment{gather}{%
               1239 \start@gather\st@rredfalse
               1240 }{%
               1241
                     \math@cr \black@\totwidth@ \egroup
               1242 $$\ignorespacesafterend
               1243 }
               1244
               1245 \newenvironment{gather*}{%
               1246 \start@gather\st@rredtrue
               1247 }{%
               1248
                     \endgather
               1249 }
     \gather@
```

1250 \def\gather@#1{%

```
1251
                     \ingather@true \let\split\insplit@
            1252
                     \let\tag\tag@in@align \let\label\label@in@display
            1253
                     \chardef\dspbrk@context\z@
            1254
                     \intertext@ \displ@y@ \Let@
                     \let\math@cr@@@\math@cr@@@gather
            1255
                     \gmeasure@{#1}%
            1256
                     \global\shifttag@false
            1257
                     \tabskip\z@skip
            1258
                     \global\row@\@ne
            1259
             1260
                     \halign to\displaywidth\bgroup
             1261
                          \strut@
             1262
                          \setboxz@h{$\m@th\displaystyle{##}$}%
             1263
                          \calc@shift@gather
             1264
                          \set@gather@field
             1265
                          \tabskip\@centering
                        \scriptstyle \ \setboxz@h{\strut@{##}}%
             1266
            1267
                          \place@tag@gather
                          \tabskip \iftagsleft@ \gdisplaywidth@ \else \z@skip \span\fi
            1268
            1269
                          \crcr
            1270
                         #1%
            1271 }
\gmeasure@
            1272 \def\gmeasure@#1{%
            1273
                     \begingroup
            1274
                          \measuring@true
                          \totwidth@\z@
            1275
                          \global\let\tag@lengths\@empty
            1276
                          \savecounters@
            1277
            1278
                          \setbox\@ne\vbox{%
                              \everycr{\noalign{\global\tag@false
            1279
                                \global\let\raise@tag\@empty \global\column@\z@}}%
            1280
                              \let\label\@gobble
             1281
            1282
                              \halign{%
                                   \setboxz@h{$\m@th\displaystyle{##}$}%
            1283
                                   \ifdim\wdz@>\totwidth@
            1284
                                       \global\totwidth@\wdz@
            1285
                                  \fi
            1286
                                 \scriptstyle \ \setboxz@h{\strut@{##}}%
            1287
                                  \savetaglength@
            1288
            1289
                                  \crcr
                                  #1%
            1290
                                   \math@cr@@@
            1291
            1292
                              }%
                         }%
            1293
                          \restorecounters@
            1294
                          \if@fleqn
            1295
                              \global\advance\totwidth@\@mathmargin
            1296
                          \fi
            1297
            1298
                          \iftagsleft@
             1299
                              \ifdim\totwidth@>\displaywidth
                                  \global\let\gdisplaywidth@\totwidth@
             1300
             1301
                                   \global\let\gdisplaywidth@\displaywidth
             1302
             1303
                              \fi
                          \fi
             1304
                     \endgroup
            1305
            1306 }
```

\math@cr@@@gather Modified \math@cr@@@gather so that it always puts in the final field, which

needs to be done under the new method for determining tag placement. This is probably more efficient anyway.

```
1307 \def\math@cr@@@gather{%
1308 \ifst@rred\nonumber\fi
1309 &\relax
1310 \make@display@tag
1311 \ifst@rred\else\global\@eqnswtrue\fi
```

We advance \row@ here, rather than at the beginning of the preamble, because otherwise the split environment will cause \row@ to be advanced twice instead of once.

```
1312     \global\advance\row@\@ne
1313     \cr
1314 }
```

\calc@shift@gather

\calc@shift@gather has must make two decisions: (1) whether the equation tag for the current line should be put on a separate line and (2) what the distance between the equation and the equation tag should be. We implement TEX's built-in tag-placement as well as possible, with one improvement: the minimum separation between tag and equation is now a user-settable parameter.

[1995/01/17] Added a check to make sure that the width of the tag on the current line is > 0 before testing to see if tagwidth + linewidth + mintagsep > displaywidth. Since an imbedded align shows up as line with width  $\land$  displaywidth, and even lines without a tag get processed as if an empty tag were present, the result was that the empty tag assigned to the line containing the align was being shifted downwards, creating extra space after the align.

```
1315 \def\calc@shift@gather{%
1316 \dimen@\mintagsep\relax
1317 \tagwidth@\tag@width\row@\relax
```

If we're in fleqn mode, there is no flexibility about placement of the equation, so all we can do is see if there's room for the tag in the given margin.

```
\if@fleqn
1318
             \global\eqnshift@\@mathmargin
1319
1320
             \ifdim\tagwidth@>\z@
                  \advance\dimen@\tagwidth@
1321
                  \iftagsleft@
1322
                      \ifdim\dimen@>\@mathmargin
                           \global\shifttag@true
1324
1325
                      \fi
1326
                  \else
1327
                      \advance\dimen@\@mathmargin
                      \advance\dimen@\wdz@
1328
                      \ifdim\dimen@>\displaywidth
1329
                          \global\shifttag@true
1330
                      \fi
1331
1332
                  \fi
             \fi
1333
         \else
1334
             \global\eqnshift@\displaywidth
1335
1336
             \global\advance\eqnshift@-\wdz@
             \left\langle \frac{1}{2}\right\rangle 
1337
                  \multiply\dimen@\tw@
1338
                  \advance\dimen@\wdz@
1339
                  \advance\dimen@\tagwidth@
1340
                  \ifdim\dimen@>\displaywidth
1341
1342
                      \global\shifttag@true
1343
                  \else
```

```
1344
                                           \ifdim\eqnshift@<4\tagwidth@
                     1345
                                                \global\advance\eqnshift@-\tagwidth@
                     1346
                                           \fi
                                       \fi
                     1347
                                  \fi
                     1348
                                  \global\divide\eqnshift@\tw@
                     1349
                                  \iftagsleft@
                     1350
                                       \global\eqnshift@-\eqnshift@
                     1351
                                       \global\advance\eqnshift@\displaywidth
                     1352
                     1353
                                       \global\advance\eqnshift@-\wdz@
                     1354
                                  \fi
                     1355
                                  \ifdim\eqnshift@<\z@
                                       \global\eqnshift@\z@
                     1356
                                  \fi
                     1357
                              \fi
                     1358
                     1359 }
\place@tag@gather
\set@gather@field
                     1360 \ensuremath{\mbox{\sc QtagQgather}} \%
                              \iftagsleft@
                     1361
                     1362
                                  \kern-\gdisplaywidth@
                     1363
                                  \ifshifttag@
                     1364
                                       \rlap{\vbox{%
                     1365
                                           \normalbaselines
                     1366
                                           \boxz@
                     1367
                                           \vbox to\lineht@{}%
                     1368
                                           \raise@tag
                                       }}%
                     1369
                                       \global\shifttag@false
                     1370
                                  \else
                     1371
                                       \rlap{\boxz@}%
                     1372
                                  \fi
                     1373
                              \else
                     1374
                                  \ifdim\totwidth@>\displaywidth
                     1375
                                       \dimen@\totwidth@
                     1376
                     1377
                                       \advance\dimen@-\displaywidth
                     1378
                                       \kern-\dimen@
                     1379
                                  \fi
                                  \ifshifttag@
                     1380
                                       \displaystyle \prod_{v \in \mathbb{N}} 
                     1381
                                           \raise@tag
                     1382
                                           \normalbaselines
                     1383
                                           \setbox\@ne\null
                     1384
                                           \dp\@ne\lineht@
                     1385
                                           \box\@ne
                     1386
                                           \boxz@
                     1387
                     1388
                                       }}%
                                       \global\shifttag@false
                     1389
                                  \else
                     1390
                                       1391
                     1392
                                  \fi
                              \fi
                     1393
                     1394 }
                     1395 %
                     1396 \def\set@gather@field{%
                              \iftagsleft@
                     1397
                                  \global\lineht@\ht\z@
                     1398
                     1399
                              \else
                                  \global\lineht@\dp\z@
                     1400
```

```
1401 \fi
1402 \kern\eqnshift@
1403 \boxz@
1404 \hfil
1405 }
```

# 16.6 The align family of environments

The align, flalign, alignat, xalignat, and xxalignat environments are virtually identical, and thus will share much code. We'll refer to the environments generically as "align" and will distinguish between them explicitly only when necessary.

\ifxxat@ \ifcheckat@ \xatlevel@ The \xatlevel@ macro will be used, informally speaking, to distinguish between the alignat and xalignat, and xxalignat environments.

```
1406 \newif\ifxxat@
1407
1408 \newif\ifcheckat@
1409
1410 \let\xatlevel@\@empty
```

\start@align

\start@align will be called by all of the align-like environments. The first argument will be the \xatlevel@, i.e., 0, 1, or 2; the second argument will be either \st@rredtrue or \st@rredfalse. The third argument will be the number of aligned structures in the environment (either as supplied by the user, or -1 to indicate that checking shouldn't be done). After performing the appropriate error detection and initialization, \start@align calls \align@.

Note that the **\equation** counter is no longer stepped at the beginning of these environments.

TODO: Implement \shoveleft and \shoveright for align.

```
1411 \def\start@align#1#2#3{%
         \let\xatlevel@#1% always \z@, \@ne, or \tw@
1412
         \maxfields@#3\relax
1413
         \ifnum\maxfields@>\m@ne
1414
             \checkat@true
1415
             \ifnum\xatlevel@=\tw@
1416
1417
                  \xxat@true
1418
             \fi
1419
             \multiply\maxfields@\tw@
        \else
1420
             \checkat@false
1421
         \fi
1422
         \ifingather@
1423
             \iffalse{\fi\ifnum0='}\fi
1424
             \DN@{\vcenter\bgroup\savealignstate@\align@#2}%
1425
         \else
1426
1427
             \ifmmode
1428
               \if@display
                  \DN@{\align@recover}%
1429
               \else
1430
                 \nomath@env
1431
                 \DN0{\@namedef{end\@currenvir}{}\@gobble}%
1432
               \fi
1433
             \else
1434
1435
                 \let\split\insplit@
1436
                  \DN0{\langle align0#2}\%
1437
1438
             \fi
```

```
1439 \fi
1440 \collect@body\next@
1441 }
```

With version 1.2 of amsmath, it was possible to use align\* and relatives in certain wrong contexts without getting an error, e.g.

```
\begin{equation*}
\begin{align*}
...
\end{align*}
\end{equation*}
```

For backward compatibility we therefore give only a warning for this condition instead of a full error, and try to recover using the aligned environment. The alignment of the material may be adversely affected but it will at least remain readable.

```
1442 \def\align@recover#1#2#3{%
           1443
                \endgroup
                \@amsmath@err{%
           1445 Erroneous nesting of equation structures; \MessageBreak
           1446 trying to recover with 'aligned'%
                }\@ehc
           1448
                 \begin{aligned}\relax#1\end{aligned}%
           1449 }
          The definitions of the various align environments are quite straight-forward.
   align*
           1450 \newenvironment{alignat}{%
 flalign
                 \start@align\z@\st@rredfalse
flalign*
           1452 }{%
  alignat* 1454 }
xalignat 1455 \newenvironment{alignat*}{%
xalignat* 1456 \start@align\z@\st@rredtrue
xxalignat 1457 }{%
           1458
                 \endalign
           1459 }
           1460 \newenvironment{xalignat}{%
           1461 \start@align\@ne\st@rredfalse
           1462 }{%
           1463
                \endalign
           1464 }
           1465 \newenvironment{xalignat*}{%
           1466 \start@align\@ne\st@rredtrue
           1467 }{%
           1468 \endalign
           1469 }
           1470 \newenvironment{xxalignat}{%
                 \start@align\tw@\st@rredtrue
           1472 }{%
           1473
                 \endalign
           1474 }
           1475 \newenvironment{align}{%
                \start@align\@ne\st@rredfalse\m@ne
           1476
           1477 }{%
                 \math@cr \black@\totwidth@
           1478
                 \egroup
           1479
           1480
                 \ifingather@
                   \restorealignstate@
           1481
```

```
\egroup
                  1482
                           \nonumber
                           \ifnumO='{\fi\iffalse}\fi
                  1485 \else
                          $$%
                  1486
                        \fi
                  1487
                  1488 \ignorespacesafterend
                  1489 }
                  1490 \newenvironment{align*}{%
                  1491 \start@align\@ne\st@rredtrue\m@ne
                  1492 }{%
                  1493
                        \endalign
                  1494 }
                  1495 \newenvironment{flalign}{%
                  1496 \qquad \texttt{\start@align\tw@\st@rredfalse\m@ne}
                  1497 }{%
                  1498 \endalign
                  1499 }
                  1500 \newenvironment{flalign*}{%
                  1501 \start@align\tw@\st@rredtrue\m@ne
                  1502 }{%
                        \endalign
                  1503
                  1504 }
         \align@
                  TODO: Some of these sets of initializations show up in multiple places. It might
                  be worth making an abbreviation for them.
                  1505 \def\align@#1#2{%
                           \inalign@true \intertext@ \Let@ \chardef\dspbrk@context\z@
                  1506
                  1507
                           \ifingather@\else\displ@y@\fi
                  1508
                           \let\math@cr@@@\math@cr@@@align
                           \ifxxat@\else \let\tag\tag@in@align \fi
                           \let\label\label@in@display
                   1511
                           #1% set st@r
                           \ifst@rred\else \global\@eqnswtrue \fi
                  1512
                           \measure@{#2}%
                  1513
                           \global\row@\z@
                  1514
                           \tabskip\eqnshift@
                  1515
                           \halign\bgroup
                  1516
                               \span\align@preamble\crcr
                  1517
                  1518
                               #2%
                  1519 }
\math@cr@@@align
                   1520 \def\math@cr@@@align{%
                   1521 \ifst@rred\nonumber\fi
                  1522
                         \if@eqnsw \global\tag@true \fi
                        \global\advance\row@\@ne
                  1523
                        \add@amps\maxfields@
                  1524
                        \omit
                  1525
                        \kern-\alignsep@
                  1526
                        \iftag@
                  1527
                  1528
                           \setboxz@h{\@lign\strut@{\make@display@tag}}%
                  1529
                           \place@tag
                  1530
                        \ifst@rred\else\global\@eqnswtrue\fi
                  1532
                        \global\lineht@\z@
                  1533
                        \cr
                  1534 }
```

```
.0cr000align0measure
```

```
1535 \def\math@cr@@@align@measure{%
                                                       1536
                                                                            &\omit
                                                                               \global\advance\row@\@ne
                                                       1537
                                                                               \ifst@rred\nonumber\fi
                                                       1538
                                                        1539
                                                                               \if@eqnsw \global\tag@true \fi
                                                        1540
                                                                               \ifnum\column@>\maxfields@
                                                        1541
                                                                                           \ifcheckat@
                                                       1542
                                                                                                       \begingroup
                                                                                                             \measuring@false
                                                       1543
                                                                                                             \@amsmath@err{Extra & on this line}%
                                                       1544
                                                                                                                  {\the\andhelp@}% "An extra & here is disastrous"
                                                       1545
                                                       1546
                                                                                                       \endgroup
                                                       1547
                                                                                                       \global\maxfields@\column@
                                                       1548
                                                       1549
                                                                               \fi
                                                       1550
                                                                               \setboxz@h{\@lign\strut@{%
                                                       1551
                                                                                          \if@eqnsw
                                                       1552
                                                                                                       \stepcounter{equation}%
                                                       1553
                                                                                                       \tagform@\theequation
                                                       1554
                                                                                           \else
                                                       1555
                                                                                                       \iftag@\df@tag\fi
                                                       1556
                                                                                           \fi
                                                       1557
                                                                               }}%
                                                        1558
                                                        1559
                                                                               \savetaglength@
                                                        1560
                                                                               \ifst@rred\else\global\@eqnswtrue\fi
                                                        1561
                                                       1562 }
        \field@lengths
\savefieldlength@
                                                       1563 \let\field@lengths\@empty
        \fieldlengths@
                                                       1565 \def\savefieldlength@{%
                                                                               \begingroup
                                                       1566
                                                                                           \let\or\relax
                                                       1567
                                                                                           \xdef\field@lengths{%
                                                       1568
                                                                                                       \field@lengths
                                                       1569
                                                                                                       \ifnum\column@=0
                                                       1570
                                                       1571
                                                                                                                   \or
                                                                                                       \else
                                                        1572
                                                       1573
                                                                                                       \fi
                                                        1574
                                                       1575
                                                                                                       \the\wdz@
                                                                                          }%
                                                       1576
                                                                               \endgroup
                                                       1577
                                                       1578 }
                                                       1579
                                                       1580 \def\fieldlengths@#1{%
                                                                               \ifcase\@xp#1\field@lengths\fi
                                                       1581
                                                        1582 }
                                                       extract a given width using \ifcase.
                                                       1583 \let\maxcolumn@widths\@empty
                                                       \mbox{\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$}\mbox{$\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox{$}\mbox
           \maxcol@width
```

\maxcolumn@widths

\maxcolumn@widths will be used to hold the widths of the fields of the alignat environment. The widths will be separated by the token \or, making it easy to

the nth field of  $\mbox{maxcolumn@widths.}$ ) It expands to a  $\langle dimen \rangle$ , so it can be used

as the right-hand side of a  $\langle variable \ assignment \rangle$  or  $\langle arithmetic \rangle$  statement. It's argument can be any  $\langle number \rangle$ ,  $\langle integer \ variable \rangle$  or macro that expands to one of these. [Check to make sure this is true.]

This is subtler than it looks.

1584 \def\maxcol@width#1{% 1585 \ifcase\@xp#1\maxcolumn@widths\fi\relax 1586 }

Now comes the real fun. A typical align environments looks something like this, where the vertical bars mark the edges of the fields of the underlying \halign:

Note that each align structure consists of two fields, with no space between them (a small space has been added here to highlight the boundaries). Furthermore, the text inside the odd-numbered fields is flushright, while the text inside the even-numbered fields is flushleft. The equation tags (shown on the right here) can be on either the right or the left. If there is not room (in a sense to be defined shortly) for the tag on the same line as the equation, the tag will be shifted to a separate line.

Each environment also has a certain number of "flexible spaces," meaning spaces whose width we are allowed to adjust to take up the amount of "free space" in the line, meaning the space not taken up by the equation tag and the fields of the underlying \halign.

The flexible spaces come in two flavors: interalign spaces and margin spaces. If there are n align structures (n=3 in the illustration above), there are n-1 interalign spaces, unless we are in an alignat environment, in which case there are no flexible interalign spaces.

The number of margin spaces is a little more complicated: Normally, there are two, but if we're in fleqn mode, there is only one. Furthermore, if we're in an xxalignat or flalign environment (corresponding to  $\xet valevel 0 = 2$ , then there are no flexible margin spaces.

Calculating the interalign and margin spaces is done in two stages.

First, the total amount of free space is divided uniformly among all the flexible spaces, without regard for the lengths of the tags on the various lines. For the non-fleqn case, this corresponds to centering the align structures between the margins. Note that in fleqn mode, the right margin is still allowed to be larger than \@mathmargin. This introduces an element of asymmetry into the appearance of the environment, but it has the advantage of leaving more space for equation tags in the right margin. If the right margin were constrained to be equal to the left margin in this case, tags would need to be shifted to a separate line more often than would be desirable.

Ordinarily, all flexible spaces will be given the same width. However, this is not invariably true, since the interalign spaces are constrained to be at least \minalignsep wide, while—in the absence of equation tags, at least—the margin spaces are allowed to shrink to zero. As we shall see in a minute, if there are tags in the environment, then the margins are also bounded below by \mintagsep.

Next, we examine each line of the environment that has a tag to see if there is a gap of at least \mintagsep between the equation and its tag. If there isn't, we attempt to center the equation between the tag and the opposite margin,

leaving a gap of at least  $\mbox{mintagsep}$  on either side, in order to preserve some symmetry, i.e., we want the equation to look like it's centered between the margin and the tag, so we don't want the margin space to be less than the gap between the tag and the equation. (Arguably, it would be better to allow the margin space to shrink to zero in this case in order to avoid shifting the tag to a separate line at any cost, but that would require all of our calculations to be a little more complicated and hence a little slower.) Finally, if no values of the interalign spaces and the margins (with the constraints outlined above) will produce an acceptable distance between the equation and its tag, then the tag will be shifted to a separate line.

\measure@

\measure@ collects the various bits of information that we'll need to perform the calculations outlined above, namely, the number of align structures in the environment, the natural lengths of the fields on each row, the maximum widths of each column, and the widths of the equation tags on each line. It also calculates the number of flexible interalign and margin spaces and computes the initial values of the parameters \eqnshift@ and \alignsep@, which correspond to the widths of the margins and the interalign spaces, respectively.

```
1587 \def\measure@#1{%
        \begingroup
1588
1589
             \measuring@true
1590
             \global\eqnshift@\z@
             \global\alignsep@\z@
1591
             \global\let\tag@lengths\@empty
1592
             \global\let\field@lengths\@empty
1593
             \savecounters@
1594
             \global\setbox0\vbox{%
1595
                 \let\math@cr@@@\math@cr@@@align@measure
1596
                 \everycr{\noalign{\global\tag@false
1597
                   \global\let\raise@tag\@empty \global\column@\z@}}%
1598
                 \let\label\@gobble
1599
                 \global\row@\z@
1600
                 \tabskip\z@
1601
1602
                 \halign{\span\align@preamble\crcr
1603
                     #1%
1604
                      \math@cr@@@
1605
                      \global\column@\z@
1606
                      \add@amps\maxfields@\cr
                 }%
1607
            }%
1608
             \restorecounters@
1609
```

It's convenient to have \maxfields@ rounded up to the nearest even number, so that \maxfields@ is precisely twice the number of align structures.

```
1610 \ifodd\maxfields@
1611 \global\advance\maxfields@\@ne
1612 \fi
```

It doesn't make sense to have a single align structure in either flalign or xxalignat. So, we check for that case now and, if necessary, switch to an align or alignat. Arguably, we should issue a warning message, but why bother?

```
1613 \ifnum\xatlevel@=\tw@
1614 \ifnum\maxfields@<\thr@@
1615 \let\xatlevel@\z@
1616 \fi
1617 \fi
```

\box0 now contains the lines of the \halign. After the following maneuver, \box1 will contain the last line of the \halign, which is what we're interested in. (Incidentally, the penalty we're removing is the \@eqpen inserted by \math@cr. Normally, this is \interdisplaylinepenalty, unless the user has overridden that with a \displaybreak command.)

```
1618 \setbox\z@\vbox{%

1619 \unvbox\z@\unpenalty \global\setbox\@ne\lastbox

1620 }%
```

\box1 begins with \tabskip glue and contains alternating \hboxes (the fields whose widths we're trying to get) and \tabskip glue [need better diagram]:

```
\hbox{\tabskip\hbox\tabskip...\hbox\tabskip}
```

In fact, all the \tabskip glue will be 0pt, because all the \tabskips in an alignat environment have a natural width of 0pt, and the \halign has been set in its natural width.

One nice result of this is that we can read \totwidth@ off immediately, since it is just the width of \box1, plus \@mathmargin if we're in fleqn mode. (Actually, we also have to take \minalignsep into account, but we'll do that later):

```
1621 \global\totwidth@\\d\@ne
1622 \if@fleqn \global\advance\totwidth@\\@mathmargin \fi
```

Now we initialize \align@lengths and start peeling the boxes off, one by one, and adding their widths to \align@lengths. We stop when we run out of boxes, i.e., when \lastbox returns a void box. We're going to build a list using \or as a delimiter, so we want to disable it temporarily.

```
\global\let\maxcolumn@widths\@empty
1623
            \begingroup
1624
               \let\or\relax
1625
1626
                 \global\setbox\@ne\hbox{%
1627
1628
                   \unhbox\@ne \unskip \global\setbox\thr@@\lastbox
                 ጉ%
1629
               \ifhbox\thr@@
1630
                \xdef\maxcolumn@widths{ \or \the\wd\thr@@ \maxcolumn@widths}%
1631
               \repeat
1632
1633
            \endgroup
```

Now we calculate the number of flexible spaces and the initial values of \eqnshift@ and \alignsep@. We start by calculating \displaywidth — \totwidth@, which gives us the total amount of "free space" in a row.

```
1634 \dimen@\displaywidth
1635 \advance\dimen@-\totwidth@
```

Next we calculate the number of columns of flexible spaces in the display, which depends on whether we're in fleqn mode and in which particular environment we are in.

We use \@tempcnta to store the total number of flexible spaces in the align and \@tempcntb for the number of interalign spaces.

```
1636 \ifcase\xatlevel@
```

In alignat, the interalign spaces are under user control, not ours. So, we set \alignsep@ and \minalignsep both equal to 0pt. Later, when calculating a new value for \alignsep@, we will only save the new value if it is less than the current value of \alignsep@ (i.e., \alignsep@ will never increase). Since the values we calculate will never be negative, this will ensure that \alignsep@ remains zero in alignat.

```
\begin{tabular}{ll} 1637 & $\global\alignsep@\z@\\ 1638 & $\end{tabular} $$ 1639 & $\end{tabular} $$ \end{tabular}
```

In fleqn mode, the left margin—and hence the right margin in this case—is fixed. Otherwise, we divide the free space equally between the two margins.

```
\if@fleqn
1640
1641
                      \@tempcnta\@ne
                      \global\eqnshift@\@mathmargin
1642
1643
                  \else
                      \@tempcnta\tw@
1644
                      \global\eqnshift@\dimen@
1645
                      \global\divide\eqnshift@\@tempcnta
1646
1647
                  \fi
1648
             \or
```

In an align or xalignat environment with n aligned structures, there are n-1 interalign spaces and either 1 or 2 flexible margins, depending on whether we're in fleqn mode or not.

```
        1649
        (@tempcntb\maxfields@

        1650
        \divide\@tempcntb\tw@

        1651
        \@tempcnta\@tempcntb

        1652
        \advance\@tempcntb\m@ne
```

If we are in fleqn mode, we fix the left margin and divide the free space equally among the interalign spaces and the right margin.

```
1653 \ifOfleqn
1654 \global\eqnshift@\@mathmargin
1655 \global\alignsep@\dimen@
1656 \global\divide\alignsep@\@tempcnta
1657 \else
```

Otherwise, we divide the free space equally among the interalign spaces and both margins.

```
        1658
        \global\advance\@tempcnta\@ne

        1659
        \global\eqnshift@\dimen@

        1660
        \global\divide\eqnshift@\@tempcnta

        1661
        \global\alignsep@\eqnshift@

        1662
        \fi

        1663
        \or
```

Finally, if we're in an flalign or xxalignat environment, there are no flexible margins and n-1 flexible interalign spaces.

```
1664 \Qtempcntb\maxfieldsQ

1665 \divide\Qtempcntb\twQ

1666 \global\advance\Qtempcntb\mQne

1667 \global\Qtempcnta\Qtempcntb

1668 \global\eqnshiftQ\zQ

1669 \global\alignsepQ\dimenQ
```

If we're in fleqn mode, we need to add back the \@mathmargin that was removed when \dimen@ was originally calculated above.

```
1670 \if@fleqn
1671 \global\advance\alignsep@\@mathmargin\relax
1672 \fi
1673 \global\divide\alignsep@\@tempcntb
1674 \fi

Now we make sure \alignsep@ isn't too small.
```

1675 \ifdim\alignsep@<\minalignsep\relax
1676 \global\alignsep@\minalignsep\relax

```
\ifdim\eqnshift@>\z@
1677
                     \if@fleqn\else
1678
                          \global\eqnshift@\displaywidth
1679
                          \global\advance\eqnshift@-\totwidth@
1680
1681
                          \global\advance\eqnshift@-\@tempcntb\alignsep@
                          \global\divide\eqnshift@\tw@
1682
                     \fi
1683
                 \fi
1684
             \fi
1685
             \ifdim\eqnshift@<\z@
1686
1687
                 \global\eqnshift@\z@
1688
             \fi
             \calc@shift@align
```

Next, we calculate the value of **\tagshift@**. This is the glue that will be inserted in front of the equation tag to make sure it lines up flush against the appropriate margin.

```
1690
             \global\tagshift@\totwidth@
1691
             \global\advance\tagshift@\@tempcntb\alignsep@
1692
             \if@flegn
1693
                 \ifnum\xatlevel@=\tw@
                      \global\advance\tagshift@-\@mathmargin\relax
1694
1695
                 \fi
1696
             \else
1697
                 \global\advance\tagshift@\eqnshift@
             \fi
1698
             \iftagsleft@ \else
1699
1700
                 \global\advance\tagshift@-\displaywidth
            \fi
1701
```

Finally, we increase \totwidth@ by an appropriate multiple of \minalignsep. If the result is greater than \displaywidth, it means that at least one line in the align is overfull and we will issue an appropriate warning message (via \block) at the end of the environment.

```
\dimen@\minalignsep\relax
1702
             \global\advance\totwidth@\@tempcntb\dimen@
1703
             \ifdim\totwidth@>\displaywidth
1704
                 \global\let\displaywidth@\totwidth@
1705
             \else
1706
1707
                 \global\let\displaywidth@\displaywidth
1708
             \fi
1709
        \endgroup
1710 }
```

The code for calculating the appropriate placement of equation tags in the align environments is quite complicated and varies wildly depending on the settings of the tagsleft@ and @fleqn switches. To minimize memory and hash space usage, we only define the variant appropriate for the current setting of those switches.

It would be worthwhile to examine this code more closely someday and see if it could be optimized any.

Tag placement when \tagsleft@true, \Offleqntrue. We begin with the version of \calc@shift@align appropriate for flush-left equations with tags on the left.

\calc@shift@align

This is the simplest case. Since the left margin is fixed, in general the only thing to do is check whether there is room for the tag in the left margin. The only exception is that if \eqnshift@ = 0 pt—meaning that we're in a flalign

environment and this is the first line with a tag that we've encountered—then we set \eqnshift@ = \@mathmargin and recalculate \alignsep@. This is done by \x@calc@shift@lf.

```
1711 \iftagsleft@\if0fleqn
1712 \def\calc@shift@align{%
1713 \global\let\tag@shifts\@empty
1714 \begingroup
```

\Otempdima is initialized to \Omathmargin—\mintagsep, which yields the maximum size of a tag that will not be shifted to another line.

```
1715 \@tempdima\@mathmargin\relax
1716 \advance\@tempdima-\mintagsep\relax
```

Now we examine each row in turn. If the width of the tag on the line is non-positive—meaning either that there is no tag or else that the user has forced it to have zero width—we mark the tag to remain unshifted. Otherwise, we call \x@calc@shift@lf to determine whether any adjustments need to be made to \eqnshift@ and \alignsep@. Note the difference in treatment of zero-width tags between this code and TEX's built-in algorithm: here, a width of zero prohibits the tag from being shifted, while in TEX's built-in algorithm, a width of zero forces the tag to be shifted.

```
1717
                  \loop
1718
                       \ifnum\row@>0
                           \ifdim\tag@width\row@>\z@
1719
                                \x@calc@shift@lf
1720
                           \else
1721
                                \saveshift@0%
1722
                           \fi
1723
                           \advance\row@\m@ne
1724
1725
                  \repeat
1726
              \endgroup
1727
```

\x@calc@shift@lf

As mentioned above, \x@calc@shift@lf first checks to see if the current left margin is set to 0 and, if so, resets it to \@mathmargin and recalculates \alignsep@. Next, it checks whether the length of the current tag exceeds the previously calculated limit and, if so, marks the tag to be shifted to a separate line.

```
1728
        \def\x@calc@shift@lf{%
1729
             \ifdim\eqnshift@=\z@
                 \global\eqnshift@\@mathmargin\relax
1730
                 \alignsep@\displaywidth
1731
                 \advance\alignsep@-\totwidth@
1732
                 \global\divide\alignsep@\@tempcntb
1733
                 \ifdim\alignsep@<\minalignsep\relax
1734
                     \global\alignsep@\minalignsep\relax
1735
1736
             \fi
1737
             \ifdim\tag@width\row@>\@tempdima
1738
1739
                 \saveshift@1%
1740
             \else
                 \saveshift@0%
1741
             \fi
1742
        }
1743
1744 \fi\fi
```

Tag placement when \tagsleft@false, \@fleqntrue. Next we consider the case when equations are flush-left, but tags are on the right. This case

is somewhat more complicated than the previous one, since we can adjust the right margin by varying the inter-align separatin. Thus, when a tag is found to be too close to its equation, we first attempt to decrease \alignsep@ enough to move the equation off to an acceptable distance. Only if that would require a value of \alignsep@ less than \minalignsep do we move the tag to a separate line.

\calc@shift@align

This version of \calc@shift@align differs from the previous version only in calling \x@calc@shift@rf rather than \x@calc@shift@lf.

```
1745 \iftagsleft@\else\if@fleqn
         \def\calc@shift@align{%
1746
1747
             \global\let\tag@shifts\@empty
             \begingroup
1748
1749
                  \loop
1750
                      \ifnum\row@>0
                           \ifdim\tag@width\row@>\z@
1751
                               \x@calc@shift@rf
1752
                           \else
1753
1754
                               \saveshift@0%
1755
                           \fi
                           \advance\row@\m@ne
1756
1757
                  \repeat
1758
             \endgroup
1759
```

\x@calc@shift@rf

To start, we need to know two quantities: the number of align structures in the current row and the "effective length" of the row, defined as the distance from the left margin to the right edge of the text assuming that \eqnshift@ and \alignsep@ are both 0. To get the number of align structures, we first count the number of columns by counting the number of entries in the \fieldlengths@ for the current row. The effective length is calcuated by \x@rcalc@width and put in the temporary register \@tempdimc, using \@tempdimb as an auxiliary variable.

```
\def\x@calc@shift@rf{%
1760
             \column@\z@
1761
             \@tempdimb\z@
1762
             \@tempdimc\z@
1763
1764
             \edef\@tempb{\fieldlengths@\row@}%
1765
             \@for\@tempa:=\@tempb\do{%
1766
                 \advance\column@\@ne
1767
                 \x@rcalc@width
             }%
1768
1769
             \begingroup
```

If there are n columns in the current row, then there are  $\lfloor (n+1)/2 \rfloor$  align structures and  $\lfloor (n-1)/2 \rfloor$  interalign spaces.

```
1770 \advance\column@\m@ne
1771 \divide\column@\tw@
```

If this is smaller than the maximum number of interalign spaces in the environment, then we need to reduce \@tempcnta (the total number of flexible spaces in the current line) by \@tempcntb-\column@ and reset \@tempcntb to \column@.

```
      1772
      \ifnum\@tempcntb>\column@

      1773
      \advance\@tempcnta-\@tempcntb

      1774
      \advance\@tempcnta\column@

      1775
      \@tempcntb\column@

      1776
      \fi
```

Next, we add the width of the tag and the (fixed) left margin to the effective length calculated above. This can be used to calculate how much "free space" there is in the current line and thus how much leeway we have to increase the amount of space between the tag and the equation.

```
1777 \tagwidth@\tag@width\row@\relax
1778 \@tempdima\eqnshift@
1779 \advance\@tempdima\@tempdimc\relax
1780 \advance\@tempdima\tagwidth@
```

The first thing to check is whether the tag should be shifted to a separate line. To do this, we add the minimum interalign separation and the \mintagsep to the value of \@tempdima just calculated. This yields the minimum acceptable length of the current line. If that is greater than \displaywidth, we mark the tag to be calculated. Otherwise, we mark the tag to be kept on the same line and then check to see if the \alignsep@ needs to be reduced to make room for the tag.

Now we perform essentially the same calculation, but using the current value of \alignsep@ instead of \minalignsep. This gives the current length of the line. If this is greater than \displaywidth, we recalculate \alignsep@ to make room for the tag.

```
1789
                      \dimen@\alignsep@\relax
1790
                      \multiply\dimen@\@tempcntb
                      \advance\dimen@\@tempdima
1791
                      \advance\dimen@\tagwidth@
1792
                      \ifdim\dimen@>\displaywidth
1793
                          \dimen@\displaywidth
1794
                          \advance\dimen@-\@tempdima
1795
                          \ifnum\xatlevel@=\tw@
1796
1797
                               \advance\dimen@-\mintagsep\relax
1798
                          \fi
1799
                          \divide\dimen@\@tempcnta
1800
                          \ifdim\dimen@<\minalignsep\relax
                               \global\alignsep@\minalignsep\relax
1801
1802
                          \else
1803
                               \global\alignsep@\dimen@
                          \fi
1804
                      \fi
1805
                 \fi
1806
1807
             \endgroup
1808
1809 \fi\fi
```

Tag placement when \tagsleft@false, \@fleqnfalse. This is similar to the previous case, except for the added complication that both \alignsep@ and \eqnshift@ can vary, which makes the computations correspondingly more complicated.

\calc@shift@align

56 THE AMSMATH PACKAGE

```
1811
                           \def\calc@shift@align{%
                   1812
                               \global\let\tag@shifts\@empty
                   1813
                               \begingroup
                   1814
                                    \loop
                                        \ifnum\row@>0
                   1815
                                            1816
                                                 \x@calc@shift@rc
                   1817
                                            \else
                   1818
                                                 \saveshift@0%
                   1819
                   1820
                                            \advance\row@\m@ne
                   1822
                                    \repeat
                   1823
                               \endgroup
                   1824
\x@calc@shift@rc
                           \def\x@calc@shift@rc{%
                   1825
                               \column@\z@
                   1826
                                \@tempdimb\z@
                   1827
                                \@tempdimc\z@
                   1828
                                \edef\@tempb{\fieldlengths@\row@}%
                   1829
                   1830
                                \@for\@tempa:=\@tempb\do{%
                   1831
                                    \advance\column@\@ne
                   1832
                                    \x@rcalc@width
                   1833
                               }%
                   1834
                                \begingroup
                                    \advance\column@\m@ne
                   1835
                                    \divide\column@\tw@
                   1836
                                    \ifnum\@tempcntb>\column@
                   1837
                                        \advance\@tempcnta-\@tempcntb
                   1838
                                        \advance\@tempcnta\column@
                   1839
                                        \@tempcntb\column@
                   1840
                                    \fi
                   1841
                                    \tagwidth@\tag@width\row@\relax
                   1842
                                    \@tempdima\@tempdimc
                   1843
                   1844
                                    \advance\@tempdima\tagwidth@
                   1845
                                    \dimen@\minalignsep\relax
                                    \multiply\dimen@\@tempcntb
                   1846
                   1847
                                    \advance\dimen@\mintagsep\relax
                                    \ifnum\xatlevel@=\tw@ \else
                   1848
                                        \advance\dimen@\mintagsep\relax
                   1849
                   1850
                   1851
                                    \advance\dimen@\@tempdima
                                    \ifdim\dimen@>\displaywidth
                   1852
                                        \saveshift@1%
                   1853
                                    \else
                   1854
                                        \saveshift@0%
                   1855
                                        \dimen@\eqnshift@
                   1856
                                        \advance\dimen@\@tempdima
                   1857
                                        \advance\dimen@\@tempcntb\alignsep@
                   1858
                                        \advance\dimen@\tagwidth@
                   1859
                                        \ifdim\dimen@>\displaywidth
                   1860
                   1861
                                            \dimen@\displaywidth
                                            \advance\dimen@-\@tempdima
                   1862
                                            \ifnum\xatlevel@=\tw@
                   1863
                                                 \advance\dimen@-\mintagsep\relax
                   1864
                   1865
                                            \fi
                   1866
                                            \divide\dimen@\@tempcnta
                   1867
                                            \ifdim\dimen@<\minalignsep\relax
```

```
1868
                                                   \global\alignsep@\minalignsep\relax
                    1869
                                                   \eqnshift@\displaywidth
                    1870
                                                   \advance\eqnshift@-\@tempdima
                                                   \advance\eqnshift@-\@tempcntb\alignsep@
                    1871
                                                   \global\divide\eqnshift@\tw@
                    1872
                                              \else
                    1873
                                                   \ifdim\dimen@<\eqnshift@
                    1874
                                                       \ifdim\dimen@<\z@
                    1875
                                                           \global\eqnshift@\z@
                    1876
                    1877
                    1878
                                                            \global\eqnshift@\dimen@
                    1879
                                                       \fi
                    1880
                                                   \fi
                                                   \ifdim\dimen@<\alignsep@
                    1881
                                                       \verb|\global\alignsep@\dimen@|
                    1882
                                                   \fi
                    1883
                                              \fi
                    1884
                                          \fi
                    1885
                                     \fi
                    1886
                                 \endgroup
                    1887
                    1888
                    1889 \fi\fi
   \x@rcalc@width
                    1890 \iftagsleft@\else
                             \def\x@rcalc@width{%
                    1891
                                 \ifdim\@tempa > \z@
                    1892
                                      \advance\@tempdimc\@tempdimb
                    1893
                    1894
                                      \ifodd\column@
                                          \advance\@tempdimc\maxcol@width\column@
                    1895
                                          \@tempdimb\z@
                    1896
                                      \else
                    1897
                    1898
                                          \advance\@tempdimc\@tempa\relax
                    1899
                                          \@tempdimb\maxcol@width\column@
                    1900
                                          \advance\@tempdimb-\@tempa\relax
                                      \fi
                    1901
                                 \else
                    1902
                                      \advance\@tempdimb\maxcol@width\column@\relax
                    1903
                                 \fi
                    1904
                    1905
                             }
                    1906 \fi
                    Tag placement when \tagsleft@true, \@fleqnfalse.
\calc@shift@align
                    1907 \iftagsleft@\if@fleqn\else
                             \def\calc@shift@align{%
                    1908
                                 \global\let\tag@shifts\@empty
                    1909
                    1910
                                 \begingroup
                    1911
                                      \loop
                    1912
                                          \ifnum\row@>\z@
                    1913
                                              \ifdim\tag@width\row@>\z@
                                                   \x@calc@shift@lc
                    1914
                    1915
                                              \else
                                                   \saveshift@0%
                    1916
                    1917
                                              \advance\row@\m@ne
                    1918
                    1919
                                      \repeat
                                 \endgroup
                    1920
```

```
1921 }
```

#### \x@calc@shift@lc

```
1922 \def\x@calc@shift@lc{%
1923 \column@\z@
```

\@tempdima will (eventually) be set to the effective width of the current row, defined as the distance from the leftmost point of the current line to the end of the last field of the \halign, ignoring any intervening \tabskips, plus the width of the current tag. That is, it will be the width of the first non-empty field plus the sum of the maximum widths of all following fields, plus the tag width.

\@tempdimb will be the "indentation" of leftmost end of text, ignoring the \tabskip glue, i.e., it will be the sum of the maximum widths of any fields to the left of the first non-empty field, plus whatever empty space there is at the beginning of the first non-empty field.

```
1924
              \@tempdima\z@ % ''width of equation''
              \@tempdimb\z@ % ''indent of equation''
1925
              \edef\@tempb{\fieldlengths@\row@}%
1926
              \ensuremath{\texttt{Qfor}\ensurema:=\ensuremath{\texttt{Qtempb}}\do{\%}}
1927
                    \advance\column@\@ne
1928
1929
                    \x@lcalc@width
              }%
1930
1931
               \begingroup
                    \tagwidth@\tag@width\row@\relax
```

\@tempdima is now easy to calculate, since it is just \totwidth@-\@tempdimb+\tagwidth@.

```
1933 \@tempdima\totwidth@
1934 \advance\@tempdima-\@tempdimb
1935 \advance\@tempdima\tagwidth@
```

Next, we check to see whether there is room for both the equation and the tag on the same line, by calculating the minimum acceptable length of the current row and comparing that to \displaywidth. Note that here we use \@tempcntb, i.e., the number of interalign spaces after the first non-empty align structure.

```
1936 \dimen@\minalignsep\relax
1937 \multiply\dimen@\@tempcntb
1938 \advance\dimen@\mintagsep\relax
1939 \ifnum\xatlevel@=\tw@\else
1940 \advance\dimen@\mintagsep\relax
1941 \fi
1942 \advance\dimen@\@tempdima
```

If the minimum acceptable width of the current line is greater than \displaywidth, we mark the current tag to be shifted to a separate line.

```
1943 \ifdim\dimen@>\displaywidth
1944 \saveshift@1%
1945 \else
```

Otherwise, the tag can stay on the same line as the equation, but we need to check whether it is too close to the equation. So, we calculate the distance between the left margin and the left side of the equation, using the current values of \eqnshift@ and \alignsep@. Note that we use \count@ here, not \@tempcntb, as above.

```
1946 \saveshift@0%

1947 \dimen@\alignsep@

1948 \multiply\dimen@\count@

1949 \advance\dimen@\eqnshift@

1950 \advance\dimen@\@tempdimb
```

If the left margin is less than twice the tag width, we calculate new values of \eqnshift@ and \alignsep@ to move the equation further away from the tag. In particular, we center the current line between its tag and the right margin. Note that although we later will need to transform \dimen@ into a value suitable for use as \eqnshift@, for the time being it is more useful to think of it as the space separating the tag from the equation.

```
      1951
      \ifdim\dimen@<2\tagwidth@</td>

      1952
      \dimen@\displaywidth

      1953
      \advance\dimen@-\@tempdima

      1954
      \ifnum\xatlevel@=\tw@

      1955
      \advance\dimen@-\mintagsep\relax

      1956
      \fi
```

In certain circumstances we will get a divide-by-zero error here unless we guard against it. Use of \@tempcnta is complicated, sometimes it is assigned globally, sometimes locally. Need to sort it out one of these days [mjd,2000/06/02].

```
1957 \ifnum\@tempcnta>\z@
1958 \divide\dimen@\@tempcnta
1959 \else \dimen@\z@
1960 \fi
```

As usual, we check to make sure we don't set \alignsep@ smaller than \minalignsep and, in any case, that we don't replace \alignsep@ by a larger value.

```
1961
                          \ifdim\dimen@<\minalignsep\relax
1962
                              \global\alignsep@\minalignsep\relax
1963
                              \dimen@\displaywidth
1964
                              \advance\dimen@-\@tempdima
                              \advance\dimen@-\@tempcntb\alignsep@
1965
                              \global\divide\dimen@\tw@
1966
                          \else
1967
                              \ifdim\dimen@<\alignsep@
1968
                                  \global\alignsep@\dimen@
1969
                              \fi
1970
                          \fi
1971
```

Next, we calculate an appropriate value of \eqnshift@, assuming that \dimen@ is the desired separation between the tag and equation of the current line. This means that we first need to adjust \dimen@ if we're in an flalign environment.

```
1972 \ifnum\xatlevel@=\tw0
1973 \dimen@\mintagsep\relax
1974 \fi
```

Now we calculate the value of \eqnshift@ needed to produce a separation of \dimen@ between the equation tag and the beginning of the equation. To do this, we need the following equation to hold:

```
\ensuremath{\texttt{\colored}} + \ensuremath{\texttt{\colo
```

where  $n = \count@$  is the number of interalign spaces before the first non-empty field of the current line.

```
1975 \advance\dimen@\tagwidth@
1976 \advance\dimen@-\@tempdimb
1977 \advance\dimen@-\count@\alignsep@
```

The value of \eqnshift@ just calculated is the minimum acceptable value; thus, we save it only if it is larger than the current value.

```
1978 \ifdim\dimen@>\eqnshift@
1979 \global\eqnshift@\dimen@
1980 \fi
```

```
1981 \fi
1982 \fi
1983 \endgroup
1984 }
```

\x@lcalc@width

This macro calculates the "indentation" of the current row, as defined above under the description of \x@calc@shift@lc. This macro is called for each field of the current line, with \@tempa set to the width of the current field. Ideally, the loop enclosing \x@lcalc@width would terminate as soon as \@tempa is nonzero, but that would be a bit tricky to arrange. Instead, we use \@tempdima as a flag to signal when we've encountered the first non-empty field.

```
1985 \def\x@lcalc@width{%
1986 \ifdim\@tempdima = \z@
```

If the current field is empty (i.e., \Otempa = 0 pt, then we increment \Otempdimb by the width of the current field). Otherwise, we set \Otempdima = 1 pt as a signal value and increment \Otempdimb by the width of whatever empty space there might be at the left of the current field.

```
1987 \ifdim\@tempa > \z@
1988 \@tempdima\p@
1989 \ifodd\column@
1990 \advance\@tempdimb \maxcol@width\column@
1991 \advance\@tempdimb-\@tempa
1992 \fi
```

In addition, we need to adjust the values of \@tempcnta and \@tempcntb to account for any empty align structures that might occur at the beginning of the current line. More specifically, we first set \count@ equal to the number of interalign spaces preceding the current field (namely,  $\lfloor (\column@-1)/2 \rfloor$ ), and then subtract \count@ from both \@tempcnta and \@tempcntb. The rationale is that for the purposes of adjusting the spacing between the tag and the equation, the only flexible interalign spaces are those after the first non-empty align structure, so we need to treat those different from the ones before the first non-empty align structure.

```
1993
                      \count@\column@
1994
                      \advance\count@\m@ne
                      \divide\count@\tw@
1995
1996
                      \advance\@tempcnta-\count@
1997
                      \advance\@tempcntb-\count@
1998
                 \else
1999
                      \advance\@tempdimb \maxcol@width\column@\relax
                 \fi
2000
             \fi
2001
2002
        }
2003 \fi\fi
```

\place@tag \place@tag takes care of the placment of tags in the align environments.

```
2004 \def\place@tag{%
         \iftagsleft@
2005
2006
             \kern-\tagshift@
2007
             \if1\shift@tag\row@\relax
                  \rlap{\vbox{%
2008
                      \normalbaselines
2009
                      \boxz@
2010
                      \vbox to\lineht@{}%
2011
                      \raise@tag
2012
2013
                 }}%
             \else
```

```
2015
                                     \rlap{\boxz@}%
                   2016
                                 \fi
                   2017
                                 \kern\displaywidth@
                   2018
                            \else
                                 \kern-\tagshift@
                   2019
                                 \if1\shift@tag\row@\relax
                   2020
                   Added depth to correct vertical spacing of shifted equation tags.—dmj, 1994/12/29
                                     \displaystyle \frac{\t}{\t} 
                   2021
                                          \raise@tag
                   2022
                                          \normalbaselines
                   2023
                   2024
                                          \setbox\@ne\null
                                          \dp\@ne\lineht@
                   2025
                   2026
                                          \box\@ne
                                          \boxz@
                   2027
                                     }}%
                   2028
                                 \else
                   2029
                                     \displaystyle \frac{\position{boxz@}}{\position{boxz@}}
                   2030
                                 \fi
                   2031
                            \fi
                   2032
                   2033 }
\align@preamble
                   2034 \def\align@preamble{%
                   2035
                           &\hfil
                   2036
                            \strut@
                   2037
                            \setboxz@h{\@lign$\m@th\displaystyle{##}$}%
                   2038
                            \ifmeasuring@\savefieldlength@\fi
                            \set@field
                   2039
                            \tabskip\z@skip
                   2040
                   2041
                           &\setboxz@h{\@lign$\m@th\displaystyle{{}##}$}%
                   2042
                            \ifmeasuring@\savefieldlength@\fi
                   2043
                            \set@field
                   2044
                            \hfil
                   2045
                            \tabskip\alignsep@
                   2046 }
                   \setOfield increments the column counter, tracks the value of \linehtO and
     \set@field
                   finally inserts the box containing the contents of the current field.
                   2047 \def\set@field{%
                            \column@plus
                   2048
                            \iftagsleft@
                   2049
                   2050
                                 \left\langle \frac{z}{z}\right\rangle 
                   2051
                                     \global\lineht@\ht\z@
                   2052
                                 \fi
                   2053
                            \else
                                 \ifdim\dp\z@>\lineht@
                   2054
                                     \global\lineht@\dp\z@
                   2055
                   2056
                                 \fi
                   2057
                            \fi
                   2058
                            \boxz@
                   2059 }
                            The split environment
                   16.7
                   A special error function for split to conserve main mem (at a cost of string
     \split@err
                   pool/hash size.
                   2060 \edef\split@err#1{%
                            \@nx\@amsmath@err{%
                   2061
                   2062
                                 \string\begin{split} won't work here%
```

```
}{%
       2063
                    \@xp\@nx\csname
       2064
       2065
             Did you forget a preceding \string\begin{equation}?^^J%
       2066
             If not, perhaps the 'aligned' environment is what
             you want.\endcsname}%
       2067
       2068 }
split
       If the split environment occurs inside align or gather, it can make use of
       the enclosing halign; if it is called inside a simple equation, we add an implicit
       'gather' container.
       2069 \newenvironment{split}{%
       2070
             \if@display
       2071
                \ifinner
                  \verb|@xp|@xp|split@aligned|
       2072
       2073
                \else
                  \ifst@rred \else \global\@eqnswtrue \fi
       2074
               \fi
       2075
       2076
             \else \let\endsplit\@empty \@xp\collect@body\@xp\split@err
       2077
             \collect@body\gather@split
       2078
       2079 }{%
                  \crcr
       2080
       2081
                \egroup
       2082
              \egroup
              \iftagsleft@ \@xp\lendsplit@ \else \@xp\rendsplit@ \fi
       2083
       2084 }
       2085 \let\split@tag\relax % init
       2086 \def\gather@split#1#2#3{%
             \@xp\endgroup \reset@equation % math@cr will handle equation numbering
       2087
              \iftag@
       2088
                 \toks@\@xp{\df@tag}%
       2089
                 \edef\split@tag{%
       2090
       2091
                   \gdef\@nx\df@tag{\the\toks@}%
       2092
                   \global\@nx\tag@true \@nx\nonumber
                 }%
       2093
       2094
              \else \let\split@tag\@empty
       2095
       2096
              \spread@equation
       The extra vcenter wrapper here is not really a good thing but without it there are
       compatibility problems with old documents that throw in some extra material
       between \begin{equation} and \begin{split} (for example, \hspace{-1pc})
       or \left[ \frac{1999}{09} \right]
             \vcenter\bgroup
       2097
       2098
                \gather@{\split@tag \begin{split}#1\end{split}}%
                \def\endmathdisplay@a{%
       2099
                  \math@cr \black@ \totwidth@ \egroup
       2100
       2101
                  \egroup
       2102
       2103 }
```

\insplit@

```
2104 \def\insplit@{%
      \global\setbox\z@\vbox\bgroup
2105
        \Let@ \chardef\dspbrk@context\@ne \restore@math@cr
2106
2107
        \default@tag % disallow use of \tag here
2108
        \ialign\bgroup
          \hfil
2109
```

```
2110 \strut@
2111 $\m@th\displaystyle{##}$%
2112 &$\m@th\displaystyle{{}##}$%
2113 \hfill % Why not \hfil?---dmj, 1994/12/28
2114 \crcr
2115 }
```

\rendsplit@ Moved the box maneuvers inside the \ifinalign@, since that is the only place they are needed.—dmj, 1994/12/28

TODO: Explore interaction of tag-placement algorithm with split. Is there any way for split to pass the relevant information out to the enclosing gather or align?

```
2116 \def\rendsplit@{%
2117 \ifinalign@
```

Changed \box9 into a \vtop here for better spacing.

```
\global\setbox9 \vtop{%
2118
2119
                 \unvcopy\z@
2120
                 \global\setbox8 \lastbox
2121
                 \unskip
2122
             }%
             \setbox\@ne\hbox{%
2123
2124
                 \unhcopv8
                 \unskip
2125
                 \global\setbox\tw@\lastbox
2126
                 \unskip
2127
                 \global\setbox\thr@@\lastbox
2128
            }%
2129
2130
             \ifctagsplit@
                 \gdef\split@{%
2131
                     \hbox to\wd\thr@@{}%
2132
2133
                    &\vcenter{\vbox{\moveleft\wd\thr@@\boxz@}}%
2134
                 }%
2135
             \else
                 \global\setbox7 \hbox{\unhbox\tw@\unskip}%
2136
```

Added \add@amps to make sure we put the last line of the split into the proper column of an align environment with multiple align structures.—dmj, 1994/12/28

Special care has to be taken in this case because the split turns into two lines of the align instead of just one. So, we have to make sure that the first line produced by the split doesn't upset our bookkeeping, hence we call \savetaglength@ to insert 0 pt as the tag for this pseudo-line, and we advance the \row@ counter and reset \lineht@ afterwards. It would be nice if we could just replace the \crcr by \math@cr@@@, but that would cause problems with the tag processing.

```
2137
                 \gdef\split@{%
                     \global\@tempcnta\column@
2138
                    &\setboxz@h{}%
2139
                     \savetaglength@
2140
2141
                      \global\advance\row@\@ne
                      \vbox{\moveleft\wd\thr@@\box9}%
2142
2143
                      \crcr
                      \noalign{\global\lineht@\z@}\%
2144
                      \add@amps\@tempcnta
2145
                      \box\thr@@
2146
                    &\box7
2147
                 }%
2148
             \fi
2149
```

```
2150  \else
2151  \ifctagsplit@
2152  \gdef\split@{\vcenter{\boxz@}}%
2153  \else
```

Changed to just \boxz@, otherwise last line gets centered rather than aligned properly with respect to the rest of the lines. But this means that we can't see inside of the last line to decide whether the tag needs to be moved. Will have to think about this.—dmj, 1994/12/28

```
2154
                  \gdef\split@{%
2155
                       \boxz@
2156 %
                        \box9
2157 %
                        \crcr
2158 %
                        \hbox{\box\thr@@\box7}%
2159
                  }%
             \fi
2160
2161
         \fi
2162
         \aftergroup\split@
2163 }
```

### \lendsplit@

```
2164 \def\lendsplit@{%
2165 \global\setbox9\vtop{\unvcopy\z@}%
2166 \ifinalign@
```

Moved following two boxes inside the \ifinalign@, since they are only used in that case. In fact, if we just kept track of the width of the first column, we could dispense with this entirely. Surely that would be more efficient than all these box copies.—dmj, 1994/12/28

```
\setbox\@ne\vbox{%
2167
2168
                \unvcopy\z@
                \global\setbox8\lastbox
2169
            }%
2170
            \setbox\@ne\hbox{%
2171
                \unhcopy8%
2172
                \unskip
2173
                \setbox\tw@\lastbox
2174
2175
                \unskip
2176
                \global\setbox\thr@@\lastbox
2177
            }%
2178
            \ifctagsplit@
                \gdef\split@{%
2179
                    \hbox to\wd\thr@@{}%
2180
                   2181
                }%
2182
            \else
2183
                \gdef\split@{%
2184
                    \hbox to\wd\thr@@{}%
2185
                   &\vbox{\moveleft\wd\thr@@\box9}%
2186
                }%
2187
2188
            \fi
2189
        \else
2190
            \ifctagsplit@
2191
                \gdef\split@{\vcenter{\box9}}%
2192
            \else
                \gdef\split@{\box9}%
2193
2194
            \fi
2195
        \fi
2196
        \aftergroup\split@
2197 }
```

With amsmath 1.2 it was possible to put things like \left\{ between \begin{equation} and \begin{split} without getting any error message. For backward compatibility we try to avoid a fatal error in this case and instead attempt recovery with aligned.

```
2198 \def\split@aligned#1#2{%

2199 \iffalse{\fi\ifnum0='}\fi

2200 \collect@body\split@al@a}

2201 \def\split@al@a#1#2#3{%

2202 \split@warning

2203 \endgroup
```

If the fleqn and tbtags options are both in effect then we will need to add an optional argument on the aligned environment.

```
2204 \toks@{\begin{aligned}}%
2205 \ifOfleqn \splitOalOtagcheck \fi
```

The \relax here is to prevent \@let@token from being left equal to an ampersand if that happens to be the first thing in the body.

```
\the\toks@\relax#1\end{aligned}%
      \ifnumO='{\fi\iffalse}\fi
2207
2208 }
2209 \texttt{\def\split@al@tagcheck} \%
       \ifctagsplit@
2210
2211
       \else
         \iftagsleft@ \toks@\@xp{\the\toks@ [t]}%
2212
         \else \toks@\@xp{\the\toks@ [b]}%
2213
2214
         \fi
2215
       \fi
2216 }
2217 \def\split@warning{%
2218 \PackageWarning{amsmath}{%
2219 Cannot use 'split' here;\MessageBreak trying to recover with 'aligned'}%
2220 }
```

# 16.8 The multline environment

In the original  $\mathcal{A}\mathcal{MS}$ -TEX, \multlinegap is a macro with an argument that resets an internal dimension (one with an @ character in its name). Here, to save control sequence names, we define \multlinegap to be the dimension itself and the documentation instructs users to use \setlength if they need to change it.

\multlinegap \multlinetaggap Changed \multlinegap and \multlinetaggap to skip registers. Also changed name to \multlinetaggap from \multlinetaggap@.

```
2221 \newskip\multlinegap
2222 \multlinegap10pt
2223 \newskip\multlinetaggap
2224 \multlinetaggap10pt
```

\start@multline

```
2225 \def\start@multline#1{%
2226 \RIfM@
2227 \nomath@env
2228 \DN@{\@namedef{end\@currenvir}{}\@gobble}%
2229 \else
2230 $$%
2231 #1%
2232 \ifst@rred
```

```
2233
                             \nonumber
                        \else
           2234
                             \global\@eqnswtrue
           2235
           2236
                        \fi
           2237
                        \let\next@\multline@
                    \fi
           2238
           2239
                    \collect@body\next@
           2240 }
 multline
multline*
           2241 \newenvironment{multline}{%
                 \start@multline\st@rredfalse
           2243 }{%
           2244
                  \iftagsleft@ \@xp\lendmultline@ \else \@xp\rendmultline@ \fi
           2245
                  \ignorespacesafterend
           2246 }
           2247 \newenvironment{multline*}{\start@multline\st@rredtrue}{\endmultline}
```

\multline@

```
2248 \def\multline@#1{%
2249 \Let@
```

For multline neither \displ@y no \displ@y@ is quite right; we want to advance the row number and (I suppose?) the display-pagebreak level, but we only want to do tag-related stuff once before the first line, not repeat it for every line. (Recall that the arg of \@display@init goes into \everycr.)

```
2250 \@display@init{\global\advance\row@\@ne \global\dspbrk@lvl\m@ne}%

2251 \chardef\dspbrk@context\z@

2252 \restore@math@cr
```

The multline environment is somewhat unusual, in that \tag and \label are enabled only during the measuring phase and disabled during the production phase. Here we disable \tag and \label; \mmeasure@ will re-enable them temporarily.

```
\let\tag\tag@in@align
2253
        \global\tag@false \global\let\raise@tag\@empty
2254
        \mmeasure@{#1}%
2255
2256
        \let\tag\gobble@tag \let\label\@gobble
        \tabskip \if@fleqn \@mathmargin \else \z@skip \fi
2257
        \totwidth@\displaywidth
2258
2259
        \if@fleqn
2260
            \advance\totwidth@-\@mathmargin
2261
        \halign\bgroup
2262
2263
            \hbox to\totwidth@{%
```

In order to get the spacing of the last line right in flequ mode, we need to play a little game here. Normally the stretchability of the \hskip here will be suppressed by the \hfil at the end of the template, except inside the last line, when that \hfil will be removed by the \hfilneg in \lendmultline@.

```
2264
                  \if@fleqn
2265
                      \hskip \@centering \relax
2266
                  \else
                      \hfil
2267
                  \fi
2268
                  \strut@
2269
                  $\m@th\displaystyle{}##\endmultline@math
2270
2271
                  \hfil
             }%
2272
```

```
2273 \crcr
```

In fleqn mode, it's the \tabskip of \Omathmargin that needs to be removed in the first line, not the \hfil at the beginning of the template.

```
\if@fleqn
2274
2275
                 \hskip-\@mathmargin
                 \def\multline@indent{\hskip\@mathmargin}% put it back
2276
             \else
2277
                 \hfilneg
2278
2279
                 \def\multline@indent{\hskip\multlinegap}%
             \fi
2280
             \iftagsleft@
2281
                 \iftag@
2282
2283
                      \begingroup
2284
                          \ifshifttag@
                              \rlap{\vbox{%
2285
2286
                                       \normalbaselines
                                       \hbox{%}
2287
                                            \strut@
2288
                                            \make@display@tag
2289
2290
                                       }%
                                       \<page-header>
2291
2292
                                       \raise@tag
2293
                              }}%
```

If the equation tag doesn't fit on the same line with the first line of the display, we'll indent the first line by \multlinegap. This is a change from amstex, where the first line would have been flush against the left margin in this case. A corresponding change will be made in \rendmultline@.

```
2294
                            \multline@indent
2295
                        \else
                            2296
                            \dimen@\@mathmargin \advance\dimen@-\wd\z@
2297
                            \ifdim\dimen@<\multlinetaggap
2298
                             \dimen@\multlinetaggap
2299
                            \fi
2300
                            \box\z@ \hskip\dimen@\relax
2301
2302
                        \fi
2303
                    \endgroup
                \else
2304
2305
                    \multline@indent
2306
                \fi
            \else
2307
2308
                \multline@indent
2309
            \fi
       #1%
2310
2311 }
```

An extra level of indirection for the closing \$ in multline allows us to avoid getting an extra thinmuskip from a final mathpunct in the equation contents, when equation numbers are on the right. If we did not use this workaround, the sequence of elements for a final comma would be, e.g.,

```
..., <hskip><box containing equation number>
```

which is equivalent to a sequence <mathpunct><mathord> as far as the automatic math spacing is concerned.

```
2312 \def\endmultline@math{$}
```

\lendmultlineO Bug fix: changed \crcr to \mathOcr so that \Oeqpen gets reset properly if \displaybreak is used on the penultimate line of an align.

```
2313 \def\lendmultline@{%
2314 \hfilneg
2315 \hskip\multlinegap
2316 \math@cr
2317 \egroup
2318 $$%
2319 }
```

### \rendmultline@

```
2320 \def\rendmultline@{%
2321 \iftag@
2322 $\let\endmultline@math\relax
2323 \ifshifttag@
2324 \hskip\multlinegap
```

Added depth to correct vertical spacing of shifted equation tags.—dmj, 1994/12/29

```
\displaystyle \prod_{v \in \mathbb{N}} 
                             \raise@tag
2326
                             \normalbaselines
2327
2328
                             \setbox\@ne\null
2329
                             \dp\@ne\lineht@
2330
                             \box\@ne
                             \hbox{\strut@\make@display@tag}%
2331
                        }}%
2332
                   \else
2333
                        \hskip\multlinetaggap
2334
                        \make@display@tag
2335
2336
                   \fi
2337
         \else
2338
              \hskip\multlinegap
2339
         \fi
2340
         \hfilneg
```

Use \math@cr rather than just \crcr so that \@eqpen gets reset properly if \displaybreak is used.

```
2341 \math@cr
2342 \egroup$$%
2343 }
```

#### \mmeasure@

```
2344 \def\mmeasure@#1{%
2345 \begingroup
2346 \measuring@true
```

We use \begin/endgroup rather than  $\{\}$  in this definition of \label because the latter would create an extra (wasteful of main mem) null box in the current math list. [mjd, 1995/01/17]

```
2347
            \def \label ##1{%}
               \begingroup\measuring@false\label@in@display{##1}\endgroup}%
2348
            \def\math@cr@@@{\cr}%
2349
            \let\shoveleft\@iden \let\shoveright\@iden
2350
            \savecounters@
2351
2352
            \global\row@\z@
2353
            \setbox\@ne\vbox{%
                 \global\let\df@tag\@empty
2354
2355
                     \setboxz@h{\@lign$\m@th\displaystyle{}##$}%
2356
```

```
\iftagsleft@
2357
                          \ifnum\row@=\@ne
2358
                               \global\totwidth@\wdz@
2359
2360
                               \global\lineht@{ht\z@}
                          \fi
2361
                      \else
2362
                           \global\totwidth@\wdz@
2363
                           \global\lineht@\dp\z@
2364
                      \fi
2365
                      \crcr
2366
2367
                      #1%
2368
                      \crcr
2369
                 }%
             }%
2370
             \ifx\df@tag\@empty\else\global\tag@true\fi
2371
2372
             \if@eqnsw\global\tag@true\fi
             \iftag@
2373
                 \setboxz@h{%
2374
                      \if@eqnsw
2375
                          \stepcounter{equation}%
2376
2377
                          \tagform@\theequation
2378
                      \else
                           \df@tag
2379
                      \fi
2380
2381
                 }%
2382
                 \global\tagwidth@\wdz@
2383
                 \dimen@\totwidth@
                 \advance\dimen@\tagwidth@
2384
                 \advance\dimen@\multlinetaggap
2385
                 \iftagsleft@\else
2386
2387
                      \if@fleqn
                           \advance\dimen@\@mathmargin
2388
2389
                 \fi
2390
2391
                 \ifdim\dimen@>\displaywidth
2392
                      \global\shifttag@true
2393
                 \else
                      \global\shifttag@false
2394
                 \fi
2395
             \fi
2396
             \restorecounters@
2397
        \endgroup
2398
2399 }
```

\shoveleft \shoveright \shoveleft and \shoveright need to do slightly different things depending on whether tags are on the left or the right and whether we're in fleqn mode. For compactness of code, we make the appropriate decisions at "compile" time rather than at load time.

TODO: Investigate making \shoveright behave "properly"(?) if used on the first line of a multline and make \shoveleft behave properly if used on the last line of a multline. But in his amstex.doc Spivak indicates those commands should never be used on a first or last line. Perhaps better to leave the question open unless/until real-life examples turn up.

```
2400 \iftagsleft@ 2401 \quad \text{def\shoveright#1}{\%} \\ 2402 \quad \text{#1}{\%} \\ 2403 \quad \text{hfilneg} \\ 2404 \quad \text{hskip\multlinegap}
```

```
2405
         }
2406 \ensuremath{\setminus} \mathtt{else}
2407
         \def\shoveright#1{%
2408
             #1%
              \hfilneg
2409
2410
             \iftag@
2411
                  \ifshifttag@
2412
                       \hskip\multlinegap
2413
                  \else
2414
                       \hskip\tagwidth@
                       \hskip\multlinetaggap
                  \fi
2417
              \else
2418
                  \hskip\multlinegap
              \fi
2419
         }
2420
2421 \fi
2422
2423 \if@fleqn
         \def\shoveleft#1{#1}%
2424
2425 \ensuremath{\setminus} \mathtt{else}
         \iftagsleft@
2427
             \def\shoveleft#1{%
2428
                  \setboxz@h{$\m@th\displaystyle{}#1$}%
2429
                  \setbox\@ne\hbox{$\m@th\displaystyle#1$}%
2430
                  \hfilneg
2431
                  \iftag@
                       \ifshifttag@
2432
                            \hskip\multlinegap
2433
2434
                       \else
2435
                            \hskip\tagwidth@
                            \hskip\multlinetaggap
2436
2437
                       \fi
2438
                  \else
2439
                       \hskip\multlinegap
                  \fi
2440
                  \hskip.5\wd\@ne
2441
                  \hskip-.5\wdz@
2442
                  #1%
2443
             }
2444
         \else
2445
              \def\shoveleft#1{%
2446
                  \setboxz@h{$\m@th\displaystyle{}#1$}%
2447
                  \setbox\@ne\hbox{$\m@th\displaystyle#1$}%
2449
                  \hfilneg
2450
                  \hskip\multlinegap
                  \hskip.5\wd\@ne
2451
                  \hskip-.5\wdz@
2452
                  #1%
2453
2454
2455
         \fi
2456 \fi
```

## 16.9 The equation environment

Rewritten from the ground up for version 2.0 to fix no-shrink and no-shortskips bugs [mjd, 2000/01/06].

Standard IATEX provides three environments for one-line equations: \[\], equation, and displaymath. We add equation\* as a synonym for

\hfuzz\maxdimen

2498

```
displaymath.
2457 \@saveprimitive\leqno\@@leqno
2458 \@saveprimitive\eqno\@@eqno
2459 \def\eqno{\@@eqno\let\eqno\relax\let\leqno\relax}
2460 \ensuremath{\mbox{def}\ensuremath{\mbox{leqno}\ensuremath{\mbox{leqno}\ensuremath{\mbox{relax}}}}
2461 %
2462 \let\veqno=\@@eqno
2463 \iftagsleft@ \let\veqno=\@@leqno \fi
   Support for the showkeys package: provide no-op definitions for a couple
of SK functions, if they are not already defined. Then we can just call them
directly in our code without any extra fuss. If the showkeys package is loaded
later, our trivial definitions will get overridden and everything works fine.
2464 \ensuremath{\texttt{Qifundefined}\{SK@@label\}}{\%}
2465 \let\SK@@label\relax \let\SK@equationtrue\relax
2466 }{}
2467 \let\reset@equation\@empty
   Cf \tag@in@align. This is a bit of a mess though. Could use some work.
[mjd, 1999/12/21]
2468 \let\alt@tag\@empty
2469 \ensuremath{\tt def\tag@in@display\#1\#{\tt relax\tag@in@display@a\{\#1\}}}
2470 \def\tag@in@display@a#1#2{%
2471
        \invalid@tag{Multiple \string\tag}\relax
2472
2473
      \else
2474
        \global\tag@true \nonumber \reset@equation \st@rredtrue
2475
        \if *\string#1%
           \gdef\alt@tag{\def\SK@tagform@{#2\@gobble}%
2476
             \ifx\SK@@label\relax \let\tagform@\SK@tagform@ \fi
2477
           }%
2478
           \make@df@tag@@{#2}%
2479
         \else
2480
           \make@df@tag@@@{#2}%
2481
        \fi
2482
2483
2484 }
2485 \let\restore@hfuzz\@empty
2486 \def\mathdisplay#1{%
2487
      \ifmmode \@badmath
      \else
        $$\def\@currenvir{#1}%
Allow use of \displaybreak.
        \let\dspbrk@context\z@
Although in some cases simpler label handling would seem to be sufficient, al-
ways using \label@in@display makes it easier to support the showkeys pack-
age.
2491
        \let\tag\tag@in@display \let\label\label@in@display \SK@equationtrue
        \global\let\df@label\@empty \global\let\df@tag\@empty
2492
2493
        \global\tag@false
        \let\mathdisplay@push\mathdisplay@@push
2494
        \let\mathdisplay@pop\mathdisplay@@pop
        \if@fleqn
Turn off overfull box messages temporarily—otherwise there would be unwanted
extra ones emitted during our measuring operations.
           \edef\restore@hfuzz{\hfuzz\the\hfuzz\relax}%
2497
```

Initially set the equation body in a box of displaywidth. Then if the box is not overfull, as we find by checking \badness, we have acquired useful information for the subsequent processing.

```
2499 \setbox\z@\hbox to\displaywidth\bgroup
2500 \let\split@warning\relax \restore@hfuzz
2501 \everymath\@emptytoks \m@th $\displaystyle
2502 \fi
2503 \fi
2504 }
```

 $\operatorname{Arg}\ 1$  is not currently used. I thought it might come in handy for error messages.

```
2505 \def\endmathdisplay#1{%
2506 \ifmmode \else \@badmath \fi
2507 \endmathdisplay@a
2508 $$%
```

I guess the following code means this structure is non-reentrant. But there is plenty of scope for tricky bugs here; suppressing them by brute force at least makes it possible to get things working correctly for normal use. [mjd,2000/01/06]

```
\global\let\df@label\@empty \global\let\df@tag\@empty
2509
      \global\tag@false \global\let\alt@tag\@empty
2510
      \global\@eqnswfalse
2511
2512 }
2513 \def\endmathdisplay@a{%
      \if@eqnsw \gdef\df@tag{\tagform@\theequation}\fi
2514
      \if@fleqn \@xp\endmathdisplay@fleqn
2515
      \else \ifx\df@tag\@empty \else \veqno \alt@tag \df@tag \fi
2516
        \label\@mpty \else \@xp\ltx@label\@xp{\df@label}\fi
2517
2518
      \ifnum\dspbrk@lvl>\m@ne
2519
        \postdisplaypenalty -\@getpen\dspbrk@lvl
2520
2521
        \global\dspbrk@lvl\m@ne
2522
2523 }
```

A boolean variable: Was that last box overfull or not? A value of 0 means yes, it was overfull.

#### $2524 \left( \frac{0}{2} \right)$

Special handling is needed for flush-left equations. We need to measure the equation body (found in box 0 after we close it with the \egroup). Then after a fairly normal test to see if it fits within the available space, we need to consider overlapping into the displayindent area if displayindent is nonzero (as in an indented list). If there is an equation number we may have to shift it by hand to a separate line when there is not enough room; we can no longer take advantage of the automatic shifting provided by the \leqno, \eqno primitives.

We initially add \@mathmargin glue at the end of box 0 to get an accurate overfull test. If \@mathmargin contains any shrink then we cannot reliably tell whether the box will be overfull or not simply by doing hand calculations from the actual width of the equation body. We have to actually set the box and find out what happens.

On the other hand if we put the **\@mathmargin** glue at the beginning of the box it's awkward to remove it afterwards. So we first put it in at the end and later we will move it to the beginning as needed.

```
2525 \def\endmathdisplay@fleqn{%
2526 $\hfil\hskip\@mathmargin\egroup
```

We need to save the information about whether box 0 was overfull in a variable, otherwise it will disappear in the next setbox operation. And we couldn't set the equation number box earlier than now, because the body of the equation might have contained a \tag command (well, it could have been done, but this way we can reuse the tag-handling code from elsewhere).

```
\ifnum\badness<\inf@bad \let\too@wide\@ne \else \let\too@wide\z@ \fi
2527
     \ifx\@empty\df@tag
2528
     \else
2529
       \setbox4\hbox{\df@tag
2530
2531
         \ifx\df@label\@empty \else \@xp\ltx@label\@xp{\df@label}\fi
       ጉ%
2532
     \fi
2533
     \csname emdf@%
2534
       2535
     \endcsname
2536
2537 }
```

For an unnumbered flush-left equation we hope first that the the contents fit within displaywidth. If not we need to fall back on a more complicated reboxing operation.

```
2538 \def\emdf@U{%
2539 \restore@hfuzz
2540 \ifodd\too@wide % not too wide: just need to swap the glue around
2541 \hbox to\displaywidth{\hskip\@mathmargin\unhbox\z@\unskip}%
2542 \else % M+B > displaywidth
2543 \emdf@Ua
2544 \fi
2545 }
```

Some notation:  $M \setminus \mathfrak{Q}$  with margin, B the width of the equation body,  $I \setminus \mathfrak{Q}$  with the tag),  $S \setminus \mathfrak{Q}$  with the tag,  $S \setminus \mathfrak{Q}$  with the tag,  $S \setminus \mathfrak{Q}$  with the tag assume S columnwidth. If S displaywidth, and if we assume S contains shrink, then the only solution left is to encroach into the displayindent space.

```
2546 \def\emdf@Ua{%
2547 \hbox to\columnwidth{%
2548 \ifdim\displayindent>\z@
2549 \hskip\displayindent minus\displayindent
2550 \fi
2551 \hskip\@mathmargin \unhbox\z@ \unskip
2552 }%
2553 \displayindent\z@ \displaywidth\columnwidth
2554 }
```

Find out first if the tag fits in ideal position. If so we can just plunk down box 2. Otherwise we need to do something more complicated.

```
2555 \def\emdf@R{%
2556 \setbox\tw@\hbox to\displaywidth{%
2557 \hskip\@mathmargin \unhcopy\z@\unskip\hfil\hskip\mintagsep\copy4
2558 }%
2559 \restore@hfuzz
2560 \ifnum\badness<\inf@bad \box\tw@ \else \emdf@Ra \fi
2561 }
```

We shift the equation number to line 2 if it does not fit within \displaywidth. Note that we do not first attempt to let the equation body shift leftward into the \displayindent space. If that is desired it will have to be done by hand by adding negative space at the beginning of the equation body. I don't expect

this to arise very often in practice since most of the time \displayindent is zero anyway.

```
2562 \def\emdf@Ra{%
                                          \skip@\displayindent minus\displayindent
 2563
                                          \displayindent\z@ \displaywidth\columnwidth
 2564
                                          \spread@equation \everycr{}\tabskip\z@skip
                                          \halign{\hbox to\displaywidth{##}\cr
 2566
 2567
                                                         \relax
                                                         \ifdim\skip@>\z@ \hskip\skip@ \fi
 2568
                                                         \hskip\@mathmargin\unhbox\z@\unskip\hfil\cr
2569
                                                         \noalign{\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noalign{}\noal
2570
2571
                                                         \hfil\box4 \cr}%
2572 }
```

Find out first if the tag fits in ideal position. If so we can just plunk down box 2. Otherwise we need to do something more complicated.

```
2573 \def\emdf@L{%
```

Calculate the difference between M and N+S. If the latter is greater, we don't want to add any extra glue between the number and the equation body. Otherwise the amount that we want to add is  $\mathbf{x}$  minus  $\mathbf{x}$  where x = M - (N+S). I.e., the distribution of spaces across the line is N, S, xminusx, B, hfil.

```
2574
      \@tempdima\@mathmargin
      \advance\@tempdima-\wd4 \advance\@tempdima-\mintagsep
2575
      \skip@\@tempdima minus\@tempdima
2576
      \setbox\tw@\hbox to\displaywidth{%
2577
2578
        \copy4\hskip\mintagsep
        \ifdim\skip@>\z@ \hskip\skip@\fi
2579
        \unhcopy\z@\unskip
2580
2581
2582
      \restore@hfuzz
      \ifnum\badness<\inf@bad \box\tw@ \else \emdf@La \fi
2583
2584 }
```

If the equation body and equation number will not fit on the same line, we put the number on line 1 and the body on line 2, with the body positioned as for an unnumbered equation.

```
2585 \def\emdf@La{%
2586 \spread@equation \everycr{}\tabskip\z@skip
2587 \halign{\hbox to\displaywidth{##}\cr
2588 \box4 \hfil \cr
2589 \noalign{\raise@tag}%
\hskip\@mathmargin\unhbox\z@\unskip\hfil\cr}%
2591 }
```

If someone has \[ \] nested inside a minipage environment nested inside a numbered equation, the mathdisplay variables that are global will get out of whack unless we take extra care. So we make a stack and push all the variables before entering mathdisplay and pop them afterwards. But we can save a little work by not doing this at the top level, only at inner levels.

```
2592 \newtoks\mathdisplay@stack
2593 \let\mathdisplay@push\@empty
2594 \def\mathdisplay@@push{%
2595
      \begingroup
      \label $$ \operatorname{Qxp}(df@label)\emptokena\empth{\colored} \
2596
      \toks8\@xp{\alt@tag}%
2597
      \edef\@tempa{%
2598
        \global\if@eqnsw\@nx\@eqnswtrue\else\@nx\@eqnswfalse\fi
2599
2600
        \global\iftag@\@nx\tag@false\else\@nx\tag@true\fi
        \gdef\@nx\df@label{\the\toks@}\gdef\@nx\df@tag{\the\@temptokena}%
```

17. CREDITS 75

```
\gdef\@nx\alt@tag{\the\toks8}%
2602
        \global\mathdisplay@stack{\the\mathdisplay@stack}%
2603
2604
2605
      \global\mathdisplay@stack\@xp{\@tempa}
2606
      \endgroup
2607 F
2608 \let\mathdisplay@pop\@empty
2609 \def\mathdisplay@@pop{\the\mathdisplay@stack}
2610 \response equation} {\%}
2611
      \incr@eqnum
2612
      \mathdisplay@push
      \st@rredfalse \global\@eqnswtrue
2613
2614
      \mathdisplay{equation}%
2615 }{%
      \endmathdisplay{equation}%
2616
      \mathdisplay@pop
2617
      \ignorespacesafterend
2618
2619 }
2620 \newenvironment{equation*}{%
      \mathdisplay@push
2621
      \st@rredtrue \global\@eqnswfalse
2622
      \mathdisplay{equation*}%
2623
2624 }{%
2625
      \endmathdisplay{equation*}%
2626
      \mathdisplay@pop
2627
      \ignorespacesafterend
2628 }
   Note: LATEX defines the displaymath environment in terms of \[ and \].
2629 \DeclareRobustCommand{\[}{\begin{equation*}}
```

The usual \endinput to ensure that random garbage at the end of the file doesn't get copied by docstrip.

2630 \DeclareRobustCommand{\]}{\end{equation\*}}

2631 \endinput

## 17 Credits

Much of the code for the amsmath package had its orgin in amstex.tex, written by Michael Spivak. The initial work of porting amstex.tex to amstex.sty was done in 1988–1989 by Frank Mittelbach and Rainer Schöpf. In 1994 David M. Jones added the support for the fleqn option and did extensive improvements to the align[at] family of environments and to the equation number handling in general. Michael Downes at the AMS served as coordinator for the efforts of Mittelbach, Schöpf, and Jones, and has contributed various bug fixes and additional refinements over time.

Versions 1.0 and 1.1 of the package carried the name amstex instead of amsmath, to indicate its origins; the name was changed in 1994 to make it user-oriented rather than history-oriented.

## Index

Numbers written in italic refer to the page where the corresponding entry is described; numbers underlined refer to the code line of the definition; numbers in roman refer to the code lines where the entry is used.

\) 10, 16	\@eha 214,	\@mathstyle 174, 179
<b>\*</b> 10, 16	215, 874, 897, 942	\@medpenalty 27
\+ 10, 16	\@ehd 665	\@nocnterr 849
10, 16, 38, 102, 103,	\@elt 1084	\@nocounterr 848
340, 341, 342,	\@empty 19	\@saveprimitive
343, 409, 411,	\@emptytoks	145, 146, 147,
415, 429, 430,	95, 267, 1121, 2501	148, 149, 150,
431, 673, 765,	\@envbody $36$ ,	260,  2457,  2458
771, 1152, 1216	<i>37</i> , <u>1116</u> , 1117,	\@spread@equation
\ 10, 16, 697, 700	1119, 1120, 1121	991, 1049
\ 10, 16	\@eqnnum 30, 925, 928	$\c$ osptoken $223$ , $229$ ,
.toc 6	\@eqnswfalse $983$ ,	294, 299, 315, 323
\: 106, 107	2511, 2599, 2622	\@temp $4, 7, 9, 14$
\; 109, 110,	\@eqnswtrue	\@tempa 60, 60, 60
263, 264, 265, 448	1233, 1311,	\@tempcnta
\< 11, 17	1512,   1531,	50, 54, 59, 60, 60
\= 11, 17, 698, 701	1560, 2074,	\@tempcntb . $50$ , $54$ ,
\> 11, 17	2235, 2599, 2613	54, 58, 58, 60, 60
\@@above 147	\@eqpen $27, 35, 50, 68,$	\@tempd 544
$\0$ 00abovewithdelims $150$	68, 886, 887, 1061	\@tempdima $\dots$ $53$ ,
\@@atop 146	\@fleqnfalse <i>55</i> , <i>57</i>	55, 58, 58, 60,
\@@atopwithdelims 149	\@fleqntrue . 43, 52, 53	60, 1715, 1716,
\@@eqno 2458, 2459, 2462	\Ogenfrac 7, 174, 178	1738,   1778,
\@@italiccorr 923	\@getpen . 27, 889, 2520	1779,   1780,
\@@leqno 2457, 2460, 2463	\@gobblethree $572, 578$	1784,   1791,
\@@over 6, 145, 166	$\ensuremath{\texttt{Qgtempa}}$ $1086$ ,	1795,   1843,
\@@overline 260, 261	1091, 1098, 1105	1844, 1851,
\@@overwithdelims 148	\@highpenalty 27	1857, 1862,
\@@sqrt 8, 240	\@iden 2350	1870, 1924,
\@@undefined . 123, 138	\@ifnotempty . 745, 747	1933, 1934,
\@addtoreset 850	\@ifpackagewith $55$	1935, 1942,
\@amsmath@err	\@ignoretrue 834	1953, 1964,
. <u>90, 214, 215,</u>	\@ldots $10$ , $332$ , $340$ ,	1986, 1988,
566, 664, 789,	409, 411, 425,	2574, 2575, 2576
874, 879, 897,	429, 430, 431, 810	\@tempdimb 54,
917, 941, 1183,	\@let@token 65	58, 58, 59,
1444, 1544, 2061	\@lign 1528, 1551,	60, 60, 1762,
\@arrayboxrestore 947	2037, 2041, 2356	1827, 1893,
\@arrayparboxrestore	\@lowpenalty 27	1896, 1899, 1900, 1903,
	\@mathmargin 2,	1900, 1903,
\@backslashchar $\frac{55}{153}$	2, 3, 3, 3, 3,	1925, 1934, 1950, 1976,
\@badmath 2487, 2506	39, 40, 44, 45,	1990, 1991, 1999
\@car 94	47, 48, 48, 50,	\@tempdimc 54,
\@cdots 11, 376,	51, 53, 53, 53,	1763, 1779,
377, 378, 421, 456	67,  72,  72,	1828, 1843,
\@centering	72, 73, 1296,	1893, 1895, 1898
. 2, 40, 1265, 2265	1319, 1323,	\@testopt 39, 1197, 1206
\@checkend 1134	1327, 1622, 1642, 1654,	\@totalleftmargin
\@currentlabel		28, 28, 905
30, 934, 936	1671, 1694, 1715, 1730,	\[ 3, 11, 17, 70, 75, 2629
\@currenvir	, , ,	\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\
783, 1120,	$2257, \qquad 2260, \\ 2275, \qquad 2276,$	27, 28, 28, 28,
1123, 1124,	2215, 2216, 2297, 2388,	30, 32, 38, 280,
1149, 1229,	2526, 2541,	308, 321, 894, 900
1432, 2228, 2489	2520,   2541,   2551,   2557,	\\*
\@display@init	2569, 2574, 2590	\} 383
35, 66, 1050, 2250		\] 3, 11, 17, 70, 75, 2630
\@displaytrue 452	513, 682, 685, 686	\^

\ 11, 18	\alignedat@a 1207, 1211	amstex.doc 69
	_	
\' 5	\alignsafe@testopt	amstex.sty 75
	. <u>1190</u> , 1197, 1206	amstex.tex 1, 32, 75, 75
	\alignsep@ $49$ ,	amstext package 4
\	50, 50, 50, 50,	\And 265
	50, 50, 51, 53,	\andhelp@ $34$ ,
$\mathbf{A}$	53, 53, 54, 54,	<u>1014</u> , 1184, 1545
\above 147, 162	54, 55, 55, 55,	
\abovedisplayskip 908		\arabic 847
\abovewithdelims .	<i>55</i> , <i>58</i> , <i>59</i> , <i>59</i> ,	array environment 23,
150, 165	59, 59, 1018,	24, 24, 24, 25, 26
\acc@check	1143,   1158,	\array 24, 780, 830
. 19, 562, 564, 639	1161,   1176,	\arraycolsep 24, 776, 778
	1526,   1591,	\arraystretch 829
\acc@error 563, 564, 565	1637.   1655.	\arrowfill@
\accentclass@ 15,	1656, 1661,	705, 711, 712,
520, 521, 584, 610	1669, 1671,	713, 714, 715, 716
accents package 18	1673,   1675,	
\Acute 657		\AtBeginDocument .
\acute 548, 657	· · · · · · · · · · · · · · · · · · ·	46, 507, 699
\add@amp <u>1006</u>	1691, 1731,	\AtEndOfPackage 8
\add@amps 63, 1006,	1732, 1733,	\atop 6, 23, 23, 146, 161
1524, 1606, 2145	1734,   1735,	\atopwithdelims 149, 164
	1789,   1801,	
\addto@envbody	1803, 1858,	В
. <u>1117</u> , 1135, 1137	1868, 1871,	\badness 72,
\addto@hook 499, 506, 516	1881, 1882,	2527, 2560, 2583
\addtocounter 980	1947, 1962,	
\aftergroup . 2162, 2196	1965, 1968,	\Bar 662
align environment .		\bar 553, 662
31, 31, 32,	1969, 1977, 2045	\bBigg 14
34, 36, 39, 44,	\allowbreak 669, 672	\bBigg@ 508,
44, 44, 44, 44,	\allowdisplaybreaks	509, 510, 511, <u>512</u>
		\begin 28, 37, 37, 37
45, 48, 49, 51,	\alph 841	\begin/endgroup 68
52, 52, 60, 62,	\alt@tag 2468,	\begin@stack
63, 63, 63, 68, <u>1450</u>	2476, 2510,	. 1121, 1131, 1132
align* environment	2516, 2597, 2602	
45, 1450		\begingroup 28
\align@ 44,	\AmS 4, <u>91</u>	\belowdisplayskip 902
1425, 1437, 1505	amsbsy package 4, 4	\bgroup 235,
\align@lengths . $50$ , $50$	\AmSfont 4, 91, 93	484, 753, 759,
\align@preamble	amsfonts package 1,	765, 768, 1153,
. 1517, 1602, 2034	2, 2, 3, 3, 16, 16	1167,   1217,
\align@recover	amsldoc.tex 1	1220, 1260,
	AMSMATH package	1425, 1516,
1429, 1442	$\dots  2, 4, 6, 8,$	2097, 2105,
align[at] environ-		2108, 2262, 2499
ment $$ $75$	10, 12, 14, 16,	
alignat environment	18, 20, 22, 24,	\Big 15, <u>508</u>
44,	26, 28, 30, 32,	\big $15$ , $15$ , $508$
44, 47, 47, 48,	34, 36, 38, 40,	\big@size $514$ , $516$
49, 50, 50, 50, 1450	42, 44, 46, 48,	\bigcap 196, 197
alignat* environment	50, 52, 54, 56,	\bigcap@ 196, 197
	58, 60, 62, 64,	\bigcup 198, 199
	66, 68, 70, 72, 74	\bigcup@ 198, 199
aligned environment	amsmath package $1, 1,$	\Bigg <u>508</u>
38,		
38, 39, 39, 39,	1, 2, 3, 3, 3, 16,	\bigg <u>508</u>
<i>39</i> , <i>45</i> , <i>65</i> , <i>65</i> , <u>1196</u>	16, 16, 24, 30,	\Biggr 394
\aligned@a . 1198, 1204	37, 45, 65, 75, 75	\biggr 392
alignedat environ-	$amsmath.sty \dots 3$	\bigl 15, 15
ment $\dots$ 38,	amsopn package 4	\bigodot 208, 209
38, 38, 39,	amstex package	\bigodot@ 208, 209
39, 39, 39, 1205		\bigoplus 206, 207
, -,,	, , , -,	J 1

\bigoplus@ 206, 207	\checkat@true $1415$	769, 771, 1177,
\bigotimes $204, 205$	\cl@@ckpt 1087	$1200, \qquad 1222,$
\bigotimes@ $\dots$ 204, 205	\classnum@ 288, 289, 290	1269,   1289,
\Bigr 393	\cleaders 708	1517,   1602,
\bigr 15, 391	cmex	2080, 2114,
\bigsqcup 210, 211	cmex10 4	$2143, \qquad 2157,$
\bigsqcup@ 210, 211	cmex10 option $2, 3$	2273, 2366, 2368
\biguplus 194, 195	\cmex@opt 3, 33,	\ctagsplit@false 31
\biguplus@ 194, 195	34, 36, 70, 77, 84	\ctagsplit@true 30
\bigvee 190, 191	\collect@@body	
\bigvee@ 190, 191	37, 37,	$\mathbf{D}$
\bigwedge 192, 193	<i>37</i> , <i>37</i> , 1123, <u>1130</u>	\dag 9
\bigwedge@ 192, 193	\collect@body $37$ ,	\dbinom 6, 170
\binom 6, 6, 169	37, <u>1118</u> , 1236,	\dddot 527
\binrel@ 21, 677, 679	1440, 2076,	\dddot 524
\binrel@@ . 21, 678, 680	2078, 2200, 2239	\Ddot 660
\bl@ck 52	\colon 9, 272	\ddot 551, 660
\black@ <u>1070</u> ,	\column@ 33,	\DeclareFontEncoding
1241, 1478, 2100	35, 39, 39, 54,	522, 523
bm package 4		\DeclareFontShape . 71
\bmod 20, 666	54, 60, 1001, 1000	\DeclareMathAccent
\bold@false 375	1003, 1009,	
\bold@true 374	1067, 1111,	16, 18, 556
	1142, 1166,	\DeclareMathDelimiter
\boldsymbol . 4, 348, 375	1180, 1187,	125, 127, 139, 141
\boldsymboldots@ .	1280, 1540,	\DeclareMathOperator
11, 348, 373	1548, 1570,	
\boxed 9, 262	1598, 1605,	\DeclareMathSymbol
\boxz@ 64,	1761,   1766,   1770	248,
246, 1366, 1372,	1770, 1771,	249, 250, 251,
1387, 1391,	1772, 1774,	252, 253, 254,
1403, 2010, 2015, 2027, 2030 2058	1775, 1826,	255, 256, 257, 258
$2015, \qquad 2027, \\ 2030, \qquad 2058,$	1831, 1835,	\DeclareOption
2000, 2000,	1836, 1837,	19, 20, 21, 22,
2133, 2152, 2155	1839, 1840,	23, 24, 28, 29,
\Breve 661	1894, 1895,	30, 31, 32, 42, 52
\breve 552, 661	1899, 1903,	\DeclareRobustCommand
\buildrel 13	1923, 1928,	5, 5, 100,
G	1989, 1990,	151, 166, 169,
C	1993, 1999, 2138	172, 261, 333,
\c@MatrixCols 24	_	336, 421, 424,
\c@MaxMatrixCols .	33, 1002,	428, 2629, 2630
780, <u>781</u>	1168, 1173, 2048	9 , ,
\cal 15	\columnwidth 28, 73	754, 766, <u>918,</u>
\calc@shift@align	\coprod 7, 186, 188, 189	990, 1164, 2107
	\coprod@ 188, 189	\delayed@ 374, 408
<i>54</i> , 1689, <u>1711</u> ,	\copy 245, 490,	\delimiter 114,
$\frac{1745}{1}$ , $\frac{1810}{1}$ , $\frac{1907}{1}$	501, 505, 685,	119, 121, 134, 136
\calc@shift@gather	741, 2557, 2578	\df@label $30$ ,
<i>33</i> , <i>42</i> , 1263, <u>1315</u>	\count@ 58, 59, 60, 60	31,  937,  955,
cases environment $25$ , $821$	\cr 23, 28,	957, 958, 2492,
\cases 25, 822	895, 1145, 1188,	2509,   2517,
\cdotp 376, 457, 458, 459	1313,   1533,	2531, 2596, 2601
\cdots <u>11</u> ,	1561,   1606,	\df@tag <i>30</i> ,
12, 421, 422, 423	2349, 2566,	$30, 31, 31, \underline{931},$
\cfrac 674	2569, 2571,	951, 1556, 2089,
\Check 655	2587, 2588, 2590	2091,   2354,
\check $546, 655$	\crcr 63, 68, 68,	2371, 2379,
\check@mathfonts 14	717, 718, 726,	2492, 2509,
\checkat@false $1421$	727, 760, 762,	2514, 2516,

2528, 2530,	35, 35, 39, 66,	316, 319, 324,
2535, 2596, 2601	1050, 1254, 1507	325, 340, 411,
\dfrac 6, 6, 167	\displaybreak $\frac{26}{27}$ ,	415, 421, 425,
\dft@tag 29, 918	50, 68, 68, 71, 864	429, 965, 1229,
\dimen@ . 51, 59, 59,	\displayindent	1425,   1429,
59, 59, 59, 242,	73, 73,	1432, 1437, 2228
244, 245, 637,	74, 2548, 2549,	docstrip
638, 651, 652,	2553, 2563, 2564	\Dot 659
687, 688, 1073,	\displaylimits . $7$ ,	\dot 550, 659
1078, 1316,	7, 19, 21, 477, 478	\doteq 13, 449
1321, 1323,	displaymath environ-	\dots 10, 11, 336
1327,   1328,	ment . 70, 71, 75	\DOTS@ 309,
1329,   1338,	\displaystyle . $181$ ,	315, 319, 362, 401
1339,   1340,	238, 262, 674,	\DOTS@@ 310, 314
1341,   1376,	682, 685, 686,	\DOTSB
1377, 1378,	737, 1171,	189, 191, 193,
1634, 1635,	1174,   1221,	195, 197, 199,
1645, 1655,	1262, 1283,	201, 203, 205,
1659, 1669,	2037, 2041,	207, 209, 211,
1702,   1703,   1702	2111, 2112,	263, 264, 265,
1781, 1782,	2270, 2356,	278, 435, 437,
1783, 1784, 1785, 1789,	2428, 2429, 2447, 2448, 2501	439, 441, 442,
		443, 444, 445,
1790, 1791, 1792, 1793,	\displaywidth 35,	446, 447, 448, 450
1792, 1795, 1794, 1795,	42, 50, 52, 55, 55, 58, 58, 73,	\dotsb 422
1797, 1799,	73, 926, 1072,	\dotsb@ 290, 291,
1800, 1803,	1260, 1299,	350, 352, 361,
1845, 1846,	1302, 1329,	364, 368, 370, 378
1847, 1849,	1335, 1341,	\dotsc 349, 428
1851, 1852,	1352, 1375,	\DOTSCASE@ 307, 317,
1856, 1857,	1377, 1634,	318, 319, 364, 403
1858, 1859,	1679, 1700,	\DOTSI 277, 453, 454,
1860, 1861,	1704, 1707,	461, 462, 463, 464
1862,   1864,	1731, 1785,	\dotsi 365, 377
1866, 1867,	1793,   1794,	\dotsm 423
1874,   1875,	1852, 1860,	\dotso 424
1878, 1881,	1861,   1869,	\dotso@ 347, 406
1882, 1936,	1943,   1952,	\dotsspace@
1937,   1938,	1963, 2258,	813, 816, 817, 819
1940, 1942,	2391, 2499,	\DOTSX 279
1943, 1947,	2541, 2553,	\dp 242, 497, 518, 641,
1948, 1949,	2556, 2564,	683, 691, 1076,
1950, 1951,	2566, 2577, 2587	1385, 1400,
1952, 1953,	\displaywidth@	2025, 2054,
1955, 1958, 1959, 1961,	. 1705, 1707, 2017	2055, 2329, 2364
1963, 1964,	\divide 289, 1349, 1646,	\dspbrk@ <u>864</u>
1965, 1966,		\dspbrk@context 864,
1968, 1969,	1650,   1656,   1660,   1665,	1163,   1218,
1973, 1975,	1673, 1682,	1253, 1506,
1976, 1977,	1733, 1771,	2106, 2251, 2490
1978, 1979,	1799, 1836,	\dspbrk@lvl . 26, 27,
2297, 2298,	1866, 1872,	35, 855, 870,
2299, 2301,	1958, 1966, 1995	888, 889, 1061,
2383, 2384,	\DNQ 219, 223,	1067, 2250,
2385, 2388, 2391	224, 230, 231,	2519, 2520, 2521
\displ@y <i>35</i> , <i>66</i> , <u>1050</u>	268, 295, 296,	\dt@pfalse 1057
\displ@y@	300, 301, 309,	\dt@ptrue 1052
	, , ,,	•

${f E}$	alignoda+	1696 1697
	alignedat	1686, 1687, 1697, 1729,
\edef 26	38, 38, 38,	$   \begin{array}{ccc}     1697, & 1729, \\     1730, & 1778,   \end{array} $
\egroup 72, 239, 486,	<i>39</i> , <i>39</i> , <i>39</i> , <u>1205</u>	
762, 771, 1200,	array 23,	1856, 1869,
1202, 1241,	24, 24, 24, 25, 26	1870, 1871,
1479,   1482,	cases 25, <u>821</u>	1872, 1874,
2081, 2082,	displaymath	1876, 1878,
2100, 2101,	70, 71, 75	1949, 1978, 1979
2317, 2342, 2526	eqnarray 26, 30	\eqref 26, 854
\emdf@L 2573	equation 70, 70	equation environment
\emdf@La 2583, 2585	equation* 70	
$\verb \emdf@R 2555 $	flalign . 44, 48,	\equation 3, 30, 44
\emdf@Ra 2560, 2562	49, 51, 52, 59, 1450	equation* environ-
\emdf@U 2538	flalign* <u>1450</u>	ment 70
\emdf@Ua 2543, 2546	gather	\every@math@size 14,
\end 37, 37, 37, 37	32, 33, 34, 36,	14, 499, 506, 516
\endalign 1453,	<i>38</i> , <i>40</i> , <i>62</i> , <i>63</i> , <u>1238</u>	\everycr 35,
1458, 1463,	gather* <u>1238</u>	66, 1053, 1279,
1468, 1473,	gathered $40, \frac{1212}{500}$	1597, 2565, 2586
1493, 1498, 1503	matrix 24, 24, <u>773</u>	\everydisplay 452
\endaligned . 1209, 1224	multline 33, 35,	\everymath 2501 \ex@ . 525, 528, 727, 767
\endarray . 24, 776, 824	65, 66, 69, 69, <u>2241</u>	
\endgather 1248	multline* 2241	\ExecuteOptions 53
\endinput 75	pmatrix 24	\expandafter 37
<del>-</del>	Sb	\ext@arrow
\endmathdisplay	smallmatrix $23, \frac{765}{23}$	734, 735, 750, 751
. 2505, 2616, 2625	Sp	\extra@ 396,
\endmathdisplay@a . 2099, 2507, 2513	split 42,	409, 411, 418, 431 \extrap@ . 414, 421, 425
\endmathdisplay@fleqn	61, 61, 62, 63, 63, 63, 63, 63, 63, 63, 63, 63, 63	(extrape : 414, 421, 425
	05. 05. 05. 05. 2009	
		F
2515, 2525	subarray	F \f@series 4.4.94
$\begin{array}{ccc} & \dots & 2515,  2525 \\ \texttt{\ } & \dots & 800, \end{array}$	subarray 23, 23, 23, 23, 752	\f@series 4, 4, 94
2515, 2525 \endmatrix 800, 802, 806, 808, 809	subarray 23, 23, 23, 23, <u>752</u> xalignat	\f@series 4, 4, 94 \fbox 9, 262
2515, 2525 \endmatrix 800, 802, 806, 808, 809 \endmultline 2247	subarray 23, 23, 23, 23, 752 xalignat 44, 44, 51, 1450	\f@series 4, 4, 94 \fbox 9, 262 \fi 28, 28
2515, 2525 \endmatrix 800, 802, 806, 808, 809 \endmultline 2247 \endmultline@math	subarray 23, 23, 23, 23, 752  xalignat 44, 44, 51, 1450  xalignat* 1450	\f@series 4, 4, 94 \fbox 9, 262 \fi 28, 28 \field@lengths
2515, 2525 \endmatrix 800, 802, 806, 808, 809 \endmultline 2247 \endmultline@math 2270, 2312, 2322	subarray 23, 23, 23, 23, 752  xalignat	\f@series 4, 4, 94 \fbox 9, 262 \fi 28, 28 \field@lengths
2515, 2525 \endmatrix 800, 802, 806, 808, 809 \endmultline 2247 \endmultline@math 2270, 2312, 2322 \endsplit 2076	subarray 23, 23, 23, 23, 752  xalignat	\f@series 4, 4, 94 \fbox 9, 262 \fi 28, 28 \field@lengths
2515, 2525  \endmatrix 800, 802, 806, 808, 809 \endmultline 2247 \endmultline@math 2270, 2312, 2322 \endsplit 2076 \endsubarray 764	subarray 23, 23, 23, 23, 752  xalignat	\f@series 4, 4, 94 \fbox 9, 262 \fi 28, 28 \field@lengths
\text{2515}, 2525 \endmatrix \therefore 800, 802, 806, 808, 809 \endmultline \therefore 2247 \endmultline@math 2270, 2312, 2322 \endsplit \therefore 2076 \endsubarray \therefore 764 \env@cases \therefore 822, 826	subarray 23, 23, 23, 23, 752  xalignat	\f@series 4, 4, 94 \fbox 9, 262 \fi 28, 28 \field@lengths
\text{2515}, 2525 \endmatrix \times 800, \text{802}, 806, 808, 809 \endmultline \times 2247 \endmultline@math \times 2270, 2312, 2322 \endsplit \times 2076 \endsubarray \times 764 \env@cases \times 822, 826 \env@matrix \times \times	subarray 23, 23, 23, 23, 752  xalignat	\f@series 4, 4, 94 \fbox 9, 262 \fi 28, 28 \field@lengths
\tag{2515, 2525} \\ \text{endmatrix} \tag{800}, \text{800}, \text{808}, \text{809} \\ \text{endmultline} \tag{2247} \\ \text{endmultline} \text{gmath} \tag{270, 2312, 2322} \\ \text{endsplit} \tag{2076} \\ \text{endsubarray} \tag{64} \\ \text{env@cases} \tag{822, 826} \\ \text{env@matrix} \tag{774, 778, 798,} \end{array}	subarray 23, 23, 23, 23, 752  xalignat	\f@series 4, 4, 94 \fbox 9, 262 \fi 28, 28 \field@lengths
\tag{2515, 2525} \\ \text{endmatrix} \tag{800}, \text{806, 808, 809} \\ \text{endmultline} \tag{2247} \\ \text{endmultline@math} \tag{2270, 2312, 2322} \\ \text{endsplit} \tag{2076} \\ \text{endsubarray} \tag{764} \\ \text{env@cases} \tag{822, 826} \\ \text{env@matrix} \tag{774, \frac{778}{778, 798, 802, 804, 808, 809} \end{array} \tag{800}	subarray 23, 23, 23, 23, 752  xalignat	\f@series 4, 4, 94 \fbox 9, 262 \fi 28, 28 \field@lengths
\tag{2515, 2525} \tendmatrix \tag{800, 808, 809} \tendmultline \tag{2247} \tendmultline@math \tag{2270, 2312, 2322} \tendsplit \tag{2076} \tendsubarray \tag{64} \tenv@cases \tag{822, 826} \tenv@matrix \tag{774, 778, 798, 802, 804, 808, 809} \tenvironments:	subarray 23, 23, 23, 23, 752  xalignat	\f@series 4, 4, 94 \fbox 9, 262 \fi 28, 28 \field@lengths
\tag{2515, 2525} \\ endmatrix \tag{800, 806, 808, 809} \\ endmultline \tag{2247} \\ endmultline@math \tag{2270, 2312, 2322} \\ endsplit \tag{2076} \\ endsubarray \tag{64} \\ env@cases \tag{822, 826} \\ env@matrix \tag{774, 778, 798, 802, 804, 808, 809} \\ environments: \tag{align 31, 31, 32, } \end{align 31, 31, 32, } \end{align}	subarray 23, 23, 23, 23, 752  xalignat	\f@series 4, 4, 94 \fbox 9, 262 \fi 28, 28 \field@lengths
\tag{2515, 2525} \\ \text{endmatrix} \tag{800}, 806, 808, 809 \\ \text{endmultline} \tag{2247} \\ \text{endmultline@math} \tag{2270, 2312, 2322} \\ \text{endsplit} \tag{64} \\ \text{endsubarray} \tag{764} \\ \text{env@cases} \tag{822, 826} \\ \text{env@matrix} \tag{774, 778, 798, 802, 804, 808, 809} \\ \text{environments:} \tag{81, 31, 31, 32, 34, 36, 39, 44,} \end{800}	subarray 23, 23, 23, 23, 752  xalignat	\f@series 4, 4, 94 \fbox 9, 262 \fi 28, 28 \field@lengths
\tag{2515, 2525} \text{ endmatrix } \tag{800}, 806, 808, 809 \text{ endmultline } \tag{2247} \text{ endmultline@math } \tag{270, 2312, 2322} \text{ endsplit } \tag{2076} \text{ endsubarray } \tag{64} \text{ env@cases } \tag{822, 826} \text{ env@matrix } \tag{774, 778, 798, } \text{ 802, 804, 808, 809} \text{ environments: } \text{ align } \text{ 31, 31, 32, } \text{ 34, 36, 39, 44, }  44, 44, 44, 44, 44, 44, 44, 44, 44, 44	subarray 23, 23, 23, 23, 752  xalignat	\f@series 4, 4, 94 \fbox 9, 262 \fi 28, 28 \field@lengths
\tag{2515}, 2525 \endmatrix \tag{800}, 802, 806, 808, 809 \endmultline \tag{2247} \endmultline@math \tag{2270}, 2312, 2322 \endsplit \tag{2076} \endsubarray \tag{764} \env@cases \tag{822}, 826 \env@matrix \tag{774}, 778, 798, 802, 804, 808, 809 environments:  align \tag{31}, \tag{31}, \tag{32}, \tag{34}, \tag{36}, \tag{39}, 44, 44, 44, 44, 44, 44, 44, 45, 48, 49, 51,	subarray 23, 23, 23, 23, 752  xalignat	$\begin{tabular}{lllllllllllllllllllllllllllllllllll$
\tag{2515}, 2525 \endmatrix \tag{800}, 808, 809 \endmultline \tag{2247} \endmultline@math \tag{2270}, 2312, 2322 \endsplit \tag{200}, 2366 \env@cases \tag{822}, 826 \env@matrix \tag{774}, 778, 798, 802, 804, 808, 809 environments:  align \tag{31}, 31, 32, \tag{34}, 36, 39, 44, 44, 44, 44, 44, 44, 44, 45, 48, 49, 51, 52, 52, 60, 62,	$\begin{array}{c} \text{subarray} & \dots & \\ 23, \ 23, \ 23, \ 23, \ 752 \\ \text{xalignat} & \dots & \\ & \  \   \cdot \   \cdot \   44, \ 44, \ 51, \ \underline{1450} \\ \text{xalignat} * & \dots & \underline{1450} \\ \text{xxalignat} & \dots & 44, \\ & \   44, \ 48, \ 49, \ 51, \ \underline{1450} \\ \text{eqnarray environment} & \dots & 26, \ 30 \\ \text{leqnarray} & \dots & 3 \\ \text{leqno} & 72, \ 2458, \ 2459, \ 2460 \\ \text{leqnshift@} & 34, \ 49, \\ & 50, \ 52, \ 53, \ 53, \\ & 54, \ 55, \ 58, \ 59, \\ & 59, \ 59, \ 59, \ 59, \ 59, \\ & 59, \ \underline{1017}, \ 1319, \\ & 1335, \ 1336, \\ \end{array}$	\f@series 4, 4, 94 \fbox 9, 262 \fi 28, 28 \field@lengths
\tag{2515}, 2525 \endmatrix \tag{800}, 802, 806, 808, 809 \endmultline \tag{2247} \endmultline@math \tag{2270}, 2312, 2322 \endsplit \tag{2076} \endsubarray \tag{764} \env@cases \tag{822}, 826 \env@matrix \tag{774}, 778, 798, 802, 804, 808, 809 environments:  align \tag{31}, 31, 32, \tag{34}, 36, 39, 44, 44, 44, 44, 44, 44, 44, 44, 44, 4	subarray 23, 23, 23, 23, 752  xalignat	\f@series 4, 4, 94 \fbox 9, 262 \fi 28, 28 \field@lengths
\tag{2515}, 2525 \endmatrix \tag{800}, 808, 809 \endmultline \tag{2247} \endmultline@math \tag{2270}, 2312, 2322 \endsplit \tag{200}, 2006 \endsubarray \tag{64}, 764 \env@cases \tag{822}, 826 \env@matrix \tag{774}, 778, 798, 802, 804, 808, 809 environments: align \tag{31}, 31, 32, \tag{34}, 36, 39, 44, 44, 44, 44, 44, 44, 44, 45, 48, 49, 51, 52, 52, 60, 62, 63, 63, 63, 63, 68, 1450} align* \tag{450}	$\begin{array}{c} \text{subarray} & \dots & \\ 23, \ 23, \ 23, \ 23, \ 752 \\ \text{xalignat} & \dots & \\ & \  \   \cdot \   \cdot \   44, \ 44, \ 51, \ 1450 \\ \text{xalignat*} & \dots & 1450 \\ \text{xxalignat} & \dots & 44, \\ & \   44, \ 48, \ 49, \ 51, \ 1450 \\ \text{eqnarray environment} & \dots & 26, \ 30 \\ \text{eqnarray} & \dots & \dots & 3 \\ \text{eqno } 72, \ 2458, \ 2459, \ 2460 \\ \text{eqnshift@} & 34, \ 49, \\ & 50, \ 52, \ 53, \ 53, \\ & 54, \ 55, \ 58, \ 59, \\ & 59, \ 59, \ 59, \ 59, \\ & 59, \ 59, \ 59, \ 59, \\ & 59, \ 1017, \ 1319, \\ & 1335, \ 1336, \\ & 1344, \ 1345, \\ & 1349, \ 1351, \\ & 1352, \ 1353, \\ & 1355, \ 1356, \\ \end{array}$	\f@series 4, 4, 94 \fbox 9, 262 \fi
\tag{2515, 2525} \\ \text{endmatrix} \tag{800}, \text{806, 808, 809} \\ \text{endmultline} \tag{2247} \\ \text{endmultline} \text{Gmath} \tag{270, 2312, 2322} \\ \text{endsplit} \tag{270, 2312, 2322} \\ \text{endsplit} \tag{270, 2312, 2322} \\ \text{endsplit} \tag{64} \tag{2076} \\ \text{endsubarray} \tag{764} \\ \text{env@cases} \tag{822, 826} \\ \text{env@matrix} \tag{774, 778, 798, 802, 804, 808, 809} \\ \text{environments:} \text{align} 31, 31, 32, 34, 36, 39, 44, 44, 44, 44, 44, 44, 44, 44, 44, 4	$\begin{array}{c} \text{subarray} & \dots & \\ 23, \ 23, \ 23, \ 23, \ 752 \\ \text{xalignat} & \dots & \\ & \  \   \cdot \   \cdot \   44, \ 44, \ 51, \ 1450 \\ \text{xalignat*} & \dots & 1450 \\ \text{xxalignat} & \dots & 44, \\ & \   44, \ 48, \ 49, \ 51, \ 1450 \\ \text{eqnarray environment} & \dots & 26, \ 30 \\ \text{eqnarray} & \dots & \dots & 3 \\ \text{eqno } 72, \ 2458, \ 2459, \ 2460 \\ \text{eqnshift@} & 34, \ 49, \\ & 50, \ 52, \ 53, \ 53, \\ & 54, \ 55, \ 58, \ 59, \\ & 59, \ 59, \ 59, \ 59, \ 59, \\ & 59, \ 59, \ 59, \ 59, \ 59, \\ & 59, \ 1017, \ 1319, \\ & 1335, \ 1336, \\ & 1344, \ 1345, \\ & 1349, \ 1351, \\ & 1352, \ 1353, \\ & 1355, \ 1356, \\ & 1402, \ 1515, \end{array}$	\f@series 4, 4, 94 \fbox 9, 262 \fi 28, 28 \field@lengths 1563, 1593 \fieldlengths@ 54, 1563, 1764, 1829, 1926 \finsm@sh 692 flalign environment 44, 48, 49, 51, 52, 59, 1450 flalign* environment 1450 fleqn option 2, 3, 42, 48, 48, 48, 50, 50, 51, 51, 51, 51, 51, 65, 67, 69, 75 fleqn.clo 3, 3, 3 \FN@ 222, 223, 224, 228, 230, 231,
2515, 2525 \endmatrix 800,	$\begin{array}{c} \text{subarray} & \dots & \\ 23, \ 23, \ 23, \ 23, \ 752 \\ \text{xalignat} & \dots & \\ & \  \   \cdot \   \cdot \   44, \ 44, \ 51, \ 1450 \\ \text{xalignat*} & \dots & 1450 \\ \text{xxalignat} & \dots & 44, \\ & \   44, \ 48, \ 49, \ 51, \ 1450 \\ \text{eqnarray environment} & \dots & 26, \ 30 \\ \text{eqnarray} & \dots & \dots & 26, \ 30 \\ \text{eqnarray} & \dots & \dots & 3 \\ \text{eqno } 72, \ 2458, \ 2459, \ 2460 \\ \text{eqnshift@} & 34, \ 49, \\ & 50, \ 52, \ 53, \ 53, \\ & 54, \ 55, \ 58, \ 59, \\ & 59, \ 59, \ 59, \ 59, \ 59, \\ & 59, \ 59, \ 59, \ 59, \ 59, \\ & 59, \ 1017, \ 1319, \\ & 1335,  1336, \\ & 1344,  1345, \\ & 1349,  1351, \\ & 1352,  1353, \\ & 1355,  1356, \\ & 1402,  1515, \\ & 1590,  1642, \end{array}$	\f@series 4, 4, 94 \fbox 9, 262 \fi 28, 28 \field@lengths
\tag{2515}, 2525 \endmatrix \tag{800}, 808, 809 \endmultline \tag{2247} \endmultline@math \tag{2270}, 2312, 2322 \endsplit \tag{200}, 2312, 2322 \endsplit \tag{200}, 2312, 2322 \endsplit \tag{200}, 2312, 2322 \endsplit \tag{200}, 2076 \endsubarray \tag{200}, 764 \env@cases \tag{22}, 826 \env@matrix \tag{200}, 822, 826 \env@matrix \tag{200}, 804, 808, 809 \environments:  align \tag{31}, 31, 32, 34, 36, 39, 44, 44, 44, 44, 44, 44, 44, 44, 44, 4	$\begin{array}{c} \text{subarray} & \dots & \\ 23, \ 23, \ 23, \ 23, \ 752 \\ \text{xalignat} & \dots & \\ & \  \   \cdot \   \cdot \   44, \ 44, \ 51, \ 1450 \\ \text{xalignat*} & \dots & 1450 \\ \text{xxalignat*} & \dots & 44, \\ & \   44, \ 48, \ 49, \ 51, \ 1450 \\ \text{eqnarray environment} & \dots & 26, \ 30 \\ \text{eqnarray} & \dots & \dots & 26, \ 30 \\ \text{eqnarray} & \dots & \dots & 3 \\ \text{eqno } 72, \ 2458, \ 2459, \ 2460 \\ \text{eqnshift@} & 34, \ 49, \\ & 50, \ 52, \ 53, \ 53, \\ & 54, \ 55, \ 58, \ 59, \\ & 59, \ 59, \ 59, \ 59, \ 59, \\ & 59, \ 59, \ 59, \ 59, \ 59, \\ & 59, \ 1017, \ 1319, \\ & 1335, \qquad 1336, \\ & 1344, \qquad 1345, \\ & 1349, \qquad 1351, \\ & 1352, \qquad 1353, \\ & 1355, \qquad 1356, \\ & 1402, \qquad 1515, \\ & 1590, \qquad 1642, \\ & 1645, \qquad 1646, \end{array}$	$\begin{tabular}{lllllllllllllllllllllllllllllllllll$
\tag{2515}, 2525 \endmatrix \tag{800}, 808, 809 \endmultline \tag{2247} \endmultline@math \tag{2270}, 2312, 2322 \endsplit \tag{200}, 2312, 2322 \endsplit \tag{200}, 2312, 2322 \endsplit \tag{200}, 2312, 2322 \endsplit \tag{200}, 2076 \endsubarray \tag{200}, 764 \env@cases \tag{22}, 826 \env@matrix \tag{200}, 822, 826 \env@matrix \tag{200}, 804, 808, 809 environments:  align \tag{31}, \tag{31}, \tag{32}, \tag{34}, \tag{36}, \tag{39}, \tag{44}, \tag{45}, \tag{48}, \tag{49}, 51, \tag{52}, 52, 60, 62, \tag{63}, 63, 63, 68, \tag{1450} \tag{1450} \tag{1450} \tag{147}, \tag{47}, \tag{47}, \tag{48}, \tag{49}, 50, 50, 50, \tag{1450}	$\begin{array}{c} \text{subarray} & \dots & \\ 23, \ 23, \ 23, \ 23, \ 752 \\ \text{xalignat} & \dots & \\ & \  \   \cdot \   \cdot \   44, \ 44, \ 51, \ 1450 \\ \text{xalignat*} & \dots & 1450 \\ \text{xxalignat*} & \dots & 44, \\ & \   44, \ 48, \ 49, \ 51, \ 1450 \\ \text{eqnarray environment} & \dots & 26, \ 30 \\ \text{eqnarray} & \dots & \dots & 26, \ 30 \\ \text{eqnarray} & \dots & \dots & 3 \\ \text{eqno} & 72, \ 2458, \ 2459, \ 2460 \\ \text{eqnshift@} & 34, \ 49, \\ & 50, \ 52, \ 53, \ 53, \\ & 54, \ 55, \ 58, \ 59, \\ & 59, \ 59, \ 59, \ 59, \ 59, \\ & 59, \ 59, \ 59, \ 59, \ 59, \\ & 59, \ 1017, \ 1319, \\ & 1335, \qquad 1336, \\ & 1344, \qquad 1345, \\ & 1349, \qquad 1351, \\ & 1352, \qquad 1353, \\ & 1355, \qquad 1356, \\ & 1402, \qquad 1515, \\ & 1590, \qquad 1642, \\ & 1645, \qquad 1646, \\ & 1654, \qquad 1659, \end{array}$	\f@series 4, 4, 94 \fbox 9, 262 \fi 28, 28 \field@lengths
\tag{2515}, 2525 \endmatrix \tag{800}, 808, 809 \endmultline \tag{2247} \endmultline@math \tag{2270}, 2312, 2322 \endsplit \tag{200}, 2312, 2322 \endsplit \tag{200}, 2312, 2322 \endsplit \tag{200}, 2312, 2322 \endsplit \tag{200}, 2076 \endsubarray \tag{200}, 764 \env@cases \tag{22}, 826 \env@matrix \tag{200}, 802, 804, 808, 809 environments:  \tag{31}, 31, 32, 34, 36, 39, 44, 44, 44, 44, 44, 44, 44, 44, 44, 4	$\begin{array}{c} \text{subarray} & \dots & \\ 23, \ 23, \ 23, \ 23, \ 752 \\ \text{xalignat} & \dots & \\ & \  \   \cdot \   \cdot \   44, \ 44, \ 51, \ 1450 \\ \text{xalignat*} & \dots & 1450 \\ \text{xxalignat*} & \dots & 44, \\ & \   44, \ 48, \ 49, \ 51, \ 1450 \\ \text{eqnarray environment} & \dots & 26, \ 30 \\ \text{eqnarray} & \dots & \dots & 26, \ 30 \\ \text{eqnarray} & \dots & \dots & 3 \\ \text{eqno} & 72, \ 2458, \ 2459, \ 2460 \\ \text{eqnshift@} & 34, \ 49, \\ & 50, \ 52, \ 53, \ 53, \\ & 54, \ 55, \ 58, \ 59, \\ & 59, \ 59, \ 59, \ 59, \ 59, \\ & 59, \ 59, \ 59, \ 59, \ 59, \\ & 59, \ 1017, \ 1319, \\ & 1335, \qquad 1336, \\ & 1344, \qquad 1345, \\ & 1349, \qquad 1351, \\ & 1352, \qquad 1353, \\ & 1355, \qquad 1356, \\ & 1402, \qquad 1515, \\ & 1590, \qquad 1642, \\ & 1645, \qquad 1646, \\ & 1654, \qquad 1659, \\ & 1660, \qquad 1661, \\ \end{array}$	\f@series 4, 4, 94 \fbox 9, 262 \fi 28, 28 \field@lengths 1563, 1593 \fieldlengths@ 54, 1563, 1764, 1829, 1926 \finsm@sh 692 flalign environment 44, 48, 49, 51, 52, 59, 1450 flalign* environment 1450 fleqn option 2, 3, 42, 48, 48, 48, 50, 50, 51, 51, 51, 51, 51, 65, 67, 69, 75 fleqn.clo 3, 3, 3 \FN@ . 222, 223, 224, 228, 230, 231, 235, 267, 270, 296, 301, 316, 325, 345, 346, 411, 421, 427, 433
\tag{2515}, 2525 \endmatrix \tag{800}, 808, 809 \endmultline \tag{2247} \endmultline@math \tag{2270}, 2312, 2322 \endsplit \tag{200}, 2312, 2322 \endsplit \tag{200}, 2312, 2322 \endsplit \tag{200}, 2312, 2322 \endsplit \tag{200}, 2076 \endsubarray \tag{200}, 764 \env@cases \tag{22}, 826 \env@matrix \tag{774}, 778, 798, 802, 804, 808, 809 \environments:  align \tag{31}, \tag{31}, \tag{32}, \tag{34}, \tag{36}, \tag{39}, 44, 44, 44, 44, 44, 44, 44, 44, 44, 4	$\begin{array}{c} \text{subarray} & \dots & \\ 23, \ 23, \ 23, \ 23, \ 752 \\ \text{xalignat} & \dots & \\ & \  \   \cdot \   \cdot \   44, \ 44, \ 51, \ 1450 \\ \text{xalignat*} & \dots & 1450 \\ \text{xxalignat*} & \dots & 44, \\ & \   44, \ 48, \ 49, \ 51, \ 1450 \\ \text{eqnarray environment} & \dots & 26, \ 30 \\ \text{eqnarray} & \dots & \dots & 3 \\ \text{eqno } 72, \ 2458, \ 2459, \ 2460 \\ \text{eqnshift@} & \   34, \ 49, \\ & 50, \ 52, \ 53, \ 53, \\ & 54, \ 55, \ 58, \ 59, \\ & 59, \ 59, \ 59, \ 59, \ 59, \\ & 59, \ 1017, \ 1319, \\ & 1335, \ 1336, \\ & 1344, \ 1345, \\ & 1349, \ 1351, \\ & 1352, \ 1353, \\ & 1355, \ 1356, \\ & 1402, \ 1515, \\ & 1590, \ 1642, \\ & 1645, \ 1646, \\ & 1654, \ 1659, \\ & 1660, \ 1661, \\ & 1668, \ 1677, \\ \end{array}$	\f@series 4, 4, 94 \fbox 9, 262 \fi 28, 28 \field@lengths 1563, 1593 \fieldlengths@ 54, 1563, 1764, 1829, 1926 \finsm@sh 692 flalign environment 44, 48, 49, 51, 52, 59, 1450 flalign* environment 1450 fleqn option 2, 3, 42, 48, 48, 48, 50, 50, 51, 51, 51, 51, 65, 67, 69, 75 fleqn.clo 3, 3, 3 \FN@ 222, 223, 224, 228, 230, 231, 235, 267, 270, 296, 301, 316, 325, 345, 346, 411, 421, 427, 433 \fontdimen
\tag{2515}, 2525 \endmatrix \tag{800}, 808, 809 \endmultline \tag{2247} \endmultline@math \tag{2270}, 2312, 2322 \endsplit \tag{200}, 2312, 2322 \endsplit \tag{200}, 2312, 2322 \endsplit \tag{200}, 2312, 2322 \endsplit \tag{200}, 2076 \endsubarray \tag{200}, 764 \env@cases \tag{22}, 826 \env@matrix \tag{200}, 802, 804, 808, 809 environments:  \tag{31}, 31, 32, 34, 36, 39, 44, 44, 44, 44, 44, 44, 44, 44, 44, 4	$\begin{array}{c} \text{subarray} & \dots & \\ 23, \ 23, \ 23, \ 23, \ 752 \\ \text{xalignat} & \dots & \\ & \  \   \cdot \   \cdot \   44, \ 44, \ 51, \ 1450 \\ \text{xalignat*} & \dots & 1450 \\ \text{xxalignat*} & \dots & 44, \\ & \   44, \ 48, \ 49, \ 51, \ 1450 \\ \text{eqnarray environment} & \dots & 26, \ 30 \\ \text{eqnarray} & \dots & \dots & 26, \ 30 \\ \text{eqnarray} & \dots & \dots & 3 \\ \text{eqno} & 72, \ 2458, \ 2459, \ 2460 \\ \text{eqnshift@} & 34, \ 49, \\ & 50, \ 52, \ 53, \ 53, \\ & 54, \ 55, \ 58, \ 59, \\ & 59, \ 59, \ 59, \ 59, \ 59, \\ & 59, \ 59, \ 59, \ 59, \ 59, \\ & 59, \ 1017, \ 1319, \\ & 1335, \qquad 1336, \\ & 1344, \qquad 1345, \\ & 1349, \qquad 1351, \\ & 1352, \qquad 1353, \\ & 1355, \qquad 1356, \\ & 1402, \qquad 1515, \\ & 1590, \qquad 1642, \\ & 1645, \qquad 1646, \\ & 1654, \qquad 1659, \\ & 1660, \qquad 1661, \\ \end{array}$	\f@series 4, 4, 94 \fbox 9, 262 \fi 28, 28 \field@lengths 1563, 1593 \fieldlengths@ 54, 1563, 1764, 1829, 1926 \finsm@sh 692 flalign environment 44, 48, 49, 51, 52, 59, 1450 flalign* environment 1450 fleqn option 2, 3, 42, 48, 48, 48, 50, 50, 51, 51, 51, 51, 51, 65, 67, 69, 75 fleqn.clo 3, 3, 3 \FN@ . 222, 223, 224, 228, 230, 231, 235, 267, 270, 296, 301, 316, 325, 345, 346, 411, 421, 427, 433

Variation   Vari			
Minimary of the content of	\fontfamily 79	2171, 2180,	2259,   2264,
C   C   C   C   C   C   C   C   C   C			
G	•		
G	95, 579, 599		
gather environment         2547, 2556, 2577, 2587         (ifctageplite)         (26, 2130, 2151, 2178, 2190, 2210, 2216)         (ifctageplite)         (ifctageplite)         (26, 2130, 2151, 2178, 2190, 2210, 2216, 236, 358, 358, 358, 358, 358, 358, 358, 359, 369, 361, 363, 361, 361			\ifcase 47
Sather environment   2347,   2556,   38, 40, 62, 63, 1238   38, 40, 1238   38, 40,	${f G}$	2530, 2541,	\ifcheckat@ . 1406.1541
32, 33, 34, 36,         2566, 2577, 2587         26, 2130, 2151, 2178, 2190, 2210           gather*environment 1234, 1250, 2098         (Adotsefor 812, 814, 815)         (Adotsefor 811, 1540, 156, 66, 67, 718, 1521, 1540, 156, 66, 67, 718, 1726, 759, 760, 1726, 1730, 1300, 1302, 1362, 1404, 2035, 1300, 1302, 1362, 1404, 2035, 169, 170, 171, 172, 173, 174, 175, 175, 175, 175, 175, 175, 175, 175	gather environment		
38, 40, 62, 63, 1238         khdots         810         2178, 2190, 2210           gather* environment         1234, 1250, 2098         khdotsfor         812, 814, 815         kiftlegen         1056           kgathere 1234, 1250, 2098         khdotsfor         811         kiftlegen         1056           kgathere 2012, 2008         khokster         532         kiftlegen         1056           kgathere 2012, 2018         kernumbere         532         kiftlegen         kernumbere         532         kiftlegen         kernumbere         1327, 275, 276         7276, 759, 760         352, 356, 358, 358, 358, 351, 363, 361, 363, 370, 363, 370, 363, 370, 402, 409         363, 361, 363, 370, 368, 370, 368, 370, 370, 402, 409, 411, 419, 431         367, 368, 370, 397, 400, 402, 409, 411, 419, 431         4149, 431         4149, 431         4149, 431         4149, 431         4149, 431         4149, 431         4149, 431         4149, 431         4149, 431         4149, 431         4149, 431         4149, 431         4149, 431         4149, 431         4149, 431         4149, 431         4149, 431         4149, 431         4148         4148         4148         4148         4148         4148         4148         4148         4148         4148         4148         4148         4148         4148         4148         4148         4148			
Stather   1234   1250   2098   1250   2098   1250   2098   1250   2098   1250   2098   1250   2098   1250   2098   1250   2098   1250   2098   1250   2098   1250   2098   1250   2098   1250   2098   1250   2098   1250   2099   1263   2050   2051   2260   2050   2051   2260   2050   2051   2260   2050   2051   2260   2050   2051   2260   2050   2051   2260   2050   2051   2050   2050   2051   2050			
Vather@ 1234, 1250, 2098			2178, 2190, 2210
Vgather®split 2078, 2086 (gathered environment ygathered environment	gather* environment 1238	\hdots@for 812, 814, 815	\ifdt@p 1056
Sather@split 2078, 2086   Sather@split 207	\gather@ 1234, 1250, 2098	\hdotsfor 811	
gathered environment	\gather@split 2078, 2086	\hexnumber@ 532	
\text{Vgdisplayvidthe} \tauser 768, 769, 169, 352, 356, 358, 358, 1109, 360, 361, 363, 1175, 1221, 360, 361, 363, 361, 361			,
Variable Notation of the Nation of State 1 (19.1) and the Na	•		
1300, 1302, 1362			352, 356, 358,
1300, 1302, 1362   1404, 2035, 397, 400, 402,	\gdisplaywidth@		360. 361. 363.
1300, 1302, 1362	$\dots \dots 1268,$		
154, 167, 168, 169, 170, 171, 172	1300, 1302, 1362	1404, 2035,	
154, 167, 168, 169, 170, 171, 172		2044. 2109.	
169, 170, 171, 172		2113 2267	409, 411, 419, 431
\getdsp@pen . 859, 861 \getdsp@pen . 859, 861 \getdsp@pen . 2557, 2568, 2590 \getdsp@pen . 258, 358 \getdsp@pen . 258, 259, 368, 369, 324, 331, 394, 403 \getdsp@pen . 268, 287, 294, 299, 324, 331, 394, 403 \getdsp@pen . 257, 258, 259, 56, 58, 1260, 1602, 2262, 2355, 2566, 2587 \getdsp@pen . 268, 368, 368, 399, 399, 499, 503, 526, 529, 576, 489, 499, 526, 529, 576, 489, 499, 526, 529, 576, 646, 688, 708, 737, 739, 740, 1653, 1670, 2123, 2132, 1810, 1907, 2426, 2463, 2535 \getdsp@pen . 258, 358, 367, 362, 362, 362, 362, 362, 362, 362, 362			\ifhbox 1630
Agetmathche         289, 358         2571, 2588, 2590         64, 987, 2117, 2166           Aglb@settings         14         Ahfill         675, 708, 818, 1077, 2113         Aifinany@         32           Agmeasure@         1256, 1272         Ahfillneg         66, 2278, 2314, 2403, 2449         Aifinner         Aifinner         13, 2071           Agrave         549, 658         Ahfuzz         2497, 2498         Aifinmer         33, 867, 953, 2042           Agetst@false         9, 276, 282, 286, 295, 300, 303, 309, 324, 331, 394, 403         Ahspace         5         Aifshifttag@         33, 867, 953, 2042           Agtest@true         1, 252, 283, 284, 299, 3691, 1075, 1398, 324, 327, 379, 398, 403         517, 641, 683, 284, 2497, 3232, 2411, 2432         Aifshifttag@         33, 811, 311, 313, 314, 323, 327, 379, 398, 403         I         I         1560, 2074, 2232         2323, 2411, 2432           H         Alaign         717, 1627, 1290, 2108         1512, 1521, 1531, 1538, 1538, 1534, 323, 327, 379, 398, 403         I         1560, 2074, 2232         1512, 1521, 1521, 1531, 1538, 1538, 1536, 324, 323, 324, 343, 344, 48, 48, 50, 50, 444, 48, 48, 50, 50, 444, 48, 48, 50, 50, 444, 48, 48, 50, 50, 444, 48, 48, 50, 50, 444, 48, 48, 50, 50, 444, 48, 48, 50, 50, 444, 48, 48, 50, 50, 444, 48, 48, 50, 50, 444, 48, 48, 50, 50, 444, 48, 48, 50, 50, 444, 48, 48, 50, 50, 444, 48, 48, 50, 50, 444, 48, 48, 50, 50, 444, 48, 48, 50, 50, 444, 48, 48, 50, 50, 444, 48, 48, 50, 50, 444, 48, 48, 50, 50, 444, 48, 48			\ifinalign@ 63
Ngetwathchen         299, 388         Late of the properties	\getdsp@pen $859$ , $861$	2557, 2569,	
\text{\text{liglobs} \tau	\getmathch@ 289, 358	2571, 2588, 2590	
\[ \lambda   \cdots  9, 25 \\ \cdots \equiv   \text{ lifting a there} \cdots    \text{ lifting a there} \cdots  \qq  \qq   \qq   \qq \qq  \qq  \qq \qq \qq \qq \qq \qq \qq \qq		\hfill 675, 708,	\ifinany@ 32
\text{Vgmeasure@} 1256, \frac{1272}{1278} \text{Vhfilneg} \ldots \frac{66}{6}, \text{Vifinner} \ldots \frac{13}{2071} \ldots \frac{1278}{1507} \text{Vifinner} \ldots \frac{13}{2071} \	_		\ifingather@ $987$ ,
\( \) \( \)			
Section   Sect			
\( \) \( \)	\gobble@tag		
\Grave \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	$\dots 916, 917, 2256$	2340, 2403,	
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		2409, 2430, 2449	33, 867, 953,
\text{\colorates} \color		\hfuzz 2497, 2498	<u>998,</u> 2038, 2042
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	282, 286, 295,		_
\gtest@true \cdots \text{\text{Nt}} \text{\text{Nt}} \text{\text{\$\cdots}} \text{\text{\text{\$\cdots}}} \text{\text{\text{\$\cdots}}	300, 303, 309,	\hskip 66	<del></del> ;
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	324, 331, 394, 403	\hspace 5	1380, 2284,
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		\ht 242, 497.	2323, 2411, 2432
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			\ifst@rred 997.1233.
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		· · · · · · · · · · · · · · · · · · ·	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		2050, 2051, 2360	1912, 1921,
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	327, 379, 398, 403		1531, 1538,
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		I	1560, 2074, 2232
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	H	\ialign 717,	\iftag@ 31, 951,
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	\halign 13 23		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	1282,   1516,	\if	2373, 2410,
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	1602, 2262,	\if@display	2431, 2471, 2600
$\begin{array}{llllllllllllllllllllllllllllllllllll$	2355. 2566. 2587		\iftagsleft@ 27.
$\begin{array}{llllllllllllllllllllllllllllllllllll$			<del>-</del>
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	,		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$			
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		· · · · · · · · · · · · · · · · · · ·	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	95, 236, 243,	1552,   2372,	1397,   1699,
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	489, 492, 503,		1711, 1745,
635, 636, 639,       1295,       1318,       1907,       2005,         640, 688, 708,       1622,       1640,       2049,       2083,         737, 739, 740,       1653,       1670,       2212,       2244,         743, 817, 922,       1678,       1692,       2281,       2357,         925, 1077, 1627,       1711,       1745,       2386,       2400,         2123,       2132,       1810,       1907,       2426,       2463,       2535			1810, 1890,
640, 688, 708,       1622,       1640,       2049,       2083,         737, 739, 740,       1653,       1670,       2212,       2244,         743, 817, 922,       1678,       1692,       2281,       2357,         925, 1077, 1627,       1711,       1745,       2386,       2400,         2123,       2132,       1810,       1907,       2426,       2463,       2535			
737, 739, 740,     1653,     1670,     2212,     2244,       743, 817, 922,     1678,     1692,     2281,     2357,       925, 1077, 1627,     1711,     1745,     2386,     2400,       2123,     2132,     1810,     1907,     2426,     2463,     2535			
743, 817, 922,     1678,     1692,     2281,     2357,       925, 1077, 1627,     1711,     1745,     2386,     2400,       2123,     2132,     1810,     1907,     2426,     2463,     2535			
925, 1077, 1627,       1711,       1745,       2386,       2400,         2123,       2132,       1810,       1907,       2426,       2463,       2535			
2123, 2132, 1810, 1907, 2426, 2463, 2535	743, 817, 922,	1678,   1692,	
2123, 2132, 1810, 1907, 2426, 2463, 2535	925, 1077, 1627,	1711.   1745.	2386, 2400,
2200, 2201, \tanabel{eq:200} 111114 \frac{1400}{1400}, 1509	Z1Z3, Z13Z.		2426, 2463, 2535
		1810, 1907,	

\ignorespacesafterend	${f L}$	\linewidth
25, 834,	\label 30, 30, 30, 30,	28, 28, 904, 905
845, 1242, 1488,	30, 31, 31, 31,	\lap 1381, 1391,
2245, 2618, 2627	31, 31, 66, 66, 68	2021, 2030, 2325
\iiiint 463	\label@in@display	\Longleftarrow 264, 440
\iiint 462	30	\longleftarrow 438
	71, 937, 1252,	\Longleftrightarrow
\iint 461	1510, 2348, 2491	443, 448
\ilimits@ 19, 20, 453,		
454, 471, 478, 486	\lastbox . 50, 1619,	\longleftrightarrow 442
\impliedby $\frac{264}{}$	$   \begin{array}{ccc}     1628, & 2120, \\     2126, & 2128,   \end{array} $	\longmapsto 445
\implies 263		\Longrightarrow 263, 436
\inalign@false 990	2169, 2174, 2176	\longrightarrow 434, 445
\inalign@true 1506	\lbrace 804, 828	\loop 1626, 1717,
\incr@eqnum 950, 980,	\ldots 10, 333	1749, 1814, 1911
982, 986, 994, 2611	\left . $514, 797, 802,$	\lower 92, 504
\inf@bad $5$ , $98$ ,	804, 808, 809, 828	\lq 67
2527, 2560, 2583	\Leftarrow	\ltx@label $30$ , $937$ ,
	441, 443, 714, 716	957,  2517,  2531
\ingather@false 990	\leftarrow 439,	\lVert 134, 138, 139, 809
\ingather@true 1251	442, 447, 711, 713	\lvert 119, 123, 125, 808
\insplit@	\Leftarrowfill@ 714	
. 1251, 1436, <u>2104</u>	\leftarrowfill@	$\mathbf{M}$
\int 453	711, 722, 731, 751	\m@ne . 615, 617, 632,
\intdots@ 456, 467		980, 1061, 1067,
\interdisplaylinepenalty	\leftmargini 3, 48	1155, 1204,
26, 26, 35,	\Leftrightarrowfill@	1414,   1476,
<i>50</i> , <u>857</u> , 859, 888		1491, 1496,
\intertext 28, 28, 28, 897	\leftrightarrowfill@	1501 1050
\intertext@	$\dots$ 713, 724, 733	1501, 1652, 1666, 1724, 1756, 1770, 1821, 1835.
28, <u>897</u> , 1254, 1506	\leftroot 214,	1756 1770
	220, 225, 227, 228	1821, 1835,
\intkern@	\leftroot@ 217, 227,	1918, 1994,
455, 467, 468, 469	228, 235, 245, 246	2250, 2519, 2521
\intop 453,	\lendmultline@	\m@th 29, 96, 237,
466, 468, 469, 470	66, 2244, 2313	
\ints@a 473, 475	\lendsplit@ . $2083$ , $\overline{2164}$	241, 243, 262,
\ints@b $476, 477, 478, 482$	\leqno 72,	340, 706, 718,
\ints@c 466, 480	2457, 2459, 2460	726, 738, 760,
\Invalid@@	\let 11, 37, 37	768, 769, 816,
214, 215, 874, 897	\Let0 23, 28, 754,	817, 922, 1171,
\invalid@tag 29, 31,		1174, 1221,
<u>917,</u> 918, 965, 2472	766, <u>894</u> , 1163,	1262, 1283,
<u>==-</u> , ===, ===, ===,	1218, 1254,	2037, 2041,
J	1506, 2106, 2249	2111, 2112,
	\lhook 446	2270,   2356,
\joinrel 435,	\limits 13, 23,	2428,   2429,
437, 439, 441,	450, 476, 525,	2447, 2448, 2501
442, 443, 446, 447	528, 678, 680, 744	\macc@a 611, 628
\jot 1048	\lineht@ $34$ , $61$ ,	\macc@adjust
	$63, \ \underline{1024}, \ 1367,$	$\dots 645, 646, 650$
$\mathbf{K}$	1385,   1398,	\macc@code 610, 643, 645
\kern 92, 101,	1400,   1532,	$\mbox{\ensuremath{\texttt{macc@depth}}}$ 571, 575,
450, 505, 525,	2011, 2025,	582, 594, 632, 633
528, 643, 652,	2050, 2051,	\macc@group
676, 678, 680,	2054, 2055,	595, 599, 607, 608
688, 727, 1143,	2144, 2291,	\macc@kerna 638, 643, 651
1362, 1378,	2329, 2360, 2364	$\mbox{macc@kernb}$ . $642,651$
1402,   1526,	\lineskip 24	\macc@nested . 586, 596
2006, 2017, 2019	\lineskiplimit	\macc@nested@a
\keybin@ 327, 351	24, 758, 767, 1058	601, 602, 606
, .j. ==== · · · · · · · · · · · · · · · · ·	4, .00, 101, 1000	

\macc@nucleus	\mathaccentV $16$ , $16$ ,	\mathsm@sh 693, 703
$\dots$ 583, 589, 634	17, 17, 17, 18,	\Mathstrut@ <u>488</u>
\macc@palette	531, 573, 577, 601	
. 19, 605, 611, 631	\mathalpha 556	488, 517, 518
\macc@set@skewchar	\mathbin 666	\mathsurround 599
	\mathbin@	matrix environment
598, 600, 608, 613	293, 294, 295, 367	
		24, 24, <u>773</u>
\macc@skewchar	\mathch@ 286, 357	\matrix 24, 24, 774
624, 635, 636	\mathchar 184, 265	\matrix@check 24,
\macc@style 19, 630, 631	\mathchardef	774, <u>782</u> , 798, 822
\macc@test 577, 594	493, 610, 624,	\matrix@error 784, <u>788</u>
$\mbox{\mbox{$$^{575}$, $581, $594$}}$	697, 698, 700, 701	$\mbox{\tt maxcol@width}$
$\mbox{\colored} \ \dots \ 303,  359,  400$	\mathchoice 18,	47, <u>1584</u> , 1895. 1899.
\macro@@ 305, 306	19, 19, 23, 238,	1895, 1899,
\make@df@tag	455, 456, 483, 485	1903, 1990, 1999
<i>30</i> , <i>30</i> , <i>31</i> , <u>931</u> , 969	\mathclose 128, 142	\maxcolumn@widths
\make@df@tag@@ <u>931</u> , 2479	\mathcode 493,	. 47, 47, <u>1583</u> ,
\make@df@tag@@@	697, 698, 700, 701	1585, 1623, 1631
<u>931,</u> 2481	\mathdisplay	\maxfields0 $49$ ,
\make@display@tag	. 2486, 2614, 2623	49, <u>1005</u> , 1154,
		1155, 1154,
31, <u>949,</u> 1310,	\mathdisplay@@pop	1180, 1413,
1528, 2289,	2495, 2609	1100, 1413,
2296, 2331, 2335	\mathdisplay@@push	1414, 1419,
\makesm@sh 694	2494, 2594	1524,   1540,
\maketag@@ . $29, 30, 921$	\mathdisplay@pop .	1548, 1606,
\maketag@@@	$\dots \dots 2495,$	1610,   1611,
29, 29, 921, 934	2608, 2617, 2626	1614, 1649, 1664
\mapsto 444	\mathdisplay@push	\mb@b 691
\mapstochar 444, 445	$\dots \dots 2494,$	\mb@t 691
\math@ 282, 355, 366	2593, 2612, 2621	\mb@tb 691
\math@bgroup 598	\mathdisplay@stack	\mdots@ 337, 346
\math@cr 27, 28,	2592	\mdots@@ . 346, 347, 374
50, 68, 68, 885,	2603, 2605, 2609	\meaning 186,
894, 1241, 1478,	\mathellipsis	353, 399, 495, 534
2100, 2316, 2341	10, 332, 334	\meaning@
	\mathgroup 599, 607,	283, 287, 305,
\math@cr@ 27,		
28, 886, 890, <u>891</u>	608, 615, 617, 618	
\math@cr@@ 28, 891, 892	\mathindent . 3, 3, 3, 45	357, 358, 361,
\math@cr@@@ . 23, 23,	\mathinner 376	362, 366, 367,
28, 28, 38, 63,	\mathit 15	369, 399, 400, 401
892, 895, 1157,	\mathop	$\verb \meaning@@ 354, 359 $
1160,   1255,	13, 21, 21, 450,	\measure@ 49, 1513, <u>1587</u>
1291,   1508,	484, 525, 528,	\measuring@false .
1596, 1604, 2349	678, 680, 688, 736	. 1182, 1543, 2348
\math@cr@@@align .	\mathopen 126, 140	\measuring@true
1508, <u>1520</u>	- · · · · · · · · · · · · · · · · · · ·	. 1274, 1589, 2346
\math@cr@@@align@measure	249, 250, 251,	\medmuskip 106,
$\dots  \underline{1535}, 1596$	252, 253, 254,	108, 666, 668, 706
	255, 256, 257, 258	
\math@cr@@@aligned		\medspace 107
39,	\mathpalette	\MessageBreak
<u>1141, 1160, 1179</u>	605, 693,	153, 155, 567,
\math@cr@@@alignedat	703, 720, 722,	882, 1445, 2219
1157, 1179	724, 729, 731, 733	\minalignsep $39$ ,
\math@cr@@@gather	\mathpunct 272	48, 50, 50, 52,
$\dots$ 41, 1255, $\underline{1307}$	\mathrel $9$ ,	54, 55, 59,
\math@egroup 19, 598	450, 703, 704, 736	1021, 1161,
\mathaccent . 16, 17,	\mathrel@	1638,   1675,
17, 17, 17, 18,	298, 299, 300, 369	1676, 1702,
	\mathring 556, 558	1734, 1735,

1781, 1800,	${f N}$	\nointerlineskip .
1801, 1845,	\NeedsTeXFormat 1	718, 727, 1074
1867, 1868,	\negmedspace 108	\nolimits 7,
1936, 1961, 1962	\negthickspace 111	13, 20, 22, 23, 686
\mintagsep . 34, 48,	\negthinspace 105	\nomath@env
48, 49, 53, 55,	\new@ifnextchar 27,	. 1228, 1431, 2227
	The state of the s	
$73, \ \underline{1020}, \ 1316, \ \underline{1792}$	779, 827, 864, 891	\nonmatherr@ 591,
1716, 1783,	\newbox 488, 500	664, 1149, 1214
1797, 1847, 1849, 1864,	\newcount . 98, 216,	\nonscript 272, 666, 668
1849, 1864,	217, 288, 307,	\nonumber 31, 32, 32,
1938, 1940,	571, 781, 855,	<i>32</i> , 968, 977,
1955, 1973,	1000, 1001, 1005	<u>978,</u> 1308, 1483,
2557, 2575, 2578	\newcounter 832	1521, 1538,
\mkern 245, 246,	\newdimen $519$ , $1017$ ,	2092, 2233, 2474
273, 455, 457,	1018, 1019,	\normalbaselines .
458, 459, 483,	1022, 1023, 1024	$\dots 903, 1365,$
485, 666, 668,	\newhelp . 29, 911, 1014	1383, 2009,
670, 671, 672,	\newif	2023, 2286, 2327
673, 707, 708,	26, 27, 37, 405,	\normalcolor . $925, 928$
709, 739, 740,	451, 987, 988,	\normalfont $526$ ,
745, 746, 747,	996, 997, 998,	529, 922, 925, 928
748, 816, 817, 819	999, 1406, 1408	$\n$
\mmeasure@ $66, 2255, 2344$	\newmuskip 813	$\dots 504, 505, 1059$
\mod 20, 672	\newskip 39, 2221, 2223	\not 350
\moveleft 2133,	\next@ . 31, 31, 219,	\not@ 322, 323, 324, 361
2142, 2181, 2186	220, 221, 224,	\notag 32, 977
\mskip 101, 112, 243,	225, 226, 231,	\null 38,
272, 273, 666, 668	232, 233, 235,	765, 1152, 1216,
\mspace <u>112</u>	267, 270, 296,	1384, 2024, 2328
	301, 310, 312,	\nulldelimiterspace
\multicolumn 815	320, 326, 345,	513, 676
\MultiIntegral 461,	411, 420, 421,	\number
462, 463, 464, 465	426, 427, 433,	4, 6, 15, 32, 32,
\multilimits0 23	969, 971, 1142,	119, 121, 134,
\multiply 1156,	1143,   1145,	136, 290, 364,
1338, 1419,	1234,   1236,	624, 1011, 1111
1782, 1790,	1440, 2237, 2239	\numberwithin 847
1846, 1937, 1948	\nextii@	
multline environment	219, 222, 294,	Ο
33, 35,		\of 236
65, 66, 69, 69, 2241		\oint 454
multline* environ-	325, 409, 411, 413	\ointop 454
ment $\dots$ $\underline{2241}$	\nextiii@ 220, 228	\omit 1525, 1536
\multline@ . 2237, 2248	\nextiv@ 222, 223	\openup 26, 1048
\multline@indent .	\nextix@ 232, 234	\operator@font
2276, 2279,	\nextv@ 223, 224, 225	667, 671, 673
2294, 2305, 2308	\nextvi@ 225, 227	\or 47, 50, 182,
\multlinegap 65,	\nextvii@ 228, 229	290, 365, 862,
65, 65, 67,	\nextviii@ 230, 231, 232	871, 1031, 1032,
$\frac{2221}{2}$ , $\frac{2279}{2}$	\noaccents@ 521, 522, 523	1043, 1044,
$\frac{2221}{2315}$ , $\frac{2213}{2324}$ ,		1043, 1044, 1097, 1567,
2338, 2404,	\noalign 28, 28, 718, 727, 893,	1571,   1625,
2412, 2418,		1631, 1648, 1663
2433, 2439, 2450	901, 1054, 1071,	\over . 6, 6, 13, 145, 160
	1279, 1597, 2144, 2570, 2589	
\multlinetaggap $65$ ,		\overarrow@
65, <u>2221</u> , 2298, 2299, 2334,	\nobreakdash 9, 266	717, 720, 722, 724
2385, 2415, 2436	\nogood@displaybreak	\overlaftarrow 721
	\\noindon\ \ 007 1077	\overleftarrow 721
\multlinetaggap@ 65	/HOTHGent 301, 1011	\overleftrightarrow 723

\overline 9, 260, 261	$2254, \qquad 2292,$	\rightarrowfill@ .
\overrightarrow 719	2326, 2570, 2589	1.0
_	, ,	720, 729, 734, 750
\overset 21, 677	\raisetag 32, 32, 973	
\overwithdelims $148, 163$	\rangle 385	\rightdelim@ 11, 379, 397
_	\rbrace 384, 806	\rmoustache 389
P	\rbrack 382	\romannumeral 1011
\p@equation 936	\rceil 386	\root 218
\PackageError 90	\ref 854	\rootbox 236, 245
\PackageWarning	\refstepcounter	\row@ 42,
152, 2218	_	
\PackageWarningNoLine	. 26, 837, 986, 994	42, 63, 1000, 1000
	\relax 5, 27, 28, 65	1100, 1259,
	\relaxnext@	1312, 1317,
\par 3, 24, 37	218, 293, 298,	1514.   1523.
\parshape 905	314, 322, 339, 406	1537, 1600,
\partial 19	\Relbar 437, 441,	1718,   1719,
\PassOptionsToPackage	704, 714, 715, 716	1724, 1738,
$\dots \dots 23, 25$	\relbar 435, 439,	1750, 1751,
\place@tag $60, 1529, 2004$	703, 711, 712, 713	1756, 1764,
\place@tag@gather		
<i>32</i> , <i>33</i> , 1267, <u>1360</u>	\rendmultline@	1777, 1815,
	<i>67</i> , 2244, <u>2320</u>	1816, 1821,
plain.tex 11, 24, 25, 35	\rendsplit@ . 2083, <u>2116</u>	1829, 1842,
\plainroot@ 221, 226,	\renewenvironment	1912, 1913,
227, 233, 234, 236	24, 25	1918, 1926,
pmatrix environment 24	\repeat . 1632, 1725,	1932, 2007,
\pmatrix 24, 798	1757, 1822, 1919	2020, 2141,
\pmb 4		2250, 2352, 2358
\pmod	\RequirePackage	
\pod 20, 669, 671	87, 88, 89	\rq 67
\postdisplaypenalty	\reset@equation $992$ ,	\rVert 136, 141, 809
902, 2520	2087, 2467, 2474	\rvert 121, 127, 808
	\reset@strutbox@ .	
\predisplaypenalty 908	\reset@strutbox@ . $14, 35,$	${f s}$
$\label{eq:continuous_predisplay_penalty} \begin{array}{ll} 908 \\ \text{prevdepth} & 1073,  1078 \\ \end{array}$	14, 35,	
$\label{eq:continuous_prediction} $$ \operatorname{prevdepth} : 1073, 1078 \\ \operatorname{primfrac} : \dots : $$$	14, 35, 502, 506, 507, 1047	\savealignstate@ .
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	14, 35, 502, 506, 507, 1047 \resetMathstrut@ . 488	\savealignstate@ <u>1095</u> , 1425
$\label{eq:continuous_prediction} $$ \operatorname{prevdepth} : 1073, 1078 \\ \operatorname{primfrac} : \dots : $$$	14, 35, 502, 506, 507, 1047 \resetMathstrut@ . 488 \restore@hfuzz 2485,	\savealignstate@
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	14, 35, 502, 506, 507, 1047 \resetMathstrut@ . 488 \restore@hfuzz 2485, 2497, 2500,	\savealignstate0
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	14, 35, 502, 506, 507, 1047 \resetMathstrut@ . 488 \restore@hfuzz 2485, 2497, 2500, 2539, 2559, 2582	\savealignstate@
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	14, 35, 502, 506, 507, 1047 \resetMathstrut@ . 488 \restore@hfuzz 2485, 2497, 2500, 2539, 2559, 2582 \restore@math@cr 28,	$\begin{tabular}{lllllllllllllllllllllllllllllllllll$
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac 151, 160, 161, 162, 163, 164, 165 \print@eqnum 950, 982, 985, 993 \process@envbody .	14, 35, 502, 506, 507, 1047 \resetMathstrut@ . 488 \restore@hfuzz 2485, 2497, 2500, 2539, 2559, 2582 \restore@math@cr 28, 754, 766, 895,	\savealignstate@
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	14, 35, 502, 506, 507, 1047 \resetMathstrut@ . 488 \restore@hfuzz 2485, 2497, 2500, 2539, 2559, 2582 \restore@math@cr 28,	\savealignstate@
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac 151, 160, 161, 162, 163, 164, 165 \print@eqnum 950, 982, 985, 993 \process@envbody . 1120, 1124, 1125, 1139	14, 35, 502, 506, 507, 1047 \resetMathstrut@ . 488 \restore@hfuzz 2485, 2497, 2500, 2539, 2559, 2582 \restore@math@cr 28, 754, 766, 895,	\savealignstate@
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	14, 35, 502, 506, 507, 1047 \resetMathstrut@ . 488 \restore@hfuzz 2485, 2497, 2500, 2539, 2559, 2582 \restore@math@cr 28, 754, 766, 895, 1218, 2106, 2252 \restorealignstate@	\savealignstate@
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	$\begin{array}{c} \dots  14,\ 35,\\ 502,\ 506,\ 507,\ 1047\\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$	\savealignstate@
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	14, 35, 502, 506, 507, 1047   \resetMathstrut@ . 488   \restore@hfuzz 2485, 2497, 2500, 2539, 2559, 2582   \restore@math@cr 28, 754, 766, 895, 1218, 2106, 2252   \restorealignstate@ 1095, 1481   \restorecolumn@	$\begin{tabular}{lllllllllllllllllllllllllllllllllll$
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	14, 35, 502, 506, 507, 1047 \resetMathstrut@ . 488 \restore@hfuzz 2485, 2497, 2500, 2539, 2559, 2582 \restore@math@cr 28, 754, 766, 895, 1218, 2106, 2252 \restorealignstate@ 1095, 1481 \restorecolumn@ 1109, 1201	$\begin{tabular}{lllllllllllllllllllllllllllllllllll$
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	14, 35, 502, 506, 507, 1047 \resetMathstrut@ . 488 \restore@hfuzz 2485, 2497, 2500, 2539, 2559, 2582 \restore@math@cr 28, 754, 766, 895, 1218, 2106, 2252 \restorealignstate@ 1095, 1481 \restorecolumn@ 1109, 1201 \restorecounters@	$\begin{tabular}{lllllllllllllllllllllllllllllllllll$
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	14, 35, 502, 506, 507, 1047 \resetMathstrut@ . 488 \restore@hfuzz 2485, 2497, 2500, 2539, 2559, 2582 \restore@math@cr 28, 754, 766, 895, 1218, 2106, 2252 \restorealignstate@ 1095, 1481 \restorecolumn@ 1109, 1201 \restorecounters@ 1082,	\savealignstate@ 1095, 1425 \savecolumn@ 1109, 1151 \savecounters@ 1082,
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	$\begin{array}{c} \dots  14,35,\\ 502,506,507,1047\\ \texttt{\colored},506,507,1047\\ \texttt{\colored},2506,2485,\\ 2497,2500,\\ 2539,2559,2582\\ \texttt{\colored},2559,2582\\ \texttt{\colored},754,766,895,\\ 1218,2106,2252\\ \texttt{\colored},218,2106,2252\\ \texttt{\colored},218,2106,2252\\ \texttt{\colored},1294,1609,1201\\ \texttt{\colored},1294,1609,2397\\ \end{array}$	\savealignstate@
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	14, 35, 502, 506, 507, 1047 \resetMathstrut@ . 488 \restore@hfuzz 2485, 2497, 2500, 2539, 2559, 2582 \restore@math@cr 28, 754, 766, 895, 1218, 2106, 2252 \restorealignstate@ 1095, 1481 \restorecolumn@ 1109, 1201 \restorecounters@ 1082,	\savealignstate@
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	$\begin{array}{c} \dots  14,35,\\ 502,506,507,1047\\ \texttt{\colored},506,507,1047\\ \texttt{\colored},2506,2485,\\ 2497,2500,\\ 2539,2559,2582\\ \texttt{\colored},2559,2582\\ \texttt{\colored},754,766,895,\\ 1218,2106,2252\\ \texttt{\colored},218,2106,2252\\ \texttt{\colored},218,2106,2252\\ \texttt{\colored},1294,1609,1201\\ \texttt{\colored},1294,1609,2397\\ \end{array}$	\savealignstate@
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	\savealignstate@
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	14, 35, 502, 506, 507, 1047 \resetMathstrut@ . 488 \restore@hfuzz 2485, 2497, 2500, 2539, 2559, 2582 \restore@math@cr 28, 754, 766, 895, 1218, 2106, 2252 \restorealignstate@ 1095, 1481 \restorecolumn@ 1109, 1201 \restorecounters@ 1082, 1294, 1609, 2397 \rfloor 387 \rgroup 388 \rhook 447	\savealignstate@ $1095$ , $1425$ \savecolumn@ $1109$ , $1151$ \savecounters@ $1082$ , $1277$ , $1594$ , $2351$ \savefieldlength@ $1563$ , $2038$ , $2042$ \saveshift@ $1041$ , $1722$ , $1739$ , $1741$ , $1754$ , $1786$ ,
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	14, 35, 502, 506, 507, 1047 \resetMathstrut@ . 488 \restore@hfuzz 2485, 2497, 2500, 2539, 2559, 2582 \restore@math@cr 28, 754, 766, 895, 1218, 2106, 2252 \restorealignstate@ 1095, 1481 \restorecolumn@ 1109, 1201 \restorecounters@ 1082, 1294, 1609, 2397 \rfloor 387 \rgroup 388 \rhook 447 \RIfM@ 1148,	\savealignstate@ $\frac{1095}{1425}$ , $\frac{1425}{1425}$ \savecolumn@ $\frac{1109}{1151}$ , $\frac{1151}{152}$ , $\frac{1082}{1277}$ , $\frac{1594}{1594}$ , $\frac{2351}{1527}$ \savefieldlength@ . $\frac{1563}{152}$ , $\frac{2038}{1741}$ , $\frac{1722}{1739}$ , $\frac{1741}{1754}$ , $\frac{1786}{1788}$ , $\frac{1819}{1853}$ , $\frac{1855}{1855}$ , $\frac{1916}{1944}$ , $\frac{1946}{1944}$ \savetaglength@ $\frac{63}{1025}$ , $\frac{1288}{1559}$ , $\frac{2140}{2128}$ Sb environment
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	14, 35, 502, 506, 507, 1047 \resetMathstrut@ . 488 \restore@hfuzz 2485, 2497, 2500, 2539, 2559, 2582 \restore@math@cr 28, 754, 766, 895, 1218, 2106, 2252 \restorealignstate@ 1095, 1481 \restorecolumn@ 1109, 1201 \restorecounters@ 1082, 1294, 1609, 2397 \rfloor 387 \rgroup 388 \rhook 447 \RIfM@ 1148, 1213, 1227, 2226	\savealignstate@ $\frac{1095}{1425}$ , $\frac{1425}{1425}$ \savecolumn@ $\frac{1109}{1151}$ , $\frac{1151}{152}$ , $\frac{1082}{1277}$ , $\frac{1594}{1594}$ , $\frac{2351}{1277}$ , $\frac{1594}{1594}$ , $\frac{2351}{1288}$ , $\frac{163}{1788}$ , $\frac{1041}{1722}$ , $\frac{1739}{1741}$ , $\frac{1754}{1754}$ , $\frac{1786}{1788}$ , $\frac{1819}{1853}$ , $\frac{1855}{1855}$ , $\frac{1916}{1944}$ , $\frac{1946}{1948}$ , $\frac{1946}{1948}$ , $\frac{163}{1288}$ , $\frac{1559}{1288}$ , $\frac{1288}{1559}$ , $\frac{2140}{1288}$ , $\frac{1857}{1288}$ ,
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	14, 35, 502, 506, 507, 1047 \resetMathstrut@ . 488 \restore@hfuzz 2485, 2497, 2500, 2539, 2559, 2582 \restore@math@cr 28, 754, 766, 895, 1218, 2106, 2252 \restorealignstate@ 1095, 1481 \restorecolumn@ 1109, 1201 \restorecounters@ 1082, 1294, 1609, 2397 \rfloor 387 \rgroup 388 \rhook 447 \RIfM@ 1148, 1213, 1227, 2226 \right 390,	\savealignstate@ 1095, 1425 \savecolumn@ 1109, 1151 \savecounters@ 1082,
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	14, 35, 502, 506, 507, 1047 \resetMathstrut@ . 488 \restore@hfuzz 2485, 2497, 2500, 2539, 2559, 2582 \restore@math@cr 28, 754, 766, 895, 1218, 2106, 2252 \restorealignstate@ 1095, 1481 \restorecolumn@ 1109, 1201 \restorecounters@ 1082, 1294, 1609, 2397 \rfloor 387 \rgroup 388 \rhook 447 \RIfM@ 1148, 1213, 1227, 2226 \right 390, 514, 800, 802,	\savealignstate@
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	14, 35, 502, 506, 507, 1047 \resetMathstrut@ . 488 \restore@hfuzz 2485, 2497, 2500, 2539, 2559, 2582 \restore@math@cr 28, 754, 766, 895, 1218, 2106, 2252 \restorealignstate@ 1095, 1481 \restorecolumn@ 1109, 1201 \restorecounters@ 1082, 1294, 1609, 2397 \rfloor 387 \rgroup 388 \rhook 447 \RIfM@ 1148, 1213, 1227, 2226 \right 390, 514, 800, 802, 806, 808, 809, 824	\savealignstate@
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	14, 35, 502, 506, 507, 1047 \resetMathstrut@ . 488 \restore@hfuzz 2485, 2497, 2500, 2539, 2559, 2582 \restore@math@cr 28, 754, 766, 895, 1218, 2106, 2252 \restorealignstate@ 1095, 1481 \restorecolumn@ 1109, 1201 \restorecounters@ 1082, 1294, 1609, 2397 \rfloor 387 \rgroup 388 \rhook 447 \RIfM@ 1148, 1213, 1227, 2226 \right 390, 514, 800, 802, 806, 808, 809, 824 \Rightarrow	\savealignstate@
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	14, 35, 502, 506, 507, 1047 \resetMathstrut@ . 488 \restore@hfuzz 2485, 2497, 2500, 2539, 2559, 2582 \restore@math@cr 28, 754, 766, 895, 1218, 2106, 2252 \restorealignstate@ 1095, 1481 \restorecolumn@ 1109, 1201 \restorecounters@ 1082, 1294, 1609, 2397 \rfloor 387 \rgroup 388 \rhook 447 \RIfM@ 1148, 1213, 1227, 2226 \right 390, 514, 800, 802, 806, 808, 809, 824	\savealignstate@
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	14, 35, 502, 506, 507, 1047 \resetMathstrut@ . 488 \restore@hfuzz 2485, 2497, 2500, 2539, 2559, 2582 \restore@math@cr 28, 754, 766, 895, 1218, 2106, 2252 \restorealignstate@ 1095, 1481 \restorecolumn@ 1109, 1201 \restorecounters@ 1082, 1294, 1609, 2397 \rfloor 387 \rgroup 388 \rhook 447 \RIfM@ 1148, 1213, 1227, 2226 \right 390, 514, 800, 802, 806, 808, 809, 824 \Rightarrow	\savealignstate@
\predisplaypenalty 908 \prevdepth . 1073, 1078 \primfrac	14, 35, 502, 506, 507, 1047 \resetMathstrut@ . 488 \restore@hfuzz 2485, 2497, 2500, 2539, 2559, 2582 \restore@math@cr 28, 754, 766, 895, 1218, 2106, 2252 \restorealignstate@ 1095, 1481 \restorecolumn@ 1109, 1201 \restorecounters@ 1082, 1294, 1609, 2397 \rfloor 387 \rgroup 388 \rhook 447 \RIfM@ 1148, 1213, 1227, 2226 \right 390, 514, 800, 802, 806, 808, 809, 824 \Rightarrow 437, 443, 715, 716	\savealignstate@

\set@gather@field	\slimits@ 7,	\stepcounter
1264, 1360	21, 22, 189, 191,	36, 1553, 2376
\set@mathaccent	193, 195, 197,	\strut 14, 20, 675
	199, 201, 203,	
16, 530, 544		\strut@ 14,
\setb@ck 30	205, 207, 209, 211	500, 1077, 1170,
\setbox 95,	smallmatrix environ-	1221,   1261,
236, 243, 489,	ment $\dots$ 23, $\underline{765}$	1266,   1287,
492, 503, 576,	\smash <u>21</u> , <u>690</u>	1528,   1551,
635, 636, 639,	Sp environment 23	2036, 2110,
	_	2269, 2288, 2331
640, 683, 684,	\span . 1268, 1517, 1602	\strutbox 505
737, 738, 1278,	split environment 42,	
1384,   1595,	61, 61, 62, 63,	\strutbox@
1618, 1619,	63, 63, 63, 63, <u>2069</u>	$35, \underline{500}, 1075, 1076$
1627,   1628,	\split 1251, 1436	subarray environment
2024, 2105,	\split@ 2131,	23, 23, 23, 23, <u>752</u>
2118, 2120,	2137, 2152,	\subarray 764
2123, 2126,		\substack 23, 23, 23, <u>764</u>
2120, 2120,	2154, 2162,	
2128, 2136,	2179, 2184,	\sum 202, 203
2165,   2167,	2191, 2193, 2196	\sum@ 202, 203
2169, 2171,	\split@al@a . 2200, 2201	
2174, 2176,	\split@al@tagcheck	${f T}$
$2296, \qquad 2328,$	-	\tabskip <u>50</u> ,
2353, 2429,	2205, 2209	50, 50, 50, 58,
2448, 2499,	\split@aligned	
	2072, 2198	58, 67, 1172,
2530, 2556, 2577	\split@err . <u>2060</u> , <u>2076</u>	1176,   1258,
$\scaleboxz@h \dots 241,$	\split@tag 2085,	1265, 1268,
269, 1262, 1266,		1515,   1601,
1283,   1287,	2090, 2094, 2098	2040, 2045,
1528,   1551,	\split@warning	2257, 2565, 2586
2037, 2041,	. 2202, 2217, 2500	\tag
2139, 2356,	\spread@equation .	,
, ,	14, 32,	29, 29, 29, 29,
2374, 2428, 2447	$991, \underline{1047}, 1052,$	29, 29, 29, 29,
\setcounter 839, 840, 844		$29, \ 29, \ 29, \ 29,$
\setlength 65	1165, 1219,	29, 30, 30, 30,
\shdots@for 812, 814	2096, 2565, 2586	30, 31, 31, 31,
\shift@tag	\sqrtsign 8, 8, 240, 241	31, 31, 32, 33,
_	\st@rredfalse 44,	38, 38, 66, 66,
. <u>1025</u> , 2007, 2020	1239, 1451,	
\shifttag@false	1461, 1476,	73, 918, 919,
$\dots \dots 1257,$		965, 1252, 1509,
1370, 1389, 2394	1496, 2242, 2613	$2107, \qquad 2253,$
\shifttag@true 1324,	\st@rredtrue 44,	2256, 2472, 2491
1330, 1342, 2392	1246,   1456,	\tag* 29, 29
	1466,   1471,	\tag@false
\shoveleft 44,	1491, 1501,	1068, 1279,
69, 69, 2350, 2400	2247, 2474, 2622	
\shoveright 44,		1597, 2254,
<i>69</i> , <i>69</i> , 2350, <u>2400</u>	\start@align	2493, 2510, 2600
showkeys package		
showkeys package	. 44, 44, <u>1411</u> ,	\tag@help . 29, 911, 917
NA NA NA	. 44, 44, <u>1411,</u> 1451, 1456,	\tag@help . 29, 911, 917
71, 71, 71	. 44, 44, <u>1411</u> ,	\tag@help . 29, 911, 917 \tag@in@align
71, 71, 71 \sideset 21, 681	. 44, 44, <u>1411</u> , 1451, 1456,	\tag@help . 29, 911, 917 \tag@in@align
	$\begin{array}{cccc}  & 44, & 44, & \underline{1411}, \\ 1451, & & 1456, \\ 1461, & & 1466, \\ 1471, & & 1476, \end{array}$	\tag@help . 29, 911, 917 \tag@in@align
\sideset 21, 681 \sixt@0n 865	$\begin{array}{c} \cdot  \cancel{44}, \ \cancel{44}, \ \frac{1411}{1456}, \\ 1451, \qquad 1456, \\ 1461, \qquad 1466, \\ 1471, \qquad 1476, \\ 1491,  1496,  1501 \end{array}$	\tag@help . 29, 911, 917 \tag@in@align 71, 962, 1252, 1509, 2253 \tag@in@display
\sideset 21, 681 \sixt@@n 865 \size@update 14, 14	. 44, 44, 1411, 1451, 1456, 1461, 1466, 1471, 1476, 1491, 1496, 1501 \start@aligned . 38,	\tag@help . 29, 911, 917 \tag@in@align 71, 962, 1252, 1509, 2253 \tag@in@display 2469, 2491
\sideset 21, 681 \sixt@0n 865 \size@update 14, 14 \SK@@label . 2465, 2477	. 44, 44, 1411, 1451, 1456, 1461, 1466, 1471, 1476, 1491, 1496, 1501 \start@aligned . 38, 1147, 1204, 1211	\tag@help . 29, 911, 917 \tag@in@align
\sideset 21, 681 \sixt@0n 865 \size@update 14, 14 \SK@@label . 2465, 2477 \SK@equationtrue .	. 44, 44, 1411, 1451, 1456, 1461, 1466, 1471, 1476, 1491, 1496, 1501 \start@aligned . 38, 1147, 1204, 1211 \start@gather	\tag@help . 29, 911, 917 \tag@in@align 71, 962, 1252, 1509, 2253 \tag@in@display 2469, 2491
\sideset 21, 681 \sixt@0n 865 \size@update 14, 14 \SK@@label . 2465, 2477	. 44, 44, 1411, 1451, 1456, 1461, 1466, 1471, 1476, 1491, 1496, 1501 \start@aligned . 38, 1147, 1204, 1211	\tag@help . 29, 911, 917 \tag@in@align
\sideset 21, 681 \sixt@0n 865 \size@update 14, 14 \SK@@label . 2465, 2477 \SK@equationtrue 2465, 2491	. 44, 44, 1411, 1451, 1456, 1461, 1466, 1471, 1476, 1491, 1496, 1501 \start@aligned . 38, 1147, 1204, 1211 \start@gather	\tag@help . 29, 911, 917 \tag@in@align
\sideset	. 44, 44, 1411, 1451, 1456, 1461, 1466, 1471, 1476, 1491, 1496, 1501 \start@aligned . 38, 1147, 1204, 1211 \start@gather . 1226, 1239, 1246 \start@multline	\tag@help . 29, 911, 917 \tag@in@align
\sideset	$\begin{array}{c} .  44, \ 44, \ \underline{1411}, \\ 1451, \qquad 1456, \\ 1461, \qquad 1466, \\ 1471, \qquad 1476, \\ 1491,  1496,  1501 \\ \\ \texttt{Start@aligned}  .  38, \\ \underline{1147},  1204,  1211 \\ \\ \texttt{Start@gather}  .  .  .  .  .  .  .  \underline{1226}, \ 1239, \ 1246 \\ \\ \texttt{Start@multline}  .  .  .  .  .  .  \underline{2225}, \ 2242, \ 2247 \\ \end{array}$	\tag@help . 29, 911, 917 \tag@in@align
\sideset	. 44, 44, 1411, 1451, 1456, 1461, 1466, 1471, 1476, 1491, 1496, 1501 \start@aligned . 38, 1147, 1204, 1211 \start@gather . 1226, 1239, 1246 \start@multline	\tag@help . 29, 911, 917 \tag@in@align

1747, 1812, 1909	-	${f U}$
\tag@true $967$ ,	109, 111, 706	\uccode 280,
1522,   1539,	\thickspace 110, 768	285, 292, 297,
2092, 2371,	\thinmuskip	302, 308, 313, 321
2372, 2474, 2600	102, 104, 273, 706	\underarrow@
\tag@width $\frac{1025}{}$ ,	\thinspace 103	725, 729, 731, 733
1317, 1719,	$\t 100 \dots 469$	\underleftarrow 730
1738, 1751, 1777, 1816,	757, 1614, 1628,	\underleftrightarrow
	1630, 1631, 2128, 2132,	
1842, 1913, 1932	2128,   2132,	\underrightarrow . 728
\tagform@ 26,	2133, 2142,	\underset 21, 679
29, 30, 30, 30,	2146, 2158,	\unhbox 269,
854, 921, 926,	2176, 2180,	743, 1628,
928, 930, 935, 985, 993, 1554,	2181, 2185, 2186	2136, 2541,
2377, 2477, 2514	\Tilde 20, 656	2551, 2569, 2590
\tagshift@ 52, 1019,	\tilde 20, 547, 656	\unhcopy 2124, 2172, 2557, 2580
1690, 1691,	\tmspace 5,	\unpenalty 1619
1694, 1697,	100, 102, 104,	\unskip 339,
1700, 2006, 2019	106, 108, 109, 111	923, 1628, 2121,
\tagsleft@false	\too@wide	2125, 1026, 2121, 2125, 2127,
29, 53, 55	. 2524, 2527, 2540	2125,   2127,   2136,   2173,
\tagsleft@true	\totwidth@ 50, 50, 52,	2175, 2541,
$\dots \dots 28, 52, 57$	58, <u>1023</u> , 1099,	2551, 2557,
\tagwidth@	1241, 1275, 1284, 1285,	2569, 2580, 2590
. 58, 59, <u>1022</u> ,	1284,   1285,  1296,   1299,	\unvbox 1619
1317,   1320,	1300, 1375,	\unvcopy 2119, 2165, 2168
1321, 1337,	1000 1400	\uproot 215,
1340, 1344,	1621 1622	219, 222, 232, 234
1345, 1777,	1376, 1478, 1621, 1622, 1635, 1680, 1690, 1703.	\uproot@ 216,
1780, 1792,	1690, 1703,	222, 234, 235, 243
1842, 1844,	1704, 1705,	\use@mathgroup 578
	1732, 1933,	\usefont 94
1935, 1951,	2100, 2258,	
1975, 2382,	2260, 2263,	${f V}$
2384, 2414, 2435	2359, 2363, 2383	\value 839, 844
\tbinom 6, 171	\try@load@fontshape 81	\varDelta 249
tbtags option 65	\tw@ 319, 403, 468,	\varGamma 248
\tdots@ 339, 426	510, 525, 528,	$\vortext{Numbda}$ $251$
\text	636, 637, 684,	$\vortnermal{varOmega}$ 258
\textellipsis 334, 337	685, 738, 743,	\varPhi 256
\textfont 34,	755, 756, 1020,	\varPi 253
494, 617, 621, 1020	1156,   1338,	\varPsi 257
\textstyle	1349,   1412,	\varSigma 254
. 23, 182, 238, 450	1416,   1419,	\varTheta 250
\textup 26, 854	1471,   1496,	\varUpsilon 255
\tfrac 6, 6, 168	1501, 1613,	\varXi 252
\thedots@	1644, 1650,	\vbox 23, 23, 23, 23
290, 291, 347,	1665, 1682,	\vcenter 23,
348, 349, 350,	1693, 1771,	23,  23,  514,
352, 361, 364, 365, 368, 370, 372	1796, 1836,	753, 765, 1153,
$365, 368, 370, 372$ \theequation $26,$	1848, 1863, 1872, 1939,	1217, 1425, 2097, 2133,
838, 841, 926,	1872, 1939, 1954, 1966,	2152, 2181, 2191
928, 985, 993,	1972, 1995,	\Vec 663
1554, 2377, 2514	2126, 2136,	\vec 554, 663
\theparentequation	2174,   2556,   2566,   25666,   25666,   25666,   25666,   25666,   25666,   25666,   25666,   25666,   25666,   256666,   25666,   25666,   25666,   25666,   25666,   256666,   256666,   256666,   256666,   256	\veqno 2462, 2463, 2516
26, 838, 841	2560, 2577, 2583	\Vert
\thetag $\dots$ $30$ , $930$	\typeout 56, 66	\vert
(oncode 50, <u>350</u>	(J) peculo 50, 00	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,

\vtop 63,	\widehat 16, 561	xalignat* environ-
726, 1153, 1217,	\widetilde 16, 560	ment $1450$
1381, 2021,	\write 31	\xatlevel@ . 44, 44,
2118, 2165, 2325		48, <u>1406</u> , 1412,
		1416,   1613,
$\mathbf{W}$	$\x@calc@shift@lc$ .	1615,   1636,
	$\dots 60, 1914, \underline{1922}$	
640, 642, 687,	$\x@calc@shift@lf$ .	1848, 1863,
743, 1621, 1631,	<i>53, 53</i> ,	1939, 1954, 1972
2132, 2133,	53, 54, 1720, <u>1728</u>	\xi <u>19</u>
2142, 2180,	\x@calc@shift@rc .	\xleaders 817
2181, 2185,	$\dots 1817, \underline{1825}$	\xleftarrow 21, 751
$2186, \qquad 2297,$	\x@calc@shift@rf .	\xrightarrow 21, 734, 750
2441, 2451, 2575	<i>54</i> , 1752, <u>1760</u>	xxalignat environ-
$\wdz@ \dots 1032, 1284,$	\x@lcalc@width	ment $\dots$ $\frac{44}{9}$ ,
1285,   1328,	$\dots 60, 1929, \underline{1985}$	
1336,   1339,	\x@rcalc@width . $54$ ,	\xxat@true 1417
1353,   1575,	1767, 1832, 1890	
2359,   2363,	xalignat environment	${f z}$
2382, 2442, 2452	44, 44, 51, 1450	\z@ 6, 6, 13, 28