polinomis de laguerre

$$L_n^m(x) = \sum_{k=0}^{n-m} (-1)^k \binom{n}{k+m} \frac{1}{k!} x^k = \sum_{k=0}^{n-m} (-1)^k \frac{n!}{(n-m-k)!(k+m)!k!} x^k$$

$$L_p^q(x) = c_0 \sum_{j=0}^p \frac{(-1)^j (p+q)!}{(p-j)! (q+j)! j!} x^j$$
 (2)

$$L_{n-l-1}^{2l+1}(2\rho)$$

$$L_{n-l-1}^{2l+1}(2\rho) = \sum_{j=0}^{n-l-1} \frac{(-1)^j 2^j (n+l)!}{(n-l-j-1)!(2l+j+1)!j!} \rho^j$$
 (34)

orbitals atomics

$$\psi_{n\ell m}(r,\vartheta,\varphi) = \sqrt{\left(\frac{2}{na_0}\right)^3 \frac{(n-\ell-1)!}{2n[(n+\ell)!]^3} e^{-\rho/2} \rho^\ell L_{n-\ell-1}^{2\ell+1}(\rho) Y_\ell^m(\vartheta,\varphi)}$$

$$\phi(p,\vartheta_p,\varphi_p) = \sqrt{\frac{2}{\pi} \frac{(n-l-1)!}{(n+l)!}} n^2 2^{2l+2} l! \frac{n^l p^l}{(n^2 p^2 + 1)^{l+2}} C_{n-l-1}^{l+1} \left(\frac{n^2 p^2 - 1}{n^2 p^2 + 1} \right) Y_l^m(\vartheta_p,\varphi_p),$$

$$\Phi(\phi) = e^{im\phi}$$
 $\Theta(\theta) = AP_l^m[cos(\theta)]$

on A es una constant i P es la funcio saaociada de Legendre

$$P_l^{m}(x) = (1 - x^2)^{|m|/2} \left(\frac{d}{dx}\right)^{|m|} P_l(x)$$

$$\begin{split} Y_l^m(\theta,\phi) &= \epsilon \sqrt{\frac{(2l+1)}{4\pi} \frac{(l-|m|)!}{(l+|m|)!}} e^{im\phi} P_l^m[\cos(\theta)] \\ &\epsilon = (-1)^m \;\; \text{para} \; m \geq 0 \\ &\epsilon = 1 \;\; \text{para} \; m \leq 0 \end{split}$$