System and device programming 15 July 2014

Examination Time: 1 h 45 min Evaluation: 18 marks.

Textbooks and/or course material allowed.

The final mark is the sum of the 1st and the 2nd parts; it cannot be refused (no retry for marks >= 18).

The binomial coefficient is defined as:

$$\binom{n}{k} = \frac{n!}{(n-k)!} = \frac{n \cdot (n-1) \cdot \dots \cdot (n-k+1)}{1 \cdot 2 \cdot \dots \cdot k}$$
$$\binom{n}{0} = \binom{n}{n} = 1$$

n and k are integers, and $n \ge k \ge 0$.

For example
$$\binom{15}{11} = \frac{15!}{(15-11)! \cdot 11!} = \frac{15 \cdot 14 \cdot 13 \cdot 12 \cdot 11 \cdot 10 \cdot 9 \cdot 8 \cdot 7 \cdot 6 \cdot 5}{1 \cdot 2 \cdot 3 \cdot 4 \cdot 5 \cdot 6 \cdot 7 \cdot 8 \cdot 9 \cdot 10 \cdot 11} = 1365$$

Write a concurrent **C** program in the Unix environment which receives two arguments **n**, **k**, and computes and print the binomial coefficient.

The computation has to be performed in concurrency by a **numerator** thread a **denominator**: thread.

The numerator thread loops by taking two factors at a time that must be multiplied (for example 15 and 14), computes their product, and save its result in its variable numer.

The same procedure is performed by the **denominator** threads, which save its result in its variable **denom**.

After the numerator and the denominator threads have performed their computation, they must synchronize: one of them has to perform the division of the partial contributions stored in numer and denom, and save it in a global variable result.

Then, **numerator** and **denominator** threads continue their job with the next pairs of factors that have not yet been processed.

Since it is possible that the number of remaining factors in the numerator and in the denominator is less than 2, care has to be taken to synchronize the threads also considering this possibility, so that the synchronization among the **numerator** and **denominator** threads is correct and each thread can terminate.

The main thread will print the result of the binomial coefficient computation.